

A Appendix

Proposition 1. *Given a temporal user query ρ and a trained MARL policy π , if Algorithm 1 returns YES, then the query ρ must be feasible under the policy π ; otherwise, Algorithm 1 generates correct and complete explanations \mathcal{E} .*

Proof. We prove the following two cases.

Case 1: When Algorithm 1 returns YES, the policy abstraction MMDP \mathcal{M} or the updated MMDP \mathcal{M}' satisfies the PCTL* formula φ encoding the user query ρ , indicating that there must exist a path through \mathcal{M} or \mathcal{M}' conforms with ρ . By construction, every abstract MMDP transition (s, a, s') in \mathcal{M} or \mathcal{M}' with non-zero probability maps to at least one sampled decision (x, a, x') of the given MARL policy π . Thus, there must exist an execution of policy π that conforms with the user query ρ . By definition, the user query ρ is feasible under the given MARL policy π .

Case 2: Algorithm 1 returns explanations \mathcal{E} generated via Algorithm 3. As described in Section 4.4, Algorithm 3 terminates when all failures in the user query ρ have been explained and fixed. Given a finite-length temporal query ρ , there is a finite number of failures. For any failure in the query, if the target states set \mathcal{V} is non-empty, then the failure must be fixable using a Quine-McCluskey minterm that represents a target state where the failed task is completed. If \mathcal{V} is empty, then the failure is removed from the query. Thus, the termination of Algorithm 3 is guaranteed. By definition, the generated explanations are *correct* (i.e., identifying the causes of one or more failures in ρ) and *complete* (i.e., finding the reasons behind all failures in ρ). \square