

cuRAMSES-kjhan

Technical Reference Manual

K-Section Ordering, Morton Key Octree,
Memory-Based Load Balancing, and
Performance Optimizations

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Based on RAMSES (R. Teyssier)

[git@github.com: kjhan0606/cuRAMSES-kjhan.git](https://github.com/kjhan0606/cuRAMSES-kjhan.git)

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Code Modifications

1

K-Section Ordering

1.1 Overview

The **k-section ordering** replaces the standard Hilbert curve domain decomposition with a hierarchical spatial bisection tree. Unlike the Hilbert curve approach that relies on a 1D space-filling curve, the k-section ordering partitions the 3D domain using recursive bisection along each coordinate axis, producing a balanced k-ary tree of spatial subdomains.

Key Advantage

The k-section tree enables **hierarchical MPI exchange** where communication follows the tree structure, achieving $O(\sum k_l)$ messages per exchange instead of $O(N_{\text{cpu}})$ all-to-all communication.

1.2 Hierarchical MPI Exchange

Two exchange routines are provided in `patch/cuda/ksection.f90`:

- `ksection_exchange_dp` — exclusive exchange (each item → exactly 1 destination CPU)
- `ksection_exchange_dp_overlap` — overlap exchange (items routed by spatial bounding box)

1.2.1 Exclusive Exchange

Each data item has a known destination CPU. The algorithm performs level-by-level correspondent exchange through the k-section tree, using MPI tags 100–300+level.

1.2.2 Overlap Exchange

Items have spatial extent (bounding box) and may need to reach multiple CPUs. The tree walk determines all destination CPUs whose spatial domain overlaps the item's bounding box. MPI tags 400–500+level are used.

1.2.3 Periodic Boundary Conditions

The optional `periodic=.true.` parameter enables handling of items that wrap around the domain boundary $[0, \text{scale}]$. For each wrapping dimension, $2^{n_{\text{wrap}}} - 1$ shifted copies are generated via bitmask subset enumeration before the tree walk.

Domain Decomposition $3 \times 3 \times 2 = 18$ subboxes
 4096^3 TSC density | $\log_{10}(1+\Sigma)$ projected column density

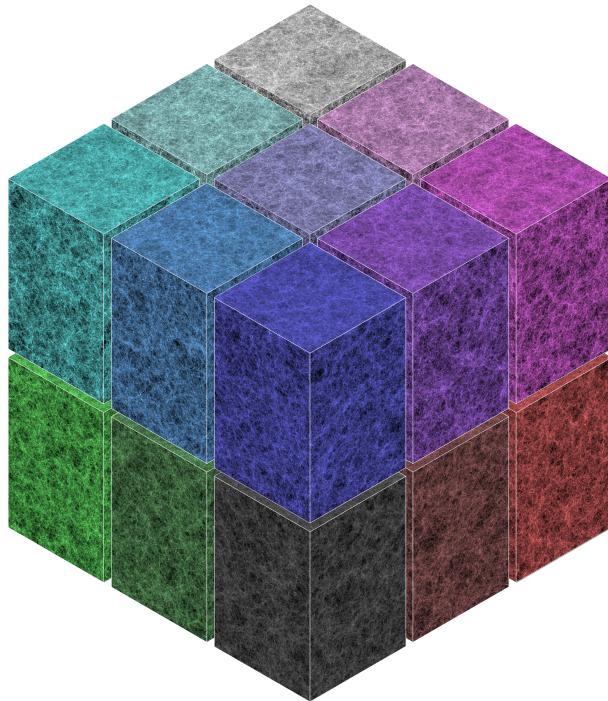


Figure 1.1: Isometric view of k-section domain decomposition with a $3 \times 3 \times 2 = 18$ uniform partition. Each subbox surface shows the projected column density $\log_{10}(1+\Sigma)$ from a 4096^3 TSC density field. Colors encode spatial position: R → x, G → y, B → z, providing a smooth gradient across adjacent subboxes.

1.3 Tree Navigation

The arrays `ksec_cpumin/cpumax` and `ksec_cpu_path` (set in `build_ksection` and at restart via `rebuild_ksec_cpuranges`) enable each CPU to navigate the tree efficiently.

1.4 Verification

The exchange routines are tested in `test_ksection_exchange` with 4 test cases:

1. Exclusive point exchange
2. Overlap point exchange
3. Full overlap exchange
4. Periodic overlap exchange (20% radius items)

All tests pass.

2

Ghost Zone Exchange via K-Section

2.1 AMR Ghost Zones

The standard RAMSES ghost zone exchange uses MPI_ISEND/IRecv with all-to-all communication patterns. This was replaced with k-section tree-routed exchange for the `ordering='ksection'` mode.

2.1.1 Modified File

`patch/cuda/virtual_boundaries.kjhan.f90`

2.1.2 Subroutines

Four k-section variants were implemented:

Subroutine	Direction	Data Type
<code>make_virtual_fine_dp_ksec</code>	Forward	<code>real(dp)</code>
<code>make_virtual_fine_int_ksec</code>	Forward	<code>integer</code>
<code>make_virtual_reverse_dp_ksec</code>	Reverse (+= accumulate)	<code>real(dp)</code>
<code>make_virtual_reverse_int_ksec</code>	Reverse (+= accumulate)	<code>integer</code>

2.1.3 Data Packing

Each emission grid is packed as:

$$\text{sendbuf}(1:\text{twotondim} + 2, i) = [\underbrace{c_1, c_2, \dots, c_8}_{\text{cell data}}, \underbrace{\text{myid}}_{\text{sender}}, \underbrace{i}_{\text{index}}]$$

The metadata (sender ID, emission index) allows the receiver to scatter data to the correct reception grid without requiring a priori knowledge of the communication pattern.

2.1.4 Dispatch

Dispatch is automatic via:

```
if (ordering=='ksection') then
    call make_virtual_fine_dp_ksec(xx, illevel)
    return
end if
```

2.1.5 Bulk Exchange

Four bulk variants exchange all columns of a 2D array (e.g., `uold`, `f`, `unew`) in a single `ksection_exchange_dp` call:

Subroutine	Description
<code>make_virtual_fine_dp_bulk</code>	Forward bulk exchange
<code>make_virtual_fine_dp_bulk_ksec</code>	Forward bulk (ksection impl.)
<code>make_virtual_reverse_dp_bulk</code>	Reverse bulk exchange
<code>make_virtual_reverse_dp_bulk_ksec</code>	Reverse bulk (ksection impl.)

Buffer layout for `ncols` variables:

$$\text{sendbuf}((v-1) \cdot 2^3 + j, \text{idx}) = \text{xx}(\text{icell}, v) \quad v = 1 \dots \text{ncols}, j = 1 \dots 8$$

plus 2 metadata words (sender ID, index). This reduces MPI exchanges from N_{var} per level to 1 per array.

2.2 build_comm via K-Section

The `build_comm` subroutine's `MPI_ALLTOALL` + `MPI_ISEND`/`IRecv` pattern was also replaced with `ksection_exchange_dp`.

2.3 MPI_ALLTOALL Replacements

Additional `MPI_ALLTOALL` calls in the following files were replaced with k-section exchange:

- `particle_tree.kjhan.f90`
- `init_part.f90`
- `multigrid_fine_commons.f90` (in `build_parent_comms_mg`)

2.4 Pre-Allocated Buffer Pool

Per-level small arrays (child count, peer list, MPI requests) were converted to save variables to eliminate ~ 100 allocations/deallocations per call. The `peer_recv` buffer uses grow-only capacity, and the first dimension must exactly match `nprops` for MPI stride correctness.

3

Multigrid Poisson K-Section Communication

3.1 Motivation

The multigrid Poisson solver (`poisson-mg`) accounts for 29–41% of total runtime. The original MPI communication used `MPI_ISEND`/`IRECV` with all-to-all patterns across all CPUs.

3.2 Implementation

Four k-section variants were added to `patch/cuda/multigrid_fine_commons.f90`:

Subroutine	Direction	Data Type
<code>make_virtual_mg_dp_ksec</code>	Forward	<code>real(dp)</code>
<code>make_virtual_mg_int_ksec</code>	Forward	<code>integer</code>
<code>make_reverse_mg_dp_ksec</code>	Reverse (+= accumulate)	<code>real(dp)</code>
<code>make_reverse_mg_int_ksec</code>	Reverse (+= accumulate)	<code>integer</code>

3.2.1 Key Differences from AMR Exchange

The MG communication uses different data structures from the standard AMR exchange:

Aspect	AMR	Multigrid
Active grids	<code>active(ilevel)</code>	<code>active_mg(myid,ilevel)</code>
Reception	<code>reception(icpu,ilevel)</code>	<code>active_mg(icpu,ilevel)</code>
Emission	<code>emission(icpu,ilevel)</code>	<code>emission_mg(icpu,ilevel)</code>
Data arrays	<code>xx(igrid+iskip)</code>	<code>active_mg%u(icell,ivar)</code>
Indexing	Global grid index	Local offset in <code>active_mg</code>

3.2.2 Forward Exchange

1. Pack: for each `emission_mg(icpu)%igrid(i)`, gather `two_tondim` values from `active_mg(myid)%u` + metadata (`sender_id, index`)
2. Exchange via `ksection_exchange_dp`
3. Scatter: use metadata to write into `active_mg(sender)%u(ridx + step, ivar)`

3.2.3 Reverse Exchange (Accumulation)

1. Pack: for each remote `active_mg(icpu)%u(i + step, ivar) + metadata`
2. Exchange via `ksection_exchange_dp`
3. Accumulate: `active_mg(myid)%u(emission_mg(sender)%igrid(ridx) + step, ivar) += recvbuf`

4

Morton Key Octree

4.1 Overview

The `nbor` array (6 neighbor pointers per grid) was replaced with a Morton key hash table for $O(1)$ neighbor lookup. This saves $6 \times 8 \times N_{\text{gridmax}}$ bytes of memory.

4.1.1 Modified Files

- `patch/oct_tree/morton_keys.f90` — Morton key computation
- `patch/oct_tree/morton_hash.f90` — Hash table and helper functions
- `patch/oct_tree/morton_init.f90` — Initialization and verification
- `patch/oct_tree/refine_utils.f90` — Hash table maintenance
- `patch/oct_tree/nbors_utils.kjhan.f90` — Neighbor lookup functions

4.2 Morton Key

A 64-bit Morton key is computed by interleaving the 3D integer coordinates (21 bits per dimension):

$$\text{key} = \text{interleave}(\lfloor x_g \cdot 2^{l-1} \rfloor, \lfloor y_g \cdot 2^{l-1} \rfloor, \lfloor z_g \cdot 2^{l-1} \rfloor)$$

4.3 Hash Table

A per-level open-addressing hash table with linear probing and power-of-2 capacity maps Morton keys to grid indices. The table is maintained in `make_grid_coarse/fine` and `kill_grid`, with a full rebuild after each time step.

4.4 Neighbor Lookup

Two helper functions in the `morton_hash` module:

- `morton_nbor_grid(igrid, ilevel, j)` — returns `son(nbor(igrid,j))` equivalent
 - `morton_nbor_cell(igrid, ilevel, j)` — returns `nbor(igrid,j)` equivalent
- Direction convention: $j = 1:-x, 2:+x, 3:-y, 4:+y, 5:-z, 6:+z$.

4.5 nbor Array Removal (Phase 4)

The `nbor` array is allocated as `allocate(nbor(1:1,1:1))` (minimum size to avoid compilation errors). All code paths use Morton lookup exclusively.

5

Memory-Based Load Balancing

5.1 Motivation

Standard RAMSES load balancing distributes cells evenly across CPUs, but cells with many particles consume significantly more memory. Memory-based balancing weights each cell by its memory footprint.

5.2 Cost Function

$$\text{cell_cost} = \frac{\text{mem_weight_grid}}{\text{twotondim}} + \text{numbp}(\text{igrid}) \times \frac{\text{mem_weight_part}}{\text{twotondim}}$$

where:

- `mem_weight_grid` = 270 (default) — memory per grid in dp-equivalents
- `mem_weight_part` = 12 (default) — memory per particle in dp-equivalents

5.3 Implementation Details

- All histogram variables use 64-bit integers (`integer(i8b)`) with `MPI_INTEGER8`
- `numbp` is synchronized for virtual/reception grids before cost computation, then restored afterwards
- The `numbp` restore uses a save/restore pattern to avoid breaking the particle tree

5.4 Parameters

Controlled by three namelist parameters in `&RUN_PARAMS`:

- `memory_balance = .true.` — enable memory-based balancing
- `mem_weight_grid = 270` — grid memory weight
- `mem_weight_part = 12` — particle memory weight

6

Memory Savings: Large Array Optimization

6.1 Overview

Several large arrays were eliminated or converted to on-demand allocation to reduce steady-state memory usage by \sim 960 MB (for `ngridmax=5M`).

Array	Strategy	Savings
<code>hilbert_key</code>	<code>allocate(1:1)</code> for ksection	\sim 640 MB
<code>bisec_ind_cell + cell_level</code>	On-demand alloc/dealloc	\sim 320 MB
<code>defrag_map</code>	Local scratch during defrag	minor
<code>nbor</code>	<code>allocate(1:1, 1:1)</code> (Morton)	\sim 240 MB

7

IC Reading with Stream Access

7.1 Motivation

Sequential Fortran I/O requires reading all preceding planes to reach a target plane, which is $O(n^2)$ for large files. Stream access enables direct byte-offset seeks.

7.2 Implementation

Fortran 2003 ACCESS='STREAM' is used with computed byte offsets:

```
hdr_bytes = 52 + (i3-1)*plane_bytes + 5
plane_bytes = n1*n2*4 + 8 ! data + 2 record markers
```

Applied to hydro IC (deltab, velocity, temperature), particle velocity and position files. Only for multiple=.false. mode.

7.2.1 Modified Files

- patch/Horizon5-master-2/init_flow_fine.f90
- init_part.f90

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Load Balance Profiling and Tuning

8.1 Internal Timing

Detailed timing breakdown was added to `load_balance` in `patch/cuda/load_balance.kjhan.f90`:

Section	Description	Typical (s/step)
<code>numbp_sync</code>	MPI sync of <code>numbp</code> for virtual grids	0.8–1.0
<code>cmp_new_cpu_map</code>	Build ksection + compute new map	0.4–0.6
<code>expand_pass</code>	<code>build_comm</code> + <code>make_virtual</code> loop	0.8–1.5
<code>grid_migration</code>	Linked-list reconnection	< 0.01
<code>allreduce+cpumap_update</code>	<code>MPI_ALLREDUCE</code> × 4 + <code>cpu_map</code>	2.3–3.3
<code>shrink_pass</code>	<code>flag_fine</code> + <code>build_comm</code> loop	0.4–1.0

8.2 nremap Tuning

The `nremap` parameter controls load balancing frequency (every N coarse steps). Testing with 200M particles on 12 ranks showed:

nremap	Total (s)	Loadbal (s)	Speedup	Note
1	303.8	64.4 (21.2%)	—	Baseline
3	269.9	24.7 (9.1%)	1.13×	
5	249.8	15.7 (6.3%)	1.22×	Optimal
10	258.6	11.6 (4.5%)	1.17×	Imbalance grows

Default Setting

`nremap=5` is set as the default. All four configurations produce **bit-identical** results: `econs=3.77E-03, epot=-1.88E-06, ekin=1.23E-06` at step 10.

8.3 Min/Max Memory Reporting

The `writemem_minmax` subroutine prints per-step min/max memory usage across all MPI ranks.



Namelist Reference

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RUN_PARAMS

Runtime control parameters.

Parameter	Type	Default	Description
cosmo	logical	.false.	Enable cosmological simulation
pic	logical	.false.	Enable Particle-In-Cell
poisson	logical	.false.	Enable Poisson gravity solver
hydro	logical	.false.	Enable hydrodynamics
rt	logical	.false.	Enable radiative transfer
sink	logical	.false.	Enable sink particles
verbose	logical	.false.	Verbose output
debug	logical	.false.	Debug mode
nrestart	integer	0	Restart file number (0 = new run)
nstepmax	integer	1000000	Maximum number of coarse steps
ncontrol	integer	1	Frequency of control variable output
nsubcycle	integer[]	2	Subcycling factor per level
nremap	integer	5	Load balancing frequency (0=never)
ordering	char	hilbert	Domain decomposition: hilbert, bisection, ksection
static	logical	.false.	Static (no refinement) mode
overload	integer	1	MPI overload factor
cost_weighting	logical	.true.	CPU time-based cost weighting
<i>Memory-based load balancing (new)</i>			
memory_balance	logical	.false.	Enable memory-weighted balancing
mem_weight_grid	integer	270	Memory per grid (dp-equivalents)
mem_weight_part	integer	12	Memory per particle (dp-equivalents)

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AMR_PARAMS

Adaptive Mesh Refinement grid parameters.

Parameter	Type	Default	Description
levelmin	integer	1	Minimum (uniform) refinement level
levelmax	integer	1	Maximum refinement level
ngridmax	integer8	0	Max grids per CPU (0 = auto)
ngridtot	integer8	0	Total grids for auto-computation
npartmax	integer	0	Max particles per CPU (0 = auto)
nparttot	integer	0	Total particles for auto-computation
nexpand	integer[]	1	Mesh expansion layers per level
boxlen	real(dp)	1.0	Box side length in code units



OUTPUT_PARAMS

Output control parameters.

Parameter	Type	Default	Description
noutput	integer	1	Number of scheduled outputs
foutput	integer	1000000	Output every N steps
fbackup	integer	1000000	Backup every N steps
aout	real[]	1.1	Output expansion factors (cosmo)
tout	real[]	0.0	Output times (non-cosmo)
output_mode	integer	0	Hi-res output mode
gadget_output	logical	.false.	Write Gadget-format snapshots
walltime_hrs	real(dp)	-1	Job walltime (hours, < 0 = ignore)
minutes_dump	real(dp)	1.0	Dump this many minutes before walltime

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INIT_PARAMS

Initial conditions parameters.

Parameter	Type	Default	Description
filetype	char(20)	ascii	IC file format: ascii, grafic, gadget
initfile	char[]	' '	IC file path per level
multiple	logical	.false.	Multiple IC files per rank
nregion	integer	0	Number of IC regions

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REFINE_PARAMS

Refinement criteria parameters.

Parameter	Type	Default	Description
m_refine	real[]	-1	Lagrangian mass threshold per level
ivar_refine	integer	-1	Variable index for gradient refinement
var_cut_refine	real(dp)	-1	Variable threshold
mass_cut_refine	real(dp)	-1	Particle mass threshold
interpol_var	integer	0	Interpolation variable (0=conservative, 1=primitive)
interpol_type	integer	1	Interpolation type (0=MinMod, 1=MonCen)
sink_refine	logical	.false.	Fully refine around sinks
jeans_ncells	real(dp)	-1	Jeans length in cells (> 0 enables polytropic EOS)

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HYDRO_PARAMS

Hydrodynamics solver parameters.

Parameter	Type	Default	Description
gamma	real(dp)	$\frac{5}{3}$	Adiabatic index γ
courant_factor	real(dp)	0.8	Courant–Friedrichs–Lowy number
scheme	char(20)	muscl	Hydro scheme (muscl)
slope_type	integer	1	Slope limiter (1=MinMod, 2=MonCen, 3=unlimited)
pressure_fix	logical	.false.	Pressure floor for strong shocks
beta_fix	real(dp)	0.0	Pressure fix strength
isothermal	logical	.false.	Isothermal mode

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POISSON_PARAMS

Gravity and Poisson solver parameters.

Parameter	Type	Default	Description
epsilon	real(dp)	10^{-4}	Multigrid convergence criterion
gravity_type	integer	0	Gravity type (0=self-gravity, > 0=analytic)
cg_levelmin	integer	999	Min level for CG solver fallback
cic_levelmax	integer	0	Max level for CIC particle interpolation

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PHYSICS_PARAMS

Subgrid physics parameters (star formation, feedback, cooling).

Parameter	Type	Default	Description
cooling	logical	.false.	Enable radiative cooling
metal	logical	.false.	Enable metal tracking
haardt_madau	logical	.false.	UV background
z_reion	real(dp)	8.5	Reionization redshift
<i>Star formation</i>			
n_star	real(dp)	0.1	SF density threshold (H/cc)
t_star	real(dp)	0.0	SF timescale (Gyr)
eps_star	real(dp)	0.0	SF efficiency
T2_star	real(dp)	0.0	ISM polytropic temperature
g_star	real(dp)	1.6	ISM polytropic index
sf_birth_properties	logical	.true.	Output stellar birth properties
<i>Cosmology (read from IC header or namelist)</i>			
omega_b	real(dp)	0.0	Baryon density Ω_b
omega_m	real(dp)	1.0	Matter density Ω_m
omega_l	real(dp)	0.0	Dark energy Ω_Λ
h0	real(dp)	1.0	Hubble constant H_0 (km/s/Mpc)
<i>Feedback</i>			
f_ek	real(dp)	1.0	SN kinetic energy fraction
rbubble	real(dp)	0.0	SN superbubble radius (pc)
yieldtable- filename	char	—	Yield table file path

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Example Namelist

17.1 Cosmological Simulation with Memory Balancing

`cosmo_ksection_membal.nml`

```
&RUN_PARAMS
cosmo=.true.
pic=.true.
poisson=.true.
hydro=.true.
nrestart=0
nremap=5
nsubcycle=1,1,2
ncontrol=1
nstepmax=10
ordering='ksection'
memory_balance=.true.
/

&OUTPUT_PARAMS
noutput=1
aout=1.0
/

&INIT_PARAMS
filetype='grafic'
initfile(1)='/path/to/ics/level_008'
/

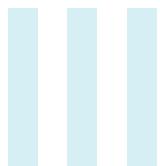
&AMR_PARAMS
levelmin=8
levelmax=10
nexpand=1
ngridtot=40000000
nparttot=200000000
/

&REFINE_PARAMS
m_refine=3*8.,
ivar_refine=0
interpol_var=1
interpol_type=0
/
```

```
&HYDRO_PARAMS
gamma=1.6666667
courant_factor=0.8
scheme='muscl'
slope_type=1
/

&POISSON_PARAMS
/

&PHYSICS_PARAMS
sf_birth_properties=.false.
yieldtablefilename='yield_table.asc'
/
```



Build and Testing

18 Build Instructions

18.1 Prerequisites

- Intel Fortran Compiler (`ifx`) with MPI support (`mpiifx`)
- OpenMP support (`-qopenmp`)

18.2 Build

Build Commands

```
cd bin  
make clean  
make
```

The binary is produced as `bin/ramses_final3d`.

18.3 Compile-Time Options

Key preprocessor flags set in the Makefile:

Flag	Meaning
<code>-DNDIM=3</code>	Three-dimensional simulation
<code>-DNVECTOR=32</code>	Vector length for grid sweeps
<code>-DLONGINT</code>	64-bit integer grid indices
<code>-DQUADHILBERT</code>	Quad-precision Hilbert keys
<code>-DNVAR=11</code>	Number of hydro variables
<code>-DNPRE=8</code>	Passive scalar variables

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Verification Tests

19.1 Test Configuration

Setting	Value
IC	MUSIC level_008 (GRAFIC2 format)
MPI ranks	12
Levels	8–10
Steps	10
Ordering	ksection

19.2 Reference Values (nremap=5)

Test	nparttot	econs	epot	ekin	mcons
membal	200M	3.77E-03	-1.88E-06	1.23E-06	-1.84E-16
nomembal	80M	3.77E-03	-1.88E-06	1.23E-06	-1.84E-16

19.3 Running Tests

Membal Test

```
cd test_ksection/run_cosmo_membal
cp ../../bin/ramses_final3d .
mpirun -np 12 ./ramses_final3d \
    ./cosmo_ksection_membal.nml
```

Verify that at step 10: econs=3.77E-03, epot=-1.88E-06, ekin=1.23E-06.



Modified Files Summary

File	Modifications
<i>patch/cuda/</i>	
amr_parameters.jaehyun.f90	Memory balance params, nremap=5 default
amr_commons.kjhan.f90	grid_level array, communicator type
read_params.jaehyun.f90	Read new namelist params
bisection.f90	nc_in parameter, 64-bit histograms
ksection.f90	K-section tree + exchange routines
load_balance.kjhan.f90	numbp sync, bulk exchange, internal timing
virtual_boundaries.kjhan.f90	Ksec ghost exchange + bulk + build_comm
multigrid_fine_commons.f90	MG ksection communication
init_amr.f90	Memory savings, Morton init
update_time.f90	Memory reporting
adaptive_loop.jaehyun.f90	writemem_minmax, Morton rebuild, bulk exchange
<i>patch/oct_tree/</i>	
morton_keys.f90	Morton key computation
morton_hash.f90	Hash table + neighbor helpers
morton_init.f90	Build and verify
refine_utils.f90	Hash maintenance in grid ops
nbors_utils.kjhan.f90	Morton-based neighbor lookup
<i>patch/Horizon5-master-2/</i>	
init_flow_fine.f90	Stream access IC reading
init_part.f90	Stream access particle IC
particle_tree.kjhan.f90	$\text{MPI_ALLTOALL} \rightarrow \text{ksection}$
amr_step.jaehyun.f90	Bulk virtual exchange