UE TSM - Les Séries de Volterra TD - Partie 2

KANG Jiale

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Problem 1. Euler implicite is defined by

$$s = \frac{1 - z^{-1}}{T}$$

Question 7. Define $\nu = T\omega$, use Euler implicite to transform $F_1(s)$ to $F_1(z)$. Show the recurrence equation of input u_n and output y_n .

Solution. Recall that $F_1(s) = \frac{1}{1+s/\omega}$, in \mathbb{Z} -domain, $F_1(z) = \frac{\nu}{\nu+1-z^{-1}}$.

The relation between input and output is $Y(z) = F_1(z)U(z)$. Simplify this equation, we obtain

$$Y(z)(\nu + 1 - z^{-1}) = \nu U(z) \tag{1}$$

Transform equation (1) to time domain,

$$y_n = \frac{\nu}{\nu + 1} u_n + \frac{1}{\nu + 1} y_{n-1} \tag{2}$$

Problem 2. Program with FAUST.

Question 8. Implement F_1 with FAUST.

Solution. Equation (2) is a recurrent expression, we denote $a = \frac{\nu}{\nu+1}$, $b = \frac{1}{\nu+1}$. Code for the implementation is shown as Listing 1.

Listing 1: Code for the implementation of F_1

```
import("stdfaust.lib");
process = F1(1000);

F1(fc) = *(a) : + ~ *(b) with {
    nu = 2 * ma.PI * fc / ma.SR;
    a = nu / (nu + 1);
    b = 1 / (nu + 1);
};
```

Question 9. Implement a 1-layer 3-order none linear system.

Solution. Recall that block diagram of 3-order none linear system is shown as Figure 1.

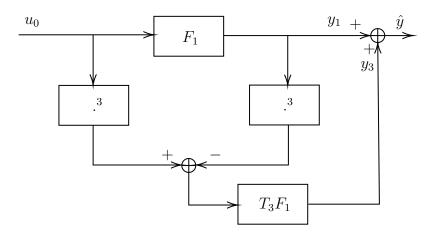


Figure 1: Block Diagram of 3-order None Linear System

According to this diagram, we could implement this system with help of Figure 2, the code of implementation for this system is shown as Listing 2.

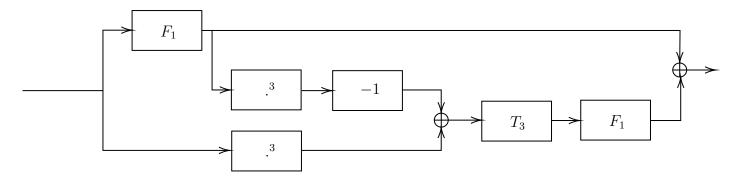


Figure 2: Diagram of Implementation with FAUST

Listing 2: Code for the implementation of 3-order None Linear System

```
import("stdfaust.lib");

process = E(1000);

F1(fc) = *(a) : + ~ *(b) with {
    nu = 2 * ma.PI * fc / ma.SR;
    a = nu / (nu + 1);
    b = 1 / (nu + 1);
};
```

Question 10. Implement a 4-layer 3-order none linear system.

Solution. Recall that the kernel of a 4-layer 3-order none linear system could be expressed as

$$H_1(s_1) = F_1(s_1)^4$$

$$H_2(s_1, s_2) = 0$$

$$H_3(s_1, s_2, s_3) = \sum_{k=0}^{3} F_1(s_1)^k F_1(s_2)^k F_1(s_3)^k F_3(s_1, s_2, s_3) F_1(s_1 + s_2 + s_3)^{3-k}$$

Therefore, block diagram of 4-layer 3-order none linear system is shown as Figure 3. Obviously, it parallels 4 \mathcal{M} and 1 \mathcal{S} with input $\{u_0, 0\}$.

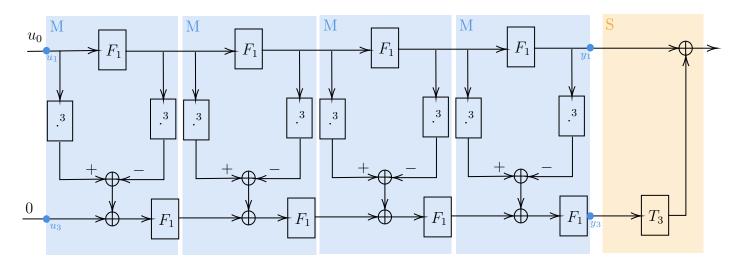


Figure 3: Block Diagram of 4-layer 3-order None Linear System

The code of implementation for this system is shown as Listing 3.

Listing 3: Code for the implementation of 4-layer 3-order None Linear System

```
import("stdfaust.lib");
```

```
process = fmoog(1000);

T3 = -1/3;
fmoog(fc) = _,0 : M : M : M : S with {
    F1 = *(a) : + ~ *(b) with {
        nu = 2 * ma.PI * fc / ma.SR;
        a = nu / (nu + 1);
        b = 1 / (nu + 1);
    };

M(u1, u3) = F1(u1), F1(u3 + u1^3 - F1(u1)^3);

S(y1, y3) = y1 + T3 * y3;
};
```

Question 11. At what amplitude does distortion begin to be perceptible? To what order the sound seems to be real?

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Solution. When we augment amplitude of the sound, the distortion begins to happen. We could perceive this distortion until its amplitude > 1.5. When its amplitude < 2, the sound seems to be real, because higher the amplitude could be, more non-harmonic frequencies will appear.

Question 12. When changing ω , is the stability of this filter still guaranteed?

Solution. As the cutoff frequency ω increases, the stability of the system can no longer be guaranteed. Because high frequencies non-harmonic components appear when we increase ω . This indicates that the system has entered the nonlinear region, resulting in non-harmonic distortion, and it may generate self-excited oscillations under the high cut off frequency. \square

A Simulation code in FAUST

```
import("stdfaust.lib");

process = source(freq, delta) : drive(fmoog(fc));

T3 = -1/3 * checkbox("NL");

fmoog(fc) = _,0 : M : M : M : S with {
    F1 = *(a) : + ~ *(b) with {
        nu = 2 * ma.PI * fc / ma.SR;
        a = nu / (nu + 1);
        b = 1 / (nu + 1);
    };

M(u1, u3) = F1(u1), F1(u3 + u1^3 - F1(u1)^3);
```

```
S(y1, y3) = y1 + T3 * y3;
};

drive(C) = *(g) : C : /(g) with {
    g = vslider("drive[style:knob]", 1, 0.1, 20, 0.1);
};

source(f1, df) = os.square(f1) + os.square(f1 + df) : *(0.5);
freq = vslider("freq[style:knob][scale:log][unit:Hz]", 330, 20, 5000, 1);
delta = vslider("delta[style:knob][unit:Hz]", 0.1, 0.05, 2, 0.05);
fc = vslider("fc[style:knob][scale:log][unit:Hz]", 1000, 20, 5000, 1);
```

B Auto Documentation

fmoog

November 15, 2024

compile options	-lang cpp -ct 1 -es 1 -mcd 16 -mdd 1024 -mdy 33 -single -ftz 0
filename	fmoog.dsp
${ m maths.lib/author}$	GRAME
${ m maths.lib/copyright}$	GRAME
maths.lib/license	LGPL with exception
maths.lib/name	Faust Math Library
maths.lib/version	2.8.0
name	fmoog
oscillators.lib/lf sawpos:author	Bart Brouns, revised by Stéphane Letz
oscillators.lib/lf sawpos:licence	STK-4.3
${ m oscillators.lib/name}$	Faust Oscillator Library
${ m oscillators.lib/sawN:} { m author}$	Julius O. Smith III
oscillators.lib/sawN:license	STK-4.3
${ m oscillators.lib/version}$	1.5.1
${ m platform.lib/name}$	Generic Platform Library
platform.lib/version	1.3.0

This document provides a mathematical description of the Faust program text stored in the fmoog.dsp file. See the notice in Section 3 (page 4) for details.

1 Mathematical definition of process

The *fmoog* program evaluates the signal transformer denoted by **process**, which is mathematically defined as follows:

1. Output signal y such that

$$y(t) = p_{28}(t) \cdot (r_2(t) - p_{27}(t) \cdot r_1(t))$$

- 2. Input signal (none)
- 3. User-interface input signals u_{si} for $i \in [1, 4]$ and u_{c1} such that

4. Intermediate signals p_i for $i \in [1, 28]$, s_i for $i \in [1, 12]$, r_i for $i \in [1, 11]$ and q_i for $i \in [1, 2]$ such that

$$p_{1}(t) = \max(u_{s2}(t) + u_{s1}(t), 23.4489496824621)$$

$$p_{2}(t) = \max(20, |p_{1}(t)|)$$

$$p_{3}(t) = k_{2} \cdot p_{2}(t)$$

$$p_{4}(t) = \left(\frac{k_{3}}{p_{2}(t)}\right)$$

$$p_{5}(t) = \max\left(0, \min\left(2047, \frac{k_{4}}{p_{1}(t)}\right)\right)$$

$$p_{6}(t) = \inf(p_{5}(t))$$

$$p_{7}(t) = |p_{5}(t)|$$

$$p_{8}(t) = (p_{7}(t) + (1 - p_{5}(t)))$$

$$p_{9}(t) = \max(u_{s2}(t), 23.4489496824621)$$

$$p_{10}(t) = \max(20, |p_{9}(t)|)$$

$$p_{11}(t) = k_{2} \cdot p_{10}(t)$$

$$p_{12}(t) = \left(\frac{k_{3}}{p_{10}(t)}\right)$$

$$p_{13}(t) = \max\left(0, \min\left(2047, \frac{k_{4}}{p_{9}(t)}\right)\right)$$

$$p_{14}(t) = \inf(p_{13}(t))$$

$$p_{15}(t) = p_{14}(t) \oplus 1$$

$$p_{16}(t) = |p_{13}(t)|$$

$$p_{17}(t) = (p_{13}(t) - p_{16}(t))$$

$$p_{18}(t) = (p_{16}(t) + (1 - p_{13}(t)))$$

$$p_{19}(t) = p_{6}(t) \oplus 1$$

$$p_{20}(t) = (p_{5}(t) - p_{7}(t))$$

$$p_{21}(t) = \left(\frac{1}{p_{10}(t)}\right)$$

 $p_{23}(t) = k_5 \cdot u_{s4}(t) \cdot u_{s3}(t)$

$$q_1(t) = \left\{ \begin{array}{ll} p_3(t) + r_6(t-1) & \text{if } s_1(t) = 0 \\ 0 & \text{if } s_1(t) = 1 \end{array} \right. \\ q_2(t) = \left\{ \begin{array}{ll} p_{11}(t) + r_{10}(t-1) & \text{if } s_1(t) = 0 \\ 0 & \text{if } s_1(t) = 1 \end{array} \right.$$

5. Constants k_i for $i \in [1, 6]$ such that

$$k_{1} = \min (192000, \max (1, f_{S}))$$

$$k_{2} = \left(\frac{1}{k_{1}}\right)$$

$$k_{3} = 0.25 \cdot k_{1}$$

$$k_{4} = 0.5 \cdot k_{1}$$

$$k_{5} = \left(\frac{\pi}{k_{1}}\right)$$

$$k_{6} = \left(\frac{2 \cdot \pi}{k_{1}}\right)$$

2 Block diagram of process

The block diagram of process is shown on Figure 1 (page 4).

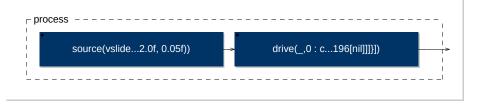


Figure 1: Block diagram of process

3 Notice

- This document was generated using Faust version 2.75.16 on November 15, 2024.
- The value of a Faust program is the result of applying the signal transformer denoted by the expression to which the **process** identifier is bound to input signals, running at the f_S sampling frequency.
- Faust (Functional Audio Stream) is a functional programming language designed for synchronous real-time signal processing and synthesis applications. A Faust program is a set of bindings of identifiers to expressions

that denote signal transformers. A signal s in S is a function mapping¹ times $t \in \mathbb{Z}$ to values $s(t) \in \mathbb{R}$, while a signal transformer is a function from S^n to S^m , where $n, m \in \mathbb{N}$. See the Faust manual for additional information (http://faust.grame.fr).

- Every mathematical formula derived from a Faust expression is assumed, in this document, to having been normalized (in an implementation-dependent manner) by the Faust compiler.
- A block diagram is a graphical representation of the Faust binding of an identifier I to an expression E; each graph is put in a box labeled by I.
 Subexpressions of E are recursively displayed as long as the whole picture fits in one page.
- $\forall x \in \mathbb{R}$,

$$\operatorname{int}(x) = \left\{ \begin{array}{ll} \lfloor x \rfloor & \text{if } x > 0 \\ \lceil x \rceil & \text{if } x < 0 \\ 0 & \text{if } x = 0 \end{array} \right..$$

• This document uses the following integer operations:

operation	name	semantics
$i \oplus j$	integer addition	normalize $(i+j)$, in \mathbb{Z}
$i\ominus j$	integer substraction	normalize $(i-j)$, in \mathbb{Z}

Integer operations in Faust are inspired by the semantics of operations on the n-bit two's complement representation of integer numbers; they are internal composition laws on the subset $[-2^{n-1}, 2^{n-1}-1]$ of \mathbb{Z} , with n=32. For any integer binary operation \times on \mathbb{Z} , the \otimes operation is defined as: $i \otimes j = \text{normalize}(i \times j)$, with

$$\operatorname{normalize}(i) = i - N \cdot \operatorname{sign}(i) \cdot \left\lfloor \frac{|i| + N/2 + (\operatorname{sign}(i) - 1)/2}{N} \right\rfloor,$$

where $N = 2^n$ and sign(i) = 0 if i = 0 and i/|i| otherwise. Unary integer operations are defined likewise.

- The fmoog-mdoc/ directory may also include the following subdirectories:
 - cpp/ for Faust compiled code;
 - pdf/ which contains this document;
 - src/ for all Faust sources used (even libraries);
 - svg/ for block diagrams, encoded using the Scalable Vector Graphics format (http://www.w3.org/Graphics/SVG/);
 - tex/ for the LATEX source of this document.

¹Faust assumes that $\forall s \in S, \forall t \in \mathbb{Z}, s(t) = 0$ when t < 0.

4 Faust code listings

This section provides the listings of the Faust code used to generate this document, including dependencies.

Listing 1: fmoog.dsp

```
declare filename "fmoog.dsp";
    declare name "fmoog"
2
    import("stdfaust.lib");
    process = source(freq, delta) : drive(fmoog(fc));
    T3 = -1/3 * checkbox("NL");
    fmoog(fc) = _,0 : M : M : M : M : S with { F1 = *(a) : + \tilde{\ } *(b) with {
             nu = 2 * ma.PI * fc / ma.SR;
             a = nu / (nu + 1);
             b = 1 / (nu + 1);
         M(u1, u3) = F1(u1), F1(u3 + u1^3 - F1(u1)^3);
         S(y1, y3) = y1 + T3 * y3;
20
    drive(C) = *(g) : C : /(g) with {
        g = vslider("drive[style:knob]", 1, 0.1, 20, 0.1);
22
24
    source(f1, df) = os.square(f1) + os.square(f1 + df) : *(0.5);
freq = vslider("freq[style:knob][scale:log][unit:Hz]", 330, 20, 5000, 1);
25
    delta = vslider("delta[style:knob][unit:Hz]", 0.1, 0.05, 2, 0.05);
    fc = vslider("fc[style:knob][scale:log][unit:Hz]", 1000, 20, 5000, 1);
```

Listing 2: stdfaust.lib

```
// The purpose of this library is to give access to all the Faust standard libraries
// through a series of environments.
aa = library("aanl.lib");
sf = library("all.lib");
an = library("analyzers.lib");
ba = library("basics.lib");
co = library("compressors.lib");
de = library("delays.lib");
dm = library("demos.lib");
dx = library("dx7.lib");
en = library("envelopes.lib");
fd = library("fds.lib");
fi = library("filters.lib");
ho = library("hoa.lib");
it = library("interpolators.lib");
ma = library("maths.lib");
mi = library("mi.lib");
ef = library("misceffects.lib");
os = library("oscillators.lib");
```

```
no = library("noises.lib");
23
   pf = library("phaflangers.lib");
    pl = library("platform.lib");
25
    pm = library("physmodels.lib");
    qu = library("quantizers.lib");
27
    rm = library("reducemaps.lib");
28
    re = library("reverbs.lib");
29
    ro = library("routes.lib");
30
    sp = library("spats.lib");
31
    si = library("signals.lib");
32
    so = library("soundfiles.lib");
33
    sy = library("synths.lib");
34
    ve = library("vaeffects.lib");
35
    vl = library("version.lib");
36
    wa = library("webaudio.lib");
    wd = library("wdmodels.lib");
```

Listing 3: oscillators.lib

```
// This library contains a collection of sound generators. Its official prefix is 'os'.
   // The oscillators library is organized into 9 sections:
   // * [Wave-Table-Based Oscillators] (#wave-table-based-oscillators)
   // * [Low Frequency Oscillators] (#low-frequency-oscillators)
   // * [Low Frequency Sawtooths] (#low-frequency-sawtooths)
   // * [Alias-Suppressed Sawtooth] (#alias-suppressed-sawtooth)
   // * [Alias-Suppressed Pulse, Square, and Impulse Trains] (#alias-suppressed-pulse-square-and-
        impulse-trains)
   // * [Filter-Based Oscillators] (#filter-based-oscillators)
11
   // * [Waveguide-Resonator-Based Oscillators] (#waveguide-resonator-based-oscillators)
12
   // * [Casio CZ Oscillators] (#casio-cz-oscillators)
13
   // * [PolyBLEP-Based Oscillators] (#polyblep-based-oscillators)
14
15
   // #### References
16
   // * <https://github.com/grame-cncm/faustlibraries/blob/master/oscillators.lib>
17
   18
19
   20
    *******************************
21
   FAUST library file, GRAME section
22
23
    Except where noted otherwise, Copyright (C) 2003-2017 by GRAME,
24
   Centre National de Creation Musicale.
25
26
   GRAME LICENSE
27
28
    This program is free software; you can redistribute it and/or modify
29
30
    it under the terms of the GNU Lesser General Public License as
   published by the Free Software Foundation; either version 2.1 of the
31
32
   License, or (at your option) any later version.
33
   This program is distributed in the hope that it will be useful,
35
   but WITHOUT ANY WARRANTY; without even the implied warranty of
   MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the
36
37
   GNU Lesser General Public License for more details.
    You should have received a copy of the GNU Lesser General Public
    License along with the {\it GNU~C~Library;} if not, write to the Free
41
   Software Foundation, Inc., 59 Temple Place, Suite 330, Boston, MA
42
   02111-1307 USA.
   EXCEPTION TO THE LGPL LICENSE : As a special exception, you may create a
```

```
larger FAUST program which directly or indirectly imports this library
45
    file and still distribute the compiled code generated by the FAUST
    compiler, or a modified version of this compiled code, under your own
47
    copyright and license. This EXCEPTION TO THE LGPL LICENSE explicitly
48
    grants you the right to freely choose the license for the resulting
49
    compiled code. In particular the resulting compiled code has no obligation
50
    to be LGPL or GPL. For example you are free to choose a commercial or
51
    closed source license or any other license if you decide so.
52
    53
54
55
    ma = library("maths.lib");
56
    ba = library("basics.lib");
57
    fi = library("filters.lib");
58
    si = library("signals.lib");
59
60
    declare name "Faust Oscillator Library";
61
62
    declare version "1.5.1";
63
64
    // This library contains platform specific constants
65
    pl = library("platform.lib");
66
67
    68
    /\!/ Note that there is a numerical problem with several phasor functions built using the
69
    // 'phasor_imp'. The reason is that the incremental step is smaller than 'ma.EPSILON', which
         happens with very small frequencies,
    // so it will have no effect when summed to 1, but it will be enough to make the fractional
71
         function wrap
    /\!/ around when summed to 0. An example of this problem can be observed when running the
         following code:
73
    // 'process = os.phasor(1.0, -.001);'
74
75
76
    // The output of this program is the sequence 1, 0, 1, 0, 1... This happens because the
         negative incremental
    // step is greater than '-ma.EPSILON', which will have no effect when summed to 1, but it
77
         will be significant
    // enough to make the fractional function wrap around when summed to 0.
78
79
80
    // The incremental step can be clipped to guarantee that the phasor will
    // always run correctly for its full cycle, otherwise, for increments smaller than 'ma.
81
    // phasor would initially run but it'd eventually get stuck once the output gets big enough.
82
83
    // All functions using 'phasor_imp' are affected by this problem, but a safer
84
    // version is implemented, and can be used alternatively by setting 'SAFE=1' in the
85
         environment using
    // [explicit sustitution] (https://faustdoc.grame.fr/manual/syntax/#explicit-substitution)
86
         svntax.
87
    // For example: 'process = os[SAFE=1;].phasor(1.0, -.001); 'will use the safer implementation
88
          of 'phasor imp'.
89
90
91
    // Oscillators using tables. The table size is set by the
92
    // [pl.tablesize](https://github.com/grame-cncm/faustlibraries/blob/master/platform.lib)
93
         constant.
94
95
    // Global parameter to use the safer version of 'phasor_imp', but which
96
    // could be used in other functions as well.
97
98
99
    SAFE = 0; // 0: use the faster version, 1: use the safer version
100
    //-----'(os.)sinwaveform'-----
```

```
// Sine waveform ready to use with a 'rdtable'.
102
103
     // #### Usage
104
     11
105
     11 ...
106
     // sinwaveform(tablesize) : _
107
     11 ...
108
     //
109
     // Where:
110
111
     // * 'tablesize': the table size
112
113
     sinwaveform(tablesize) =
114
        sin(float(ba.period(tablesize)) * (2.0 * ma.PI) / float(tablesize));
115
116
117
     //-----'(os.)coswaveform'-----
118
     // Cosine waveform ready to use with a 'rdtable'.
119
120
     // #### Usage
121
122
     //
123
     // coswaveform(tablesize) : _
124
125
     //
126
     // Where:
127
128
129
     // * 'tablesize': the table size
130
131
     coswaveform(tablesize) =
132
        cos(float(ba.period(tablesize)) * (2.0 * ma.PI) / float(tablesize));
133
134
     // Possibly faster version using integer arithmetic
     phasor_env(freq, N) = environment {
135
136
137
         //---- GLOBAL PARAMS
        nbits = 31;
138
         tablesize = 1<<N;
139
        accuracy = int(nbits - N);
140
141
         mask = (1 < nbits) -1;
        inc(step) = int(tablesize * step * (1<<accuracy));</pre>
142
143
         //---- LAMBDA DSP CASE
144
        lambda(inc_op) = (inc_op : &(mask)) ~ _ : >>(accuracy) : /(tablesize);
145
146
         //---- MINIMAL CASE
147
        hsp(0,0) = lambda(+(inc(freq/ma.SR)'));
148
149
         //---- GENERAL CASE
150
        hsp(reset,phase) = lambda(select2(hard_reset,+(inc(freq/ma.SR)),inc(phase)))
151
152
        with {
            hard_reset = (1-1')|reset;
153
154
     }:
155
     declare phasor_env author "Pierre Mascarade Relano, Maxime Sirbu, Stéphane Letz";
156
157
     // Generic phasor with 'reset' and 'phase' parameters to be specialised in concrete use-cases
158
     phasor_imp(freq, reset, phase) = (select2(hard_reset, +(incr(SAFE)), phase) : ma.decimal) ~
159
     with {
160
        incr_aux = freq/ma.SR;
161
162
         // Faster but less accurate version
163
        incr(0) = incr_aux;
164
165
         // To make sure that the incremental step is greater or equal to \ensuremath{\textit{EPSILON}} or
166
        // less than or equal to -EPSILON to avoid numerical problems.
167
```

```
// A frequency of OHz can still be used to freeze the phasor.
168
         incr(1)= (freq != 0) * ba.if(freq < 0, min(-1.0 * ma.EPSILON, incr_aux), max(ma.EPSILON,
169
              incr_aux));
170
         // To correctly start at 'phase' at the first sample
171
         hard_reset = (1-1')|reset;
172
     };
173
174
     // Possibly faster version using integer arithmetic
175
     // phasor_imp(freq, reset, phase) = phasor_env(freq, 16).hsp(reset, phase);
176
177
     // Version to be used with tables
178
     phasor_table(tablesize, freq, reset, phase) = phasor_imp(freq, reset, phase) : *(float(
179
          tablesize)):
180
181
     //----'(os.)phasor'-----
182
     \ensuremath{//} A simple phasor to be used with a 'rdtable'.
183
184
     // 'phasor' is a standard Faust function.
185
     // #### Usage
186
    // ...
187
188
     // phasor(tablesize,freq) : _
189
190
     //
191
    // Where:
192
193
    //
// * 'tablesize': the table size
194
195
     // * 'freq': the frequency in {\rm Hz}
     // Note that 'tablesize' is just a multiplier for the output of a unit-amp phasor // so 'phasor(1.0, freq)' can be used to generate a phasor output in the range [0, 1[.
197
199
    phasor(tablesize, freq) = phasor_table(tablesize, freq, 0, 0);
202
     //-----'(os.)hs_phasor'-----
203
     // Hardsyncing phasor to be used with a 'rdtable'.
204
205
    // #### Usage
206
207
208
209
     // hs_phasor(tablesize,freq,reset) : _
    // "
210
211
    // Where:
212
213
     // * 'tablesize': the table size
214
    // * 'freq': the frequency in Hz
// * 'freset': a reset signal, reset phase to 0 when equal to 1
215
216
217
     declare hs_phasor author "Mike Olsen, revised by Stéphane Letz";
218
219
     hs_phasor(tablesize, freq, reset) = phasor_table(tablesize, freq, reset, 0);
220
221
222
     //----·(os.)hsp_phasor'------
223
     // Hardsyncing phasor with selectable phase to be used with a 'rdtable'.
224
225
     // #### Usage
226
227
    11 ...
228
     // hsp_phasor(tablesize,freq,reset,phase)
229
230
231
    //
     // Where:
232
233
    //
```

```
// * 'tablesize': the table size
234
    // * 'freq': the frequency in Hz
235
    // * 'reset': reset the oscillator to phase when equal to 1
236
    // * 'phase': phase between 0 and 1
237
238
    declare hsp_phasor author "Christophe Lebreton, revised by Stéphane Letz";
239
240
    hsp_phasor(tablesize, freq, reset, phase) = phasor_table(tablesize, freq, reset, phase);
241
242
243
    //-----(os.)oscsin'-----
244
    // Sine wave oscillator.
245
    // 'oscsin' is a standard Faust function.
246
247
    // #### Usage
248
249
    11 ...
250
    // oscsin(freq) : _
251
    11 ...
252
253
    //
    // Where:
254
255
    // * 'freq': the frequency in Hz
256
257
258
    {\tt oscsin(freq) = rdtable(tablesize, sinwaveform(tablesize), int(phasor(tablesize,freq)))}
    tablesize = pl.tablesize;
};
260
262
    //-----'(os.)hs_oscsin'-----
    // Sin lookup table with hardsyncing phase.
    // #### Usage
267
    // (((
    // hs_oscsin(freq,reset) : _
270
272
    // Where:
274
    // * 'freq': the frequency in Hz
275
    // * 'reset': reset the oscillator to 0 when equal to 1
276
277
    declare hs_oscsin author "Mike Olsen";
278
279
    hs_oscsin(freq,reset) = rdtable(tablesize, sinwaveform(tablesize), int(hs_phasor(tablesize,
280
         freq,reset)))
    with {
281
       tablesize = pl.tablesize;
282
283
284
285
    //-----'(os.)osccos'-----
286
    // Cosine wave oscillator.
287
288
    // #### Usage
289
290
    // "
291
    // osccos(freq) : _
292
    11 "
293
    11
294
    // Where:
295
296
    // * 'freq': the frequency in Hz
297
298
    osccos(freq) = rdtable(tablesize, coswaveform(tablesize), int(phasor(tablesize,freq)))
299
   with {
```

```
tablesize = pl.tablesize;
301
302
303
304
    //-----'(os.)hs_osccos'-----
305
    // Cos lookup table with hardsyncing phase.
306
307
    // #### Usage
308
    //
309
    // "
310
    // hs_osccos(freq,reset) : _
// '''
311
312
    11
313
    // Where:
314
315
    //
    // * 'freq': the frequency in Hz
316
    // * 'reset': reset the oscillator to 0 when equal to 1
317
318
319
    declare hs_osccos author "Stéphane Letz";
320
    hs_osccos(freq,reset) = rdtable(tablesize, coswaveform(tablesize), int(hs_phasor(tablesize,
321
        freq,reset)))
    with {
    tablesize = pl.tablesize;
};
322
323
324
325
    //-----(os.)oscp'-----
327
328
    \ensuremath{//}\ \mbox{$\mathbb{A}$} sine wave generator with controllable phase.
    // #### Usage
    // ...
332
333
    // oscp(freq,phase) : _
    // Where:
336
337
    // * 'freq': the frequency in Hz
338
    // * 'phase': the phase in radian
340
    oscp(freq,phase) = oscsin(freq) * cos(phase) + osccos(freq) * sin(phase);
341
342
343
    //-----'(os.)osci'-----
344
    // Interpolated phase sine wave oscillator.
345
346
    // #### Usage
347
    //
348
    11 ...
349
    // osci(freq) : _
350
    // ""
351
    //
352
    // Where:
353
354
    // * 'freq': the frequency in Hz
355
356
    osci(freq) = s1 + d * (s2 - s1)
357
    with {
358
       tablesize = pl.tablesize;
359
       i = int(phasor(tablesize,freq));
360
361
       d = ma.decimal(phasor(tablesize,freq));
       s1 = rdtable(tablesize+1,sinwaveform(tablesize),i);
362
       s2 = rdtable(tablesize+1,sinwaveform(tablesize),i+1);
363
364
365
366
   //-----'(os.)osc'-----
```

```
// Default sine wave oscillator (same as [oscsin](#oscsin)).
368
    // 'osc' is a standard Faust function.
369
370
    //
    // #### Usage
371
    //
372
    // "
373
    // osc(freq) : _
374
    11 "
375
    //
376
    // Where:
377
378
    // * 'freq': the frequency in Hz
379
380
    osc = oscsin:
381
382
383
    //-----'(os.)m_oscsin'-----
384
    // Sine wave oscillator based on the 'sin' mathematical function.
385
386
    // #### Usage
387
388
    //
389
390
    // m_oscsin(freq) : _
391
392
    //
393
    // Where:
394
395
    // * 'freq': the frequency in Hz
396
    m_oscsin(freq) = lf_sawpos(freq) : *(2*ma.PI) : sin;
    //-----'(os.)m_osccos'-----
400
    // Sine wave oscillator based on the 'cos' mathematical function.
401
403
    // #### Usage
404
405
    // m_osccos(freq) : _
406
407
    //
408
    // Where:
409
410
    // * 'freq': the frequency in Hz
411
412
    m_osccos(freq) = lf_sawpos(freq) : *(2*ma.PI) : cos;
413
414
415
    // end GRAME section
416
    417
418
    FAUST library file, jos section
419
420
    Except where noted otherwise, The Faust functions below in this
421
    section are Copyright (C) 2003-2022 by Julius O. Smith III <jos@ccrma.stanford.edu>
422
    ([jos](http://ccrma.stanford.edu/~jos/)), and released under the
423
    (MIT-style) [STK-4.3] (#stk-4.3-license) license.
424
425
    The MarkDown comments in this section are Copyright 2016-2017 by Romain
426
    Michon and Julius O. Smith III, and are released under the
427
    [{\tt CCA4I}] ({\tt https://creative commons.org/licenses/by/4.0/}) \ {\tt license} \ ({\tt TODO:} \ {\tt if/when} \ {\tt Romain} \ {\tt agrees})
428
429
    430
431
    //=====Low Frequency Oscillators=====
432
433
    // Low Frequency Oscillators (LFOs) have prefix 'lf_'
    // (no aliasing suppression, since it is inaudible at LF).
434
    // Use 'sawN' and its derivatives for audio oscillators with suppressed aliasing.
```

```
436
437
     //----'(os.)lf_imptrain'-----
438
    // Unit-amplitude low-frequency impulse train. // 'lf_imptrain' is a standard Faust function.
439
440
441
     // #### Usage
442
443
     11 ...
444
     // lf_imptrain(freq) : _
445
     // "
446
447
     // Where:
448
449
     // * 'freq': frequency in Hz
450
451
     lf_imptrain(freq) = lf_sawpos(freq)<:-(mem)<0; // definition below</pre>
452
453
454
455
     //----'(os.)lf_pulsetrainpos'-----
     // Unit-amplitude nonnegative LF pulse train, duty cycle between 0 and 1.
456
457
     //
458
     // #### Usage
459
    // ...
460
461
     // lf_pulsetrainpos(freq, duty) : _
462
463
464
    //
465
     // Where:
     // * 'freq': frequency in Hz
467
     // * 'duty': duty cycle between 0 and 1
468
469
     lf_pulsetrainpos(freq,duty) = float(lf_sawpos(freq) <= duty);</pre>
     //pulsetrainpos = lf_pulsetrainpos; // for backward compatibility
472
473
474
475
     //-----(os.)lf_pulsetrain'-----
     // Unit-amplitude zero-mean LF pulse train, duty cycle between 0 and 1.
476
477
     // #### Usage
478
    // ...
479
480
     // lf_pulsetrain(freq,duty) : _
481
     // ""
482
     //
483
    // Where:
484
485
     // * 'freq': frequency in Hz
486
     // * 'duty': duty cycle between 0 and 1
487
488
     lf_pulsetrain(freq,duty) = 2.0*lf_pulsetrainpos(freq,duty) - 1.0;
489
490
491
    //----'(os.)lf_squarewavepos'-----
492
     // Positive LF square wave in [0,1]
493
494
     // #### Usage
495
     //
496
     11 ...
497
     // lf_squarewavepos(freq) : _
498
     // "
499
     //
500
     // Where:
501
502
     //
503 // * 'freq': frequency in Hz
```

```
504
     lf_squarewavepos(freq) = lf_pulsetrainpos(freq,0.5);
505
     // squarewavepos = lf_squarewavepos; // for backward compatibility
506
507
508
     //-----'(os.)lf_squarewave'-----
509
     // Zero-mean unit-amplitude LF square wave.
// 'lf_squarewave' is a standard Faust function.
510
511
512
     // #### Usage
513
514
     //
515
     // lf_squarewave(freq) : _
516
     // "
517
     11
518
     // Where:
519
520
     //
     // * 'freq': frequency in Hz
521
522
     lf_squarewave(freq) = 2.0*lf_squarewavepos(freq) - 1.0;
523
     // squarewave = lf_squarewave; // for backward compatibility
524
525
526
     //----'(os.)lf_trianglepos'-----
527
     // Positive unit-amplitude LF positive triangle wave.
528
529
     // #### Usage
530
531
     // ...
532
     // lf_trianglepos(freq) : _
     // ""
535
     // Where:
536
     // * 'freq': frequency in Hz
     lf_trianglepos(freq) = 1.0-abs(saw1(freq)); // saw1 defined below
540
542
     //----'(os.)lf_triangle'-----
     // Zero-mean unit-amplitude LF triangle wave.
544
     // 'lf_triangle' is a standard Faust function.
545
546
547
     // #### Usage
     //
548
549
     // lf_triangle(freq) : _
550
551
     //
552
     // Where:
553
554
     // * 'freq': frequency in Hz
555
556
     declare lf_triangle author "Bart Brouns";
557
     declare lf_triangle licence "STK-4.3";
558
559
     lf_triangle(freq) = 2.0*lf_trianglepos(freq) - 1.0;
560
561
562
     //===== Low Frequency Sawtooths =======
563
     // Sawtooth waveform oscillators for virtual analog synthesis et al.  \\
564
     // The 'simple' versions ('lf_rawsaw', 'lf_sawpos' and 'saw1'), are mere samplings of // the ideal continuous-time ("analog") waveforms. While simple, the
565
566
     // aliasing due to sampling is quite audible. The differentiated
// polynomial waveform family ('saw2', 'sawN', and derived functions)
567
568
569
     \ensuremath{//}\xspace do some extra processing to suppress aliasing (not audible for
     // very low fundamental frequencies). According to Lehtonen et al.
570
    // (JASA 2012), the aliasing of 'saw2' should be inaudible at fundamental
```

```
| // frequencies below 2 kHz or so, for a 44.1 kHz sampling rate and 60 dB SPL |
572
     // presentation level; fundamentals 415 and below required no aliasing
573
    // suppression (i.e., 'saw1' is ok).
574
575
576
    //-----'(os.)lf_rawsaw'-----
577
    // Simple sawtooth waveform oscillator between 0 and period in samples.
578
579
    // #### Usage
580
581
582
    // lf_rawsaw(periodsamps) : _
583
    // "
584
    //
585
     // Where:
586
587
     \ensuremath{//} * 'periodsamps': number of periods per samples
588
589
590
    lf_rawsaw(periodsamps) = (_,periodsamps : fmod) ~ +(1.0);
591
592
    //-----'(os.)lf_sawpos'-----
593
    // Simple sawtooth waveform oscillator between 0 and 1.
594
595
    // #### Usage
596
597
     // lf_sawpos(freq) : _
600
    // Where:
    // * 'freq': frequency in Hz
     declare lf_sawpos author "Bart Brouns, revised by Stéphane Letz";
     declare lf_sawpos licence "STK-4.3";
608
    lf_sawpos(freq) = phasor_imp(freq, 0, 0);
610
611
612
     //----'(os.)lf_sawpos_phase'-----
613
     // Simple sawtooth waveform oscillator between 0 and 1
614
     // with phase control.
615
616
    // #### Usage
617
618
619
    // lf_sawpos_phase(freq, phase) : _
620
621
622
     // Where:
623
624
    // * 'freq': frequency in Hz
// * 'phase': phase between 0 and 1
625
626
627
     declare lf_sawpos_phase author "Bart Brouns, revised by Stéphane Letz";
628
     declare lf_sawpos_phase licence "STK-4.3";
629
630
    lf_sawpos_phase(freq,phase) = phasor_imp(freq, 0, phase);
631
632
633
    //-----'(os.)lf_sawpos_reset'-----
634
    // Simple sawtooth waveform oscillator between 0 and 1
635
     // with reset.
636
637
    //
    // #### Usage
638
   //
```

```
640
    // lf_sawpos_reset(freq,reset) : _
641
    // "
642
    //
643
    // Where:
644
    //
645
    /// * 'freq': frequency in Hz
// * 'reset': reset the oscillator to 0 when equal to 1
646
647
648
649
     declare lf_sawpos_reset author "Bart Brouns, revised by Stéphane Letz";
650
     declare lf_sawpos_reset licence "STK-4.3";
651
652
    lf_sawpos_reset(freq,reset) = phasor_imp(freq, reset, 0);
653
654
655
    //-----'(os.)lf_sawpos_phase_reset'-----
656
     // Simple sawtooth waveform oscillator between 0 and 1 \,
657
658
     \ensuremath{//} with phase control and reset.
659
    // #### Usage
660
    // ...
661
662
     // lf_sawpos_phase_reset(freq,phase,reset) : _
663
664
665
    // Where:
667
    // * 'freq': frequency in Hz
668
     // * 'phase': phase between 0 and 1
     // * 'reset': reset the oscillator to phase when equal to 1
672
    //----
     declare lf_sawpos_phase_reset author "Bart Brouns, revised by Stéphane Letz";
     declare lf_sawpos_phase_reset licence "STK-4.3";
    lf_sawpos_phase_reset(freq,phase,reset) = phasor_imp(freq, reset, phase);
676
678
    //-----'(os.)lf_saw'-----
    // Simple sawtooth waveform oscillator between -1 and 1.
680
     // 'lf_saw' is a standard Faust function.
681
682
683
    // #### Usage
    //
684
685
    // lf_saw(freq) : _
686
687
    //
688
    // Where:
689
690
     // * 'freq': frequency in Hz
691
692
     declare saw1 author "Bart Brouns";
693
     declare saw1 licence "STK-4.3";
694
695
     saw1(freq) = 2.0 * lf_sawpos(freq) - 1.0;
696
    lf_saw(freq) = saw1(freq);
697
698
     //===== Alias-Suppressed Sawtooth =========
699
     //-----(os.)sawN'--
700
    // Alias-Suppressed Sawtooth Audio-Frequency Oscillator using Nth-order polynomial
701
         transitions
    // to reduce aliasing.
702
703
    //
// 'sawN(N,freq)', 'sawNp(N,freq,phase)', 'saw2dpw(freq)', 'saw2(freq)', 'saw3(freq)',
// 'saw4(freq)', 'sawtooth(freq)', 'saw2f2(freq)', 'saw2f4(freq)'
704
705
   //
```

```
// #### Usage
707
708
     //
    // "
709
    // sawN(N,freq) : _
                              // Nth-order aliasing-suppressed sawtooth using DPW method (see
710
          below)
     // sawNp(N,freq,phase) : _ // sawN with phase offset feature
711
     // saw2dpw(freq) : _
                              // saw2 using DPW
712
     // saw2ptr(freq) : _
                              // saw2 using the faster, stateless PTR method
713
     // saw2(freq) : _
                              // DPW method, but subject to change if a better method emerges
714
     // saw3(freq) : _
                              // sawN(3)
715
716
     // saw4(freq) : _
                              // sawN(4)
     // sawtooth(freq) : _
                              // saw2
717
     // saw2f2(freq) : _
                              // saw2dpw with 2nd-order droop-correction filtering
718
     // saw2f4(freq) : _
                              // saw2dpw with 4th-order droop-correction filtering
719
     // "
720
    11
721
    // Where:
722
723
     // * 'N': polynomial order, a constant numerical expression between 1 and 4 \,
724
    // * 'freq': frequency in Hz
// * 'phase': phase between 0 and 1
725
726
727
     // #### Method
728
729
     // Differentiated Polynomial Wave (DPW).
730
731
     // #### Reference
     // "Alias-Suppressed Oscillators based on Differentiated Polynomial Waveforms",
     // Vesa Valimaki, Juhan Nam, Julius Smith, and Jonathan Abel,
     // IEEE Tr. Audio, Speech, and Language Processing (IEEE-ASLP), \,
     // Vol. 18, no. 5, pp 786-798, May 2010.
     // 10.1109/TASL.2009.2026507.
    // #### Notes
738
     // The polynomial order 'N' is limited to 4 because noise has been
739
     // observed at very low 'freq' values. (LFO sawtooths should of course
     // be generated using 'lf_sawpos' instead.)
742
     declare sawN author "Julius O. Smith III";
     declare sawN license "STK-4.3";
744
745
     // --- sawN for N = 1 to 4 ---
     // Orders 5 and 6 have noise at low fundamentals: MAX_SAW_ORDER = 6; MAX_SAW_ORDER_NEXTPOW2
746
     MAX_SAW_ORDER = 4;
     MAX_SAW_ORDER_NEXTPOW2 = 8; // par cannot handle the case of 0 elements
748
     sawN(N,freq) = saw11 : poly(Nc) : D(Nc-1) : gate(Nc-1)
749
     with {
750
      Nc = max(1,min(N,MAX_SAW_ORDER));
751
      clippedFreq = max(20.0,abs(freq)); // use lf_sawpos(freq) for LFOs (freq < 20 Hz)</pre>
752
      saw11 = 2*lf_sawpos(clippedFreq) - 1; // zero-mean, amplitude +/- 1
753
      poly(1,x) = x;
754
      poly(2,x) = x*x;
755
      poly(3,x) = x*x*x - x;
756
      poly(4,x) = x*x*(x*x - 2.0);
757
      poly(5,x) = x*(7.0/3 + x*x*(-10.0/3.0 + x*x));
758
      poly(6,x) = x*x*(7.0 + x*x*(-5.0 + x*x));
759
       pOn = float(ma.SR)/clippedFreq; // period in samples
760
      diff1(x) = (x - x')/(2.0/p0n);
761
      diff(N) = seq(n,N,diff1); // N diff1s in series
762
      factorial(0) = 1;
763
      factorial(i) = i * factorial(i-1);
764
765
      D(0) = :
      D(i) = diff(i)/factorial(i+1);
766
      gate(N) = *(10(N)); // delayed step for blanking startup glitch
767
768
769
             -----'(os.)sawNp'-----
770
     // Same as '(os.)sawN' but with a controllable waveform phase.
771
     //
```

```
// #### Usage
773
774
     11 ...
775
     // sawNp(N,freq,phase) : _
776
     11 00
777
     11
778
     // where
779
780
     // * 'N': waveform interpolation polynomial order 1 to 4 (constant integer expression)
781
     // * 'freq': frequency in Hz
782
     // * 'phase': waveform phase as a fraction of one period (rounded to nearest sample)
783
784
     // #### Implementation Notes
785
786
     /// The phase offset is implemented by delaying 'sawN(N,freq)' by // 'round(phase*ma.SR/freq)' samples, for up to 8191 samples.
787
788
     // The minimum sawtooth frequency that can be delayed a whole period
789
     // is therefore 'ma.SR/8191', which is well below audibility for normal
790
     // audio sampling rates.
791
792
     //---
793
     declare sawNp author "Julius O. Smith III";
794
795
     declare sawNp license "STK-4.3";
796
     // --- sawNp for N = 1 to 4 -
     // Phase offset = delay (max 8191 samples is more than one period of audio):
797
798
     sawNp(N,freq,phase) = sawN(N,freq) : @(max(0,min(8191,int(0.5+phase*ma.SR/freq))));
     //-----'(os.)saw2, (os.)saw3, (os.)saw4'-----
801
     // Alias-Suppressed Sawtooth Audio-Frequency Oscillators of order 2, 3, 4.
802
     // #### Usage
803
     // ...
805
     // saw2(freq) : _
806
     // saw3(freq) : _
     // saw4(freq) : _
809
810
     // where
811
     // * 'freq': frequency in Hz
813
814
     // ##### References
815
     // See 'sawN' above.
816
817
     // #### Implementation Notes
818
819
     // Presently, only 'saw2' uses the PTR method, while 'saw3' and 'saw4' use DPW.
820
     // This is because PTR has been implemented and tested for the 2nd-order case only.
821
822
823
     saw2 = saw2ptr; // "faustlibraries choice"
824
     saw3 = sawN(3); // only choice available right now
saw4 = sawN(4); // only choice available right now
825
826
827
                     -----'(os.)saw2ptr'---
828
     // Alias-Suppressed Sawtooth Audio-Frequency Oscillator
// using Polynomial Transition Regions (PTR) for order 2.
829
830
831
     // #### Usage
832
833
     11 ...
834
     // saw2ptr(freq) : _
835
     11 000
836
     11
837
     // where
838
839
    // * 'freq': frequency in Hz
```

```
841
          // #### Implementation
842
843
         // Polynomial Transition Regions (PTR) method for aliasing suppression.
844
845
         // ##### References
846
847
          //
          ^{\prime\prime} // * Kleimola, J.; Valimaki, V., "Reducing Aliasing from Synthetic Audio
848
                      Signals Using Polynomial Transition Regions," in Signal Processing
Letters, IEEE , vol.19, no.2, pp.67-70, Feb. 2012
          11
849
850
          // * <a href="https://aaltodoc.aalto.fi/bitstream/handle/123456789/7747/publication6.pdf?sequence=9">https://aaltodoc.aalto.fi/bitstream/handle/123456789/7747/publication6.pdf?sequence=9">https://aaltodoc.aalto.fi/bitstream/handle/123456789/7747/publication6.pdf?sequence=9">https://aaltodoc.aalto.fi/bitstream/handle/123456789/7747/publication6.pdf?sequence=9">https://aaltodoc.aalto.fi/bitstream/handle/123456789/7747/publication6.pdf?sequence=9">https://aaltodoc.aalto.fi/bitstream/handle/123456789/7747/publication6.pdf?sequence=9">https://aaltodoc.aalto.fi/bitstream/handle/123456789/7747/publication6.pdf?sequence=9">https://aaltodoc.aalto.fi/bitstream/handle/123456789/7747/publication6.pdf?sequence=9">https://aaltodoc.aalto.fi/bitstream/handle/123456789/7747/publication6.pdf?sequence=9">https://aaltodoc.aalto.fi/bitstream/handle/123456789/7747/publication6.pdf?sequence=9">https://aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aaltodoc.aa
851
          // * <http://research.spa.aalto.fi/publications/papers/spl-ptr/>
852
853
         // ##### Notes
854
855
          // Method PTR may be preferred because it requires less
856
          \ensuremath{//} computation and is stateless which means that the frequency 'freq'
857
          // can be modulated arbitrarily fast over time without filtering
858
859
          // artifacts. For this reason, 'saw2' is presently defined as 'saw2ptr'.
860
          //---
861
          declare saw2ptr author "Julius O. Smith III";
862
          declare saw2ptr license "STK-4.3";
864
          // specialized reimplementation:
          saw2ptr(freq) = y with { // newer PTR version (stateless - freq can vary at any speed)
865
            p0 = float(ma.SR)/float(max(ma.EPSILON,abs(freq))); // period in samples
             t0 = 1.0/p0; // phase increment
867
868
            p = ((_<:(-(1)<:_,_),_) <: selector1,selector2) ~(+(t0)):!,_;</pre>
869
             selector1 = select2(<(0)); // for feedback</pre>
             {\tt selector2 = select2(<(0), (\_<:\_,(*(1-p0):+(1)):+), \_); // for \ output}
871
            y = 2*p-1;
873
                            -----'(os.)saw2dpw'---
          // Alias-Suppressed Sawtooth Audio-Frequency Oscillator
          // using the Differentiated Polynomial Waveform (DWP) method.
877
          // #### Usage
878
879
          // saw2dpw(freq) : _
881
882
883
884
          // where
885
         // * 'freq': frequency in Hz
886
887
          // This is the original Faust 'saw2' function using the DPW method.
888
          // Since 'saw2' is now defined as 'saw2ptr', the DPW version
889
          // is now available as 'saw2dwp'.
890
891
          declare saw2dpw author "Julius O. Smith III";
892
          declare saw2dpw license "STK-4.3";
893
          saw2dpw(freq) = saw1(freq) <: * <: -(mem) : *(0.25'*ma.SR/freq);
894
895
                        -----'(os.)sawtooth'---
896
          // Alias-suppressed aliasing-suppressed sawtooth oscillator, presently defined as 'saw2'.
897
          // 'sawtooth' is a standard Faust function.
898
         //
899
         // #### Usage
900
901
         //
          // "
902
          // sawtooth(freq) : _
903
         11 "
904
905
         //
906
         // with
907
       // * 'freq': frequency in Hz
```

```
909
     sawtooth = saw2; // default choice for sawtooth signal - see also sawN
910
911
     //-----'(os.)saw2f2, (os.)saw2f4'-----
912
     // Alias-Suppressed Sawtooth Audio-Frequency Oscillator with Order 2 or 4 Droop Correction
913
          Filtering.
914
     // #### Usage
915
     //
916
     // "
917
     // saw2f2(freq) : _
918
     // saw2f4(freq) : _
919
     //
920
     //
921
     // with
922
923
     // * 'freq': frequency in Hz
924
925
926
     /\!/ In return for aliasing suppression, there is some attenuation near half the sampling rate
     // This can be considered as beneficial, or it can be compensated with a high-frequency
927
          boost.
     // The boost filter is second-order for 'saw2f2' and fourth-order for 'saw2f4', and both are
928
           designed
     // for the DWP case and therefore use 'saw2dpw'.
929
     // See Figure 4(b) in the DPW reference for a plot of the slight droop in the DPW case.
     declare saw2f2 author "Julius O. Smith III";
933
     declare saw2f2 license "STK-4.3";
     // --- Correction-filtered versions of saw2: saw2f2, saw2f4 ----
     saw2f2 = saw2dpw : cf2 with {
      cf2 = fi.tf2(1.155704605878911, 0.745184288225518,0.040305967265900,
937
            0.823765146386639, 0.117420665547108);
938
     declare saw2f4 author "Julius O. Smith III";
     declare saw2f4 license "STK-4.3";
     saw2f4 = saw2dpw : cf4 with {
941
      cf4 = fi.iir((1.155727435125014, 2.285861038554662,
             1.430915027294021, 0.290713280893317, 0.008306401748854),
943
             (2.156834679164532, 1.559532244409321, 0.423036498118354,
             0.032080681130972));
945
946
     };
947
     //======Alias-Suppressed Pulse, Square, and Impulse Trains=======
948
     // Alias-Suppressed Pulse, Square and Impulse Trains.
949
950
    /// 'pulsetrainN', 'pulsetrain', 'squareN', 'square', 'imptrainN', 'imptrain',
// 'triangleN', 'triangle'
951
952
953
     //
     ^{\prime\prime} // All are zero-mean and meant to oscillate in the audio frequency range.
954
     // Use simpler sample-rounded 'lf_*' versions above for LFOs.
955
956
    // #### Usage
957
    // ...
958
959
     //
// pulsetrainN(N,freq,duty) :
960
     // pulsetrain(freq, duty) : _ // = pulsetrainN(2)
961
962
     // squareN(N,freq) : _
963
     // square : _ // = squareN(2)
964
965
    // imptrainN(N,freq) : _
// imptrain : _ // = imptrainN(2)
966
967
968
     // triangleN(N,freq) :
969
    // triangle : _ // = triangleN(2)
// '''
970
971
    11
```

```
// Where:
973
974
      // * 'N': polynomial order, a constant numerical expression
975
      // * 'freq': frequency in Hz
976
977
978
979
      //-----'(os.)impulse'-----
980
      // One-time impulse generated when the Faust process is started.
981
      // 'impulse' is a standard Faust function.
982
983
      // #### Usage
 984
985
      //
     // "
 986
     // impulse : _
 987
988
      //----
 989
      impulse = 1-1';
 990
991
992
      //-----'(os.)pulsetrainN'-----
993
      // Alias-suppressed pulse train oscillator.
994
 995
      // #### Usage
996
997
      11
      11 ...
 998
      // pulsetrainN(N,freq,duty) : _
999
1000
1001
      11
      // Where:
1002
      // * 'N': order, as a constant numerical expression
      // * 'freq': frequency in Hz
1005
      // * 'duty': duty cycle between 0 and 1
1006
1008
     pulsetrainN(N,freq,duty) = diffdel(sawN(N,freqC),del) with {
1009
      // non-interpolated-delay version: diffdel(x,del) = x - x@int(del+0.5);
1010
      // linearly interpolated delay version (sounds good to me):
1011
1012
         diffdel(x,del) = x-x@int(del)*(1-ma.frac(del))-x@(int(del)+1)*ma.frac(del);
       // Third-order Lagrange interpolated-delay version (see filters.lib):
1013
      // diffdel(x,del) = x - fdelay3(DELPWR2,\max(1,\min(DELPWR2-2,ddel))); DELPWR2 = 2048; // Needs to be a power of 2 when fdelay*() used above
1014
1015
       delmax = DELPWR2-1; // arbitrary upper limit on diff delay (duty=0.5)
1016
       SRmax = 96000.0; // assumed upper limit on sampling rate
1017
       fmin = SRmax / float(2.0*delmax); // 23.4 Hz (audio freqs only)
1018
      freqC = max(freq,fmin); // clip frequency at lower limit
period = (float(ma.SR) / freqC); // actual period
1019
1020
      ddel = duty * period; // desired delay
1021
      del = max(0,min(delmax,ddel));
1022
1023
1024
1025
      //-----'(os.)pulsetrain'-----
1026
      // Alias-suppressed pulse train oscillator. Based on 'pulsetrainN(2)'.
1027
      // 'pulsetrain' is a standard Faust function.
1028
1029
      // #### Usage
1030
      11
1031
      11 ...
1032
      // pulsetrain(freq,duty) : _
1033
1034
      11
      //
1035
      // Where:
1036
1037
      // * 'freq': frequency in Hz
1038
      // * 'duty': duty cycle between 0 and 1
1039
1040
```

```
pulsetrain = pulsetrainN(2);
1041
1042
1043
              -----'(os.)squareN'----
1044
     // Alias-suppressed square wave oscillator.
1045
1046
     // #### Usage
1047
1048
     11 ...
1049
     // squareN(N,freq) : _
1050
     11 000
1051
     //
1052
     // Where:
1053
1054
     // * 'N': order, as a constant numerical expression
1055
     // * 'freq': frequency in Hz
1056
1057
     squareN(N,freq) = pulsetrainN(N,freq,0.5);
1058
1059
1060
     //-----'(os.)square'-----
1061
     // Alias-suppressed square wave oscillator. Based on 'squareN(2)'.
1062
1063
     // 'square' is a standard Faust function.
1064
     // #### Usage
1065
1066
     // square(freq) : _
// '''
1067
1068
1069
1070
     // Where:
1071
1072
     // * 'freq': frequency in Hz
1073
1074
     square = squareN(2);
1077
     //-----'(os.)imptrainN'-----
1078
     // Alias-suppressed impulse train generator.
1079
1080
     // #### Usage
1081
1082
1083
1084
     // imptrainN(N,freq) : _
1085
1086
     // Where:
1087
1088
     // * 'N': order, as a constant numerical expression
1089
     // * 'freq': frequency in Hz
1090
1091
     imptrainN(N,freq) = impulse + 0.5*ma.diffn(sawN(N,freq));
1092
1093
1094
     //-----'(os.)imptrain'-----
1095
     // Alias-suppressed impulse train generator. Based on 'imptrainN(2)'. // 'imptrain' is a standard Faust function.
1096
1097
1098
     // #### Usage
1099
     // ...
1100
1101
     // imptrain(freq) : _
// '''
1102
1103
     11
1104
     // Where:
1105
1106
     // * 'freq': frequency in Hz
1107
1108
```

```
imptrain = imptrainN(2); // default based on saw2
1109
1110
1111
              -----'(os.)triangleN'----
1112
     // Alias-suppressed triangle wave oscillator.
1113
1114
     // #### Usage
1115
1116
      11 ...
1117
      // triangleN(N,freq) : _
1118
     11 000
1119
      //
1120
     // Where:
1121
1122
     // * 'N': order, as a constant numerical expression // * 'freq': frequency in Hz
1123
1124
1125
      \label{eq:triangleN(N,freq) = squareN(N,freq) : fi.pole(p) : *(gain) with \{ \\
1126
      gain = 4.0*freq/ma.SR; // for aproximate unit peak amplitude
1127
1128
       p = 0.999;
1129
1130
1131
      //-----'(os.)triangle'-----
1132
     // Alias-suppressed triangle wave oscillator. Based on 'triangleN(2)'.
1133
      // 'triangle' is a standard Faust function.
1134
1135
      // #### Usage
1136
1137
1138
      // triangle(freq) : _
1139
1140
     11
1141
     // Where:
1142
      // * 'freq': frequency in Hz
1144
1145
      triangle = triangleN(2); // default based on saw2
1146
1147
1148
                              ======Filter-Based Oscillators======
1149
      // Filter-Based Oscillators.
1150
1151
      // #### Usage
1152
1153
1154
      // osc[b|rq|rs|rc|s](freq), where freq = frequency in Hz.
1155
1156
     11
1157
     // #### References
1158
1159
      // * <http://lac.linuxaudio.org/2012/download/lac12-slides-jos.pdf>
1160
      // * <https://ccrma.stanford.edu/~jos/pdf/lac12-paper-jos.pdf>
1161
1162
1163
             -----'(os.)oscb'--
1164
      // Sinusoidal oscillator based on the biquad.
1165
1166
      // #### Usage
1167
     // ...
1168
1169
     // oscb(freq) : _
// '''
1170
1171
     //
1172
     // Where:
1173
1174
      // * 'freq': frequency in Hz
1175
1176
```

```
oscb(f) = impulse : fi.tf2(1,0,0,a1,1)
1177
      with {
1178
      a1 = -2*\cos(2*ma.PI*f/ma.SR);
1179
1180
1181
1182
     //-----
// Sinusoidal (sine and cosine) oscillator based on 2D vector rotation,
1183
1184
      // = undamped "coupled-form" resonator
1185
      // = lossless 2nd-order normalized ladder filter.
1186
1187
      // #### Usage
1188
1189
     // ...
1190
     // oscrq(freq) : _,_
// '''
1191
1192
      11
1193
     // Where:
1194
1195
      // * 'freq': frequency in Hz
1196
1197
      // #### Reference
1198
1199
      // * <https://ccrma.stanford.edu/~jos/pasp/Normalized_Scattering_Junctions.html>
1200
1201
      oscrq(f) = impulse : fi.nlf2(f,1); // sine and cosine outputs
1202
      //-----'(os.)oscrs'-----
1205
      // Sinusoidal (sine) oscillator based on 2D vector rotation,
     // = undamped "coupled-form" resonator
// = lossless 2nd-order normalized ladder filter.
1207
1208
     // #### Usage
1209
1210
1212
      // oscrs(freq) : _
1213
1214
     // Where:
1215
     // * 'freq': frequency in Hz
1217
1218
     // #### Reference
1219
1220
     // * <https://ccrma.stanford.edu/~jos/pasp/Normalized_Scattering_Junctions.html>
1221
1222
      oscrs(f) = impulse : fi.nlf2(f,1) : _,!; // sine
1223
1224
                        -----'(os.)oscrc'---
1225
      // Sinusoidal (cosine) oscillator based on 2D vector rotation,
1226
      // = undamped "coupled-form" resonator
1227
      // = lossless 2nd-order normalized ladder filter.
1228
     11
1229
      // #### Usage
1230
1231
      11 ...
1232
      // oscrc(freq) : _
1233
      11 000
1234
1235
      // Where:
1236
1237
     // * 'freq': frequency in Hz
1238
1239
      // #### Reference
1240
1241
      // * <https://ccrma.stanford.edu/~jos/pasp/Normalized_Scattering_Junctions.html>
1242
1243
     oscrc(f) = impulse : fi.nlf2(f,1) : !,_; // cosine
```

```
1245
      \operatorname{oscrp}(f,p) = \operatorname{oscrq}(f) : *(\cos(p)), *(\sin(p)) : +; // p=0 \text{ for sine, } p=PI/2 \text{ for cosine, etc.}
1246
1247
      oscr = oscrs; // default = sine (starts without a pop)
1248
1249
                          -----'(os.)oscs'-----
1250
      /// Sinusoidal oscillator based on the state variable filter
// = undamped "modified-coupled-form" resonator
1251
1252
      // = "magic circle" algorithm used in graphics.
1253
1254
      // #### Usage
1255
      11
1256
      11 ...
1257
      // oscs(freq) : _
1258
      11 000
1259
      11
1260
      // Where:
1261
1262
      // * 'freq': frequency in Hz
1263
1264
      oscs(f) = (*(-1) : sint(wn) : sintp(wn,impulse)) ~ _
1265
1266
      with {
1267
       wn = 2*ma.PI*f/ma.SR; // approximate
       // wn = 2*sin(PI*f/SR); // exact

sint(x) = *(x) : + ~_ ; // frequency-scaled integrator

sintp(x,y) = *(x) : +(y) : + ~_ ; // same + state input
1268
1269
1270
1271
1272
1273
      //-----'(os.)quadosc'-----
1274
      // Quadrature (cosine and sine) oscillator based on Quad0sc by Martin Vicanek.
1275
      // #### Usage
1277
      11
1278
      // quadosc(freq) : _,_
// '''
1280
1281
      // where
1282
1283
      // * 'freq': frequency in Hz
1285
      // #### Reference
1286
      // * <https://vicanek.de/articles/QuadOsc.pdf>
1287
1288
1289
      // Dario Sanfilippo <sanfilippo.dario@gmail.com>
1290
      // and Oleg Nesterov (jos ed.)
1291
      quadosc(f) = tick ~ (_,_)
1292
      with {
1293
         k1 = tan(f * ma.PI / ma.SR);
1294
         k2 = 2 * k1 / (1 + k1 * k1);
1295
          tick(u_0,v_0) = u_1,v_1
1296
          with {
1297
              tmp = u_0 - k1 * v_0;
1298
              v_1 = v_0 + k2 * tmp;
1299
              u_1 = tmp - k1 * v_1 : select2(1',1);
1300
         };
1301
      };
1302
1303
      //-----'(os.)sidebands'-----
1304
      \ensuremath{//} Adds harmonics to quad oscillator.
1305
1306
      // #### Usage
1307
      // ...
1308
1309
      // cos(x),sin(x) : sidebands(vs) : _,_
1310
      11 ...
1311
     //
1312
```

```
// Where:
1313
1314
      // * 'vs' : list of amplitudes
1315
1316
     // #### Example test program
1317
1318
     // cos(x),sin(x) : sidebands((10,20,30))
// '''
1319
1320
1321
     //
1322
      // outputs:
1323
1324
     //
      11 ...
1325
      // 10*cos(x) + 20*cos(2*x) + 30*cos(3*x),
1326
     // 10*sin(x) + 20*sin(2*x) + 30*sin(3*x);
// '''
1327
1328
1329
      //
      // The following:
1330
1331
     //
     // process = os.quadosc(F) : sidebands((10,20,30))
// '''
1332
1333
1334
1335
      \ensuremath{//} is (modulo floating point issues) the same as:
1336
     // "
1337
1338
     // c = os.quadosc : _,!;
// s = os.quadosc : !,_;
1339
1340
1341
      // process =
1342
      //
               10*c(F) + 20*c(2*F) + 30*c(F),
               10*s(F) + 20*s(2*F) + 30*s(F);
     // "
1345
     //
      // but much more efficient.
1346
      // #### Implementation Notes
1349
      // This is based on the trivial trigonometric identities:
1350
1351
1352
     \frac{1}{1/2} \cos((n+1)x) = 2\cos(x)\cos(nx) - \cos((n-1)x)
1353
           \sin((n + 1) x) = 2 \cos(x) \sin(n x) - \sin((n - 1) x)
1354
1355
1356
     // Note that the calculation of the cosine/sine parts do not depend
1357
      // on each other, so if you only need the sine part you can do:
1358
1359
1360
     // process = os.quadosc(F) : sidebands(vs) : !,_;
// ""
1361
1362
1363
      \ensuremath{//} and the compiler will discard the half of the calculations.
1364
1365
      sidebands(vs. c0.s0)
1366
         = c0*vn(0), s0*vn(0), 1, c0, 0, s0
1367
         : seq(n, outputs(vs)-1, add(vn(n+1)))
1368
      : _,_,!,!,!,!
with {
1369
1370
         // ba.take(n+1, vs)
1371
          vn(n) = vs : route(outputs(vs),1, n+1,1);
1372
1373
1374
          add(vn, co, so, cn_2, cn_1, sn_2, sn_1) =
1375
            co+cn*vn, so+sn*vn, cn_1,cn, sn_1,sn
          with {
1376
             cn = 2*c0*cn_1 - cn_2;
1377
1378
             sn = 2*c0*sn_1 - sn_2;
1379
          };
1380
    };
```

```
1381
                      -----'(os.)sidebands_list'-----
1382
      // Creates the list of complex harmonics from quad oscillator.
1383
1384
      ^{\prime\prime} // Similar to 'sidebands' but doesn't sum the harmonics, so it is more
1385
      // generic but less convenient for immediate usage.
1386
1387
      // #### Usage
1388
     // ...
1389
1390
      ...

// cos(x),sin(x) : sidebands_list(N) : si.bus(2*N)

// '''
1391
1392
1393
      11
      // Where:
1394
1395
      // * 'N' : number of harmonics, compile time constant > 1
1396
1397
      // #### Example test program
1398
1399
      11 000
      // cos(x),sin(x) : sidebands_list(3)
// '''
1400
1401
1402
1403
      // outputs:
1404
1405
      //
1406
      // cos(x),sin(x), cos(2*x),sin(2*x), cos(3*x),sin(3*x);
// '''
1407
1408
1409
      11
      // The following:
1410
     // process = os.quadosc(F) : sidebands_list(3)
// '''
1414
1416
      \ensuremath{//} is (modulo floating point issues) the same as:
1417
1418
      /// process = os.quadosc(F), os.quadosc(2*F), os.quadosc(3*F);
// '''
1419
1420
1421
      // but much more efficient.
1422
1423
      sidebands_list(N, c0,s0)
1424
        = c0,s0, 1,c0, 0,s0
: seq(n, N-1, si.bus(2*(n+1)), add)
1425
1426
          : si.bus(2*N), !,!, !,!
1427
      with {
1428
        add(cn_2, cn_1, sn_2, sn_1) =
1429
             cn,sn, cn_1,cn, sn_1,sn
1430
1431
          with {
             cn = 2*c0*cn_1 - cn_2;
sn = 2*c0*sn_1 - sn_2;
1432
1433
         };
1434
      };
1435
1436
      //====== Waveguide-Resonator-Based Oscillators =========
1437
      // Sinusoidal oscillator based on the waveguide resonator 'wgr'.
1438
1439
1440
                       ----'(os.)oscwc'----
1441
      // Sinusoidal oscillator based on the waveguide resonator 'wgr'. Unit-amplitude
1442
      // cosine oscillator.
1443
1444
      // #### Usage
1445
1446
      //
      // "
1447
    // oscwc(freq) : _
1448
```

```
1449
1450
     // Where:
1451
1452
     // * 'freq': frequency in Hz
1453
1454
     // #### Reference
1455
1456
     // * <https://ccrma.stanford.edu/~jos/pasp/Digital_Waveguide_Oscillator.html>
1457
1458
1459
     oscwc(fr) = impulse : fi.wgr(fr,1) : _,!; // cosine (cheapest at 1 mpy/sample)
1460
      //-----'(os.)oscws'-----
1461
     // Sinusoidal oscillator based on the waveguide resonator 'wgr'. Unit-amplitude
1462
     // sine oscillator.
1463
1464
     // #### Usage
1465
1466
1467
     // oscws(freq) : _
1468
     11 "
1469
1470
     // Where:
1471
1472
     // * 'freq': frequency in Hz
1473
1474
     // #### Reference
1475
1476
1477
     // * <https://ccrma.stanford.edu/~jos/pasp/Digital_Waveguide_Oscillator.html>
1478
     oscws(fr) = impulse : fi.wgr(fr,1) : !,_; // sine (needs a 2nd scaling mpy)
1480
     //-----'(os.)oscq'-----
1482
     // Sinusoidal oscillator based on the waveguide resonator 'wgr'.
     // Unit-amplitude cosine and sine (quadrature) oscillator.
1484
     // #### Usage
1485
     // ...
1486
1487
1488
     // oscq(freq) : _,_
1489
1490
     // Where:
1491
1492
     // * 'freq': frequency in Hz
1493
1494
     // #### Reference
1495
1496
     // * <https://ccrma.stanford.edu/~jos/pasp/Digital_Waveguide_Oscillator.html>
1497
1498
     oscq(fr) = impulse : fi.wgr(fr,1); // phase quadrature outputs
1499
1500
              -----'(os.)oscw'--
1501
     // Sinusoidal oscillator based on the waveguide resonator 'wgr'.
1502
     // Unit-amplitude cosine oscillator (default).
1503
1504
     // #### Usage
1505
1506
     11
     11 ...
1507
     // oscw(freq) : _
1508
1509
     11
1510
     // Where:
1511
1512
     // * 'freq': frequency in Hz
1513
1514
     // #### Reference
1515
1516
    11
```

```
// * <https://ccrma.stanford.edu/~jos/pasp/Digital_Waveguide_Oscillator.html>
1517
1518
     oscw = oscwc:
1519
1520
     // end jos section
1521
     1522
     1523
     FAUST library file, further contributions section
1524
1525
     All contributions below should indicate both the contributor and terms
1526
1527
     of license. If no such indication is found, "git blame" will say who
     last edited each line, and that person can be emailed to inquire about
1528
     license disposition, if their license choice is not already indicated
1529
     elsewhere among the libraries. It is expected that all software will be
1530
     released under LGPL, STK-4.3, MIT, BSD, or a similar FOSS license.
1531
     1532
1533
     //====== Casio CZ Oscillators ==========
1534
1535
     // Oscillators that mimic some of the Casio CZ oscillators.
1536
     // There are two sets:
1537
1538
     // * a set with an index parameter
1539
1540
     // * a set with a res parameter
1541
1542
     // The "index oscillators" outputs a sine wave at index=0 and gets brighter with a higher
         index.
1544
     // There are two versions of the "index oscillators":
1545
     // * with P appended to the name: is phase aligned with 'fund:sin'
1547
     // * without P appended to the name: has the phase of the original CZ oscillators
1549
     // The "res oscillators" have a resonant frequency.
1551
     // "res" is the frequency of resonance as a factor of the fundamental pitch.
1552
     // For the 'fund' waveform, use a low-frequency oscillator without anti-aliasing such as 'os.
1553
1554
1555
1556
     //----'(os.)CZsaw'-----
     // Oscillator that mimics the Casio CZ saw oscillator.
1557
     // 'CZsaw' is a standard Faust function.
1558
1559
     // #### Usage
1560
1561
     11 ...
1562
     // CZsaw(fund,index) : _
1563
     11 000
1564
1565
     // Where:
1566
1567
     // * 'fund': a saw-tooth waveform between 0 and 1 that the oscillator slaves to
1568
     //* 'index': the brightness of the oscillator, 0 to 1. 0 = sine-wave, 1 = saw-wave
1569
1570
     declare CZsaw author "Bart Brouns";
1571
     declare CZsaw licence "STK-4.3";
1572
1573
     // CZ oscillators by Mike Moser-Booth:
1574
     // <https://forum.pdpatchrepo.info/topic/5992/casio-cz-oscillators>
1575
     // Ported from pd to Faust by Bart Brouns
1576
1577
1578
     CZsaw(fund, index) = CZ.sawChooseP(fund, index, 0);
1579
     //----'(os.)CZsawP'-----
1580
     // Oscillator that mimics the Casio CZ saw oscillator,
1581
    // with it's phase aligned to 'fund:sin'.
```

```
// 'CZsawP' is a standard Faust function.
1583
1584
     // #### Usage
1585
1586
     11 ...
1587
     // CZsawP(fund,index) : _
1588
     11 ...
1589
     11
1590
     // Where:
1591
1592
     11
     //* 'fund': a saw-tooth waveform between 0 and 1 that the oscillator slaves to
1593
     // * 'index': the brightness of the oscillator, 0 to 1. 0 = sine-wave, 1 = saw-wave
1594
1595
     declare CZsawP author "Bart Brouns";
1596
     declare CZsawP licence "STK-4.3";
1597
1598
1599
      // CZ oscillators by Mike Moser-Booth:
      // <https://forum.pdpatchrepo.info/topic/5992/casio-cz-oscillators>
1600
1601
     // Ported from pd to Faust by Bart Brouns
1602
     CZsawP(fund, index) = CZ.sawChooseP(fund, index, 1);
1603
1604
     //----'(os.)CZsquare'----
1605
      // Oscillator that mimics the Casio CZ square oscillator
1606
     // 'CZsquare' is a standard Faust function.
1607
1608
     // #### Usage
1609
1610
     11 ...
1611
1612
      // CZsquare(fund,index) : _
     11 "
1614
     // Where:
1616
     // * 'fund': a saw-tooth waveform between 0 and 1 that the oscillator slaves to
1618
      // * 'index': the brightness of the oscillator, 0 to 1. 0 = sine-wave, 1 = square-wave
1619
      declare CZsquare author "Bart Brouns";
1620
     declare CZsquare licence "STK-4.3";
1621
     // CZ oscillators by Mike Moser-Booth:
1623
      // <https://forum.pdpatchrepo.info/topic/5992/casio-cz-oscillators>
1624
     // Ported from pd to Faust by Bart Brouns
1625
1626
     CZsquare(fund, index) = CZ.squareChooseP(fund, index, 0);
1627
1628
     //-----'(os.)CZsquareP'-----
1629
     // Oscillator that mimics the Casio CZ square oscillator,
1630
     // with it's phase aligned to 'fund:sin'.
1631
     // 'CZsquareP' is a standard Faust function.
1632
1633
     // #### Usage
1634
     11
1635
     11 ...
1636
     // CZsquareP(fund,index) : _
1637
     11 000
1638
     //
1639
     // Where:
1640
1641
     //* 'fund': a saw-tooth waveform between 0 and 1 that the oscillator slaves to
1642
     // * 'index': the brightness of the oscillator, 0 to 1. 0 = sine-wave, 1 = square-wave
1643
1644
     declare CZsquareP author "Bart Brouns";
1645
     declare CZsquareP licence "STK-4.3";
1646
1647
1648
      // CZ oscillators by Mike Moser-Booth:
     // <https://forum.pdpatchrepo.info/topic/5992/casio-cz-oscillators>
1649
     // Ported from pd to Faust by Bart Brouns
```

```
1651
      CZsquareP(fund, index) = CZ.squareChooseP(fund, index, 1);
1652
1653
      //----'(os.)CZpulse'---
1654
      // Oscillator that mimics the Casio CZ pulse oscillator.
1655
      // 'CZpulse' is a standard Faust function.
1656
1657
      // #### Usage
1658
      11
1659
     11 ...
1660
      // CZpulse(fund,index) : _
1661
1662
      11
1663
      // Where:
1664
1665
      // * 'fund': a saw-tooth waveform between 0 and 1 that the oscillator slaves to
1666
      //* 'index': the brightness of the oscillator, 0 gives a sine-wave, 1 is closer to a pulse
1667
1668
1669
      declare CZpulse author "Bart Brouns";
1670
      declare CZpulse licence "STK-4.3";
1671
1672
      // CZ oscillators by Mike Moser-Booth:
      // <https://forum.pdpatchrepo.info/topic/5992/casio-cz-oscillators>
1674
      // Ported from pd to Faust by Bart Brouns
1675
1676
      CZpulse(fund, index) = CZ.pulseChooseP(fund, index, 0);
      //----'(os.)CZpulseP'-----
1679
      // Oscillator that mimics the Casio CZ pulse oscillator,
      // with it's phase aligned to 'fund:sin'.
      // 'CZpulseP' is a standard Faust function.
1682
     // #### Usage
1683
1684
1686
      // CZpulseP(fund,index) : _
1687
1688
      // Where:
1689
     //* 'fund': a saw-tooth waveform between 0 and 1 that the oscillator slaves to
1691
      // * 'index': the brightness of the oscillator, O gives a sine-wave, 1 is closer to a pulse
1692
1693
      declare CZpulseP author "Bart Brouns";
1694
      declare CZpulseP licence "STK-4.3";
1695
1696
      // CZ oscillators by Mike Moser-Booth:
1697
      // <https://forum.pdpatchrepo.info/topic/5992/casio-cz-oscillators>
1698
      // Ported from pd to Faust by Bart Brouns
1699
1700
1701
      CZpulseP(fund, index) = CZ.pulseChooseP(fund, index, 1);
1702
             -----'(os.)CZsinePulse'----
1703
      // Oscillator that mimics the Casio CZ sine/pulse oscillator.
1704
      // 'CZsinePulse' is a standard Faust function.
1705
1706
      // #### Usage
1707
1708
      11
     11 ...
1709
      // CZsinePulse(fund,index) : _
1710
1711
      11
1712
      // Where:
1713
1714
      ^{\prime\prime} // * 'fund': a saw-tooth waveform between 0 and 1 that the oscillator slaves to
1715
      // \ast 'index': the brightness of the oscillator, 0 gives a sine-wave, 1 is a sine minus a
1716
           pulse
1717
```

```
declare CZsinePulse author "Bart Brouns";
1718
           declare CZsinePulse licence "STK-4.3";
1719
1720
           // CZ oscillators by Mike Moser-Booth:
1721
           // <a href="https://forum.pdpatchrepo.info/topic/5992/casio-cz-oscillators">// <a href="https://forum.pdpatchrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/sepachrepo.info/topic/s
1722
           // Ported from pd to Faust by Bart Brouns
1723
1724
           CZsinePulse(fund, index) = CZ.sinePulseChooseP(fund, index, 0);
1725
1726
           //----'(os.)CZsinePulseP'-----
1727
           // Oscillator that mimics the Casio CZ sine/pulse oscillator,
1728
           // with it's phase aligned to 'fund:sin'.
1729
           // 'CZsinePulseP' is a standard Faust function.
1730
1731
           // #### Usage
1732
1733
          11 ...
1734
           // CZsinePulseP(fund,index) : _
1735
1736
           11 000
1737
           // Where:
1738
1739
           // * 'fund': a saw-tooth waveform between 0 and 1 that the oscillator slaves to
1740
           // * 'index': the brightness of the oscillator, 0 gives a sine-wave, 1 is a sine minus a
1741
1742
1743
           declare CZsinePulseP author "Bart Brouns";
1744
           declare CZsinePulseP licence "STK-4.3";
1745
           // CZ oscillators by Mike Moser-Booth:
           // <https://forum.pdpatchrepo.info/topic/5992/casio-cz-oscillators>
            // Ported from pd to Faust by Bart Brouns
1749
           CZsinePulseP(fund, index) = CZ.sinePulseChooseP(fund, index, 1);
1750
           //----'(os.)CZhalfSine'-----
           // Oscillator that mimics the Casio CZ half sine oscillator.
1753
           // 'CZhalfSine' is a standard Faust function.
1754
1755
1756
           // #### Usage
1757
          11 ...
1758
           // CZhalfSine(fund,index) : _
1759
1760
          11
1761
           // Where:
1762
1763
           // * 'fund': a saw-tooth waveform between 0 and 1 that the oscillator slaves to
1764
           //* 'index': the brightness of the oscillator, 0 gives a sine-wave, 1 is somewhere between a
1765
                      saw and a square
1766
           declare CZhalfSine author "Bart Brouns";
1767
           declare CZhalfSine licence "STK-4.3";
1768
1769
           // CZ oscillators by Mike Moser-Booth:
1770
           // <https://forum.pdpatchrepo.info/topic/5992/casio-cz-oscillators>
1771
           // Ported from pd to Faust by Bart Brouns
1772
1773
           CZhalfSine(fund, index) = CZ.halfSineChooseP(fund, index, 0);
1774
1775
                           ----'(os.)CZhalfSineP'----
1776
           // Oscillator that mimics the Casio CZ half sine oscillator,
1777
           // with it's phase aligned to 'fund:sin'.
1778
           // 'CZhalfSineP' is a standard Faust function.
1779
1780
           // #### Usage
1781
           11
1782
         11 ...
1783
```

```
// CZhalfSineP(fund,index) : _
1784
1785
           //
1786
           // Where:
1787
           11
1788
           // * 'fund': a saw-tooth waveform between 0 and 1 that the oscillator slaves to
1789
           //* 'index': the brightness of the oscillator, 0 gives a sine-wave, 1 is somewhere between a
1790
                        saw and a square
1791
           declare CZhalfSineP author "Bart Brouns";
1792
           declare CZhalfSineP licence "STK-4.3":
1793
1794
1795
            // CZ oscillators by Mike Moser-Booth:
            // <a href="https://forum.pdpatchrepo.info/topic/5992/casio-cz-oscillators">// <a href="https://forum.pdpatchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/topic/sepacchrepo.info/top
1796
           // Ported from pd to Faust by Bart Brouns
1797
1798
           CZhalfSineP(fund, index) = CZ.halfSineChooseP(fund, index, 1);
1799
1800
1801
           //----'(os.)CZresSaw'---
1802
            // Oscillator that mimics the Casio CZ resonant sawtooth oscillator.
           // 'CZresSaw' is a standard Faust function.
1803
1804
           // #### Usage
1805
1806
           11 ...
1807
           // CZresSaw(fund,res) : _
1808
1809
           11 000
1810
           // Where:
1811
1812
           // * 'fund': a saw-tooth waveform between 0 and 1 that the oscillator slaves to
            \ensuremath{//} * 'res': the frequency of resonance as a factor of the fundamental pitch.
           declare CZresSaw author "Bart Brouns";
1816
           declare CZresSaw licence "STK-4.3";
1818
           // CZ oscillators by Mike Moser-Booth:
1819
            // <https://forum.pdpatchrepo.info/topic/5992/casio-cz-oscillators>
1820
           // Ported from pd to Faust by Bart Brouns
1821
           CZresSaw(fund,res) = CZ.resSaw(fund,res);
1823
1824
           //----'(os.)CZresTriangle'-----
1825
           // Oscillator that mimics the Casio CZ resonant triangle oscillator.
1826
           // 'CZresTriangle' is a standard Faust function.
1827
1828
           // #### Usage
1829
1830
           11 ...
1831
           // CZresTriangle(fund,res) : _
1832
           11 000
1833
           11
1834
           // Where:
1835
1836
           // * 'fund': a saw-tooth waveform between 0 and 1 that the oscillator slaves to
1837
           // * 'res': the frequency of resonance as a factor of the fundamental pitch.
1838
1839
           declare CZresTriangle author "Bart Brouns";
declare CZresTriangle licence "STK-4.3";
1840
1841
1842
            // CZ oscillators by Mike Moser-Booth:
1843
           // <a href="https://forum.pdpatchrepo.info/topic/5992/casio-cz-oscillators">https://forum.pdpatchrepo.info/topic/5992/casio-cz-oscillators</a> // Ported from pd to Faust by Bart Brouns
1844
1845
1846
           CZresTriangle(fund,res) = CZ.resTriangle(fund,res);
1847
1848
            //----'(os.)CZresTrap'-----
1849
          // Oscillator that mimics the Casio CZ resonant trapeze oscillator
```

```
// 'CZresTrap' is a standard Faust function.
1851
1852
          // #### Usage
1853
1854
          11 ...
1855
          // CZresTrap(fund,res) : _
1856
          11 000
1857
          //
1858
          // Where:
1859
1860
          // * 'fund': a saw-tooth waveform between 0 and 1 that the oscillator slaves to
1861
          // * 'res': the frequency of resonance as a factor of the fundamental pitch.
1862
1863
          declare CZresTrap author "Bart Brouns";
1864
1865
          declare CZresTrap licence "STK-4.3";
1866
1867
           // CZ oscillators by Mike Moser-Booth:
           // <https://forum.pdpatchrepo.info/topic/5992/casio-cz-oscillators>
1868
1869
          // Ported from pd to Faust by Bart Brouns
1870
1871
          CZresTrap(fund, res) = CZ.resTrap(fund, res);
1872
          CZ = environment {
1873
1874
1875
                 saw(fund, index) = sawChooseP(fund, index, 0);
1876
                 sawP(fund, index) = sawChooseP(fund, index, 1);
                 sawChooseP(fund, index, p) =
                    (((\texttt{FUND}(\texttt{fund},\texttt{align},p)*\bar{(}(.5-\texttt{INDEX})/\texttt{INDEX})),(-1*\texttt{FUND}(\texttt{fund},\texttt{align},p)+1)*((.5-\texttt{INDEX})/(1-1)))
1878
                              INDEX))):min+FUND(fund,align,p))*2*ma.PI:cos
                 with {
1880
                    INDEX = (.5-(index*.5)):max(0.01):min(0.5);
                    align = si.interpolate(index, 0.75, 0.5);
1881
1882
1883
                 square(fund, index) = squareChooseP(fund, index, 0);
1885
                 squareP(fund, index) = squareChooseP(fund, index, 1);
                 squareChooseP(fund, index, p) = (FUND(fund,align,p)>=0.5), (ma.decimal((FUND(fund,align,p
1886
                           )*2)+1)<:_-min(_,(-1*_+1)*((INDEX)/(1-INDEX)))) :+ *ma.PI:cos
1887
1888
                    INDEX = (index:pow(0.25)):max(0):min(1);
                    align = si.interpolate(INDEX, -0.25, 0);
1889
1890
1891
                 pulse(fund, index) = pulseChooseP(fund, index, 0);
1892
                 pulseP(fund, index) = pulseChooseP(fund, index, 1);
1893
                 pulseChooseP(fund, index, p) = ((FUND(fund,align,p)-min(FUND(fund,align,p),((-1*FUND(fund
1894
                           ,align,p)+1)*(INDEX/(1-INDEX)))))*2*ma.PI):cos
1895
                    INDEX = index:min(0.99):max(0);
1896
                    align = si.interpolate(index, -0.25, 0.0);
1897
1898
1899
                 sinePulse(fund, index) = sinePulseChooseP(fund, index, 0);
1900
                 sinePulseP(fund, index) = sinePulseChooseP(fund, index, 1);
1901
                 sinePulseChooseP(fund, index, p) = (min(FUND(fund,align,p)*((0.5-INDEX)/INDEX),(-1*FUND(
1902
                           fund,align,p)+1)*((.5-INDEX)/(1-INDEX)))+FUND(fund,align,p))*4*ma.PI:cos
1903
                 with {
                    INDEX = ((index*-0.49)+0.5);
1904
                    align = si.interpolate(index, -0.125, -0.25);
1905
1906
1907
                 halfSine(fund, index) = halfSineChooseP(fund, index, 0);
1908
                 halfSineP(fund, index) = halfSineChooseP(fund, index, 1);
1909
                 \label{eq:halfSineChooseP(fund, index, p) = (select2(FUND(fund, align, p) < .5, .5*(FUND(fund, align, p) < .5*(FUND(fund, p) < .5*(FUND(fund, p) < .5*(FUND(fund, p) < .5*(FUND(fund, p) < .5*(FUND(f
1910
                           -.5)/INDEX+.5, FUND(fund, align, p)):min(1))*2*ma.PI:cos
1911
1912
                    INDEX = (.5-(index*0.5)):min(.5):max(.01):
                    align = si.interpolate(index:min(0.975), -0.25, -0.5);
```

```
};
1914
1915
                   FUND =
1916
                      case {
1917
                          (fund,align,0) => fund;
1918
                          (fund,align,1) => (fund+align) : ma.frac; // align phase with fund
1919
1920
                   resSaw(fund,res) = (((-1*(1-fund))*((cos((ma.decimal((max(1,res)*fund)+1))*2*ma.PI)*-.5)) + ((-1*(1-fund))*((cos((ma.decimal((max(1,res)*fund)+1))*2*ma.PI)*-.5)) + ((-1*(1-fund))*((cos((ma.decimal((max(1,res))*fund)+1))*-.5)) + ((-1*(1-fund))*((cos((ma.decimal((max(1,res))*fund)+1))*-.5) + ((-1*(1-fund))*((-1*(1-fund))*((-1*(1-fund))*-.5)) + ((-1*(1-fund))*((-1*(1-fund))*((-1*(1-fund))*-.5)) + ((-1*(1-fund))*((-1*(1-fund))*-.5) + ((-1*(1-fund))*((-1*(1-fund))*-.5) + ((-1*(1-fund))*-.5) + ((-1*(1-fund))*((-1*(1-fund))*-.5) + ((-1*(1-fund))*-.5) + ((-1*(1-fund))*-.5) + ((-1*(1-fund))*-.5) + ((-1*(1-fund))*-.5) + ((-1*(1-fund))*-.5) + ((-1*(1-fund)))*-.5) + ((-1*(1-fund))*-.5) + (
1921
                              +.5))*2)+1:
                   resTriangle(fund,res) = select2(fund<.5, 2-(fund*2), fund*2)*INDEX*2-1</pre>
1922
1923
                   with {
                     INDEX = ((fund*(res:max(1)))+1:ma.decimal)*2*ma.PI:cos*.5+.5;
1924
                   }:
1925
                   resTrap(fund, res) = (((1-fund)*2):min(1)*sin(ma.decimal(fund*(res:max(1)))*2*ma.PI));
1926
           };
1927
1928
            1929
1930
1931
            //-----'(os.)polyblep'-----
1932
            // PolyBLEP residual function, used for smoothing steps in the audio signal.
1933
           // #### Usage
1934
1935
            // ...
1936
1937
           // polyblep(Q,phase) : _
1938
           11
1939
           //
1940
           // Where:
1941
           // * 'Q': smoothing factor between 0 and 0.5. Determines how far from the ends of the phase
                      interval the quadratic function is used.
           // * 'phase': normalised phase (between 0 and 1)
1944
           declare polyblep author "Jacek Wieczorek";
1945
1947
           polyblep(Q, phase) = (0, L(phase / Q), R((phase - 1) / Q)) : select3(sel)
1948
                  sel = (phase < Q) + 2*(phase > 1 - Q);
1949
                  L(x) = 2*x - x*x - 1; // Used near the left end of the interval
1950
1951
                  R(x) = 2*x + x*x + 1; // Used near the right end of the interval
1952
1953
            //----'(os.)polyblep_saw'-----
1954
            // Sawtooth oscillator with suppressed aliasing (using 'polyblep').
1955
1956
           // #### Usage
1957
1958
           11 ...
1959
           // polyblep_saw(freq) : _
1960
           //
1961
1962
           // Where:
1963
1964
           // * 'freq': frequency in Hz
1965
1966
           declare polyblep_saw author "Jacek Wieczorek";
1967
1968
           polyblep_saw(freq) = naive - polyblep(Q , phase)
1969
1970
           with {
                  phase = phasor(1, freq);
naive = 2 * phase - 1;
1971
1972
                 Q = freq / ma.SR;
1973
1974
1975
            //----'(os.)polyblep_square'-----
1976
1977
           // Square wave oscillator with suppressed aliasing (using 'polyblep').
1978
          // #### Usage
1979
```

```
1980
1981
     // polyblep_square(freq) : _
1982
1983
     11
1984
     // Where:
1985
1986
     // * 'freq': frequency in Hz
1987
1988
     declare polyblep_square author "Jacek Wieczorek";
1989
1990
     polyblep\_square(freq) = naive - polyblep(Q, phase) + polyblep(Q, ma.modulo(phase + 0.5, 1))
1991
1992
     with {
        phase = phasor(1, freq);
naive = 2 * (phase * 2 : int) - 1;
1993
1994
        Q = freq / ma.SR;
1995
     };
1996
1997
     //----'(os.)polyblep_triangle'-----
1998
1999
     // Triangle wave oscillator with suppressed aliasing (using 'polyblep').
2000
     // #### Usage
2001
     // ...
2002
2003
2004
     // polyblep_triangle(freq) : \_
2005
     11
2006
2007
     // Where:
2008
     // * 'freq': frequency in Hz
2009
     declare polyblep_triangle author "Jacek Wieczorek";
     polyblep_triangle(freq) = polyblep_square(freq) : fi.pole(0.999) : *(4 * freq / ma.SR);
2013
     // end further contributions section
     2016
```

Listing 4: maths.lib

```
// Mathematic library for Faust. Its official prefix is 'ma'.
2
   11
3
   // #### References
   // * <https://github.com/grame-cncm/faustlibraries/blob/master/maths.lib>
   // Some functions are implemented as Faust foreign functions of 'math.h' functions
   /\!/ that are not part of Faust's primitives. Defines also various constants and several
   // utilities.
10
   11
   // ## History
12
   //* 06/13/2016 [RM] normalizing and integrating to new libraries
13
   //* 07/08/2015 [YO] documentation comments
14
   // * 20/06/2014 [SL] added FTZ function
16
   // * 22/06/2013 [YO] added float/double/quad variants of some foreign functions
17
   // * 28/06/2005 [YO] postfixed functions with 'f' to force float version instead of double
   //*28/06/2005 [YO] removed 'modf' because it requires a pointer as argument
20
   21
   ************************************
   FAUST library file
   Copyright (C) 2003-2016 GRAME, Centre National de Creation Musicale
24
```

```
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25
    it under the terms of the GNU Lesser General Public License as
27
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    License, or (at your option) any later version.
28
29
    This program is distributed in the hope that it will be useful,
30
    but WITHOUT ANY WARRANTY; without even the implied warranty of
31
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32
    GNU Lesser General Public License for more details.
33
34
   You should have received a copy of the GNU Lesser General Public License along with the GNU C Library; if not, write to the Free Software Foundation, Inc., 59 Temple Place, Suite 330, Boston, MA
35
36
37
    02111-1307 USA.
38
39
    EXCEPTION TO THE LGPL LICENSE : As a special exception, you may create a
40
41
    larger FAUST program which directly or indirectly imports this library
42
    file and still distribute the compiled code generated by the FAUST
43
    compiler, or a modified version of this compiled code, under your own
44
    copyright and license. This EXCEPTION TO THE LGPL LICENSE explicitly
45
    grants you the right to freely choose the license for the resulting
46
    compiled code. In particular the resulting compiled code has no obligation
47
    to be LGPL or GPL. For example you are free to choose a commercial or
48
    closed source license or any other license if you decide so.
49
    50
    52
    // This library contains platform specific constants
53
   pl = library("platform.lib");
    ma = library("maths.lib"); // for compatible copy/paste out of this file
    declare name "Faust Math Library";
57
    declare version "2.8.0";
    declare author "GRAME";
    declare copyright "GRAME";
    declare license "LGPL with exception";
61
62
    //======Functions Reference=======
63
64
65
    //-----'(ma.)SR'-----
66
    // Current sampling rate given at init time. Constant during program execution.
67
68
    // #### Usage
69
70
   11 ...
71
   // SR : _
72
    11 ...
73
    //----
74
75
    SR = pl.SR:
76
                             -----'(ma.)T'----
77
    // Current sample duration in seconds computed from the sampling rate given at init time.
78
         Constant during program execution.
79
    // #### Usage
80
81
    11
   11 ...
82
    // T :
83
84
    //----
85
   T = 1.0 / SR:
86
87
    //-----'(ma.)BS'-----
88
89
    // Current block-size. Can change during the execution at each block.
90
   // #### Usage
```

```
//
92
    11 ...
93
    // BS :
94
    11 000
95
    //----
96
    BS = pl.BS;
97
98
99
    //-----'(ma.)PI'-----
100
    // Constant PI in double precision.
101
102
    // #### Usage
103
    // ...
104
105
    // PI : _
106
107
    //----
108
    PI = 3.14159265358979323846;
109
110
111
    //-----'(ma.)deg2rad'------
112
    // Convert degrees to radians.
113
    // #### Usage
115
    // ...
116
117
    // 45. : deg2rad
118
119
    //----
120
    deg2rad = _ * PI / 180.;
121
123
    //-----'(ma.)rad2deg'------
125
    // Convert radians to degrees.
126
    // #### Usage
127
    // ...
128
129
    // ma.PI : rad2deg
130
131
    //----
132
    rad2deg = _ * 180. / PI;
133
134
135
                           -----'(ma.)E'-----
136
    // Constant e in double precision.
137
138
    // #### Usage
139
    // ...
140
141
    // E : _
142
143
144
    E = 2.71828182845904523536;
145
146
147
    //-----'(ma.)EPSILON'-----
148
    // Constant EPSILON available in simple/double/quad precision,
149
    // as defined in the [floating-point standard](https://en.wikipedia.org/wiki/IEEE_754)
150
    // and [machine epsilon](https://en.wikipedia.org/wiki/Machine_epsilon), // that is smallest positive number such that '1.0 + EPSILON != 1.0'.
151
152
153
    // #### Usage
154
    // ...
155
156
    // EPSILON : _
157
    11 000
158
```

```
singleprecision EPSILON = 1.192092896e-07;
160
    doubleprecision EPSILON = 2.2204460492503131e-016;
161
    quadprecision EPSILON = 1.084202172485504434007452e-019;
162
    fixedpointprecision EPSILON = 2.2204460492503131e-016;
163
164
165
                   -----'(ma.)MIN'-----
166
    // Constant MIN available in simple/double/quad precision (minimal positive value).
167
168
    // #### Usage
169
170
    // ...
171
    // MIN : _
172
173
174
    singleprecision MIN = 1.175494351e-38;
175
    doubleprecision MIN = 2.2250738585072014e-308;
176
177
    quadprecision MIN = 2.2250738585072014e-308;
178
    fixedpointprecision MIN = 2.2250738585072014e-308;
179
180
    //-----'(ma.)MAX'-----
181
    // Constant MAX available in simple/double/quad precision (maximal positive value).
182
183
    // #### Usage
184
    11 ...
185
    // MAX : _
187
188
    singleprecision MAX = 3.402823466e+38;
    doubleprecision MAX = 1.7976931348623158e+308;
    quadprecision MAX = 1.7976931348623158e+308;
    fixedpointprecision MAX = 1.7976931348623158e+308;
193
195
     // Obsolete, kept for compatibility reasons
    INFINITY = MAX;
196
197
                           -----'(ma.)FTZ'--
198
199
    // Flush to zero: force samples under the "maximum subnormal number"
    // to be zero. Usually not needed in C++ because the architecture
200
    // file take care of this, but can be useful in JavaScript for instance.
201
202
    // #### Usage
203
    //
204
205
    // _ : FTZ : _
206
207
    11
208
    // #### Reference
209
210
    // <http://docs.oracle.com/cd/E19957-01/806-3568/ncg_math.html>
211
212
    FTZ(x) = x * (abs(x) > MIN);
213
214
215
    //-----'(ma.)copysign'------
216
    // Changes the sign of x (first input) to that of y (second input).
217
218
    // #### Usage
219
220
    11 ...
221
    //_,_ : copysign : _
// '''
222
223
    //-----
224
225
    copysign = ffunction(float copysign|copysign|copysignl (float, float), <math.h>,"");
226
```

```
-----'(ma.)neg'-----
228
    // Invert the sign (-x) of a signal.
229
230
    // #### Usage
231
   // ...
232
233
   //_: neg:_
234
235
    //----
236
237
    neg(x) = -x;
238
239
    //-----'(ma.)not'-----
240
    // Bitwise 'not' implemented with [xor](https://faustdoc.grame.fr/manual/syntax/#xor-
241
       primitive) as 'not(x) = x xor -1;'.
    // So working regardless of the size of the integer, assuming negative numbers in two's
242
       complement.
243
    // #### Usage
244
245
    // ...
246
   // _ : not : _
247
248
    //----
249
    not(x) = x xor -1;
250
251
253
   //-----'(ma.)sub(x,y)'-----
254
   // Subtract 'x' and 'y'.
    // #### Usage
256
257
    11 ...
258
    //_,_ : sub : _
259
    //----
261
    sub(x,y) = y-x;
262
263
264
265
    //-----'(ma.)inv'-----
   // Compute the inverse (1/x) of the input signal.
266
267
    // #### Usage
268
   // ...
269
270
   // _ : inv : _
271
272
    //----
273
    inv(x) = 1/x;
274
275
276
                      -----'(ma.)cbrt'---
277
    \ensuremath{//} Computes the cube root of of the input signal.
278
279
    // #### Usage
280
   // ...
281
   // _ : cbrt : _
282
283
284
    //----
285
    cbrt = ffunction(float cbrtf|cbrt|cbrtl (float), <math.h>,"");
286
287
288
    //-----'(ma.)hypot'-----
289
    // Computes the euclidian distance of the two input signals
290
   // sqrt(x*x+y*y) without undue overflow or underflow.
291
292
   // #### Usage
293
```

```
294
295
296
297
298
    hypot = ffunction(float hypotf|hypot|hypotl (float, float), <math.h>,"");
299
300
301
    //-----'(ma.)ldexp'-----
302
    // Takes two input signals: x and n, and multiplies x by 2 to the power n.
303
304
    // #### Usage
305
306
    11 ...
307
    // _,_ : ldexp : _
308
309
310
    ldexp = ffunction(float ldexpf|ldexp|ldexpl (float, int), <math.h>,"");
311
312
313
    //-----'(ma.)scalb'-----
314
    // Takes two input signals: \boldsymbol{x} and \boldsymbol{n}, and multiplies \boldsymbol{x} by 2 to the power \boldsymbol{n}.
315
316
    // #### Usage
317
318
    11
319
321
    //-----
322
    \verb|scalb| = ffunction(float scalbnf|scalbn|scalbnl (float, int), <math.h>, ""); \\
    //-----'(ma.)log1p'------
    // Computes log(1 + x) without undue loss of accuracy when x is nearly zero.
327
    // #### Usage
329
    // ...
330
331
    // _ : log1p : _
332
333
    //----
334
    log1p = ffunction(float log1pf|log1p|log1pl (float), <math.h>,"");
335
336
337
    //-----'(ma.)logb'-----
338
    // Return exponent of the input signal as a floating-point number.
339
340
    // #### Usage
341
    11
342
    11 ...
343
    // _ : logb : _
344
345
346
    logb = ffunction(float logbf|logb|logbl (float), <math.h>,"");
347
348
349
    //-----'(ma.)ilogb'-----
350
    // Return exponent of the input signal as an integer number.
351
352
    // #### Usage
353
354
    11 ...
355
    // _ : ilogb : _
// '''
356
357
358
359
    ilogb = ffunction(int ilogbf|ilogb|ilogbl (float), <math.h>,"");
360
```

```
//----·(ma.)log2'-----
362
    // Returns the base 2 logarithm of x.
363
364
    // #### Usage
365
366
    11 ...
367
    // _ : log2 : _
368
369
370
    log2(x) = log(x)/log(2.0);
371
372
373
    //-----'(ma.)expm1'-----
374
    // Return exponent of the input signal minus 1 with better precision.
375
376
    // #### Usage
377
378
    //
    11 ...
379
380
381
    //----
382
383
    expm1 = ffunction(float expm1f|expm1|expm1l (float), <math.h>,"");
384
385
    //-----'(ma.)acosh'-----
386
    // Computes the principle value of the inverse hyperbolic cosine
387
388
    // of the input signal.
389
    // #### Usage
390
    // ...
392
394
395
    acosh = ffunction(float acoshf|acosh|acoshl (float), <math.h>, "");
398
    //-----'(ma.)asinh'-----
399
    // Computes the inverse hyperbolic sine of the input signal.
400
401
    // #### Usage
402
    // ...
403
404
    // _ : asinh : _
// '''
405
406
    //----
407
    asinh = ffunction(float asinhf|asinh|asinhl (float), <math.h>, "");
408
409
410
    //-----'(ma.)atanh'-----
411
    // Computes the inverse hyperbolic tangent of the input signal.
412
413
    // #### Usage
414
    // ...
415
416
    // _ : atanh : _
// '''
417
418
419
    atanh = ffunction(float atanhf|atanh|atanhl (float), <math.h>, "");
420
421
422
    //-----'(ma.)sinh'-----
423
    // Computes the hyperbolic sine of the input signal.
424
425
    // #### Usage
426
    // ...
427
428
429 // _ : sinh : _
```

```
430
431
    sinh = ffunction(float sinhf|sinh|sinhl (float), <math.h>, "");
432
433
434
    //-----'(ma.)cosh'-----
435
    // Computes the hyperbolic cosine of the input signal.
436
437
    // #### Usage
438
439
    11 ...
440
    // _ : cosh : _
// '''
441
442
443
    cosh = ffunction(float coshf|cosh|coshl (float), <math.h>, "");
444
445
446
    //-----'(ma.)tanh'-----
447
    // Computes the hyperbolic tangent of the input signal.
448
449
    // #### Usage
450
    // ...
451
452
    // _ : tanh : _
453
454
    //----
455
456
    tanh = ffunction(float tanhf|tanh|tanhl (float), <math.h>,"");
457
459
    //-----'(ma.)erf'-----
    // Computes the error function of the input signal.
    // #### Usage
462
463
    // ...
464
    // _ : erf : _
// '''
465
466
    //----
467
    erf = ffunction(float erff|erf|erfl(float), <math.h>,"");
468
470
    //-----'(ma.)erfc'------
471
    // Computes the complementary error function of the input signal.
472
473
    // #### Usage
474
    // ...
475
476
    // _ : erfc : _
// '''
477
478
    //----
479
480
    erfc = ffunction(float erfcf|erfc|erfcl(float), <math.h>,"");
481
482
    //-----'(ma.)gamma'----
483
    // Computes the gamma function of the input signal.
484
485
    // #### Usage
486
    // ...
487
488
    //_: gamma:_
489
490
    //-----
491
    gamma = ffunction(float tgammaf|tgamma|tgammal(float), <math.h>,"");
492
493
494
    //-----'(ma.)lgamma'-----
495
    // Calculates the natural logorithm of the absolute value of
496
497 // the gamma function of the input signal.
```

```
498
    // #### Usage
499
500
    //
    11 ...
501
    // _ : lgamma : _
// '''
502
503
    //----
504
    lgamma = ffunction(float lgammaf|lgamma|lgammal(float), <math.h>,"");
505
506
507
    //-----(ma.)J0'-----
508
    509
    // of the input signal.
510
511
    // #### Usage
512
513
    11 ...
514
   // _ : JO : _
515
516
    //-----
517
    J0 = ffunction(float j0(float), <math.h>,"");
518
519
520
    //-----'(ma.)J1'-----
521
   // Computes the Bessel function of the first kind of order 1
522
    // of the input signal.
523
524
    // #### Usage
525
526
    11
    // ...
528
    ..
//-----
531
    J1 = ffunction(float j1(float), <math.h>,"");
533
                           -----'(ma.)Jn'-----
534
    // Computes the Bessel function of the first kind of order n
535
    // (first input signal) of the second input signal.
536
537
    // #### Usage
538
    // ...
539
540
    //_,_ : Jn : _
541
542
    //----
543
    Jn = ffunction(float jn(int, float), <math.h>,"");
544
545
546
                          -----'(ma.)YO'-----
547
    // Computes the linearly independent Bessel function of the second kind
548
    // of order 0 of the input signal.
549
550
    // #### Usage
551
    11
552
    11 ...
553
    // _ : YO : _
554
555
556
    Y0 = ffunction(float y0(float), <math.h>,"");
557
558
559
                           -----'(ma.)Y1'-----
560
    // Computes the linearly independent Bessel function of the second kind
561
    // of order 1 of the input signal.
562
    //
563
    // #### Usage
564
   11
```

```
566
    // _ : YO : _
567
568
569
    Y1 = ffunction(float y1(float), <math.h>,"");
570
571
572
    //-----'(ma.) Yn '-----
573
    // Computes the linearly independent Bessel function of the second kind
574
    // of order n (first input signal) of the second input signal.
575
576
    // #### Usage
577
    // ...
578
579
    // _,_ : Yn : _
580
581
    //----
582
    Yn = ffunction(float yn(int, float), <math.h>,"");
583
584
585
    //----'(ma.)fabs', '(ma.)fmax', '(ma.)fmin
586
    // Just for compatibility...
587
    // //
588
589
    // fabs = abs
590
    // fmax = max
591
592
    // fmin = min
593
    //----
    fabs = abs;
    fmax = max;
    fmin = min;
    //-----'(ma.)np2'-----
    // Gives the next power of 2 of x.
601
    // #### Usage
602
603
604
    // np2(n) : _
605
606
607
608
    // Where:
609
    // * 'n': an integer
610
611
    np2 = -(1) <: >>(1)|_ <: >>(2)|_ <: >>(4)|_ <: >>(8)|_ <: >>(16)|_ : +(1);
612
613
614
    //-----'(ma.)frac'-----
615
    // Gives the fractional part of n.
616
617
    // #### Usage
618
    11
619
    11 ...
620
    // frac(n) : _
621
    11 000
622
    11
623
    // Where:
624
625
    // * 'n': a decimal number
626
627
    frac(n) = n - floor(n);
decimal = frac;
628
629
630
    // NOTE: decimal does the same thing as frac but using floor instead. JOS uses frac a lot
631
632 // in filters.lib so we decided to keep that one... decimal is declared though for
```

```
// backward compatibility.
633
    // decimal(n) = n - floor(n);
634
635
636
                     -----'(ma.)modulo'-----
637
    // Modulus operation using the '(x/y+y)/y' formula to ensures the result is always non-
638
        negative, even if 'x' is negative.
639
    // #### Usage
640
    //
641
    // "
642
    // modulo(x,y) : _
643
    11
644
    //
645
    // Where:
646
647
    // * 'x': the numerator
648
    // * 'y': the denominator
649
650
651
    modulo(x,y) = (x % y + y) % y;
652
653
    //----'(ma.)isnan'-----
654
    // Return non-zero if x is a NaN.
655
656
    // #### Usage
657
    // ...
658
659
660
    // _ : isnan : _
// '''
    // isnan(x)
663
    // Where:
664
665
    // * 'x': signal to analyse
666
    isnan = ffunction(int isnanf|isnan|isnanl (float), <math.h>,"");
668
669
670
671
    //----'(ma.)isinf'-----
    // Return non-zero if x is a positive or negative infinity.
672
673
    // #### Usage
674
    // ...
675
676
    // isinf(x)
677
    // _ : isinf : _
678
679
    //
680
    // Where:
681
682
    // * 'x': signal to analyse
683
684
    isinf = ffunction(int isinff|isinf|isinfl (float), <math.h>,"");
685
686
    nextafter = ffunction(float nextafter(float, float), <math.h>, "");
687
688
689
    //-----'(ma.)chebychev'-----
690
    // Chebychev transformation of order {\tt N.}
691
692
    // #### Usage
693
    11
694
    11 ...
695
    // _ : chebychev(N) : _
// '''
696
697
    //
698
   // Where:
699
```

```
700
     // * 'N': the order of the polynomial, a constant numerical expression
701
702
     // #### Semantics
703
704
     11 ...
705
     // T[0](x) = 1,
706
     // T[1](x) = 1,

// T[1](x) = x,

// T[n](x) = 2x*T[n-1](x) - T[n-2](x)

// '''
707
708
709
710
     // #### Reference
711
     11
712
     // <http://en.wikipedia.org/wiki/Chebyshev_polynomial>
713
714
     chebychev(0,x) = 1;
715
     chebychev(1,x) = x;
716
     chebychev(n,x) = 2*x*chebychev(n-1, x) - chebychev(n-2, x);
717
718
719
     //-----'(ma.)chebychevpoly'-----
720
     // Linear combination of the first Chebyshev polynomials.
721
722
     // #### Usage
723
    // ...
724
    // _ : chebychevpoly((c0,c1,...,cn)) : _
// '''
725
726
727
    //
// Where:
728
729
     // * 'cn': the different Chebychevs polynomials such that:
732
     // chebychevpoly((c0,c1,...,cn)) = Sum of chebychev(i)*ci
733
     // #### Reference
734
735
     // <http://www.csounds.com/manual/html/chebyshevpoly.html>
736
737
     chebychevpoly(lcoef) = _ <: L(0,lcoef) :> _
738
739
        with {
         L(n,(c,cs)) = chebychev(n)*c, L(n+1,cs);
740
           L(n,c) = chebychev(n)*c;
741
742
743
744
     //----'(ma.)diffn'---
745
     // Negated first-order difference.
746
747
     // #### Usage
748
749
750
    // _ : diffn : _
// '''
751
752
753
     diffn(x) = x' - x; // negated first-order difference
754
755
756
     //----'(ma.)signum'-----
757
     // The signum function signum(x) is defined as
758
     // -1 for x<0, 0 for x==0, and 1 for x>0.
759
760
     // #### Usage
761
     //
762
    11 ...
763
    // _ : signum : _
// '''
764
765
766
    signum(x) = (x>0)-(x<0);
```

```
768
769
          -----'(ma.)nextpow2'-----
770
    // The nextpow2(x) returns the lowest integer m such that
771
    // 2^m >= x.
772
    //
773
    // #### Usage
774
    //
775
    // "
776
    // 2^nextpow2(n) : _
777
778
    /\!/ Useful for allocating delay lines, e.g.,
779
780
    // delay(2^nextpow2(maxDelayNeeded), currentDelay);
781
782
783
    nextpow2(x) = ceil(log(x)/log(2.0));
784
785
786
    //----·'(ma.)zc'-----
787
    // Indicator function for zero-crossing: it returns 1 if a zero-crossing
788
789
    // occurs, 0 otherwise.
790
    // #### Usage
791
    // ...
792
793
794
795
    //-----
796
797
    zc(x) = x * x' < 0;
800
    //-----'(ma.)primes'-----
    // Return the n-th prime using a waveform primitive. Note that primes(0) is 2,
801
    // primes(1) is 3, and so on. The waveform is length 2048, so the largest
    // precomputed prime is primes(2047) which is 17863.
804
    // #### Usage
805
806
    // _ : primes : _
807
808
809
810
    primes(x) = rdtable(waveform{
811
    2,3,5,7,11,13,17,19,23,29,
812
    31,37,41,43,47,53,59,61,67,71,
813
    73,79,83,89,97,101,103,107,109,113,
814
    127,131,137,139,149,151,157,163,167,173,
815
    179,181,191,193,197,199,211,223,227,229,
816
    233,239,241,251,257,263,269,271,277,281,
817
    283,293,307,311,313,317,331,337,347,349,
818
    353,359,367,373,379,383,389,397,401,409,
819
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820
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823
824
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825
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841
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      14621,14627,14629,14633,14639,14653,14657,14669,14683,14699,
 984
      14713, 14717, 14723, 14731, 14737, 14741, 14747, 14753, 14759, 14767,
      14771, 14779, 14783, 14797, 14813, 14821, 14827, 14831, 14843, 14851,
 985
 986
      14867,14869,14879,14887,14891,14897,14923,14929,14939,14947,
 987
      14951,14957,14969,14983,15013,15017,15031,15053,15061,15073,
 988
      15077, 15083, 15091, 15101, 15107, 15121, 15131, 15137, 15139, 15149,
 989
      15161,15173,15187,15193,15199,15217,15227,15233,15241,15259,
      15263,15269,15271,15277,15287,15289,15299,15307,15313,15319,
      15329,15331,15349,15359,15361,15373,15377,15383,15391,15401,
      15413, 15427, 15439, 15443, 15451, 15461, 15467, 15473, 15493, 15497
 992
      15511, 15527, 15541, 15551, 15559, 15569, 15581, 15583, 15601, 15607,
      15619, 15629, 15641, 15643, 15647, 15649, 15661, 15667, 15671, 15679,
      15683, 15727, 15731, 15733, 15737, 15739, 15749, 15761, 15767, 15773,
 995
      15787,15791,15797,15803,15809,15817,15823,15859,15877,15881,
      15887, 15889, 15901, 15907, 15913, 15919, 15923, 15937, 15959, 15971,
      15973,15991,16001,16007,16033,16057,16061,16063,16067,16069,
      16073,16087,16091,16097,16103,16111,16127,16139,16141,16183,
      16187,16189,16193,16217,16223,16229,16231,16249,16253,16267,
1000
      16273,16301,16319,16333,16339,16349,16361,16363,16369,16381,
      16411,16417,16421,16427,16433,16447,16451,16453,16477,16481,
      16487,16493,16519,16529,16547,16553,16561,16567,16573,16603,
      16607, 16619, 16631, 16633, 16649, 16651, 16657, 16661, 16673, 16691,
      16693,16699,16703,16729,16741,16747,16759,16763,16787,16811,
1005
      16823,16829,16831,16843,16871,16879,16883,16889,16901,16903,
1007
      16921,16927,16931,16937,16943,16963,16979,16981,16987,16993,
      17011,17021,17027,17029,17033,17041,17047,17053,17077,17093,
1008
      17099,17107,17117,17123,17137,17159,17167,17183,17189,17191,
1009
      17203,17207,17209,17231,17239,17257,17291,17293,17299,17317,
1010
      17321,17327,17333,17341,17351,17359,17377,17383,17387,17389,
      17393,17401,17417,17419,17431,17443,17449,17467,17471,17477,
1012
1013
      17483,17489,17491,17497,17509,17519,17539,17551,17569,17573,
      17579,17581,17597,17599,17609,17623,17627,17657,17659,17669,
1014
      17681, 17683, 17707, 17713, 17729, 17737, 17747, 17749, 17761, 17783,
1015
      17789,17791,17807,17827,17837,17839,17851,17863
1016
      }, x);
1017
```

Listing 5: platform.lib

```
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38
    closed source license or any other license if you decide so.
39
    ************************************
    40
    declare name "Generic Platform Library";
43
    declare version "1.3.0";
    //----·(p1.)SR'-----
    // Current sampling rate (between 1 and 192000Hz). Constant during
    // program execution. Setting this value to a constant will allow the
    \ensuremath{/\!/} compiler to optimize the code by computing constant expressions at
    // compile time, and can be valuable for performance, especially on
    // embedded systems.
51
    SR = min(192000.0, max(1.0, fconstant(int fSamplingFreq, <math.h>)));
52
53
                           -----'(p1.)BS'---
54
55
    // Current block-size (between 1 and 16384 frames). Can change during the execution.
56
57
    BS = min(16384.0, max(1.0, fvariable(int count, <math.h>)));
58
                   -----'(pl.)tablesize'-----
59
    // Oscillator table size. This value is used to define the size of the
60
    // table used by the oscillators. It is usually a power of 2 and can be lowered
61
    // to save memory. The default value is 65536.
62
63
    tablesize = 1 << 16;
```