We model the absorbtion via the following cascading compartmental decay model.

$$X_a \xrightarrow{k_a X_a} X \xrightarrow{KX}$$

The initial amounts are given by  $X_a(0) = FX_0$  and X(0) = 0, where F is the fraction of the drug absorbed by the mouse and  $X_0$  is the amount administered. So, we have the following system of differential equations

$$\begin{split} \frac{dX_a}{dt} &= -k_a X_a(t), \\ \frac{dX}{dt} &= k_a X_a(t) - KX(t), \\ X_a(0) &= FX_0, \quad X(0) = 0. \end{split}$$

We wish to estimate F, the fraction of drug absobed,  $k_a$  the rate of absorption into the blood, and K the rate of dispersion from the blood.

The data recorded are in terms of concentration of the drug in the cell, if V is the average volume of the cell, is introduced and then we can reparameterize X, C(t) = X(t)/V, and the parameter.

Note that this system can be solved analytically, as it is linear,

$$\frac{d}{dt}\begin{pmatrix} X_a \\ X \end{pmatrix} = \begin{pmatrix} -k_a & 0 \\ k_a & -K \end{pmatrix} \begin{pmatrix} X_a \\ X \end{pmatrix}, \quad \begin{pmatrix} X_a(0) \\ X(0) \end{pmatrix} = \begin{pmatrix} FX_0 \\ 0 \end{pmatrix}.$$

The solution for the absorption into the blood is given by

$$X_{a}(t) = FX_{0}(k_{a}e^{-k_{a}t}),$$

$$X(t) = \frac{k_{a}FX_{0}}{k_{a} - K}(e^{-Kt} - e^{-k_{a}t}).$$

## 1 Methods

We must first fit the model. Note that We fit the parameters of the model by optimizing the function that returns a numerical solution to the differential equation.

$$C(t) = \frac{X(t)}{V} = \frac{F}{V} \cdot X_0 \cdot \frac{k_a}{k_a - K} (e^{-Kt} - e^{-k_a t}).$$

by least squares with respect to the parameters F/V,  $k_a$ , and K. However the factor  $k_a - K$  in the denomonator makes this optimization step unstable. Instead we optimize the system of differential equations, with the added scaling factor 1/V to X.

## 2 Results

95% Confidence Interval for  $K_1 - K_2 : [-0.3101, -0.2296]$ .

>> CI95\_diff\_K

 $CI95_diff_K =$ 

-0.3101 -0.2296

>> CI95\_diff\_FV

CI95\_diff\_FV =

-0.1187 0.0353

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