

Localized Driving and the Role of Thrust in Unruh Radiation

Kevin Player*

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The Unruh effect tells us that what we call particles is really just a matter of perspective.

Lee Smolin

Abstract

We analyze Unruh radiation, interpreting the radiation as sourced by a driving field. In the Rindler frame, the driving modes extend over long durations and experience redshift and blueshift due to their extended support across the wedge, leading to a mixed-frequency response interpreted thermally. To refine this picture, we construct an interpolation between these long-lived driving modes and localized wave packets with peaked Fourier spectra that do not display such frequency smearing. This allows us to reinterpret Unruh radiation in terms of thrust, a localized driving effect that excites the field without inducing a thermal response, thereby offering a complementary, nonthermal perspective on acceleration-induced radiation.

1 Introduction

We first present some notation and review the Unruh effect in section 2. We then introduce a source in section 3 that exactly captures the particle creation in the cross term of the Bogoliubov transform for Rindler modes extended to Minkowski space. In section 4, we interpolate between the eternal Rindler mode source to a more localized wave packet version, and in section 5 we interpret the results.

2 Unruh Effect Review and Notation

We draw notation and standard results from Frodden and Valdés [1].

Let $\hbar = c = 1$. We consider a uniformly accelerating observer in 1+1 dimensional Minkowski spacetime with metric signature $\eta = (-1, +1)$. The extension to 1+3 dimensions does not affect the key physics of the Unruh effect, so we restrict to the (t,x) plane where the boost occurs.

Consider the free scalar massless Lagrangian

$$\mathcal{L}_{free} = -\frac{1}{2}\eta^{\mu\nu}\partial_\mu\phi\partial_\nu\phi. \tag{1}$$

*kplaye@gmail.com

We consider positive frequency modes with dispersion relation $\omega_k = |k| > 0$ as solutions to the resulting Klein-Gordon equation

$$\square\phi = -\frac{\partial^2\phi}{\partial t^2} + \frac{\partial^2\phi}{\partial x^2} = 0, \quad (2)$$

where $\square = \eta^{\mu\nu}\partial_\mu\partial_\nu$. We expand ϕ in terms of ladder operators a_k, a_k^\dagger

$$\phi(x, t) = \int dk a_k \varphi_k(x, t) + \text{h.c.} \quad (3)$$

where

$$\varphi(x, t) = \frac{1}{\sqrt{4\pi\omega_k}} e^{i(kx - \omega_k t)}. \quad (4)$$

are pure Minkowski positive frequency waves normalized with respect to the Klein-Gordon inner product at any time slice, say $t = 0$,

$$\langle f, g \rangle_{KG} = i \int dx (f^* \partial_t g - \partial_t f^* g). \quad (5)$$

2.1 Rindler Coordinates

To describe the physics from the point of view of a uniformly accelerating observer, we introduce Rindler coordinates covering a right wedge

$$W_c = \{(x, t) : x - c > |t|\} \quad (6)$$

with apex at $(t, x) = (0, c)$. We start with $W = W_0$ which is region *I* pictured in Figure 1; with coordinates

$$t = \frac{1}{a} e^{a\xi} \sinh(a\eta) \quad (7)$$

$$x = \frac{1}{a} e^{a\xi} \cosh(a\eta) \quad (8)$$

where $a > 0$ is an acceleration parameter. The coordinates (η, ξ) describe the proper time and position in the frame of a uniformly accelerating observer, with worldlines of constant ξ corresponding to hyperbolic trajectories in Minkowski spacetime.

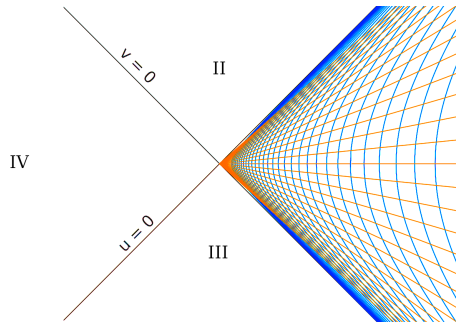


Figure 1: Rindler wedge *I* on the right.

The massless Klein-Gordon equation in Rindler coordinates is

$$\square\phi = e^{-2a\xi}(-\partial_\eta^2 + \partial_\xi^2)\phi = 0 \quad (9)$$

The wave equation retains the same structure as the Minkowski case, up to the overall conformal factor $e^{-2a\xi}$. Since this factor does not affect the null structure of the equation, the mode solutions retain the same plane wave form in the Rindler time coordinate.

$$r_k(\eta, \xi) = \frac{1}{\sqrt{4\pi\omega_k}} e^{-i(\omega_k\eta - k\xi)} + \text{h.c.} \quad (10)$$

for each wave number k and positive frequency $\omega_k = |k| > 0$. These “Rindler modes” are in terms of η and ξ and are thus confined to the Rindler wedge W . Since Rindler coordinates only cover region I (the right wedge), these modes are not defined globally in Minkowski space. This leads to an inequivalence between the Minkowski and Rindler quantizations.

2.2 Unruh Modes

For $\omega_k = k > 0$, and

$$\begin{aligned}\alpha_k &= \frac{e^{\frac{\pi\omega_k}{2a}}}{\sqrt{2 \sinh \frac{\pi\omega_k}{a}}} = \sqrt{\frac{1}{1 - e^{-2\pi\omega_k/a}}} \\ \beta_k &= \frac{e^{-\frac{\pi\omega_k}{2a}}}{\sqrt{2 \sinh \frac{\pi\omega_k}{a}}} = \sqrt{\frac{1}{e^{2\pi\omega_k/a} - 1}} \quad (\text{thermal form})\end{aligned}\tag{11}$$

noting that $\alpha_k^2 - \beta_k^2 = 1$. We analytically continue r_k, r_{-k} to the t, x plane as

$$\begin{aligned}r_{+k} &= \frac{1}{\sqrt{4\pi\omega_k}} e^{-i(\omega_k\eta - k\xi)} = \frac{1}{\sqrt{4\pi\omega_k}} (a(-t + x + i\epsilon))^{\frac{i\omega_k}{a}} \\ r_{-k} &= \frac{1}{\sqrt{4\pi\omega_k}} e^{-i(\omega_k\eta + k\xi)} = \frac{1}{\sqrt{4\pi\omega_k}} (a(-t - x + i\epsilon))^{-\frac{i\omega_k}{a}}\end{aligned}\tag{12}$$

Define also

$$\begin{aligned}\varphi_{+k} &= \frac{1}{\sqrt{4\pi\omega_k}} e^{-i(\omega_k t - kx)} \\ \varphi_{-k} &= \frac{1}{\sqrt{4\pi\omega_k}} e^{-i(\omega_k t + kx)} \\ \mu_k^R &= \alpha_k (r_k - r_{-k}^*) \\ &= \frac{e^{\frac{\pi\omega_k}{2a}}}{\sqrt{2 \sinh \frac{\pi\omega_k}{a}}} (r_k - r_{-k}^*) \\ &= \frac{1}{\sqrt{4\pi\omega_k} \sqrt{2 \sinh \frac{\pi\omega_k}{a}}} \left(e^{\frac{\pi\omega_k}{2a}} (a(-t + x + i\epsilon))^{\frac{i\omega_k}{a}} + e^{-\frac{\pi\omega_k}{2a}} (a(t + x - i\epsilon))^{\frac{i\omega_k}{a}} \right) \\ \mu_k^L &= \beta_k (r_k^* - r_{-k}) \\ &= \frac{e^{-\frac{\pi\omega_k}{2a}}}{\sqrt{2 \sinh \frac{\pi\omega_k}{a}}} (r_k^* - r_{-k}) \\ &= \frac{1}{\sqrt{4\pi\omega_k} \sqrt{2 \sinh \frac{\pi\omega_k}{a}}} \left(e^{-\frac{\pi\omega_k}{2a}} (a(-t + x + i\epsilon))^{-\frac{i\omega_k}{a}} + e^{\frac{\pi\omega_k}{2a}} (a(t + x - i\epsilon))^{-\frac{i\omega_k}{a}} \right)\end{aligned}\tag{13}$$

2.3 Bogoliubov Transforms

Let the superscripts (0) , $(0c)$, (M) etc represent frames of reference. We have a Bogoliubov transformation matrix from M to W_0 of

$$\begin{bmatrix} a_k^{(0)} \\ a_{-k}^{(0)} \\ a_k^{(0)\dagger} \\ a_{-k}^{(0)\dagger} \end{bmatrix} = \begin{bmatrix} \alpha_k & 0 & 0 & \beta_k \\ 0 & -\alpha_k & -\beta_k & 0 \\ 0 & \beta_k & \alpha_k & 0 \\ -\beta_k & 0 & 0 & -\alpha_k \end{bmatrix}_{k,q} \begin{bmatrix} c_q^R \\ c_q^L \\ c_q^{R\dagger} \\ c_q^{L\dagger} \end{bmatrix}\tag{14}$$

for a change of basis from $a^{(M)}$ to c^R and c^L

$$\phi = \int dq \mu_q^R c_q^R + \mu_q^L c_q^L + \text{h.c.}\tag{15}$$

From this we compute the usual Unruh radiation equation with Planck spectrum (compare β_k with equation (11)) to obtain

$$a_k^{(0)} = \alpha_k c_q^R + \beta_k c_q^{L\dagger}\tag{16}$$

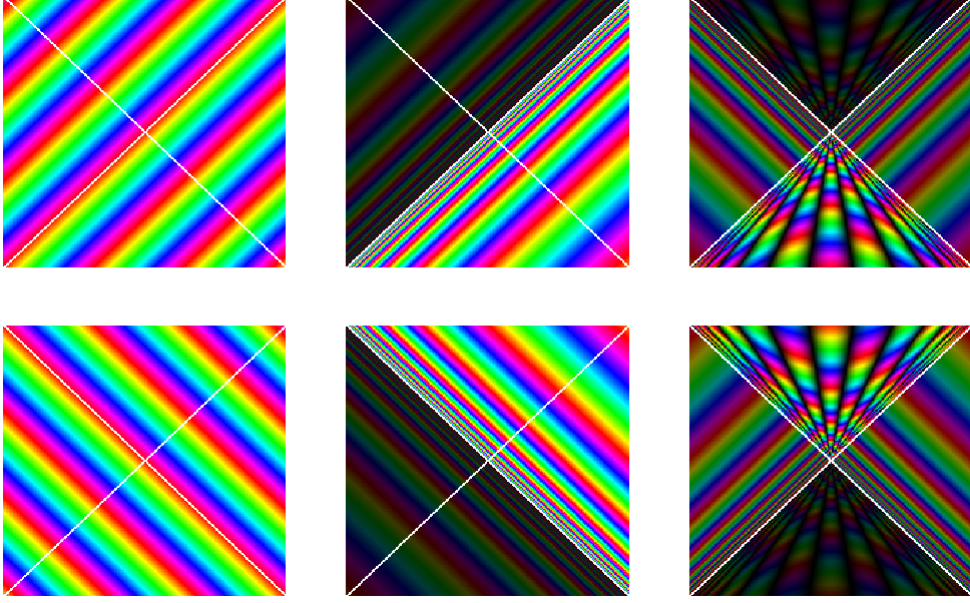


Figure 2: Space time diagrams for $\begin{bmatrix} \varphi_k & r_k & \mu_k^R \\ \varphi_{-k} & r_{-k} & \mu_k^L \end{bmatrix}$. Color represents phase; brightness shows magnitude. The consistent "rainbow" phase structure in φ_k and μ_k reflects their pure positive frequency content in Minkowski time, unlike r_k , which varies across branches. The left moving Rindler modes r_k (top) correspond to emission and the right moving mode r_{-k} (bottom) to absorption.

We compute the Bogoliubov coefficients for

$$\begin{aligned} a_k^{(c)} &= \int dq \alpha_{kq}^{(cM)} a_q^M + \beta_{kq}^{(cM)} a_q^{(M)\dagger} \\ &= \int dq \alpha_{kq}^{(c0)} a_q^{(0)} + \beta_{kq}^{(c0)} a_q^{(0)\dagger} \end{aligned} \quad (17)$$

as

$$\begin{aligned} \alpha_{kq}^{(cM)} &= \langle \varphi_q, r_k^{(c)} \rangle = \frac{1}{a\pi} \sqrt{\frac{\omega_k}{\omega_q}} \left(\frac{a}{q}\right)^{\frac{i\omega_k}{a}} e^{\frac{\pi\omega_k}{a}} \Gamma\left(\frac{i\omega_k}{a}\right) \\ \beta_{kq}^{(cM)} &= \langle \varphi_q^*, r_k^{(c)} \rangle = \frac{1}{a\pi} \sqrt{\frac{\omega_k}{\omega_q}} \left(\frac{a}{q}\right)^{\frac{-i\omega_k}{a}} e^{\frac{-\pi\omega_k}{a}} \Gamma\left(\frac{-i\omega_k}{a}\right) \\ \alpha_{kq}^{(c0)} &= \langle r_q^{(0)}, r_k^{(c)} \rangle = \frac{1}{2\pi a} \sqrt{\frac{\omega_k}{\omega_q}} (ac)^{\frac{-i(\omega_q - \omega_k)}{a}} B\left(\frac{i\omega_k}{a}, \frac{i(\omega_q - \omega_k)}{a}\right) \\ \beta_{kq}^{(c0)} &= \langle r_q^{(0)*}, r_k^{(c)} \rangle = \frac{1}{2\pi a} \sqrt{\frac{\omega_k}{\omega_q}} (ac)^{\frac{-i(\omega_q + \omega_k)}{a}} B\left(\frac{-i\omega_k}{a}, \frac{i(\omega_q + \omega_k)}{a}\right) \end{aligned} \quad (18)$$

We can compare absolute magnitudes for M v.s. W_c and see that they don't depend on q or c

$$\begin{aligned} \left| \beta_{kq}^{(c_1 M)} \right|^2 &= \left| \beta_{kq}^{(c_2 M)} \right|^2 \\ \left| \beta_{kq}^{(c_1 M)} \right|^2 &= \left| \beta_{kq}^{(c_2 M)} \right|^2 \\ \left| \beta_{kq}^{(cM)} \right|^2 / \left| \alpha_{kq}^{(cM)} \right|^2 &= e^{\frac{-2\pi\omega_k}{a}} \quad (\text{thermal factor}) \end{aligned} \quad (19)$$

The c independence is expected since Unruh radiation is translation invariant. The q independence can be strengthened as the expected number of particles in mode k

$$\int dq \left| \beta_{kq}^{(cM)} \right|^2 = \frac{e^{\frac{-2\pi\omega_k}{a}}}{2 \sinh \frac{\pi\omega_k}{a}} \int dq \frac{2}{a\pi|q|} \quad (20)$$

where we factor out the divergent part to recover the radiation equation again.

We next turn to W_c v.s. W_0 and also find c independence there

$$\begin{aligned} |\alpha_{kq}^{(0c_1)}| &= |\alpha_{kq}^{(0c_2)}| \\ |\beta_{kq}^{(0c_1)}| &= |\beta_{kq}^{(0c_2)}| \end{aligned} \quad (21)$$

$$\begin{aligned} |\beta_{kq}^{(0c)}|^2 / |\alpha_{kq}^{(0c)}|^2 &= \left| \Gamma \left(\frac{i(\omega_q + \omega_k)}{a} \right) \right|^2 / \left| \Gamma \left(\frac{i(\omega_q - \omega_k)}{a} \right) \right|^2 \\ &= \frac{(\omega_q - \omega_k) \sinh \pi(\omega_q - \omega_k)}{(\omega_q + \omega_k) \sinh \pi(\omega_q + \omega_k)} \end{aligned} \quad (22)$$

which is somewhat more surprising since this implies that $\int dq |\beta_{kq}^{(c_2 c_1)}|^2$ is a c_1 and c_2 independent factor for every shifted wedge inclusion. In other words, the expected number of particles for a mode $r_k^{(c_2)}$ of W_{c_2} in W_{c_1} 's vacuum is independent of the choice of shift c_2 and c_1 .

More explicitly we have a transform matrix of Λ_c from W_0 to W_c

$$\begin{bmatrix} a_k^{(c)} \\ a_{-k}^{(c)} \\ a_k^{(c)\dagger} \\ a_{-k}^{(c)\dagger} \end{bmatrix} = \underbrace{\begin{bmatrix} A_c & 0 & B_c & 0 \\ 0 & -A_c & 0 & -B_c \\ \overline{B_c} & 0 & \overline{A_c} & 0 \\ 0 & -\overline{B_c} & 0 & -\overline{A_c} \end{bmatrix}}_{\Lambda_c}_{k,q} \begin{bmatrix} a_q^{(0)} \\ a_{-q}^{(0)} \\ a_q^{(0)\dagger} \\ a_{-q}^{(0)\dagger} \end{bmatrix} \quad (23)$$

where $A_c = \alpha_{kq}^{(c0)} = P_c A_1 P_c^{-1}$ and $B_c = \beta_{kq}^{(c0)} = P_c B_1 P_c$ for a diagonal phase factor matrix

$$P_c = P_{c,rs} = \delta(r-s) c^{\frac{i\omega_r}{a}} = e^{\frac{iH}{a} \log c} \quad (24)$$

We can write Λ_c out compactly out as

$$\Lambda_c = Q_c \Lambda_1 Q_c^{-1} \quad (25)$$

where

$$Q_c = \begin{bmatrix} P_c & 0 & 0 & 0 \\ 0 & P_c & 0 & 0 \\ 0 & 0 & P_c^{-1} & 0 \\ 0 & 0 & 0 & P_c^{-1} \end{bmatrix} \quad (26)$$

Note that $\lim_{c \rightarrow 0} \Lambda_c = 1$ since the limit of $\lim_{c \rightarrow 0} \alpha_{kq}^{(c0)} = 1$ and $\lim_{c \rightarrow 0} \beta_{kq}^{(c0)} = 0$, which corresponds nicely to $\lim_{c \rightarrow 0} W_c = W_0$. The composition of Bogoliubov transforms, $\Lambda_{nc} = \Lambda_c^n$, yields

$$\begin{aligned} Q_{nc} \Lambda_1 Q_{nc}^{-1} &= \Lambda_{nc} \\ &= (Q_c \Lambda_c Q_c) (Q_c^{-1} \Lambda_c Q_c) \cdots (Q_c \Lambda_c Q_c) \\ &= Q_c \Lambda_c^n Q_c^{-1} \end{aligned} \quad (27)$$

so that

$$\begin{aligned} \Lambda_c^n &= Q_c^{-1} Q_{nc} \Lambda_1 Q_{nc}^{-1} Q_c \\ &= Q_n \Lambda_1 Q_n^{-1} \end{aligned} \quad (28)$$

and more generally we have a one parameter group given by

$$\{\Lambda_0^x = Q_x \Lambda_0 Q_x^{-1} : x \in \mathbb{R}\}. \quad (29)$$

These Bogoliubov transformations between shifted wedges define a one-parameter group, reflecting an underlying symmetry structure. This naturally connects to modular flow as studied in algebraic QFT, where such transformations correspond to automorphisms generated by the modular operator. This is an explicit realization of modular flow, due to the von Neumann algebra modular automorphism associated with the translation $W_0 \rightarrow$

W_c , studied in detail in Tomita-Takesaki theory [2]. There we find thermal KMS states between open set inclusions in a much more general setting.

Consider a sequence

$$W_{c_n} \subseteq \cdots \subseteq W_{c_i} \subseteq \cdots \subseteq W_{c_j} \subseteq W_{c_2} \subseteq W_{c_1} \quad (30)$$

Then each $W_{c_i} \subseteq W_{c_j}$ involves particle production with a fixed squared magnitude for mode k . We calculate this expected number of W_{c_i} particles for mode k in W_{c_j} 's vacuum

$$\langle 0_{W_{c_j}} | a_k^{(c_i)\dagger} a_k^{(c_i)} | 0_{W_{c_j}} \rangle = \frac{1}{2\pi^2 k \sinh \frac{\pi k}{a}} \int_{x=0}^{\infty} \frac{x \sinh x}{(x + \frac{\pi k}{a}) \sinh(x + \frac{\pi k}{a})} \quad (31)$$

which diverges. The integrand goes to $e^{-\frac{\pi k}{a}}$ as x gets large, so we can see that the expected number of particles in ratio goes to

$$\frac{1}{m(e^{2m} + 1)} = \frac{1}{k(e^{\frac{2\pi\omega_k}{a}} - 1)}. \quad (32)$$

3 Driving Sources

We now ask a fundamental question: “**What exactly is accelerating the observer?**” Until this point, we’ve treated acceleration as a coordinate choice, without invoking any underlying physical mechanism. We have also not specified the observer’s precise location within the Rindler wedge, nor the spatial origin of the observed excitations. These ambiguities reflect the effective coarse-graining over the observer’s details, a feature that contributes to the thermal character of the Unruh effect.

Figure 3 illustrates the situation for a sharply peaked frequency wave packet made of Rindler modes. The modes r_k are left-moving, propagating toward the future horizon and are interpreted as **emission**. The r_{-k} modes are right-moving, originating from the past horizon and are interpreted as **absorption**. The Rindler modes are constructed as superpositions of Minkowski modes φ_q , effectively smeared over a range of frequencies. This is visually evident in Figure 2, where the local frequencies increase (blue-shift) near the horizons. This is made explicitly by the Bogoliubov coefficients $\alpha_{kq}^{(cM)}$ and $\beta_{kq}^{(cM)}$ which encode the Fourier decomposition of the Rindler modes through their Klein-Gordon inner products with the Minkowski modes φ_q and φ_q^* , respectively. This frequency delocalization, tied to the observer’s acceleration horizon, underlies the apparent thermal character of the radiation.

To address this, we introduce a driving source, a physical mechanism responsible for the field’s excitation and, indirectly, for the observer’s acceleration. This reframes the interpretation: the radiation is not spontaneous but instead emerges as a coherent response to the source. The apparent thermality, then, is tied to our ignorance of the source’s detailed structure.

We aim to encode the effect of a creation operator by introducing a source term $J(x)$ into the Lagrangian at some distant time in the past, which directly excites the field in a specific mode. Since $J(x)$ couples linearly, it prepares a coherent state that excites the chosen mode in a controlled, phase-coherent manner. To replicate the action of a creation operator, the source must be engineered such that its overlap with the mode functions $u_k(x)$ matches the operator’s action on the field.

The field can be expanded as in equation (15), and the β_k -term in equation (16) is responsible for the thermal particle content of the Minkowski vacuum as seen by Rindler observers. Without loss of generality¹, we encode the effect of a creation operator $c_k^{L\dagger}$

¹We only consider a fixed frequency and the L -mode, and extend the argument linearly to any positive frequency Minkowski modes.

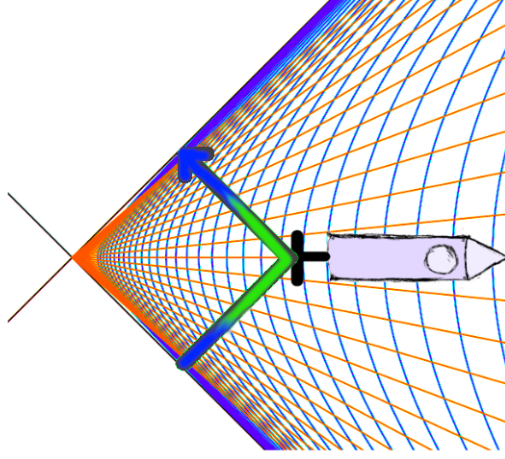


Figure 3: A Rindler mode's frequency is smeared out in Minkowski space, blue-shifted near the horizon. We diagram a particle as if it were striking a mirror at the rear of a rocket, where its reflection emerges as a combination of emission and absorption processes in the Rindler frame.

using

$$c_k^{L\dagger} = \langle \phi, \mu_k^{L*} \rangle_{KG} = \int dx \mu_k^{L*}(x) \phi(x) \quad (33)$$

and the orthogonality of the mode functions in the Klein-Gordon inner product. In the generating functional formalism, setting $J_k^L(x) = -\beta_k u_k^{L*}$ the functional derivative $\frac{\delta}{\delta J_k^L} Z[J_k^L]|_{J_k^L=0}$ inserts ϕ into time-ordered correlators. Smearing this field insertion against $\mu_k^{L*}(x)$ thus projects onto $c_k^{L\dagger}$ and we have²

$$\begin{aligned} a_k^{(0)J} &= \alpha_k c_q^R + \beta_k c_q^{L\dagger} - \beta_k c_q^{L\dagger} \\ &= \alpha_k c_q^R \end{aligned} \quad (34)$$

In Rindler coordinates, this source term prepares a modified field state in which the Rindler mode occupation differs from the thermal distribution of the Minkowski vacuum. Rather than simply adding energy, the source introduces a coherent excitation that cancels the mode structure induced by the Bogoliubov β -terms, effectively replacing their contribution. This lets us construct a state where the Rindler response is vacuum-like for mode k

$$\langle J_k^L | b_k^\dagger b_k | J_k^L \rangle = \langle 0_M | b_k^{J_k^L\dagger} b_k^{J_k^L} | 0_M \rangle = 0 \quad (35)$$

4 Localization

Consider the two wedges W_0 and W_c shown in Figure 4. The grayscale part is the Rindler mode r_q of W_0 (analytically continued to M). The rainbow piece is r_q restricted to W_c . This restriction is missing the higher frequencies of r_q that occur near the future event horizon³.

We have somewhat localized r_q by considering its restriction to W_c . The localization is not complete, the observer can still be anywhere within the wedge W_c , but we have at

²The remaining α_k factor reflects the mismatch between the squeezed Unruh vacuum and the coherent state prepared by the source.

³The same thing happens for r_{-q} but with the past event horizon instead.

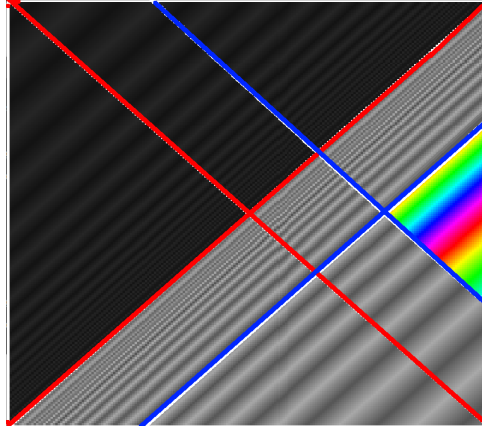


Figure 4: A Wedge W_c (blue) inside of the wedge W_0 (red). Rindler mode r_q of W_0 (grayscale) restricted to W_c (rainbow).

least isolated it from the wild oscillations of r_q near the W_0 horizons. To further study the situation, consider $\alpha_{kq}^{(c0)}$ from equation (18). We fix q and find that

$$\left| \left\langle r_q^{(0)}, r_k^{(c)} \right\rangle \right|^2 = \frac{\sinh \frac{\pi \omega_q}{a}}{4\pi a \sinh \frac{\pi \omega_k}{a} (\omega_q - \omega_k) \sinh \frac{\omega_q - \omega_k}{a}} \quad (36)$$

See Figure 5, where we now find a peaked response at $\omega_k = \omega_q$. We still find the thermal term from before $\sinh \frac{\pi \omega_k}{a}$ contributing a spread near $\omega_k = 0$ and the $(\omega_q - \omega_k) \sinh \frac{\omega_q - \omega_k}{a}$ near the peak at $\omega_k = \omega_q$, but the large scale peaked response itself is due to the localization.

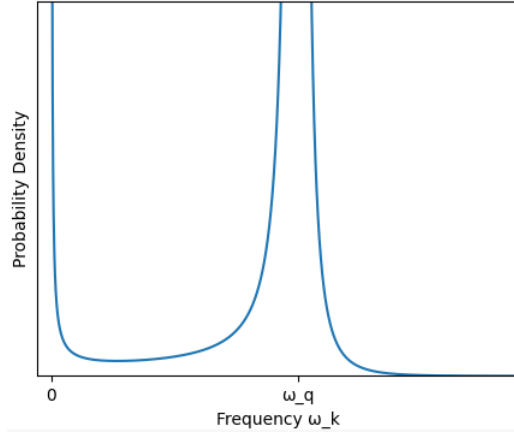


Figure 5: The Rindler modes r_k of W_c have peaked spectral response to r_q at $\omega_k = \omega_q$.

5 Appendix Formulas

Some useful formula

$$\int_c^\infty x^a (x - c)^b dx = c^{a+b+1} B(b+1, -a-b-1) \quad (37)$$

TODO, check this next one

$$\int_{-\infty}^\infty e^{ikx} x^b dx = -\frac{2i}{k^{b+1}} e^{\frac{-\pi b}{2}} \Gamma(b+1) \quad (38)$$

This is useful for the shifted wedge inner products. Let

$$f_{k,b,d} = (a(b(t - i\epsilon) + x))^{\frac{id\omega_k}{a}} \quad (39)$$

Then

$$\langle f_{k,b_k,d_k}, f_{q,d_q,d_q} \rangle = \frac{1}{2\pi} \sqrt{\frac{\omega_k}{\omega_q}} (ac)^{\frac{i(d_k\omega_k - d_q\omega_q)}{a}} \left((-d_k) \frac{b_k + b_q}{2} \right) B \left(\frac{id_k\omega_k}{a}, \frac{-i(d_k\omega_k - d_q\omega_q)}{a} \right) \quad (40)$$

We frequently use

$$|\Gamma(ib)|^2 = \frac{\pi}{b \sinh \pi b} \quad (41)$$

6 Conclusion and Prediction

If the thrust required to accelerate a detector is not explicitly accounted for, it manifests instead as an apparent thermal feature of the vacuum—Unruh radiation. However, as demonstrated in this paper, Unruh radiation can be directly explained as a consequence of thrust. This perspective leads to the prediction that neither Unruh radiation nor Hawking-Bekenstein radiation should appear independently of the thrust that drives the system.

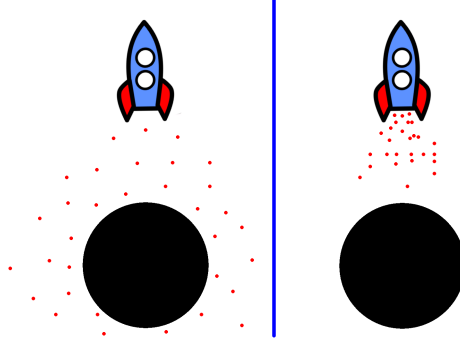


Figure 6: Hawking picture of black hole radiating on the left. Our picture of a rocket thrusting on the right.

7 Acknowledgments

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References

- [1] E. Frodden and N. Valdés, “Unruh effect: Introductory notes to quantum effects for accelerated observers,” *International Journal of Modern Physics A*, vol. 33, p. 1830026, sep 2018.
- [2] H.-J. Borchers, “On revolutionizing quantum field theory with tomita’s modular theory,” *Journal of Mathematical Physics*, vol. 41, no. 6, pp. 3604–3673, 2000.
- [3] J. Schwinger, “Particles and sources,” *Phys. Rev.*, vol. 152, pp. 1219–1226, Dec 1966.
- [4] E. Zurich, “Chapter 3 quantum field theory,” 2012.
- [5] “*NIST Digital Library of Mathematical Functions*.” <http://dlmf.nist.gov/>, Release 1.1.8 of 2022-12-15. F. W. J. Olver, A. B. Olde Daalhuis, D. W. Lozier, B. I. Schneider, R. F. Boisvert, C. W. Clark, B. R. Miller, B. V. Saunders, H. S. Cohl, and M. A. McClain, eds.

- [6] W. G. Unruh, “Notes on black-hole evaporation,” *Phys. Rev. D*, vol. 14, pp. 870–892, Aug 1976.