



Deep Learning Basic

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Chapter 1-1



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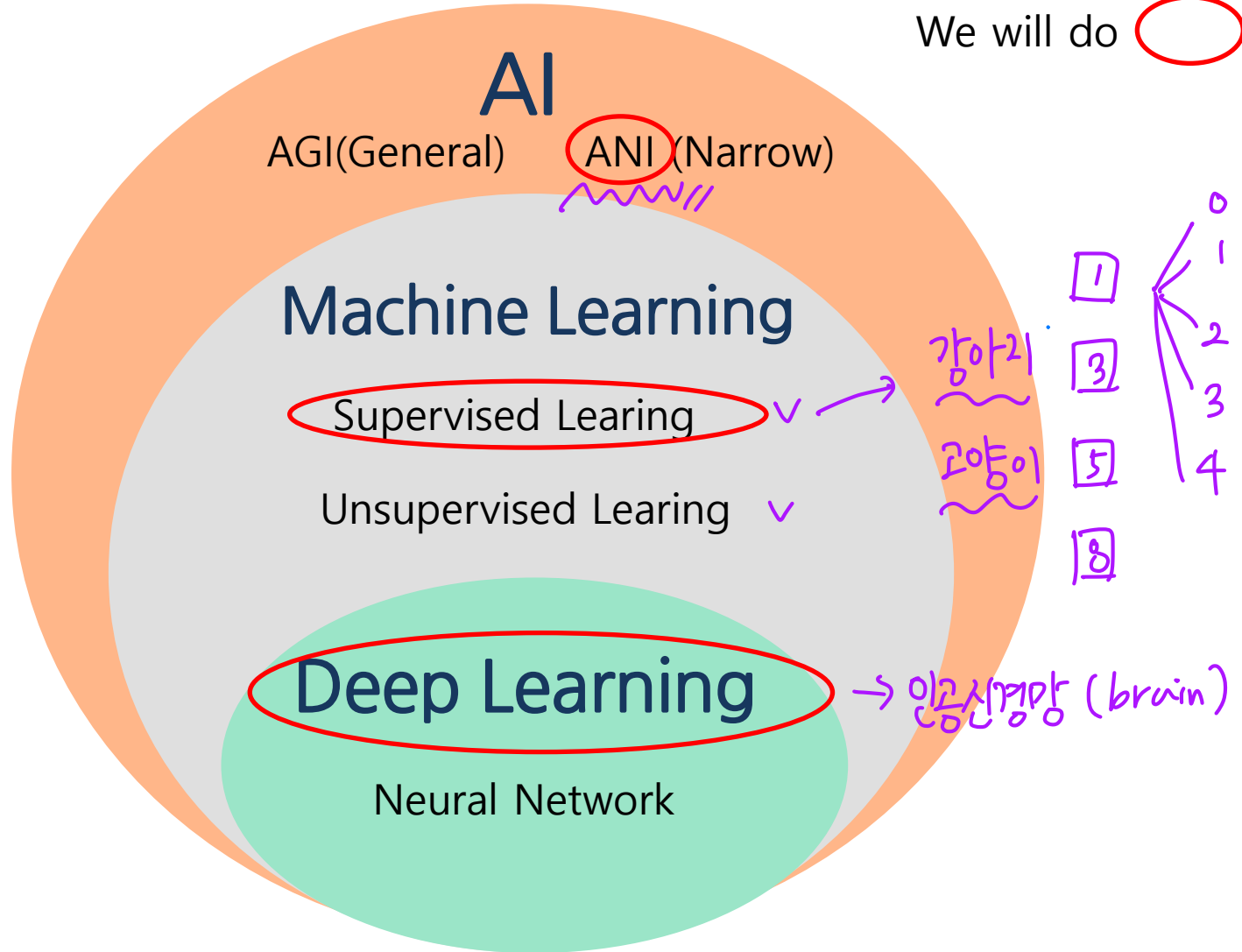
Part 1

About AI



AI vs Machine Learning vs Deep Learning

We will do ○



Machine Learning Categories

		Supervised Learning	Unsupervised Learning
Discrete	Discrete	<u>Classification</u> ✓	Clustering ✓
	Continuous	<u>Regression</u> ✓	Dimensionality Reduction ✓

x, y, z

Discrete

Continuous



* Reinforcement Learning is excluded



Regression Ex.



출처 : <https://finance.naver.com/item/fchart.nhn?code=020150>



Classification Ex.

강아지
머핀



Part 2

Basic Regression

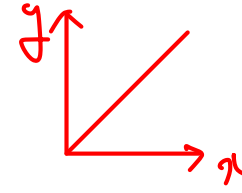


Hypothesis

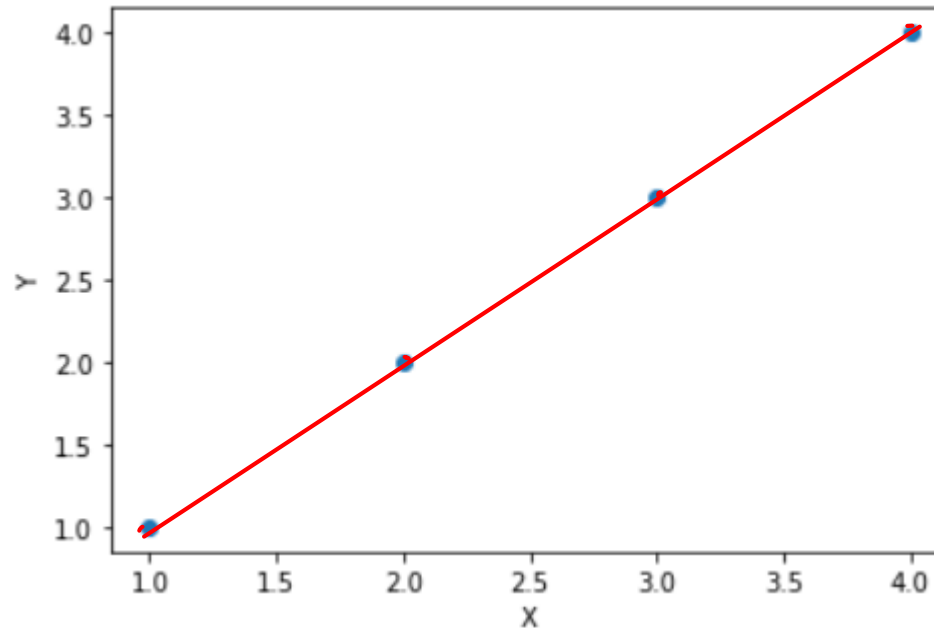
If Data is

x	y
1	1
2	2
3	3
4	4

$$f(x) = x$$

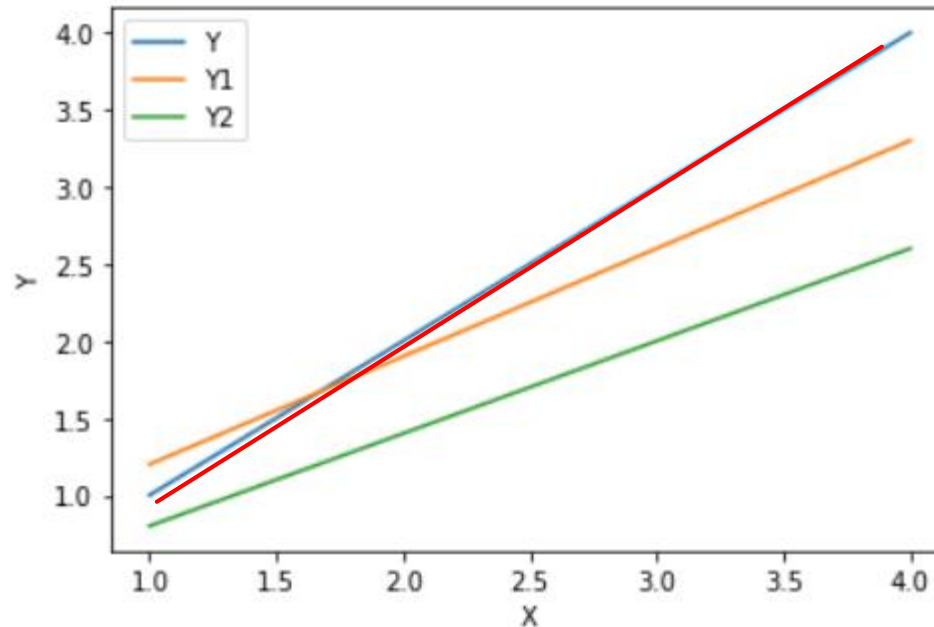


What is $f(5)$?

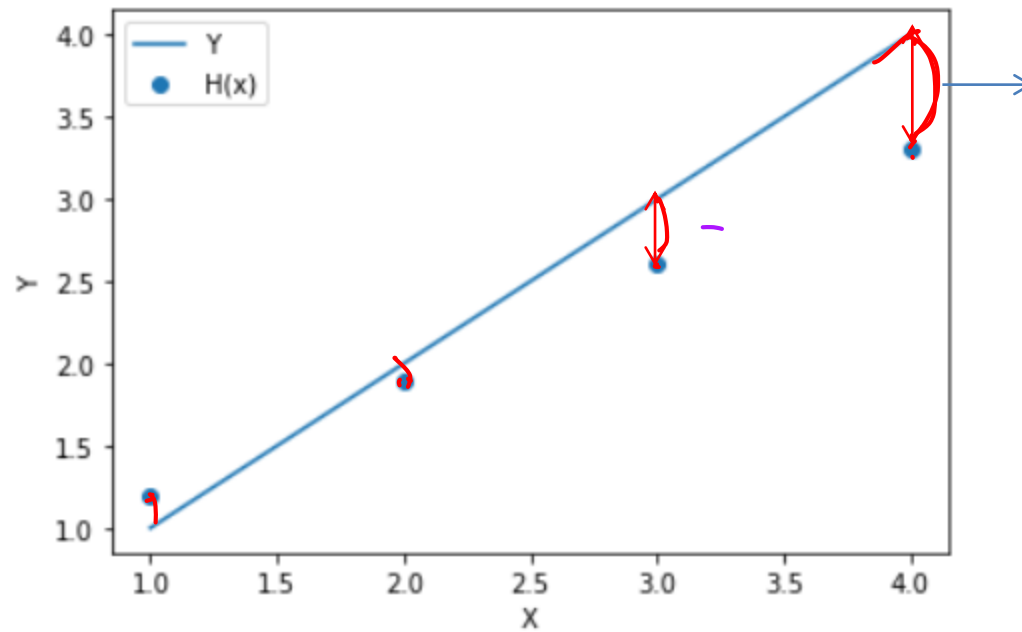


Hypothesis

$H(x) = wx + b$ 알려있는 기본식..
Approximate !!
 $w = \text{weight}$
 $b = \text{bias}$



Hypothesis



Cost:
 $H(x) - Y$

$$\text{Cost} = H(x) - \text{true_Y}, H(x) = wx + b$$

To reduce cost, Find proper w, b



Cost Function (MSE)

부족한 값이고 크기만 제공,,

Mean Square Error

$$\frac{(H(x^{(1)}) - y^{(1)})^2 + (H(x^{(2)}) - y^{(2)})^2 + (H(x^{(3)}) - y^{(3)})^2}{3}$$

$$cost = \frac{1}{m} \sum_{i=1}^m (H(x^{(i)}) - y^{(i)})^2$$

minimize
 W, b

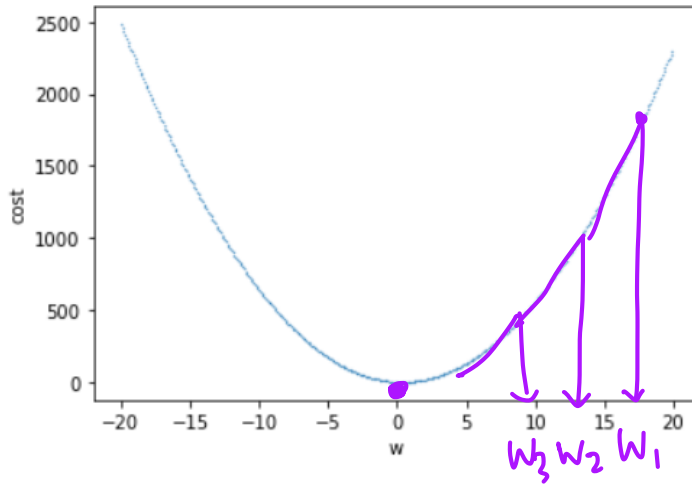
$cost(W, b)$

Now, You may have an question !

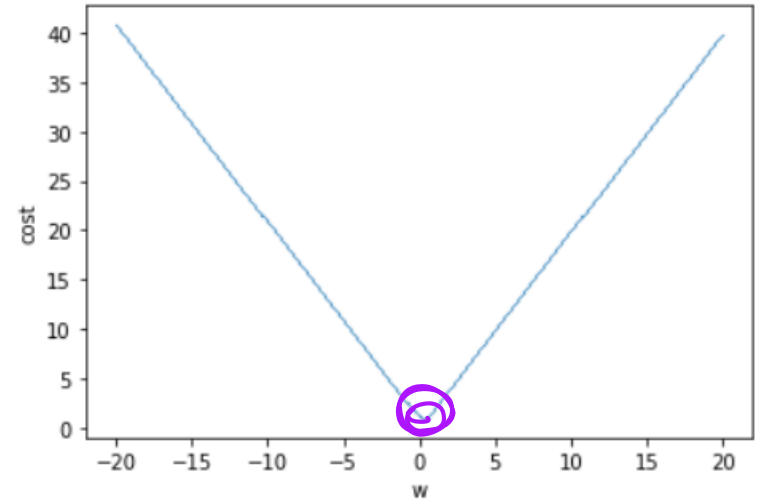


MSE vs MAE

Mean Square Error



Mean Absolute Error



Hypothesis

$$cost = \frac{1}{m} \sum_{i=1}^m (H(x^{(i)}) - y^{(i)})^2$$

Ex) $H(x) = 13x + 1$

x	2	3	4	5
Pred	25	50	42	61
True	27	40	53	66
Cost	-2	10	-9	-5

$$cost = \sum_{i=1}^n (H(x^i) - y(x))^2$$

$$24 = (-2)^2 + (10)^2 + (-9)^2 + (-5)^2 = 210$$

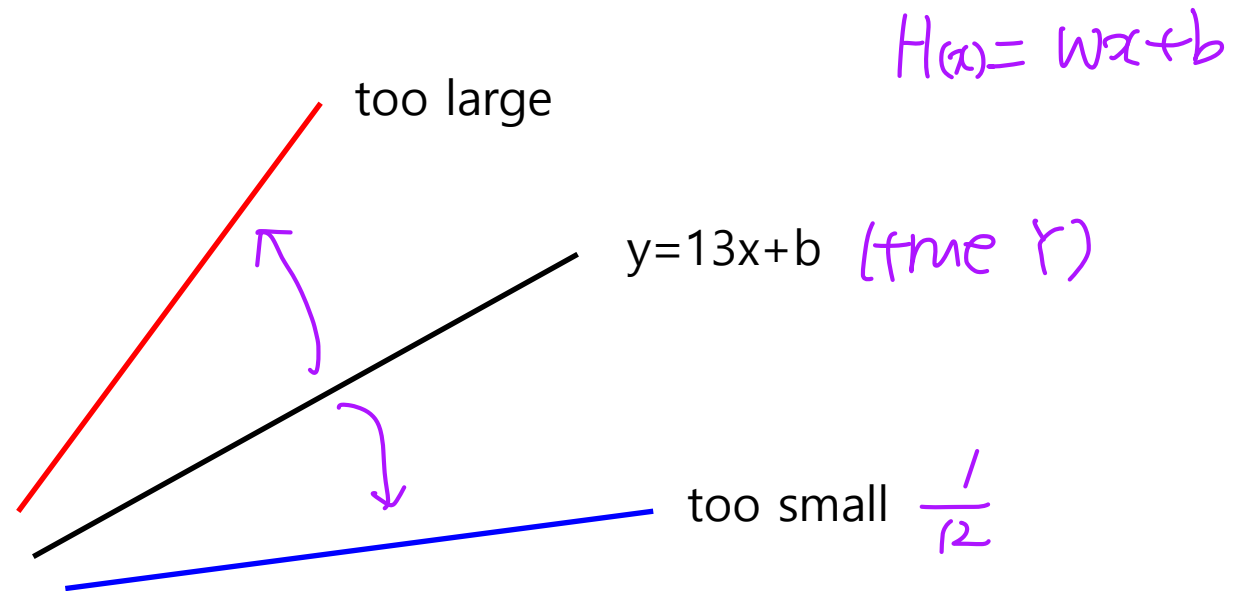
$$\therefore cost = 210/4 = 52.5$$



Hypothesis



Optimization (Gradient Decent)

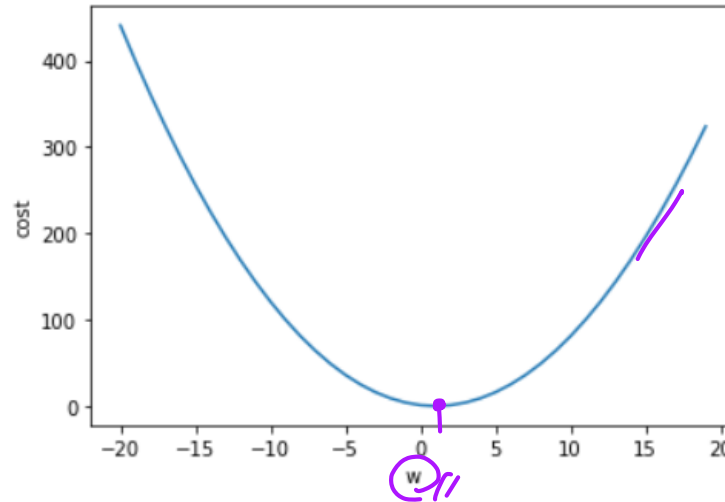


$$\underline{\text{Gradient}} \propto \underline{\text{Cost}}$$



Optimization (Gradient Decent)

Ex) $H(x) = wx$



$\frac{d}{dw} \text{Cost}$
~~~~~

$$\left( \begin{aligned} \text{Cost}(w) &= \frac{1}{n} \sum_{i=1}^n (H(x^{(i)}) - y^{(i)})^2 \\ H(x^{(i)}) &= w(x^{(i)}) \end{aligned} \right.$$

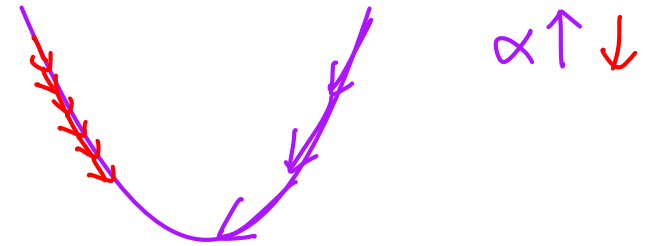


# Optimization (Gradient Decent)

$$\text{cost}(w) = \frac{1}{n} \sum_{i=1}^n \frac{1}{2} (w(x^i) - y^i)^2 //$$

$$\frac{\partial}{\partial w} \text{cost}(w) = \frac{1}{n} \sum_{i=1}^n \frac{1}{2} (w(x^i) - y^i)^2 \cdot 2 \cdot x^i$$

$$\therefore \frac{\partial}{\partial w} \text{cost}(w) = \frac{1}{n} \sum_{i=1}^n (w(x^i) - y^i) \cdot x^i //$$



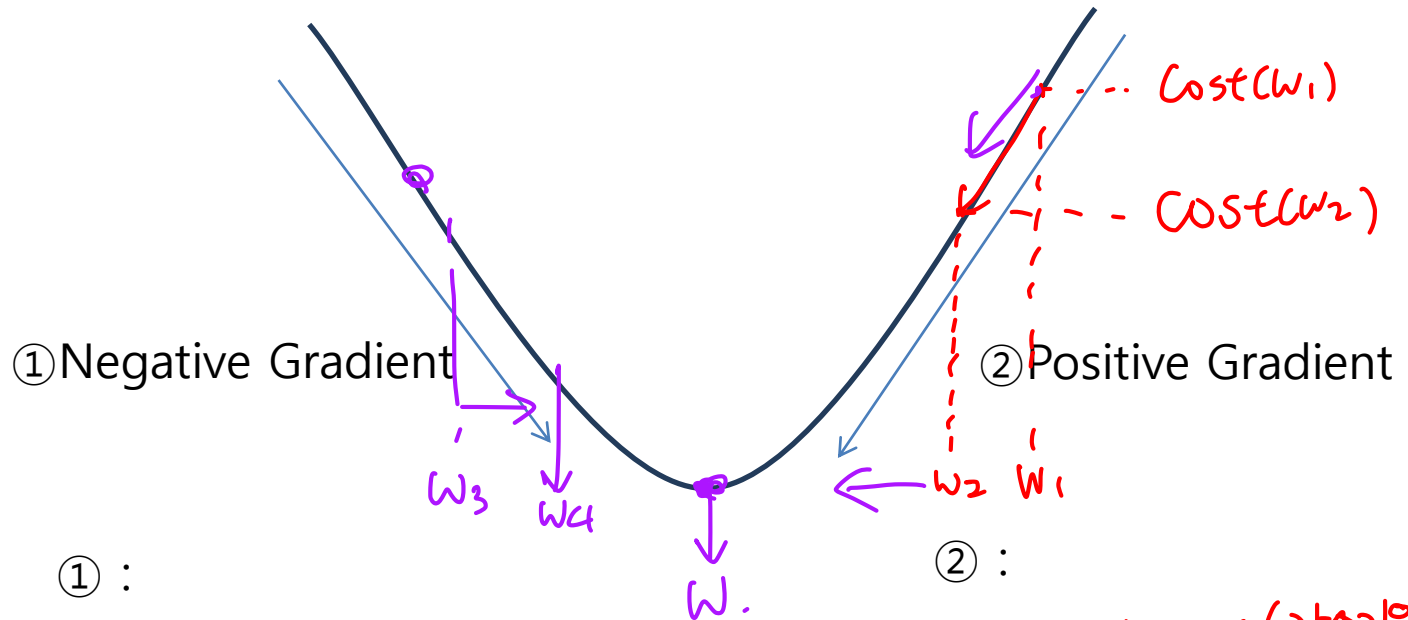
$$W := W - \alpha \frac{1}{m} \sum_{i=1}^m (Wx^i - y^i)x^i \quad \alpha : \text{Learning Rate}$$



# Optimization (Gradient Decent)

$$W := W - \alpha \frac{\partial}{\partial W} \text{cost}(W)$$

$$\frac{\text{cost}(W_1) - \text{cost}(W_2)}{W_1 - W_2}$$



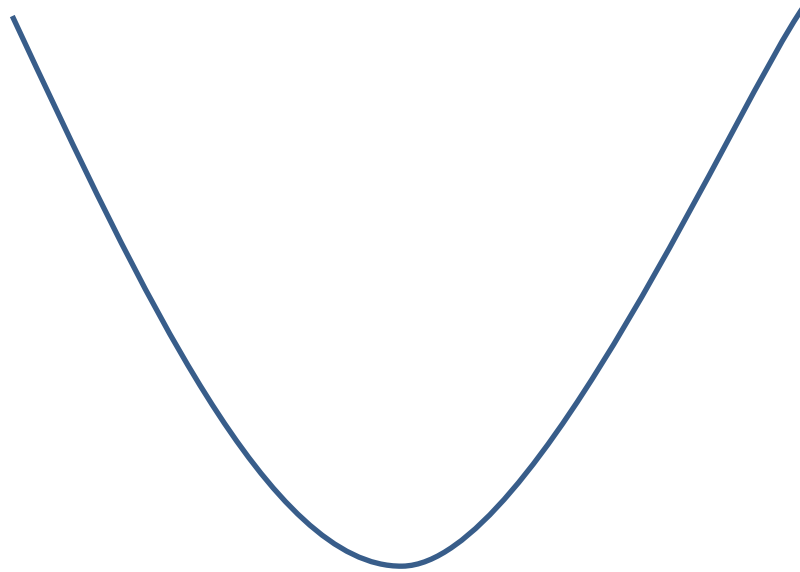
$$W := W + \alpha (\text{음수} / \text{증가})$$

$$W := W - \alpha (\text{양수} / \text{증가})$$




# Optimization (Gradient Decent) - Learning Rate

If Learning Rate is too large or small ?



# Multivariable Linear Regression


$x$  = RGB (3 channel) ,  $y$  is 4 label. 

$$H(x) = Wx + b$$

$$H(x_1, x_2, x_3) = w_1x_1 + w_2x_2 + w_3x_3 + b$$

$$\text{cost}(W, b) = \frac{1}{m} \sum_{I=1}^m (H(x_1^{(i)}, x_2^{(i)}, x_3^{(i)}) - y^{(i)})^2$$

$$w_1x_1 + w_2x_2 + w_3x_3 \quad \rightarrow$$



$$(x_1, x_2, x_3) \cdot \begin{pmatrix} w_1 \\ w_2 \\ w_3 \end{pmatrix}$$

**Matrix**

**Perceptron**



# Multivariable Linear Regression - Matrix

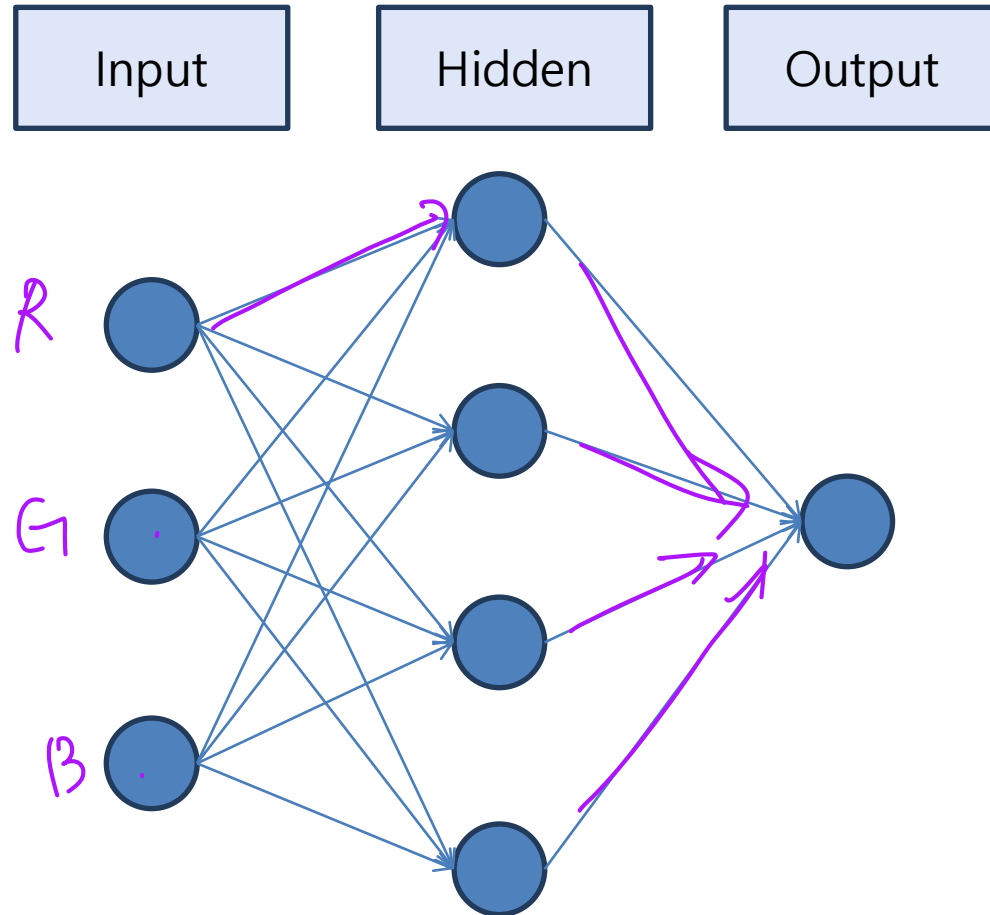
$$w_1x_1 + w_2x_2 + w_3x_3$$

$$\begin{pmatrix} x_1 & x_2 & x_3 \end{pmatrix} \cdot \begin{pmatrix} w_1 \\ w_2 \\ w_3 \end{pmatrix} = (x_1w_1 + x_2w_2 + x_3w_3)$$

$$\mathbf{H(X)} = \mathbf{XW}$$

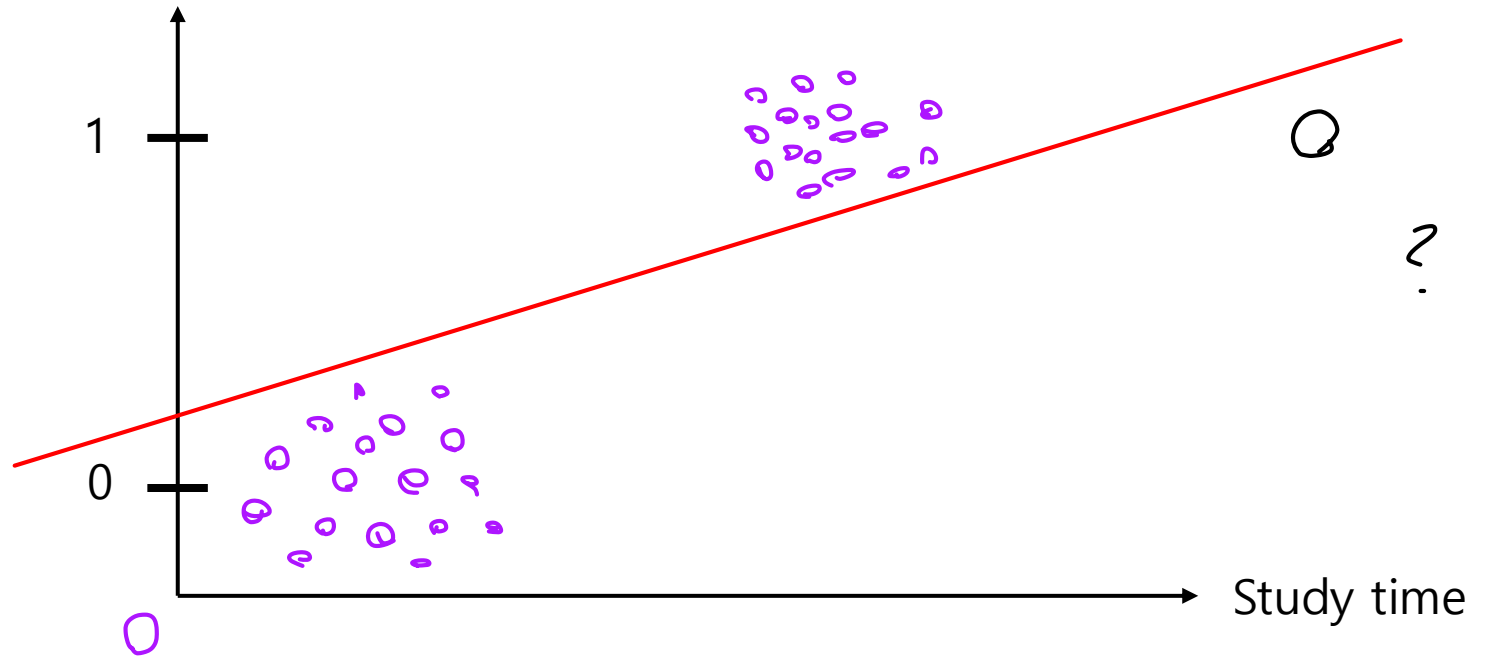


# Multivariable Linear Regression - Perceptron



# Binary Classification (이진분류) *설명해줘.*

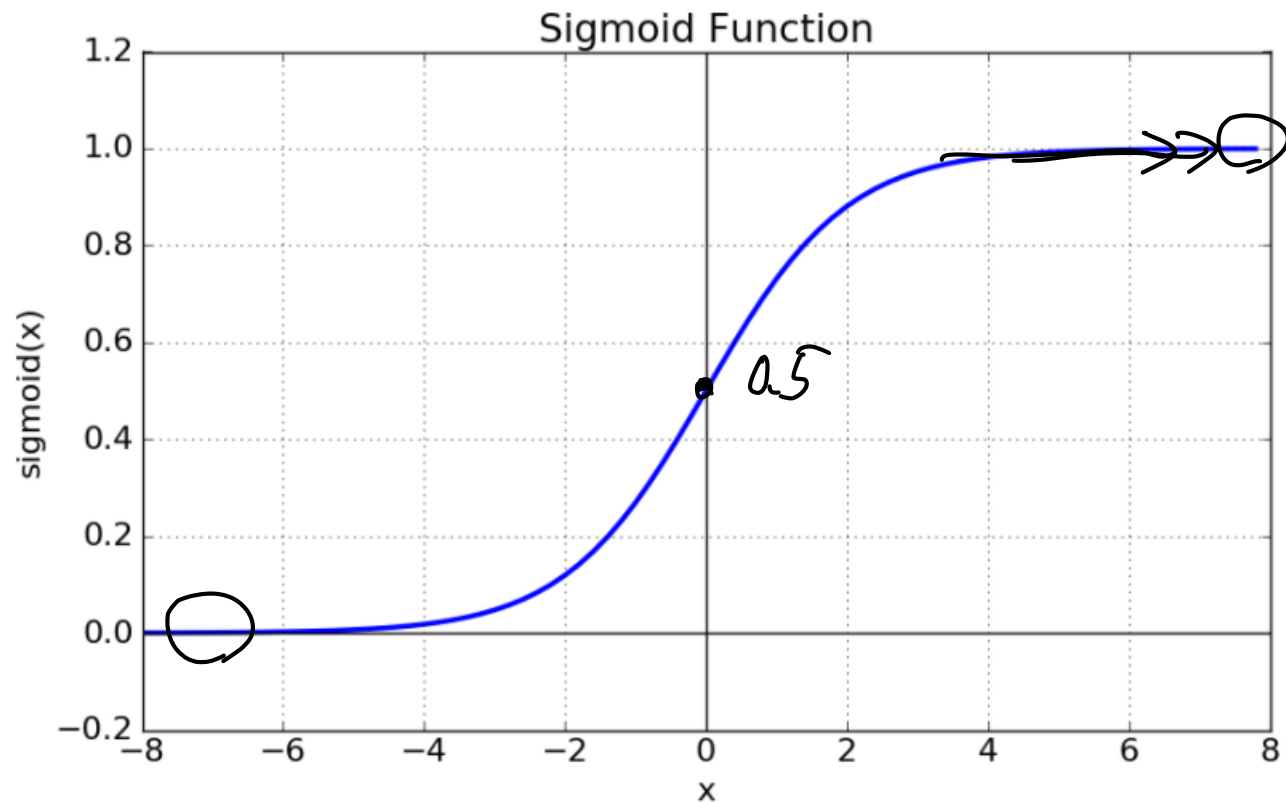
Pass(1) / Fail(0)





# Binary Classification

$$\text{Sigmoid}(x) = \frac{1}{1 + e^{-x}} \quad (0, 1)$$

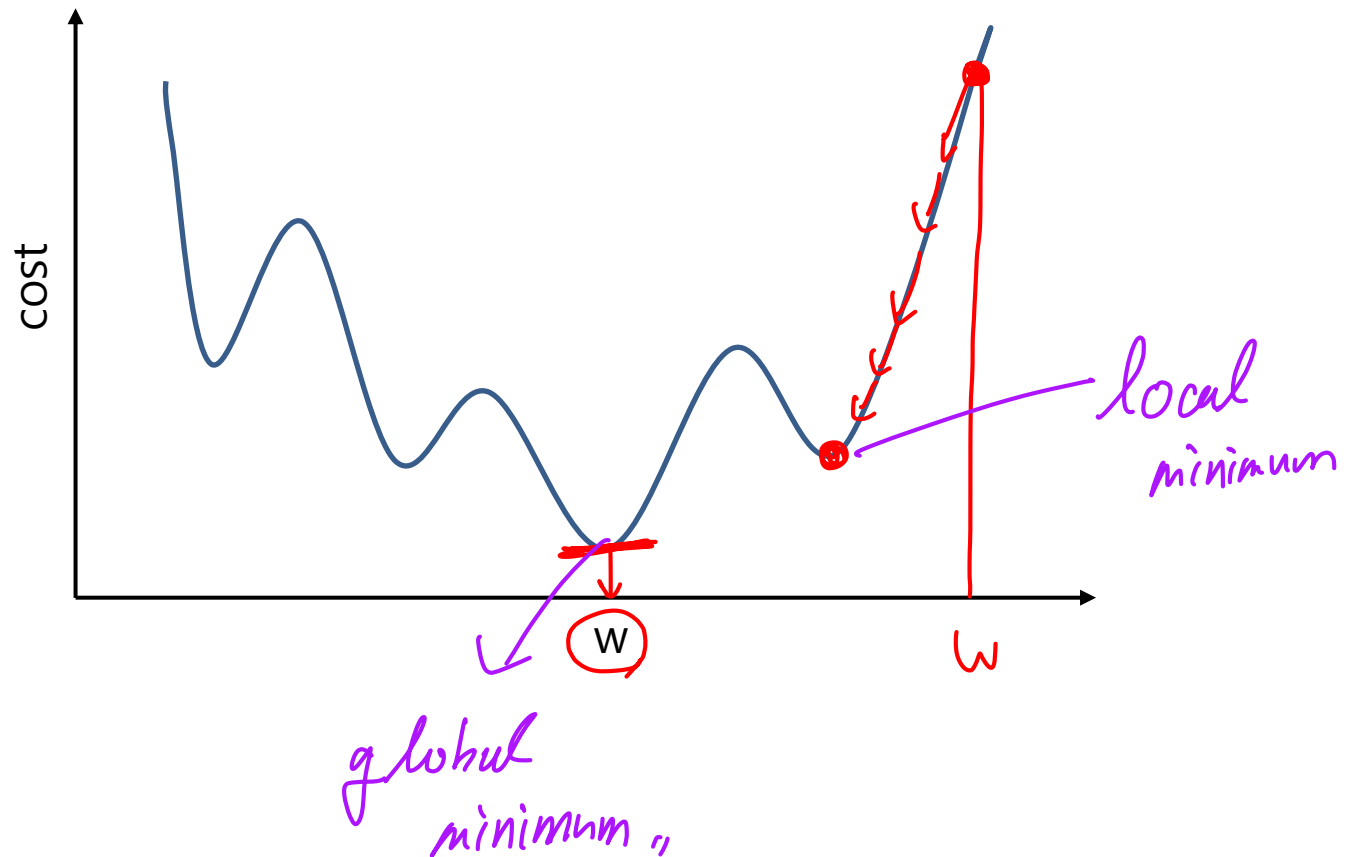


But! It has some problem.



# Binary Classification

Problem ( Cost Function )



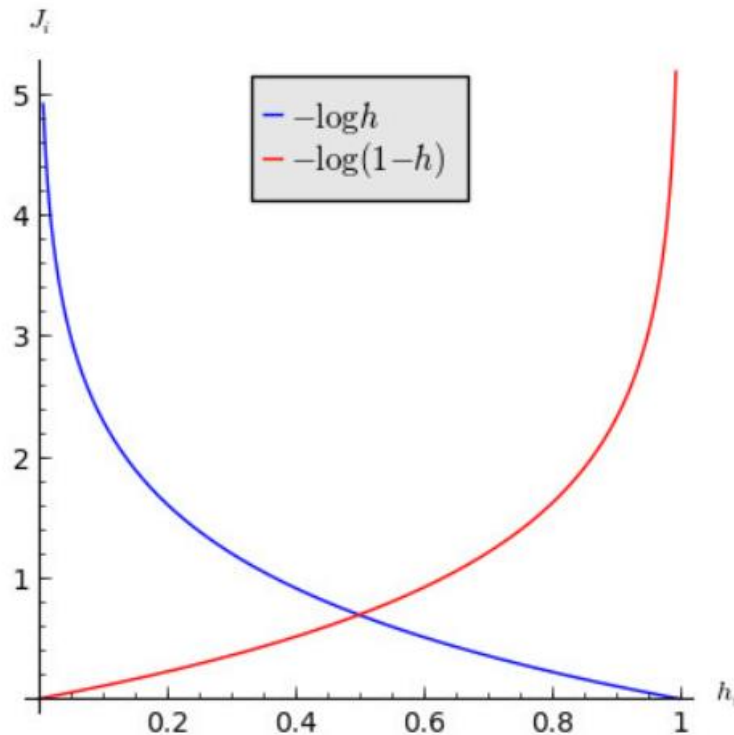
# Binary Classification - Cost Function

- Cross Entropy

$$H(P, Q) = - \sum P(x) \log(Q(x))$$

$$\text{cost}(W) = \frac{1}{m} \sum c(H(x), y)$$

$$c(H(x), y) = \begin{cases} -\log(H(x)) & : y = 1 \\ -\log(1 - H(x)) & : y = 0 \end{cases}$$



*over 1/2*



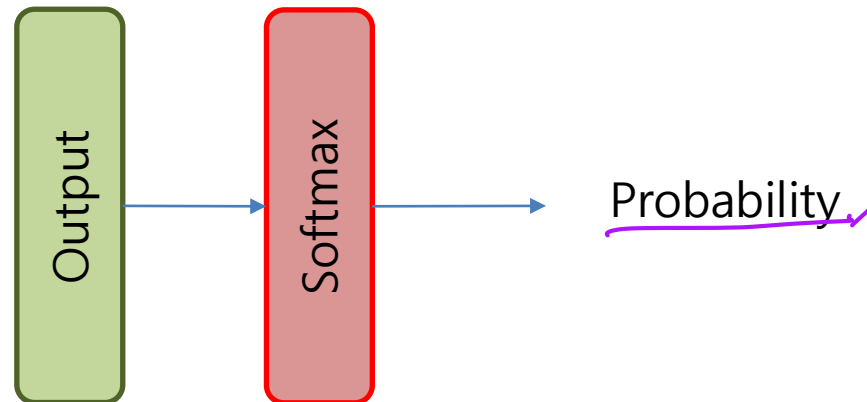
# Multinormal Classification

- Softmax Function

$$P_j = \frac{e^{x_j}}{\sum_{k=1}^k e^{x_k}} = \frac{e^{x_j}}{e^{x_1} + e^{x_2} + e^{x_3} + \dots + e^{x_k}} \text{ for } j = 1, \dots, k$$

*Handwritten notes: "한번" (once) with an arrow pointing to the exponent  $x_j$ ; double slashes under the denominator and the "for" clause.*

Sum is always 1



# AND, OR, XOR (Prove)

AND

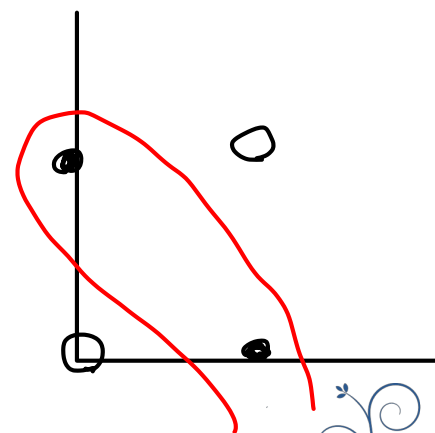
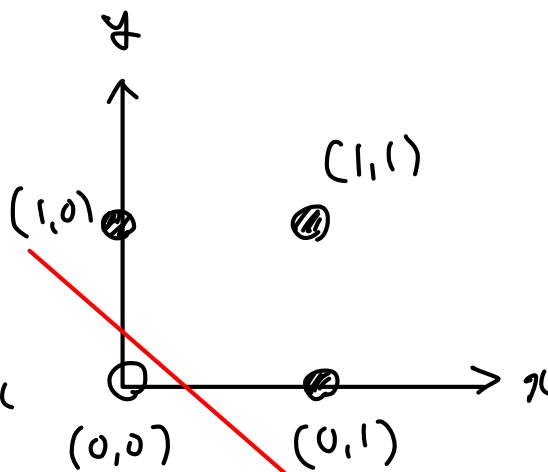
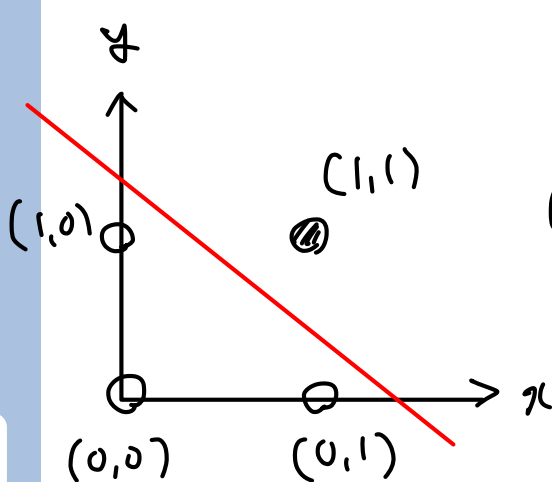
| x1 | x2 | Y |
|----|----|---|
| 0  | 0  | 0 |
| 0  | 1  | 0 |
| 1  | 0  | 0 |
| 1  | 1  | 1 |

OR

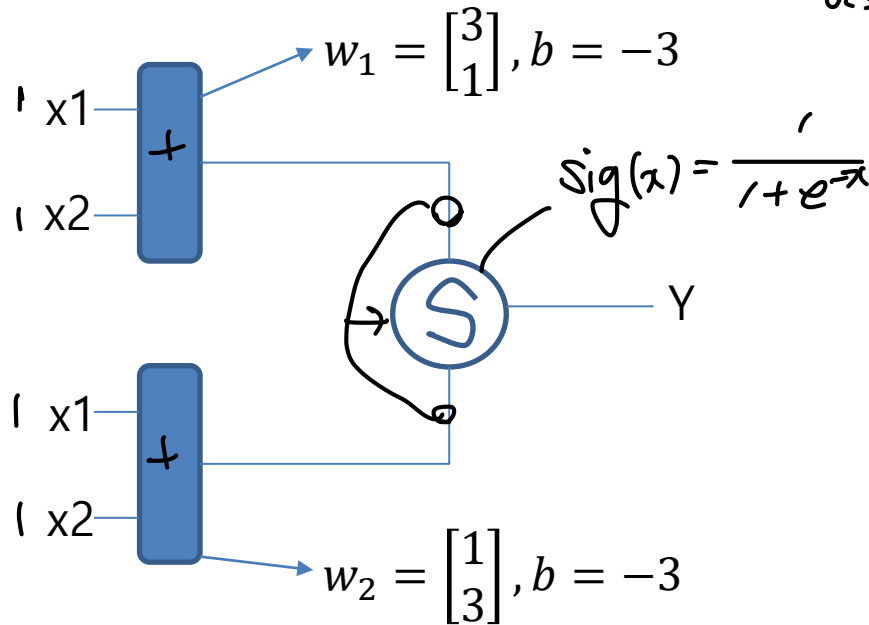
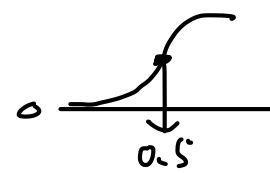
| x1 | x2 | Y |
|----|----|---|
| 0  | 0  | 0 |
| 0  | 1  | 1 |
| 1  | 0  | 1 |
| 1  | 1  | 1 |

XOR

| x1 | x2 | Y |
|----|----|---|
| 0  | 0  | 0 |
| 0  | 1  | 1 |
| 1  | 0  | 1 |
| 1  | 1  | 0 |



# AND (Prove)



| x1 | x2 | Y |
|----|----|---|
| 0  | 0  | 0 |
| 0  | 1  | 0 |
| 1  | 0  | 0 |
| 1  | 1  | 1 |

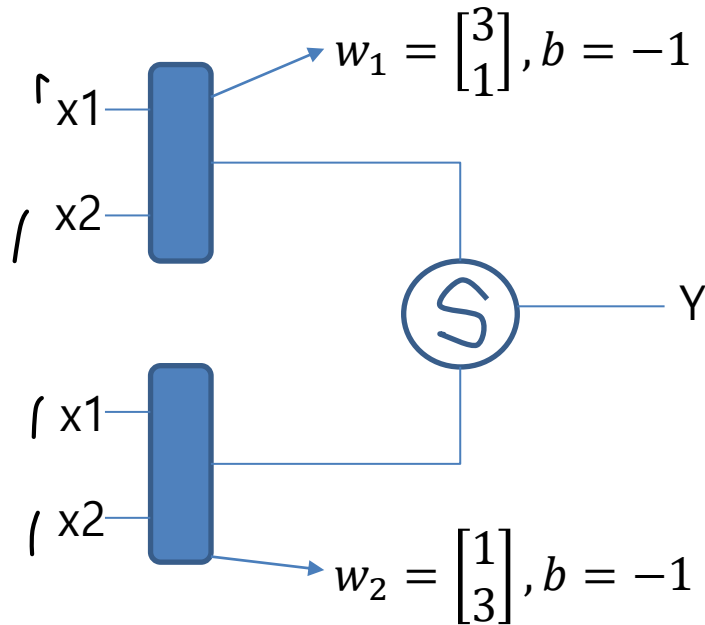
①  $3 \times 0 + 1 \times 0 - 3 = -3$   $\oplus -6 \rightarrow \text{sig} \rightarrow 0$   
 $1 \times 0 + 3 \times 0 - 3 = -3$

②  $0 \times 3 + 1 \times 1 - 3 = -2$   $\oplus -2 \rightarrow \text{sig} \rightarrow 0$   
 $0 \times 1 + 1 \times 3 - 3 = 0$

③  $1 \times 3 + 0 \times 1 - 3 = 0$   $\oplus -2 \rightarrow \text{sig} \rightarrow 0$   
 $1 \times 1 + 0 \times 3 - 3 = -2$

④  $3 \times 1 + 1 \times 1 - 3 = 1$   $\oplus 2 \rightarrow \text{sig} \rightarrow 1$   
 $1 \times 1 + 1 \times 3 - 3 = 1$

# OR (Prove)



①  $-1 + -1 = -2 \rightarrow 0$

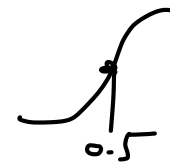
②  $0 + 2 = 2 \rightarrow 1$

③  $2 + 0 = 2 \rightarrow 1$

④  $3 + 3 = 6 \rightarrow 1$

|   | x1 | x2 | Y |
|---|----|----|---|
| ① | 0  | 0  | 0 |
| ② | 0  | 1  | 1 |
| ③ | 1  | 0  | 1 |
| ④ | 1  | 1  | 1 |

# XOR (Prove)



↳ 두 값이  $(x_1, x_2)$  같으면 0, 다르면 1

$$(0, 0) \begin{pmatrix} w_1 \\ w_2 \end{pmatrix} + b' \rightarrow b' < 0.5 \dots \textcircled{1}$$

$$(1, 1) \begin{pmatrix} w_1 \\ w_2 \end{pmatrix} + b' \rightarrow w_1 + w_2 + b' < 0.5$$

$$\downarrow$$

$$w_1 + w_2 < 0.5 - b' \dots \textcircled{2}$$

$$\left[ \begin{array}{l} (1, 0) \begin{pmatrix} w_1 \\ w_2 \end{pmatrix} + b' \\ (0, 1) \begin{pmatrix} w_1 \\ w_2 \end{pmatrix} + b' \end{array} \right] \rightarrow \left\{ \begin{array}{l} w_1 + b' > 0.5 \\ w_2 + b' > 0.5 \end{array} \right.$$

$$w_1 + w_2 + 2b' > 1$$

$$w_1 + w_2 > 1 - 2b' \dots \textcircled{3}$$

② ③ 연립.

$$\underline{1 - 2b'} < w_1 + w_2 < \underline{0.5 - b'}$$



$2(0.5 - b') < w_1 + w_2 < (0.5 - b')$  ~~불가능 !!~~ linear f. , classifi

~~XOR~~



# XOR (Solution About Contradiction)

x1 x2 Y

①

|   |   |   |
|---|---|---|
| 0 | 0 | 0 |
|---|---|---|

②

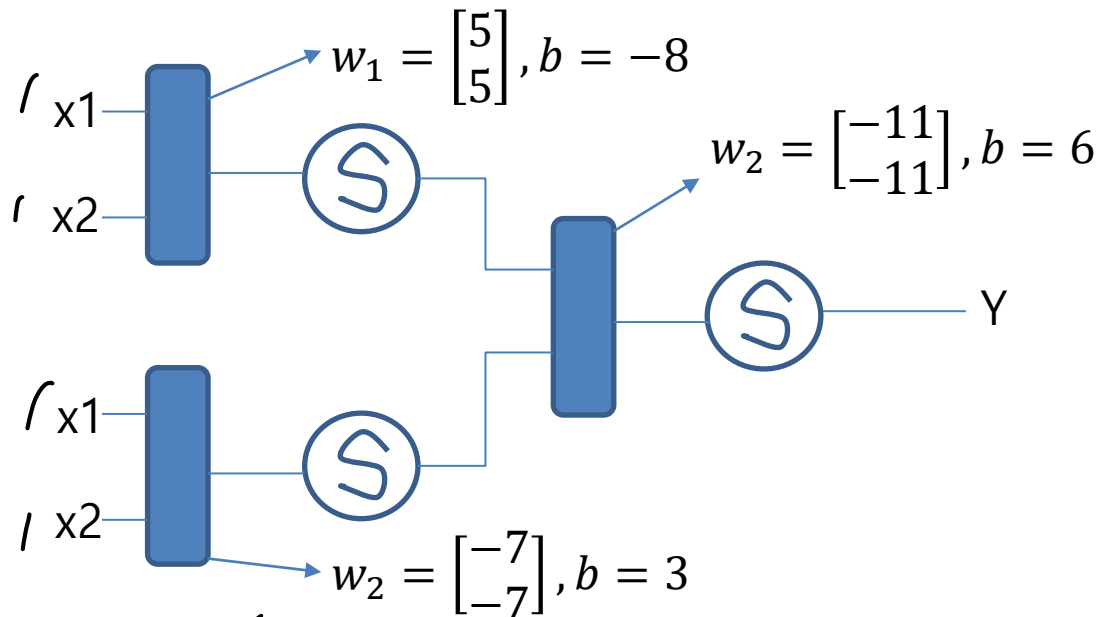
|   |   |   |
|---|---|---|
| 0 | 1 | 1 |
|---|---|---|

③

|   |   |   |
|---|---|---|
| 1 | 0 | 0 |
|---|---|---|

④

|   |   |   |
|---|---|---|
| 1 | 1 | 1 |
|---|---|---|



①  $-11 \times 0 + -11 \times 1 + 6 = -5$

②  $-3 \rightarrow 0$      $6 \rightarrow 1$   
 $-4 \rightarrow 0$

④  $10 - 8 = 2 \rightarrow 1$      $-11 + 0 + 6 = -5 \rightarrow 0$   
 $-14 + 3 = -11 \rightarrow 0$

# AND, OR, XOR (Prove)



# AND, OR, XOR (Prove)



# AND, OR, XOR (Prove)



# AND, OR, XOR (Prove)



# AND, OR, XOR (Prove)



# Thank you...!!!

## *Next Time ?*

- Live Coding in Jupyter Notebook (you prepare jupyter notebook, Colab, Anaconda or Vscode)
- Probability and Statistics
- Backpropagation

## *Assignment*

- Differentiate The Sigmoid Function

$$\text{Sigmoid}(x) = \frac{1}{1 + e^{-x}}$$
