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Deadline: 2.11.2021, 23:59

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**Exercise O2.1**

(Program a SAT solver)

In your favourite programming language, write a program that checks the satisfiability of a propositional formula in clause form.

The program should indicate if the clause set is satisfiable or not, and if it is satisfiable, give a satisfying interpretation.

You can use any of the calculi we covered in the lecture.

Check your program on the clause set consisting of all 8 clauses you can build from 3 propositional variables.

$$\{\{p, q, r\}, \{p, q, \neg r\}, \{p, \neg q, r\}, \dots\}$$

This clause set should be identified as unsatisfiable. If you delete one of the clauses, the resulting set of 7 clauses is satisfiable.

See what happens with the  $2^n$  clauses from  $n$  propositional variables for  $n > 3$ . How large  $n$  can your program cope with?

Please deliver your program, as well as a PDF explaining your code and your results.

*Hints:*

- *Building up a whole proof tree will be complicated and slow and may take a lot of memory. Try to write your program so it works on one branch at a time. Only keep track of the leaf sequent you are working on. One way of doing this is using recursion. Here's some pseudo code:*

```
Result prove(Sequent s) {
    if (s is axiom) {
        return "unsatisfiable"
    } else if (no more rule applications possible on s) {
        return literals in s as satisfying interpretation
    }
    else {
        pick a possible rule application
        List<Sequent> prems = premisses from that rule application
        for p in prems {
            answer = prove(s)
            if (answer is a satisfying interpretation I) {
                return I
            }
        }
        // the proofs for all premisses were closed, so...
        return "unsatisfiable";
    }
}
```

*It may be easier to keep the literals and the remaining clauses separate in the sequent  $s$ , i.e. pass around two arguments.*

- *You can represent a clause set as a list of lists or an array of arrays, etc., depending on what is most natural for the programming language you choose.*
- *For the literals you can use  $p$  and  $\text{not}(p)$  in Prolog, but you could also use integers, so that 1 is a propositional variable and  $-1$  its negation. Take care not to use 0 in that case... Again, it's up to you what is easiest in your programming language.*
- *Normal resolution won't easily give you a satisfying interpretation when it fails, so don't base your program on that.*
- ***And please:*** *We need to understand what your program does. So please add enough documentation and use sensible function/method/predicate/variable names.*