# Homework 2

May 2, 2019

#### 1 Homework 2

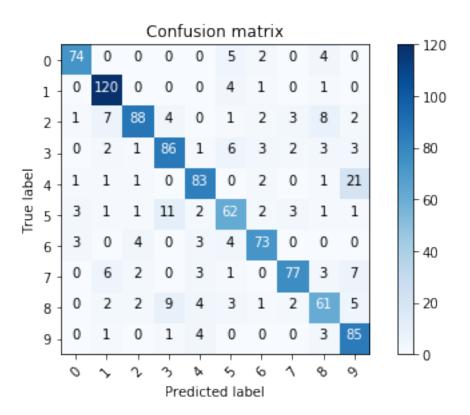
#### 1.1 Data

```
In [1]: import pandas as pd
        import numpy as np
        from sklearn.model_selection import train_test_split
        import matplotlib.pyplot as plt
In [2]: X_train = pd.read_csv('./mnist_train_data.csv', header= None)
        y_train = pd.read_csv('./mnist_train_labels.csv', names=['labels'])
        X_test = pd.read_csv('./mnist_test_data.csv', header= None)
        y_test = pd.read_csv('./mnist_test_labels.csv', names=['labels'])
1.2 Generative Learning
Problem 1:
In [3]: # Prior label probabilities:
        print(y_train['labels'].value_counts().sort_index()/len(y_train))
        prior_probs = y_train['labels'].value_counts().sort_index()/len(y_train)
        prior_prob_list = prior_probs.tolist()
0
     0.098667
     0.111833
1
2
    0.096833
3
    0.101333
4
    0.103833
5
     0.085667
6
     0.101333
7
     0.108500
8
     0.091833
     0.100167
Name: labels, dtype: float64
```

Problem 2:

```
In [20]: total_train = pd.concat([X_train, y_train], axis = 1)
        prob_tab = np.zeros(shape=[10, 784])
        for i in np.sort(y_train['labels'].unique()):
            a = total_train.loc[total_train['labels'] == i]
            # Remove label column
            a = a.drop('labels', 1)
            sum_val = (a.values).sum(axis = 0)
            # Laplacian smoothing
            probabilities = (sum_val +1 ) / (a.shape[0] + 2)
            prob_tab[i, :] = probabilities
            log_prob_tab = np.log(prob_tab.T)
Max Pji for label 0 = 0.851851851852
Max Pji for label 1 = 0.98514115899
Max Pji for label 2 = 0.728987993139
Max Pji for label 3 = 0.808196721311
Max Pji for label 4 = 0.8496
Max Pji for label 5 = 0.711240310078
Max Pji for label 6 = 0.849180327869
Max Pji for label 7 = 0.794793261868
Max Pji for label 8 = 0.875226039783
Max Pji for label 9 = 0.867330016584
  Problem 3:
In [23]: mm_1 = np.matmul(X_test, log_prob_tab)
        mm_r = np.matmul((1-X_test), np.log(1-prob_tab).T )
        final_matrix = np.add((mm_l+mm_r), np.log(prior_prob_list))
        y_pred = np.argmax(final_matrix, axis = 1)
In [24]: from sklearn import metrics
        import itertools
        print('The accuracy is', metrics.accuracy_score(y_test, y_pred))
The accuracy is 0.809
In [25]: def plot_confusion_matrix(cm, classes,
                                 normalize=False,
                                 title='Confusion matrix',
                                 cmap=plt.cm.Blues):
            11 11 11
            This function prints and plots the confusion matrix.
```

```
Normalization can be applied by setting `normalize=True`.
             plt.imshow(cm, interpolation='nearest', cmap=cmap)
             plt.title(title)
             plt.colorbar()
             tick_marks = np.arange(len(classes))
             plt.xticks(tick_marks, classes, rotation=45)
             plt.yticks(tick_marks, classes)
             print(cm)
             thresh = cm.max() / 2.
             for i, j in itertools.product(range(cm.shape[0]), range(cm.shape[1])):
                 plt.text(j, i, cm[i, j],
                          horizontalalignment="center",
                          color="white" if cm[i, j] > thresh else "black")
             plt.tight_layout()
             plt.ylabel('True label')
             plt.xlabel('Predicted label')
             plt.show()
  Problem 4:
In [26]: cnf_matrix = metrics.confusion_matrix(y_test, y_pred)
         np.set_printoptions(precision=2)
         # Plot non-normalized confusion matrix
         plt.figure()
         plot_confusion_matrix(cnf_matrix, classes=np.sort(y_test['labels'].unique()),
                               title='Confusion matrix')
[[ 74
       0
                0
                    0
                            2
                                0
                                        0]
            0
                        5
   0 120
           0
                0
                    0
                        4
                                0
                                        0]
                            1
                                    1
                                        21
 Γ
       7
          88
                4
                    0
                        1
                            2
 86
                    1
                        6
                            3
                                    3
                                        3]
 1
           1
                0
                  83
                        0
                            2
                                0
                                    1
                                       21]
 Γ
       1
           1
              11
                    2
                      62
                            2
                                3
                                    1
                                        1]
 [ 3
                    3
                                        0]
       0
          4
                0
                       4 73
                                0
                                    0
 Ο
       6
          2
                0
                    3
                       1
                            0 77
                                    3
                                        7]
 [ 0
        2
           2
                9
                    4
                        3
                                2 61
                                        5]
                            1
 Γ 0
                1
                        0
       1
           0
                    4
                            0
                                0
                                    3 85]]
```



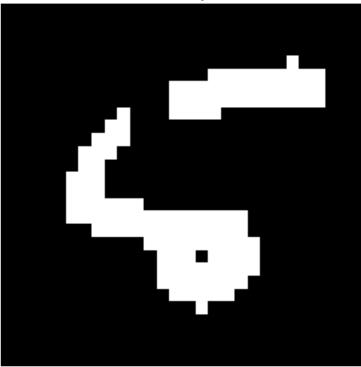
According to the confusion matrix, we can see that the biggest misclassification pairs are:

- 4 being misclassified as a 9 (21 times)
- 5 being misclassified as a 3 (11 times)
- 8 being misclassified as a 3 (9 times)

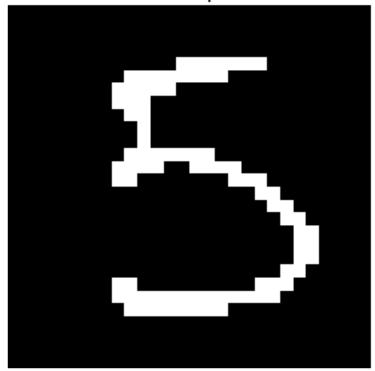
```
In [30]: def displaychar(image):
             plt.imshow(np.reshape(image, (28,28)), cmap=plt.cm.gray)
             plt.axis('off')
             plt.show()
```

```
Problem 5:
In [32]: index_error = np.array(np.where((y_test['labels'] != y_pred)==True))[0]
In [33]: incorrect = index_error[:2]
         actual = y_test.iloc[incorrect]['labels']
         miss = y_pred[incorrect]
         for i in range(len(incorrect)):
             b = incorrect[i]
             plt.figure(figsize=(10,5))
             plt.title('Actual was: %i, predicted: %i' % (actual.iloc[i], miss[i]), fontsize = 2
             displaychar(X_test.iloc[b]);
```

Actual was: 5, predicted: 4



# Actual was: 5, predicted: 3



#### Breast Cancer Data for problems 6,7:

for i in cov\_parameter:

```
clf = GaussianMixture(n_components=2, covariance_type = i)
            clf.fit(X_train, y_train)
            y_pred = clf.predict(X_valid)
            accuracy = np.sum(y_pred == y_valid)*1.0/len(y_valid)
            print('For criterion =', i, 'the validation accuracy = ' + str(accuracy))
            if (accuracy > best_acc):
                best_cov = i
                best_acc = accuracy
        print('The best criterion is', best_cov, 'with a validation accuracy of', best_acc)
         clf = GaussianMixture(n_components=2, covariance_type = best_cov)
         clf.fit(X_train_fin, y_train_fin)
         predictions = clf.predict(X_test)
         fin_accuracy = metrics.accuracy_score(y_test, predictions)
         print('\n')
        print('Final accuracy on total training data = ' + str(fin_accuracy))
For criterion = spherical the validation accuracy = 0.115044247788
For criterion = tied the validation accuracy = 0.212389380531
For criterion = diag the validation accuracy = 0.0973451327434
For criterion = full the validation accuracy = 0.83185840708
The best criterion is full with a validation accuracy of 0.83185840708
Final accuracy on total training data = 0.938596491228
  Problem 7:
In [56]: from sklearn.discriminant_analysis import LinearDiscriminantAnalysis
        clf = LinearDiscriminantAnalysis()
         clf.fit(X_train_fin, y_train_fin)
        predictions = clf.predict(X_test)
        print('The test accuracy = ' + str(sum(predictions == y_test)/len(y_test)))
The test accuracy = 0.964912280702
In [59]: print('The transformation matrix is \n', clf.coef_)
        print('\n')
        print('The intercept is', clf.intercept_[0])
The transformation matrix is
 [[ 1.35e+00 -1.27e-01 -1.36e-01 -2.44e-04 -2.24e+01
                                                           8.56e+01
   1.39e+01 -1.22e+02 1.60e+01 7.43e+00 -1.48e+01 4.83e-01
   1.73e+00 -1.64e-02 -4.69e+02 -1.96e+00 1.60e+01 -9.78e+01
   -6.14e+01 5.59e+02 -1.26e+00 -2.00e-01 -2.62e-01 1.93e-02
   3.19e+01 4.09e+00 -1.27e+01 -9.32e+00 -1.49e+01 -1.72e+02]]
```

### 1.3 Evaluating Classifiers

Problem 8:

```
In [61]: from sklearn.neighbors import KNeighborsClassifier
         from sklearn.datasets import load_digits
         digits = load_digits()
         print(digits.data.shape)
         # Last 1300 as training, beginning 497 as test
         X_train = digits.data[:497]
         y_train = digits.target[:497]
         X_test = digits.data[497:]
         y_test = digits.target[497:]
(1797, 64)
In [64]: # Fit the model:
         clf = KNeighborsClassifier(n_neighbors=5, metric = 'chebyshev')
         clf.fit(X_train, y_train)
         y_pred = clf.predict(X_test)
         # Evaluation metrics:
         TP = sum(y_pred[y_test == 3] == 3)
         FP = sum(y_pred[y_test != 3] == 3)
         TN = sum(y_pred[y_test != 3] != 3)
         FN = sum(y_pred[y_test == 3] != 3)
In [67]: print('Specificity:', TN/(TN+FP))
        print('Sensitivity:', TP/(TP+FN))
        print('True Positive Rate (TPR):', TP/(TP+FN))
         print('True Negative Rate (TNR):', TN/(TN+FP))
         print('False Negative Rate (FNR):', FN/(TP+FN))
         print('False Positive Rate (FPR):', FP/(FP+TN))
         print('Precision:', TP/(TP+FP))
         print('Recall:', TP/(TP+FN))
Specificity: 0.988888888889
Sensitivity: 0.869230769231
True Positive Rate (TPR): 0.869230769231
True Negative Rate (TNR): 0.988888888889
False Negative Rate (FNR): 0.130769230769
False Positive Rate (FPR): 0.0111111111111
Precision: 0.896825396825
```

#### Recall: 0.869230769231

From my experience, these are exceptional evaluation metrics!

## 1.4 Regression

```
Problem 9:
In [70]: from sklearn.datasets import load_diabetes
         diabetes = load_diabetes()
         # Form data-set:
         X_train, X_test, y_train, y_test = train_test_split(diabetes.data, diabetes.target, tes
In [71]: from sklearn.linear_model import LinearRegression
         clf = LinearRegression()
         clf.fit(X_train, y_train)
         predictions = clf.predict(X_test)
         print('Test MSE:', metrics.mean_squared_error(y_test, predictions))
         print('Test MAE:', metrics.mean_absolute_error(y_test, predictions))
Test MSE: 2155.96465103
Test MAE: 36.3181336987
  Problem 10:
In [73]: for i in range(10):
             X_ablation = np.delete(diabetes.data, [i], axis=1)
             X_train, X_test, y_train, y_test = train_test_split(X_ablation, diabetes.target, te
             clf = LinearRegression()
             clf.fit(X_train, y_train)
             predictions = clf.predict(X_test)
             print('Removing feature', i, ', test MSE:', metrics.mean_squared_error(y_test, pred
Removing feature 0 , test MSE: 2152.80664218
Removing feature 1 , test MSE: 2259.13307937
Removing feature 2 , test MSE: 2783.51448185
Removing feature 3 , test MSE: 2424.772348
Removing feature 4 , test MSE: 2187.59951938
```

#### Problem 11:

Removing feature 5 , test MSE: 2167.51760615 Removing feature 6 , test MSE: 2159.15148251 Removing feature 7 , test MSE: 2153.06317113 Removing feature 8 , test MSE: 2335.17338461 Removing feature 9 , test MSE: 2165.86619219

Feature 2 is the most valuable, as indicated by that the model has its test MSE increase the most without the feature included.