

# Predicting Magnetic Saturation ( $B_s$ ) and Curie Temperature ( $T_c$ ) in Magnetic Alloys

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<sup>1</sup> NOMATEN Center of Excellence, Poland

**September, 2024**

# Outline

- ❖ **Data Utilization:** Composition and processing parameters of soft magnetic alloys
- ❖ **Machine Learning Models:** Ridge Regression, SVM, CatBoost, GPR, KNN, Dense Neural Networks
- ❖ **Prediction Results:** Model performance, RMSE metric
- ❖ **Multi-Objective Optimization:** Pareto front analysis
- ❖ **Bayesian Optimization:** Inverse design and property maximization
- ❖ **Uncertainty Quantification:** Bayesian strategy, posterior distribution analysis
- ❖ **Constrained Optimization:** Refined optimization, Pareto front with constraint

# Inverse design workflow

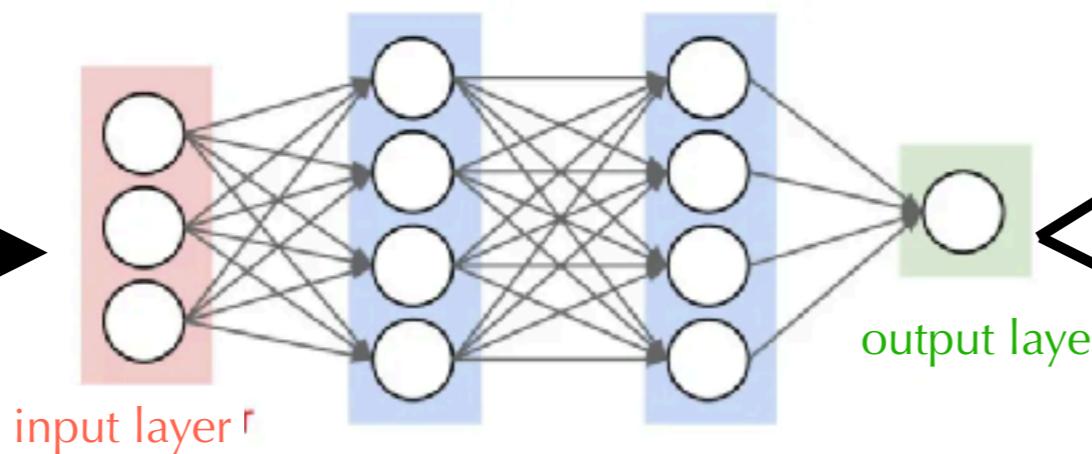
Al	B	C	Co	Cr	...
0.0	15.0	0.0	0.5	0.0	...
0.0	4.0	0.0	0.0	0.0	...
0.0	3.0	0.0	0.0	0.0	...
0.0	15.0	0.0	0.5	0.0	...

elemental compositions

processing parameters

Annealing Time (s)	Annealing Temperature (K)
0.0	0.00000
0.0	0.00000
3600.0	873.25952
1800.0	723.00000

## Machine Learning (ML)



## Magnetic Saturation (BS)

Predict  
Magnetic Properties

## Curie Temperature (TC)

Bayesian  
Optimizer

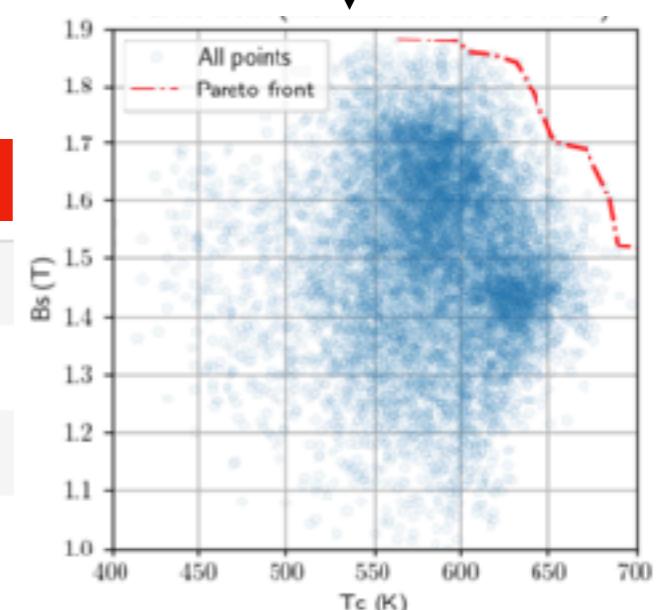
- Combine ML and Bayesian optimization:  
Inverse design of magnetic alloys

## optimized alloys

B11.8Cu0.7Fe81.7Si5.5

B9.0Cu1.4Fe83.0P1.0Si5.4

B7.5Co19.5Cu1.0Fe67.2P1.0Si4.0



# Inverse design workflow



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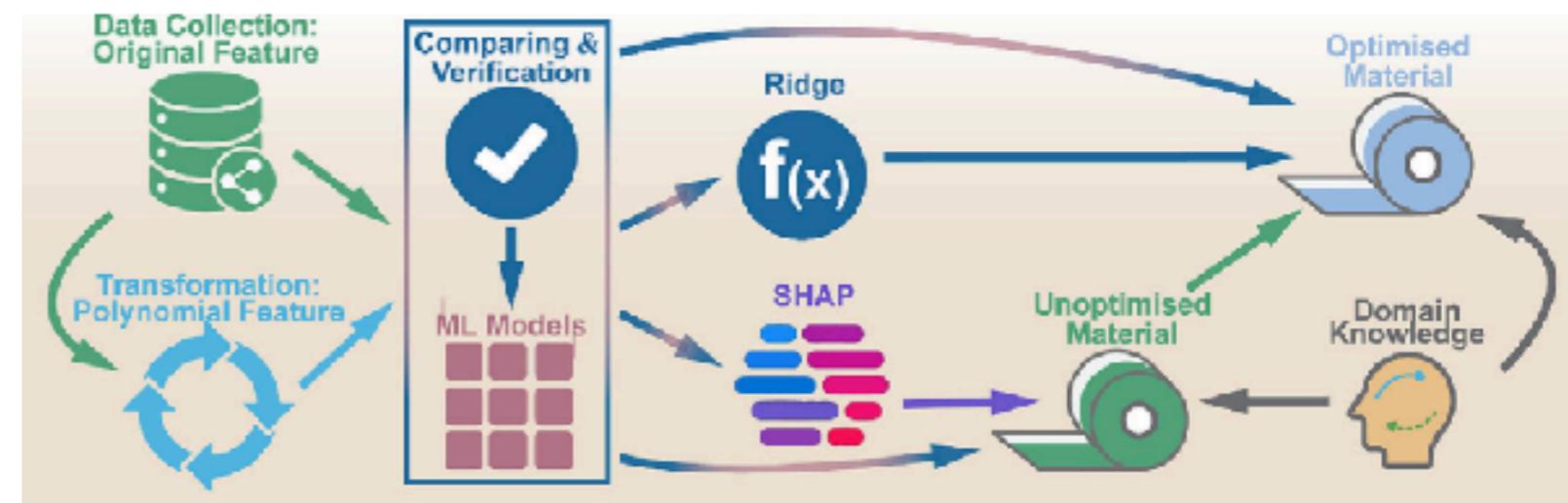
Accelerated discovery of Fe-based amorphous/nanocrystalline alloy through explicit expression and interpretable information based on machine learning



Bo Pang <sup>a</sup>, Zhilin Long <sup>b,c,\*</sup>, Tao Long <sup>a</sup>, Rong He <sup>d</sup>, Xiaowei Liu <sup>a</sup>, Mingwang Pan <sup>d</sup>

## HIGHLIGHTS

- This work considers not only composition but also the effect of ribbon thickness and annealing on  $B_s$  and  $T_c$ .
- The prediction accuracy of ML models, especially Ridge regression, has been significantly improved by transforming original features to polynomial features.
- Interpretable information of ML models based on SHAP method and explicit expressions is of great aid to researchers in alloy design.
- The predicted values of  $B_s$  and  $T_c$  are in good agreement with the measured ones in the previous literatures and an alloy  $\text{Fe}_{81.4}\text{Si}_{3.4}\text{B}_{11.4}\text{Cu}_{0.8}\text{Nb}_3$  with desired properties is designed.

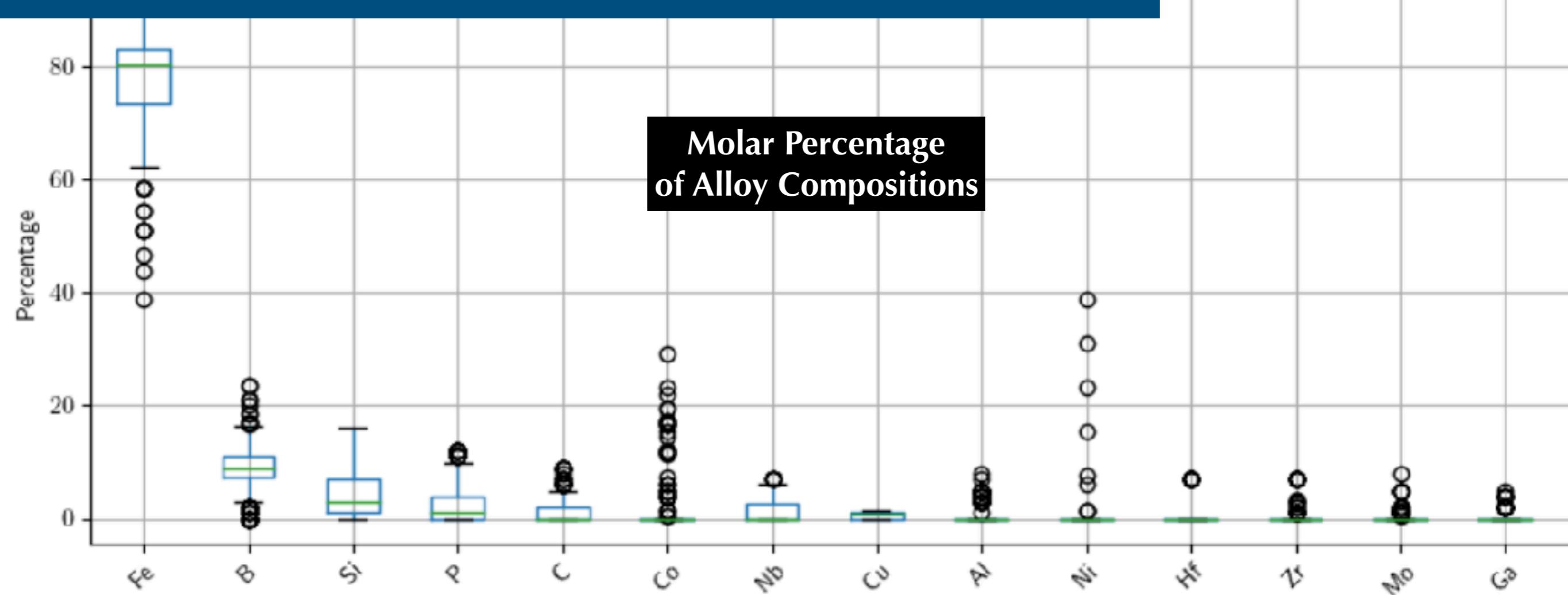


$$\begin{aligned} B_s &= 1.8 \text{ T} \\ T_c &= 662 \text{ K} \end{aligned}$$

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# Data Utilization



## Dataset Details [1]

- Experimental Dataset (Fe-based magnetic alloys):

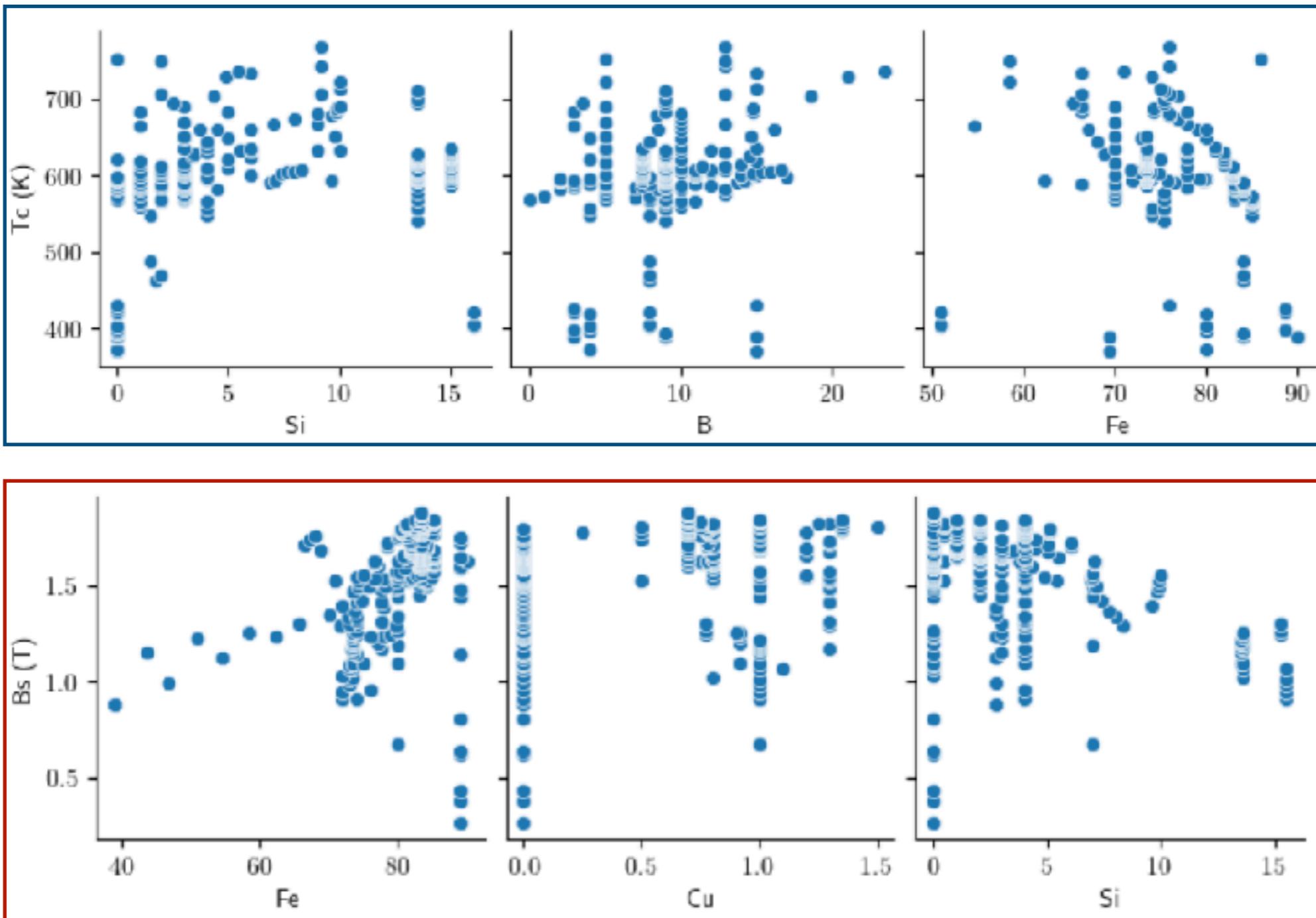
514 data items, with 294 for Bs and 220 for Tc

- Features:

Each data point includes 1 thickness, 2 annealing parameters, and compositional features

Composition	ta (s)	Ta (K)	Thickness (μm)	Bs (T)
Fe89Hf7Zr1B3	1800	648.9	32.5	0.3
Fe89Hf7Zr1B3	1800	598.7	32.5	0.4
Fe89Hf7Zr1B3	1800	748.6	32.5	0.4
Fe89Hf7Zr1B3	1800	698.8	32.5	0.6
Fe89Hf7Zr1B3	0	0.0	32.5	0.6

# Data Exploration

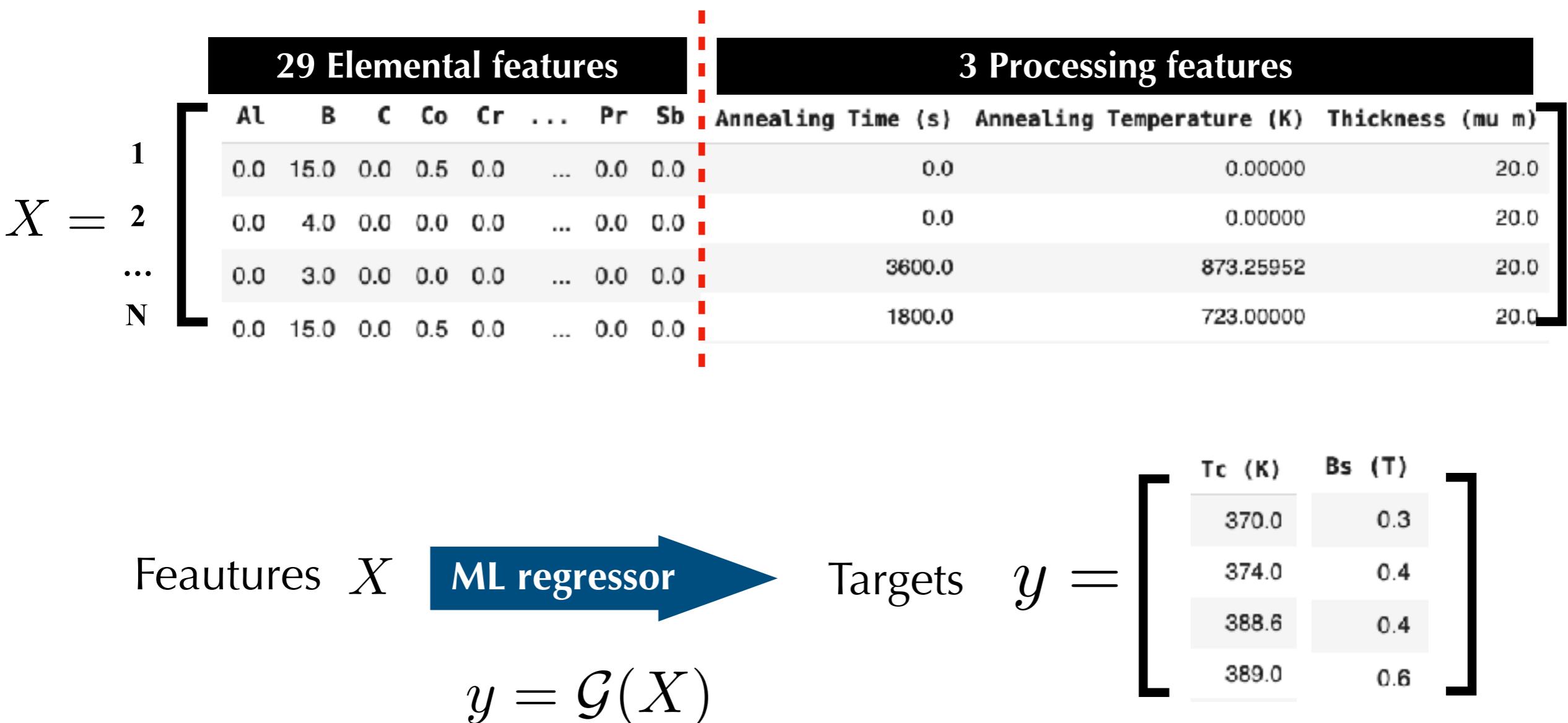


## Correlation features

- Opposite trends for  $B_s$  and  $T_c$ : increasing Fe enhances magnetic saturation but lowers Curie temperature, while increasing Si reduces  $B_s$  but improves  $T_c$ .

# Features & Outputs

- **Features:** elemental compositions, processing parameters
- **Targets:** magnetic saturation ( $B_s$ ) and Curie temperature ( $T_c$ )

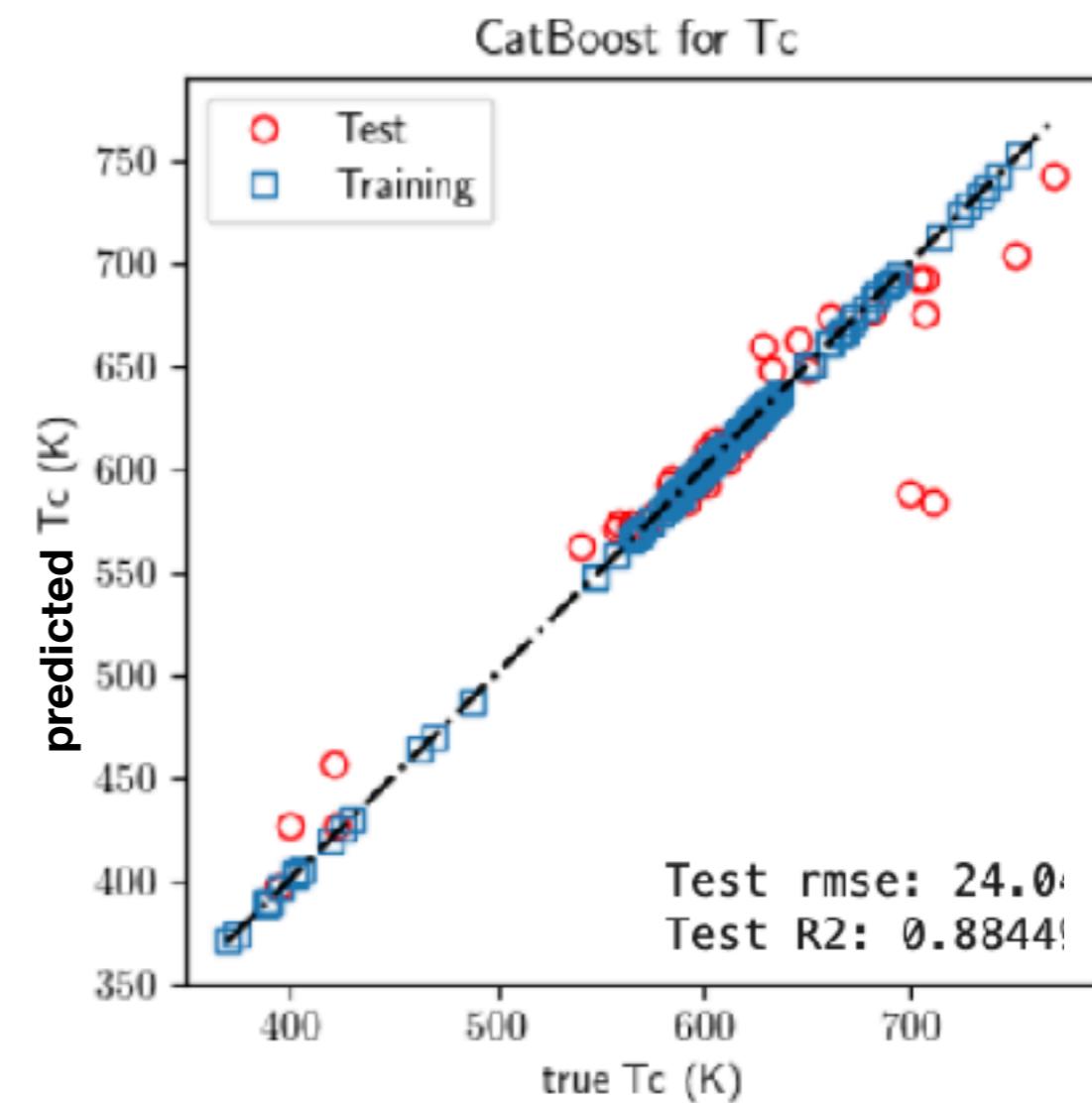
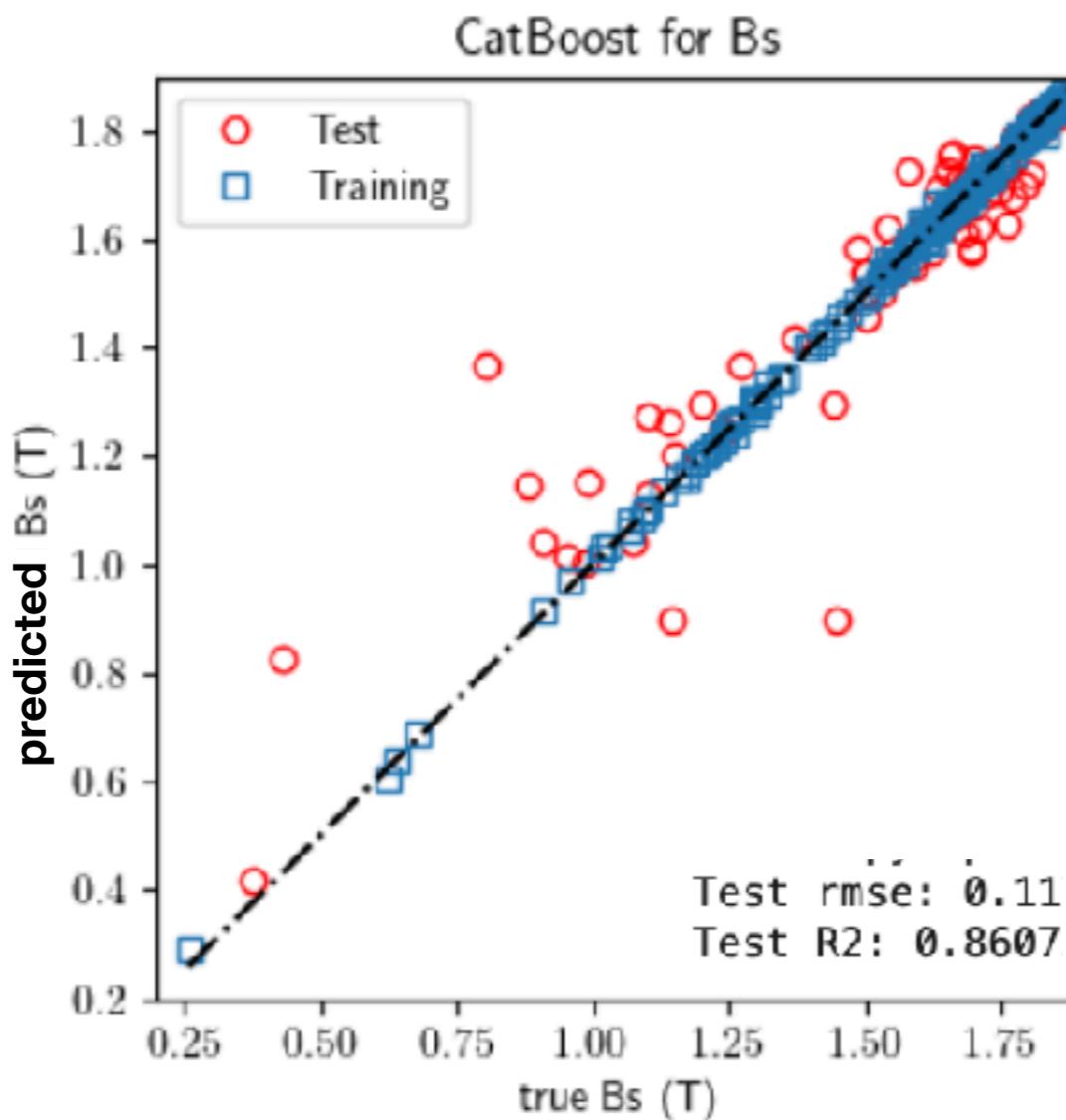


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# Machine Learning

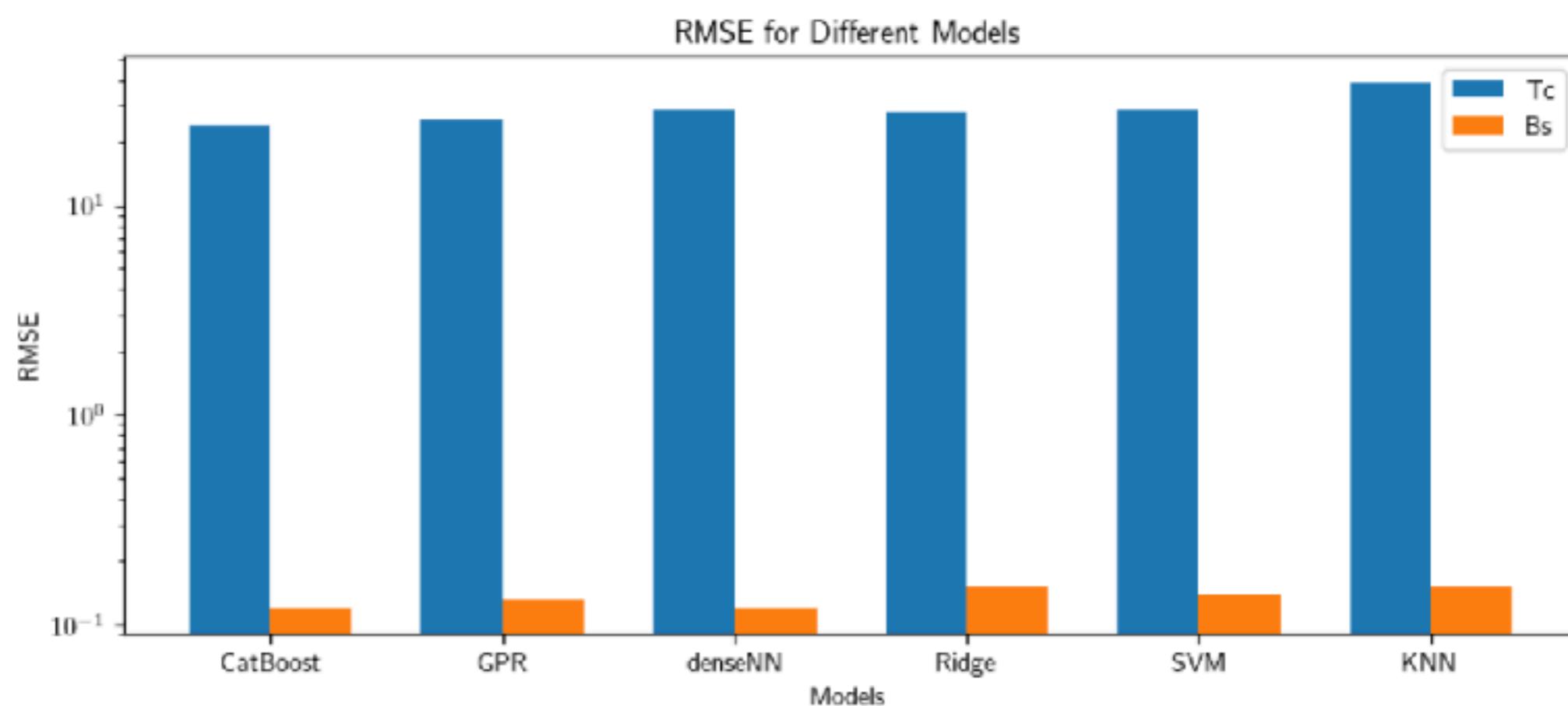
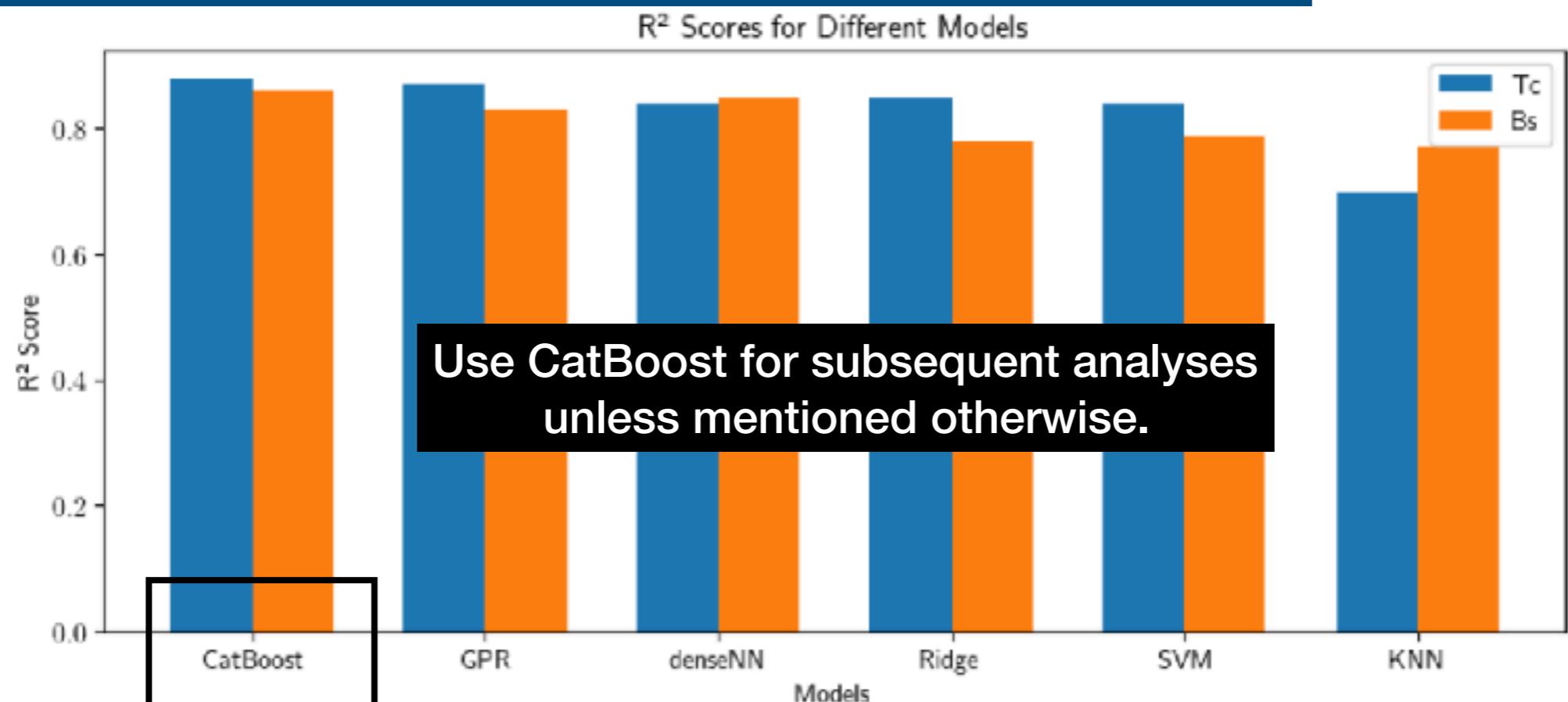
- Models Used: Ridge, SVM, CatBoost, KNN, GPR, Neural Nets.
- Hyperparameter Tuning: GridSearchCV, cross-validation.
- Training Strategy: Train-test split, standardization, evaluation metrics.



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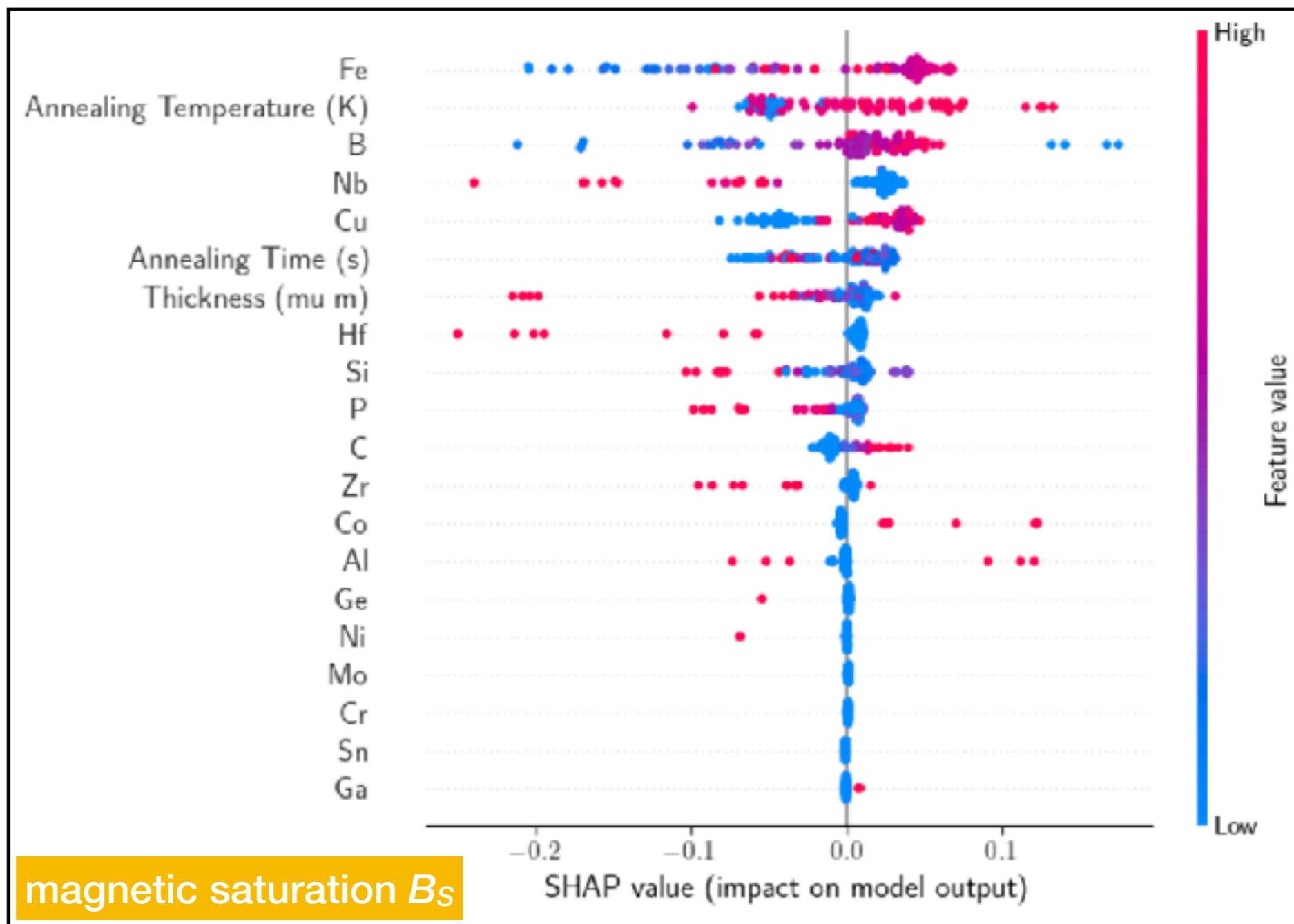
# ML Performance



# Feature Importance

## SHAP (SHapley Additive exPlanations) analysis

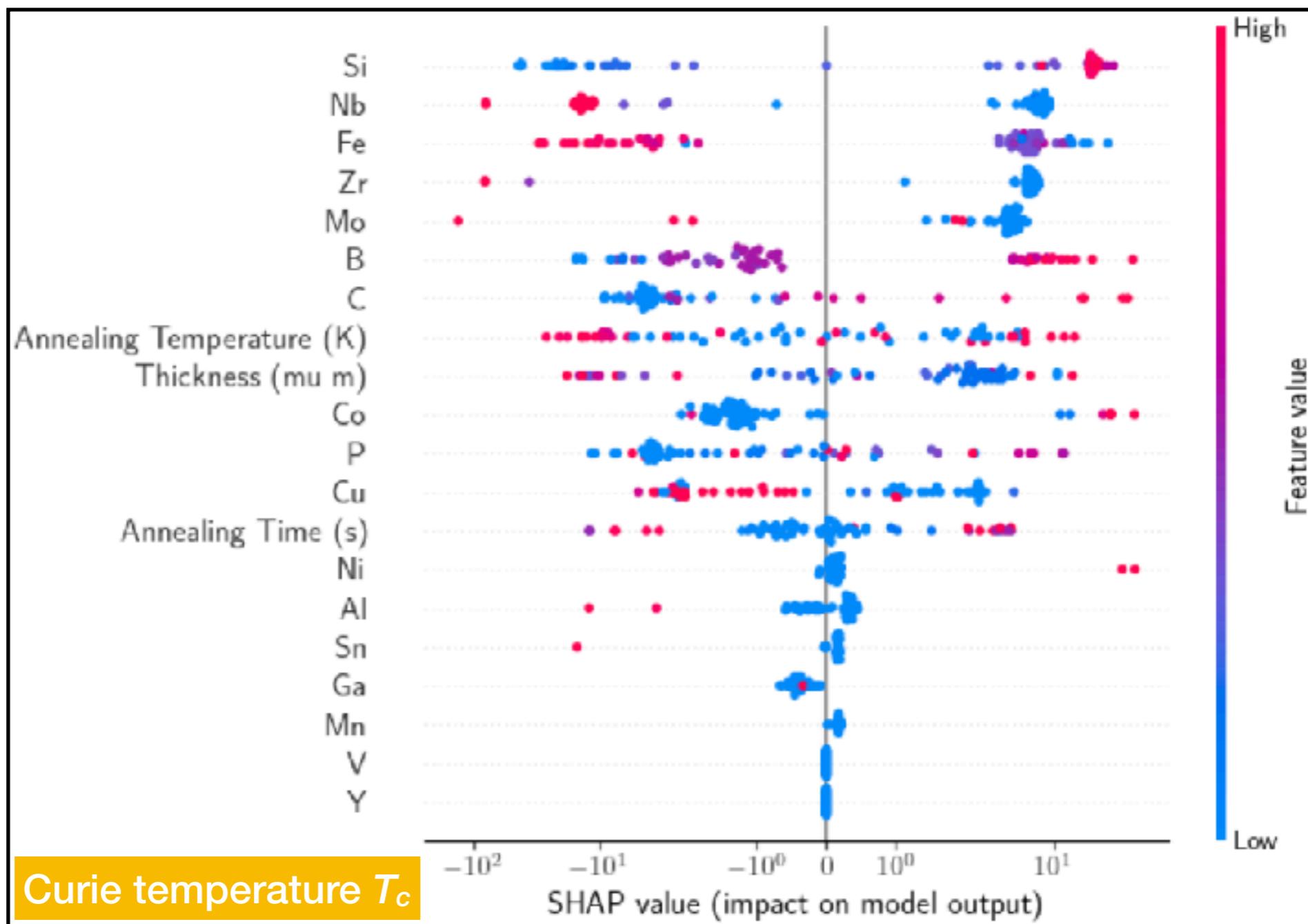
- Feature Importance: contribution of each feature to model predictions
- SHAP values: the direction and magnitude of influence



# Feature Importance

## SHAP (SHapley Additive exPlanations) analysis

- Feature Importance: contribution of each feature to model predictions
- SHAP values: the direction and magnitude of influence



# Outline

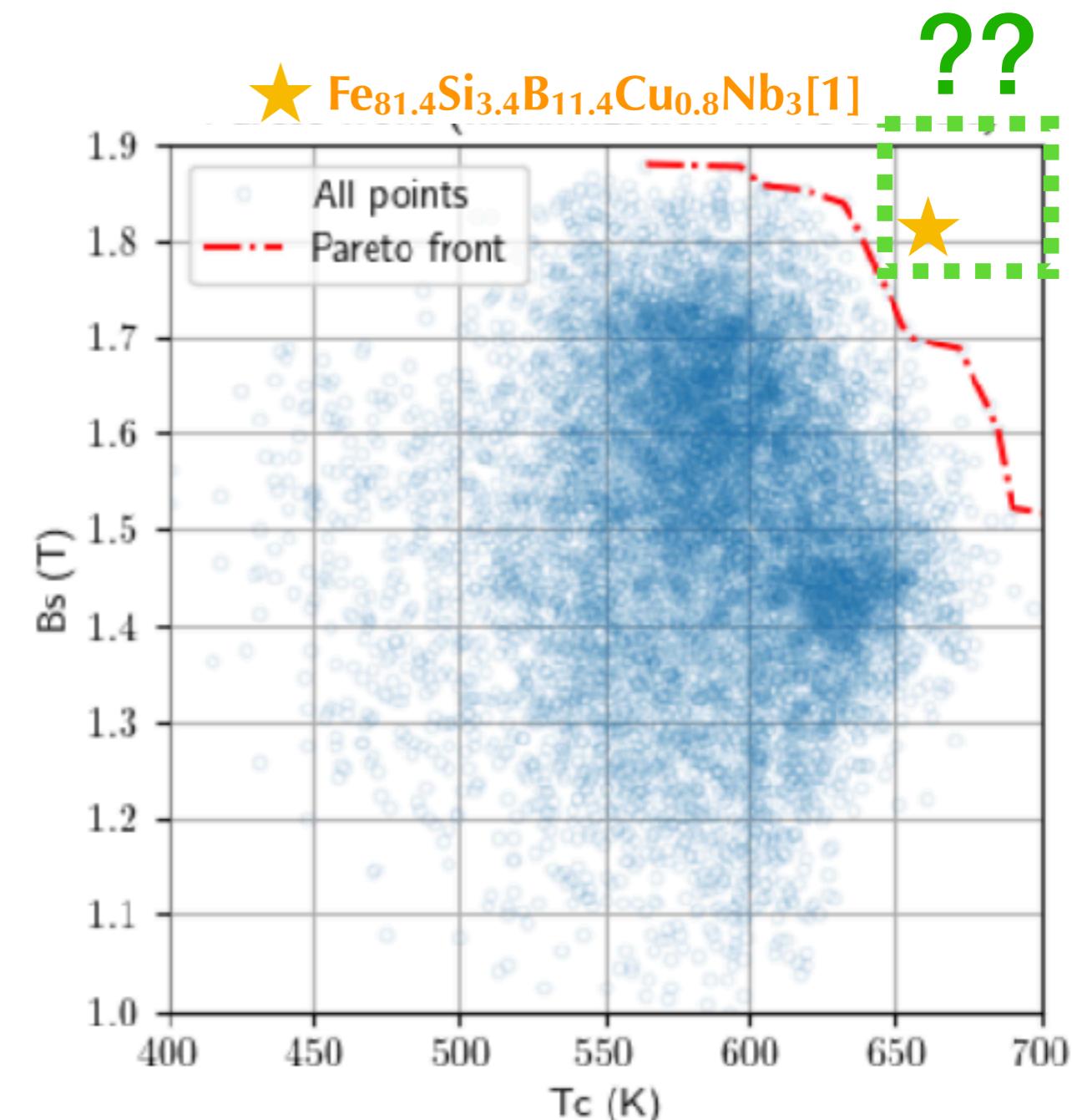
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# Pareto Front

compositions across the Pareto front

	Tc (K)	Bs (T)
B9.0C4.0Fe83.0P1.0Si2.0	594.95	1.86
<u>B13.0Fe82.0Si5.1</u>	641.29	1.76
B7.5C5.0Cu1.0Fe82.7P4.0	559.67	1.86
B9.0C5.0Cu1.0Fe83.2P1.0Si1.0	574.75	1.86
B8.0C2.0Cu1.2Fe83.0P3.0Si3.0	607.87	1.85
B8.0Co4.0Fe82.8P1.0Si4.0	616.28	1.84
B9.0C5.0Cu1.3Fe85.0	551.88	1.90
B13.0Co5.0Fe73.5P3.0Si5.4	659.17	1.66
B11.8C2.0Fe83.0Si3.0	631.10	1.84
B9.0C4.0Cu1.0Fe83.3P3.0	559.17	1.89
B9.0Fe80.4Ga2.0Ni1.3P4.0Si3.4	655.58	1.71

- The Pareto front: improving one property (Bs or Tc) may compromise the other.
- Correlations: The correlation coefficient between predicted Tc and Bs is weak ~ -0.1



- Main Question: can we access the region marked by the green box within the phase space to maximize both Bs and Tc?

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# Bayesian Optimization

$$x^* = \operatorname{argmax}_x f(x)$$

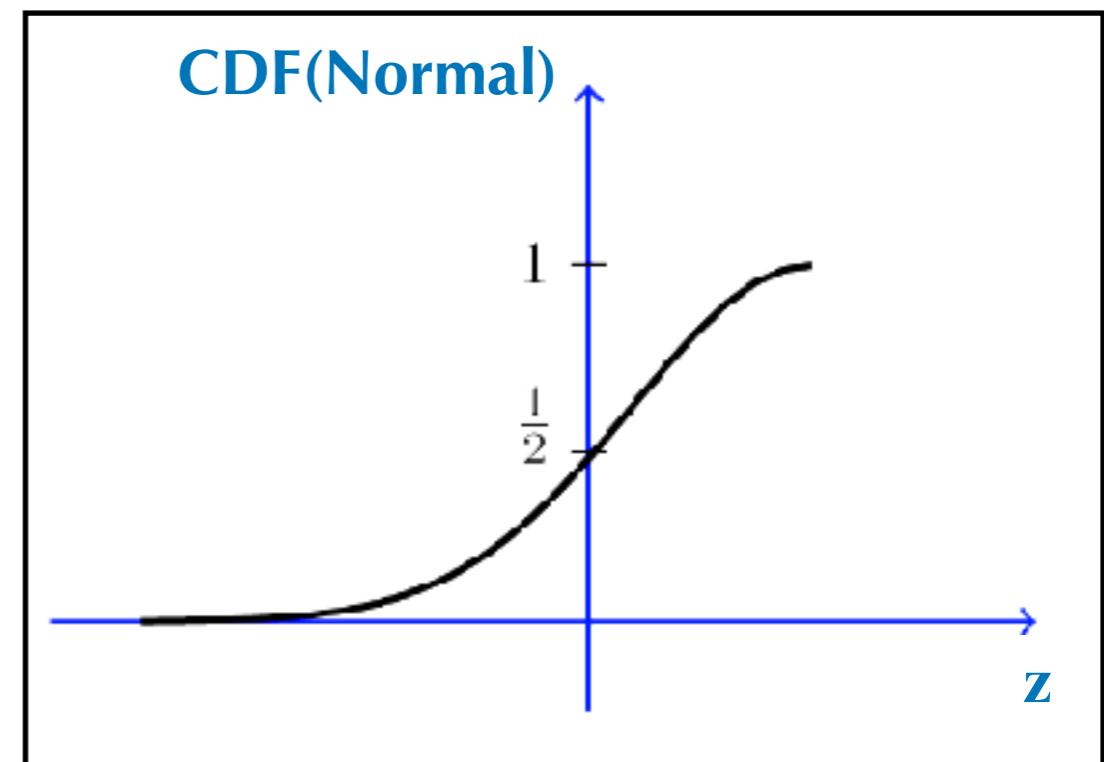
Given observations  $\mathcal{D}_{1:n} = \{(x_i, y_i)\}_{i=1:n}$ , while  $n \leq N$  repeat:

1. Update the surrogate model  $f(x)$ , i.e. the GP posterior  $p(f) = \mathcal{GP}(f; \mu, \sigma)$ , using all available data  $\mathcal{D}_{1:n}$
2. Compute the acquisition function  $u(x \mid \mathcal{D}_{1:n})$ , using the current surrogate model
3. Let  $x_{n+1}$  be the maximizer of the acquisition function, i.e.  $x_{n+1} = \operatorname{argmax}_x u(x \mid \mathcal{D}_{1:n})$
4. Evaluate  $y_{n+1} = f(x_{n+1})$
5. Augment the data  $\mathcal{D}_{1:n+1} = \{\mathcal{D}_{1:n}, (x_{n+1}, y_{n+1})\}$  and increment  $n$

Acquisition function

Standardized sampled point

$$z = \frac{\mu(x_{n+1}) - f^*}{\sigma(x_{n+1})}$$
 best observed value so far



# Bayesian Optimization

Maximize { Tc , Bs } = f(Al, B, ..., Fe, ..., Zr)

Subject to:

0 ≤ Al ≤ 3, 0 ≤ B ≤ 15, ..., 0 ≤ Fe ≤ 85, 0 ≤ Zr ≤ 1 at %,

Al + B + ... + Fe + ... + Zr = 100 at %,

0 ≤ Annealing Time (s) ≤ 3600,

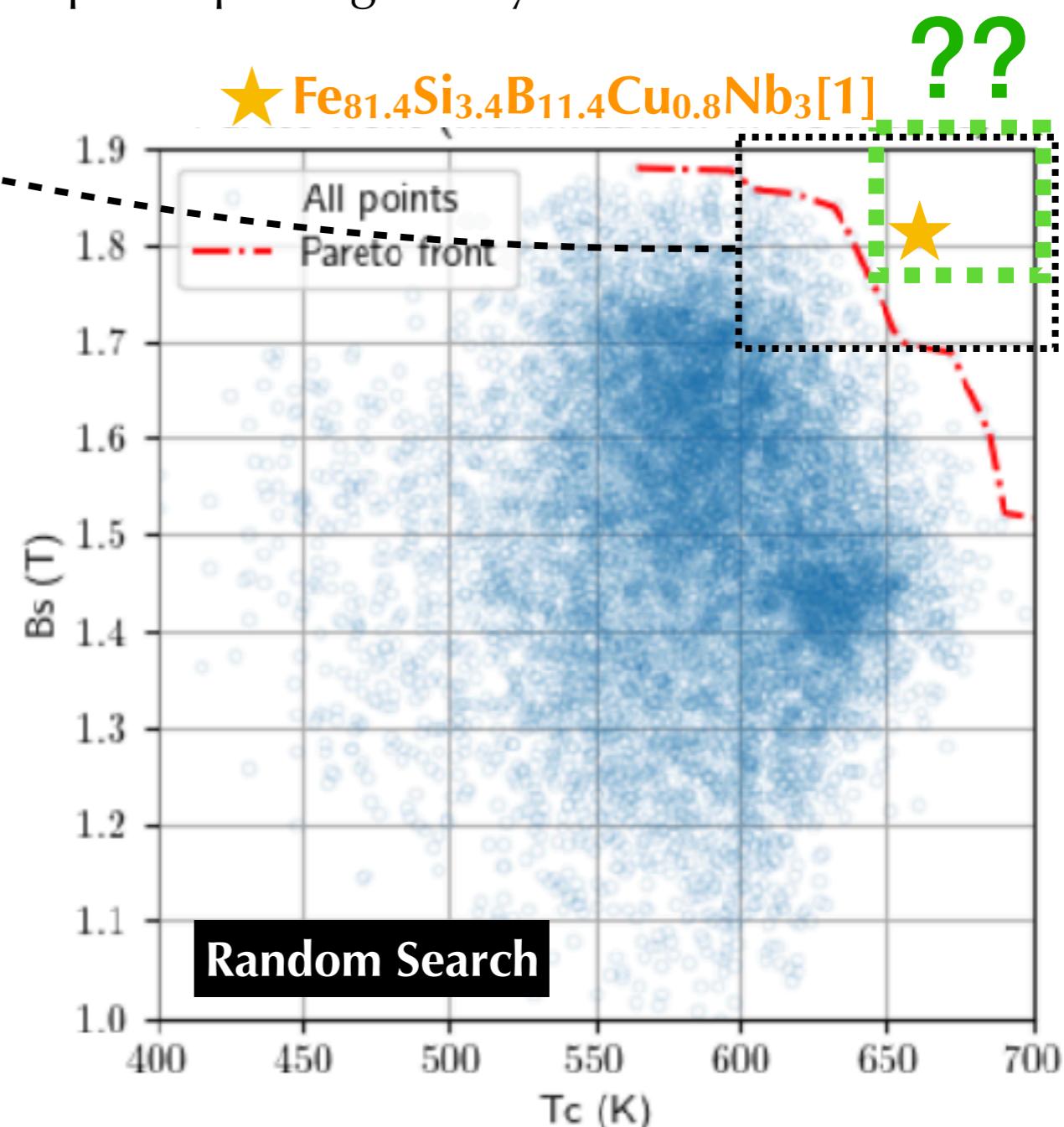
500 ≤ Annealing Temperature (K) ≤ 830,

20 ≤ Thickness (μm) ≤ 30.

- **Constrained optimization:** Let's narrow down our search space based on our random search results.

## Optimization

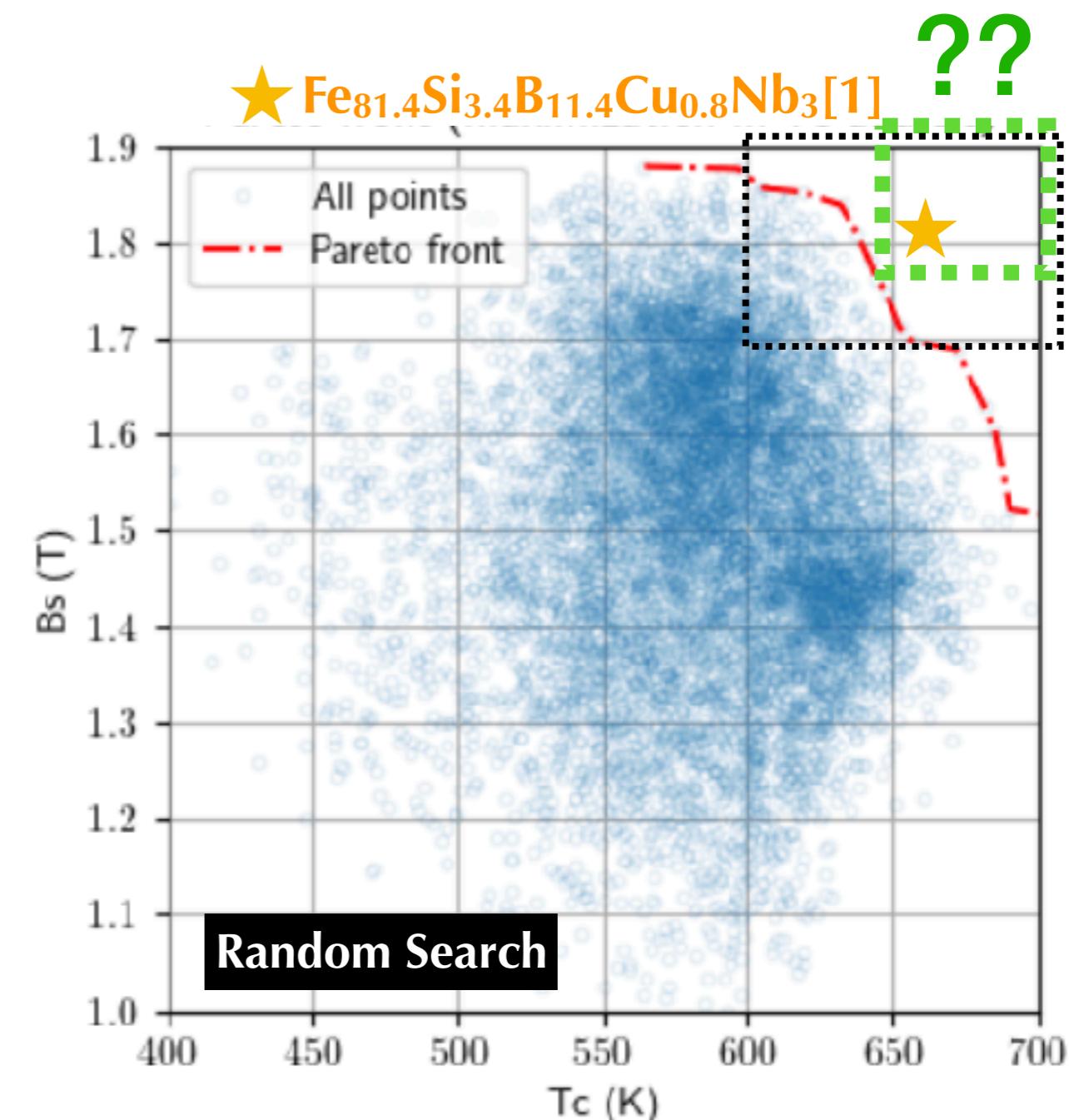
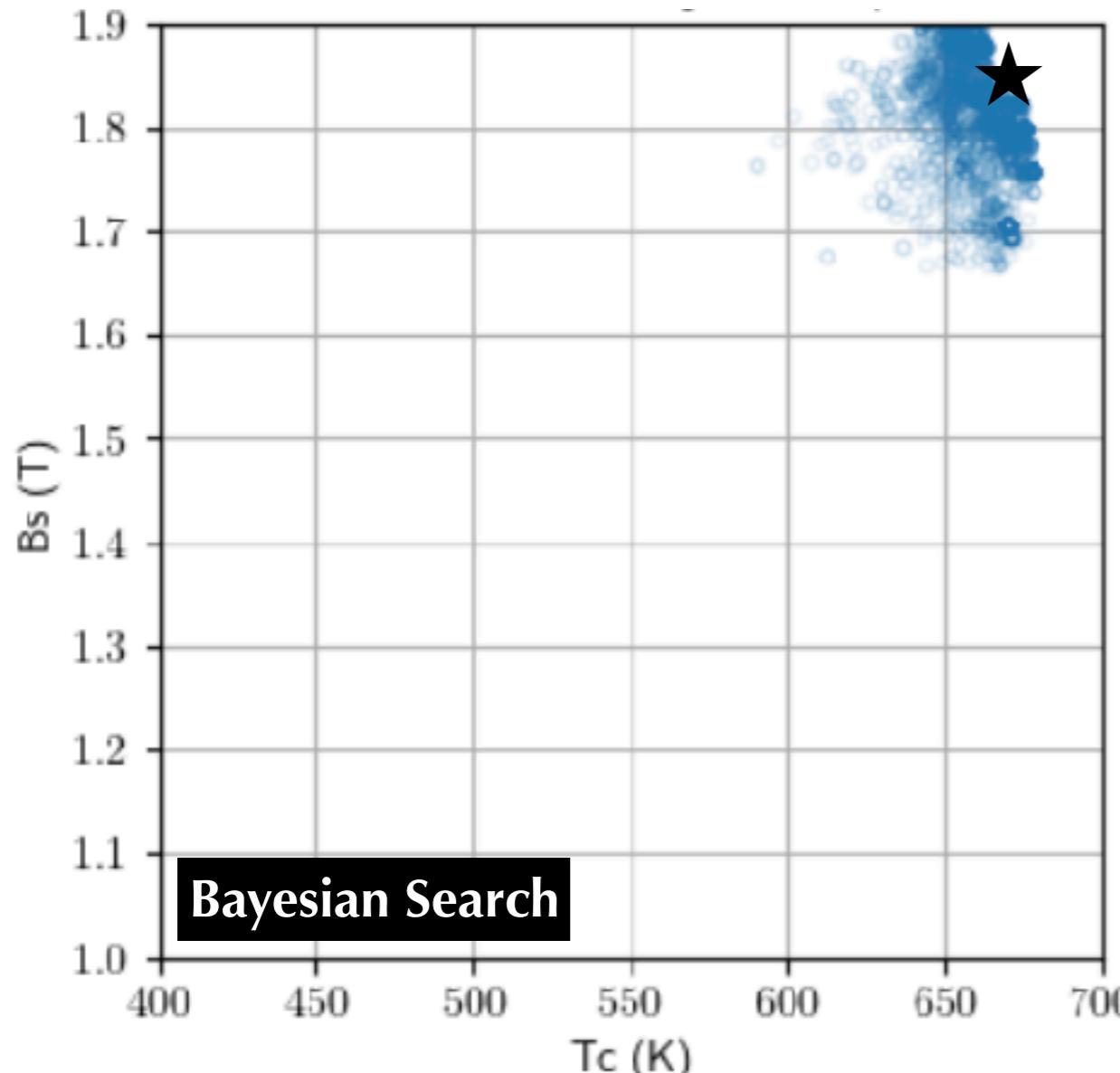
- **Objective:** Suggest new alloys that maximize Bs and Tc.
- **Methodology:** Bayesian Optimization using the Optuna package in Python.



# Bayesian Optimization

★	Annealing Time (s)	Annealing Temperature (K)	Thickness ( $\mu\text{m}$ )	Tc (K)	Bs (T)
B11.9Co2.5Fe79.3Si4.7	831.78	789.98	18.21	670.32	1.85

- Main Question: can we access the region marked by the green box within the phase space to maximize both Bs and Tc?



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# Uncertainty/sensitivity analysis

## Bayes' theorem

$$p(Fe|B_s^{obs}) \propto p(B_s^{obs}|Fe) p(Fe)$$

Posterior distribution      Likelihood function      Prior distribution

$$p(B_s^{obs}|Fe) \propto \exp[-\{B_s^{obs} -$$

## Bayesian framework

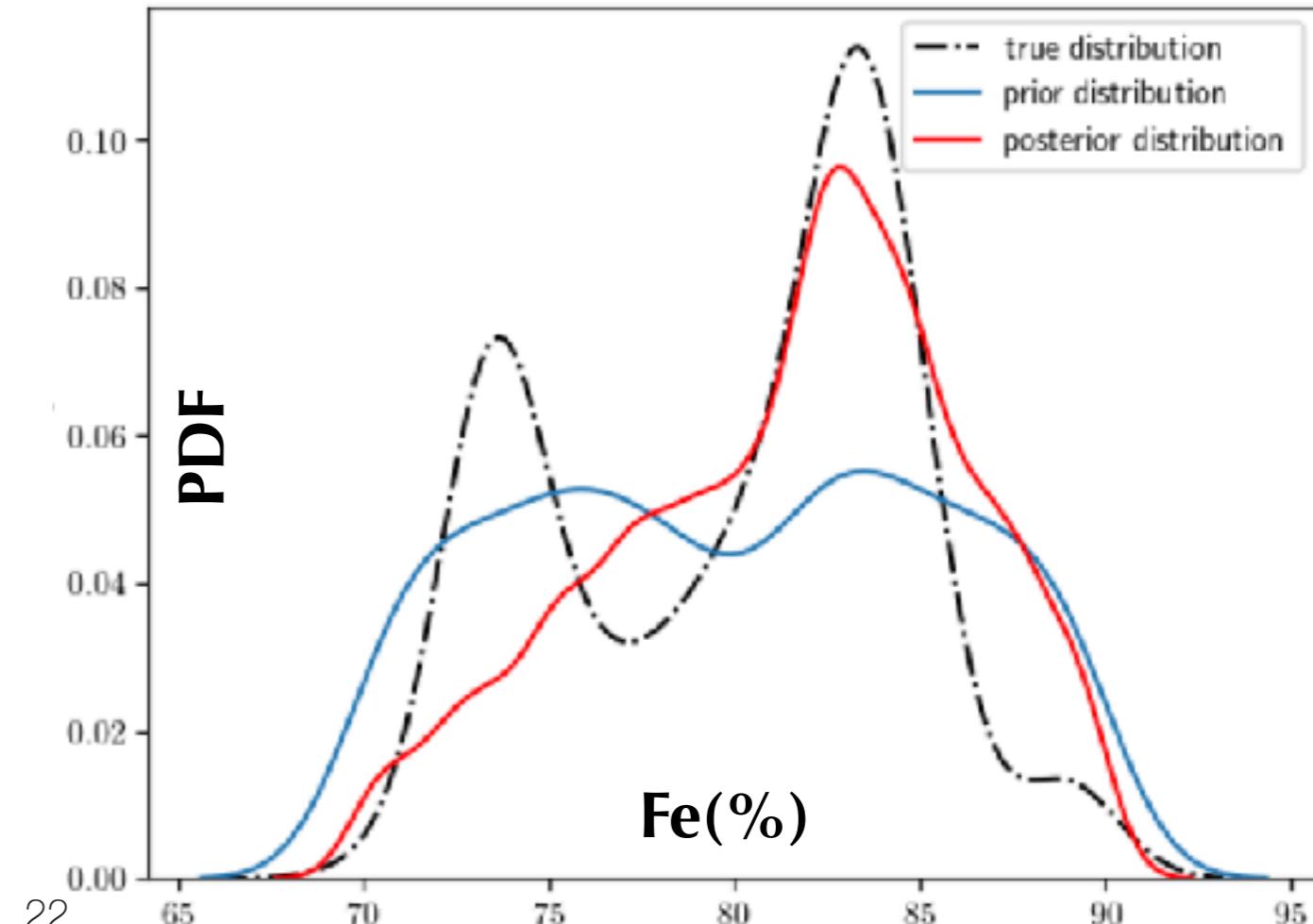
- **Uncertainties in Bs:** due to variations in Fe content within the alloy  $Fe_{83}B_9Si_5P_3$  with  $Bs=1.68 T$

GPR's prediction      GPR's variance

$$\mu_{GPR}(Fe)\}^2 \times \sigma_{GPR}^{-2}(Fe)]$$

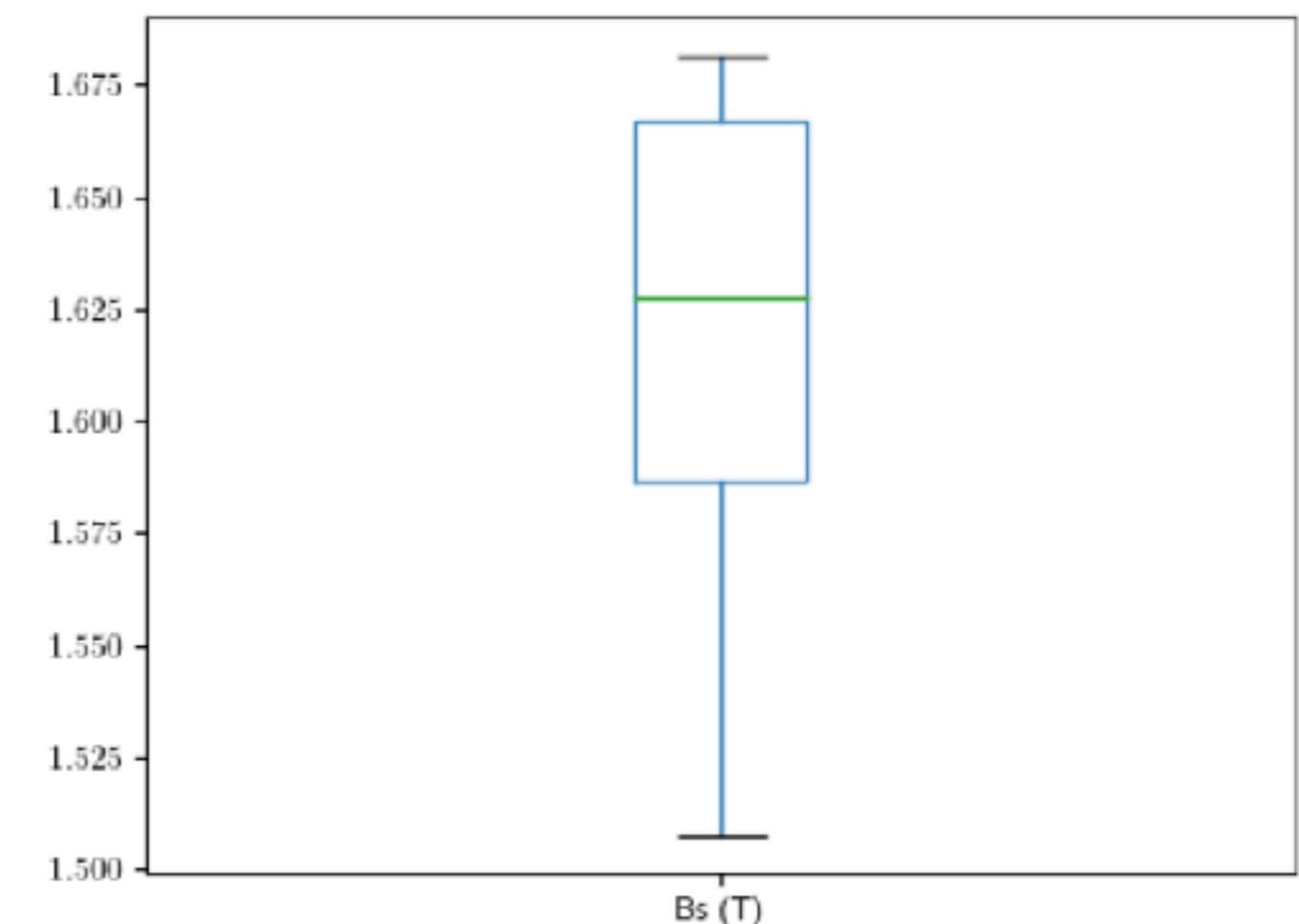
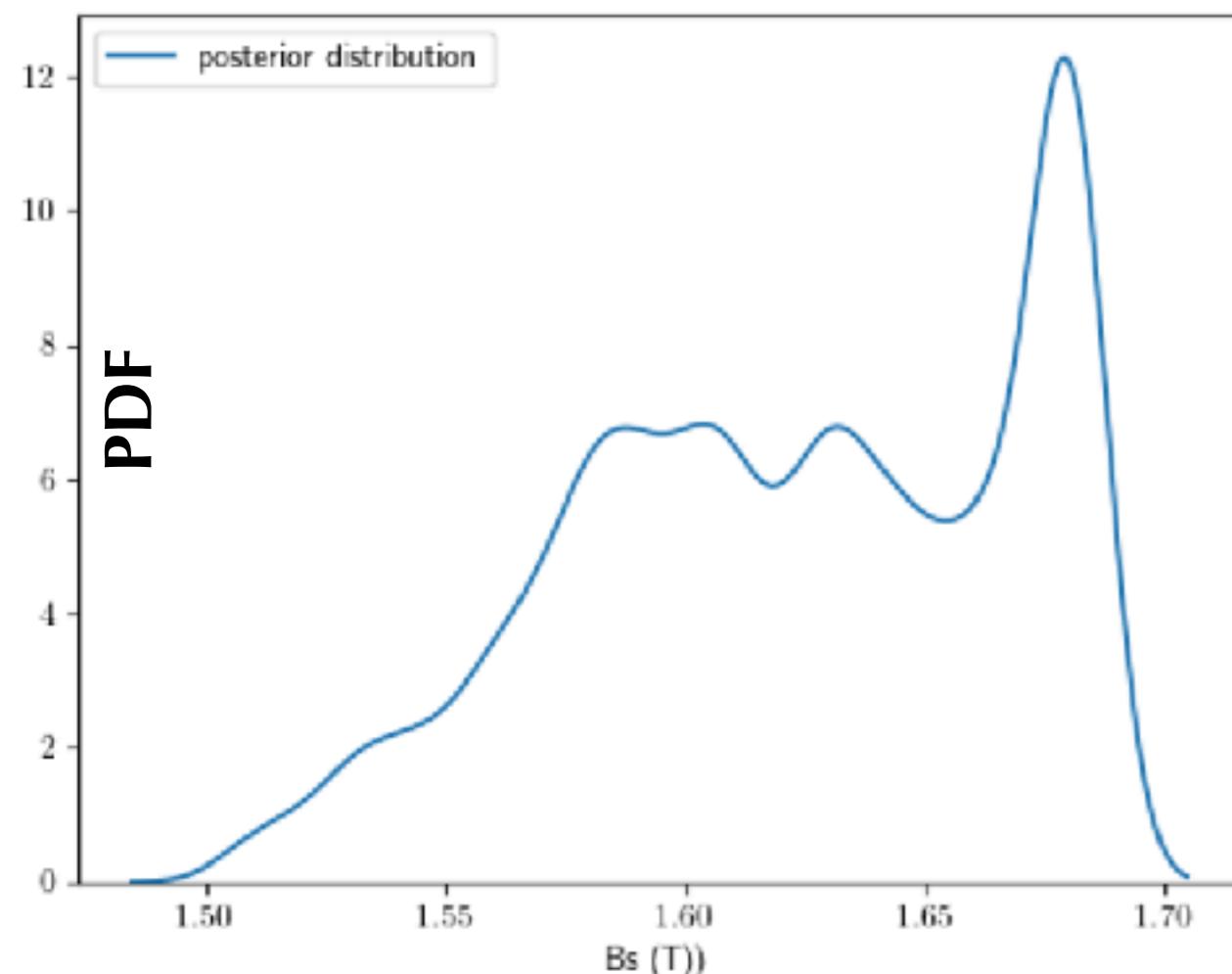
- Define likelihood:  
the difference between observed Bs and GPR-predicted values,  
weighted by the GPR's variance

- Fe's prior distribution:  
uniform around 83%
- Posterior distribution:  
combine the prior and the likelihood to obtain the posterior



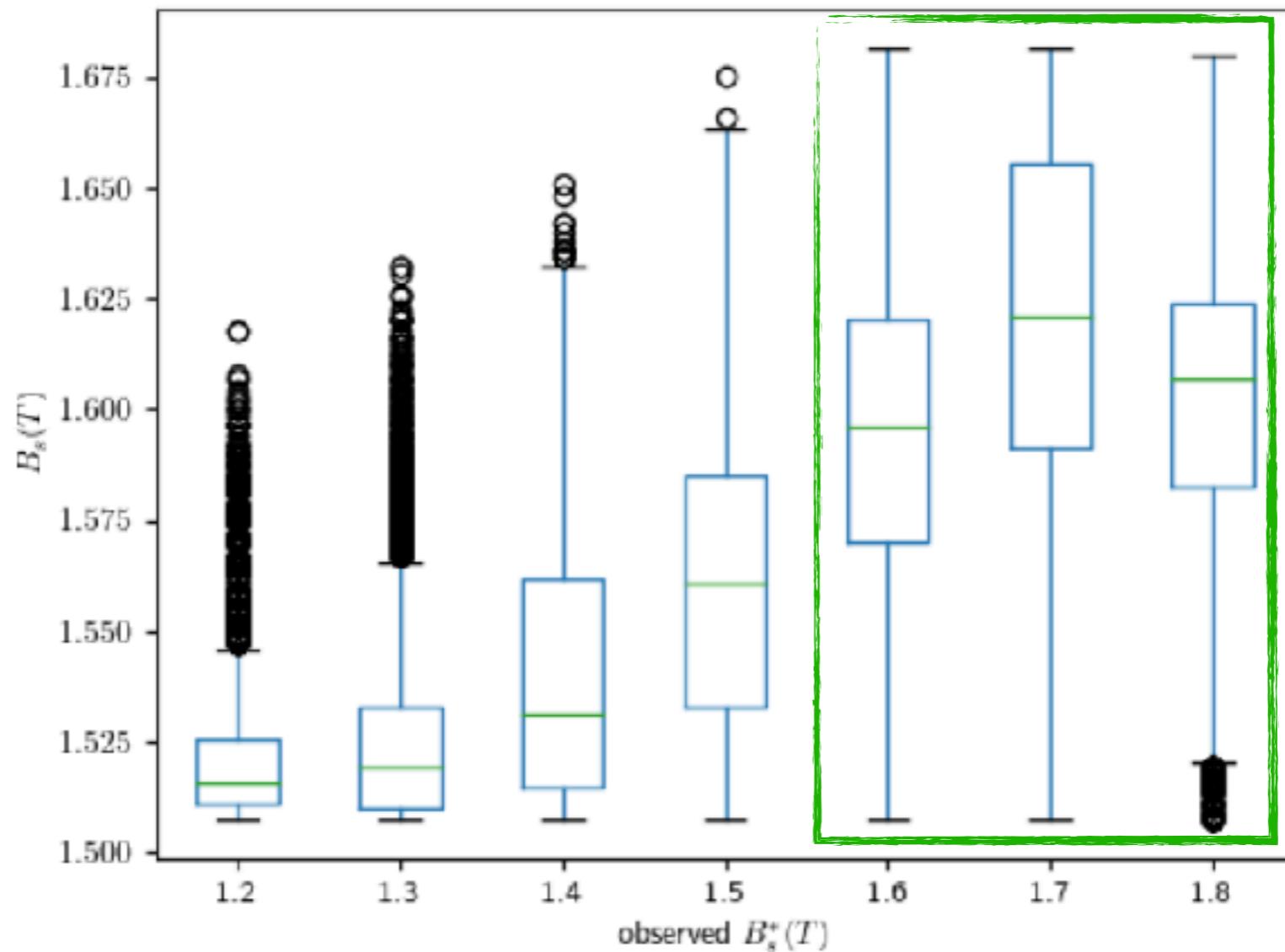
# Uncertainty/sensitivity analysis

Mean BS: 1.6226832626630308  
Standard Deviation of BS: 0.04634739613388416  
90% Confidence Interval for BS: [1.53982611 1.68114307]  
<Axes: >



# Robustness

Robust confidence limit for  
Bs with respect to variations  
in the observed value  $B_s^{\text{obs}}$



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# Constrained Optimization

ARTICLE

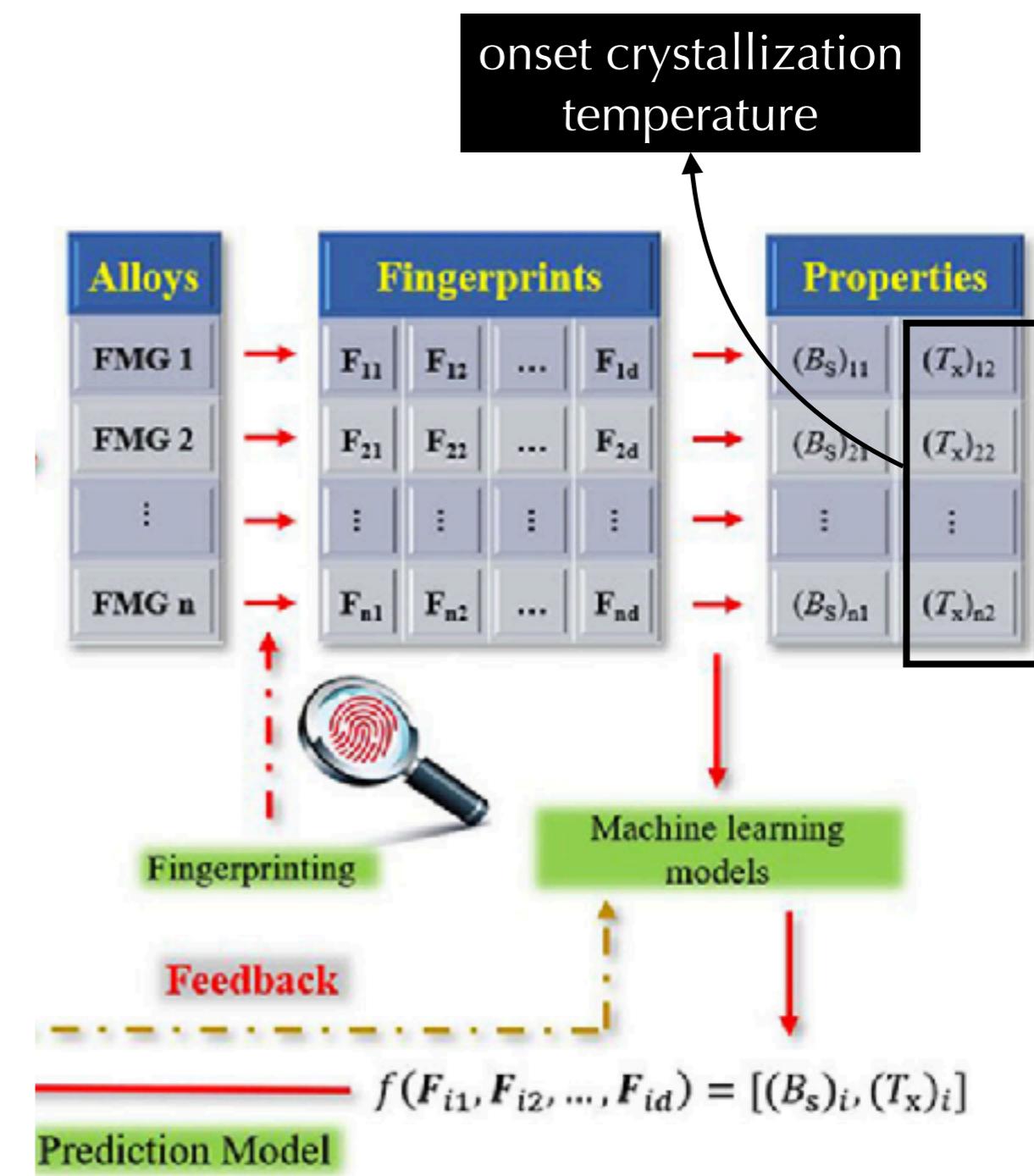
OPEN

 Check for updates

## Interpretable machine-learning strategy for soft-magnetic property and thermal stability in Fe-based metallic glasses

Zhichao Lu<sup>1</sup>, Xin Chen<sup>2</sup>, Xiongjun Liu<sup>1</sup>✉, Deye Lin<sup>2,3</sup>, Yuan Wu<sup>1</sup>, Yibo Zhang<sup>1</sup>, Hui Wang<sup>1</sup>, Suihe Jiang<sup>1</sup>, Hongxiang Li<sup>1</sup>, Xianzhen Wang<sup>4</sup> and Zhaoping Lu<sup>1</sup>✉

Composition (at. %)	Bs/T	Tx/K
Fe83Si2B11P3C1	1.67	727
Fe80P13C7	1.477	696
Fe80P11C9	1.37	720
Fe75B16.67Si8.33	1.57	839
Fe76C7.0Si3.3B5P8.7	1.52	795



# Constrained Optimization

## 3. Optimization with Constraints:

- We are providing an additional dataset containing TX values. Can you refine your optimization code from Task 1 to include a constraint that TX must stay between 600 to 800 K?
  - Provide the optimized alloy compositions that satisfy this constraint.
  - Provide the Pareto front considering this new constraint.

Composition	ta (s)	Ta (K)	Thickness (μm)	Tc (K)
Fe69.5Co0.5Mn10Mo5B15	0.0	0.0	20.0	370.0
Fe80Ni6Zr7Nb2B4Cu1	0.0	0.0	20.0	374.0
Fe90Zr7B3	3600.0	873.3	20.0	388.6
Fe69.5Co0.5Mn10Mo5B15	1800.0	723.0	20.0	389.0
Fe90Zr7B3	3600.0	822.9	20.0	389.7

Composition	ta (s)	Ta (K)	Thickness (μm)	Bs (T)
Fe89Hf7Zr1B3	1800	648.9	32.5	0.3
Fe89Hf7Zr1B3	1800	598.7	32.5	0.4
Fe89Hf7Zr1B3	1800	748.6	32.5	0.4
Fe89Hf7Zr1B3	1800	698.8	32.5	0.6
Fe89Hf7Zr1B3	0	0.0	32.5	0.6

[2] Lu, Zhichao, et al. "Interpretable machine-learning strategy for soft-magnetic property and thermal stability in Fe-based metallic glasses." *npj Computational Materials* 6.1 (2020): 187.

Composition (at. %)	Bs/T	Tx/K
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Fe75B16.67Si8.33	1.57	839
Fe76C7.0Si3.3B5P8.7	1.52	795

Combine these two datasets?

[1] Pang, Bo, et al. "Accelerated discovery of Fe-based amorphous/nanocrystalline alloy through explicit expression and interpretable information based on machine learning." *Materials & Design* 231 (2023): 112054.

# Constrained Optimization

Maximize { Tc, Bs } = f(Al, B, ..., Fe, ..., Zr)

Subject to:

0 ≤ Al ≤ 3, 0 ≤ B ≤ 15, ..., 0 ≤ Fe ≤ 85, 0 ≤ Zr ≤ 1 at %,

Al + B + ... + Fe + ... + Zr = 100 at %,

Annealing Time (s) = 600,

Annealing Temperature (K) = 660,

Thickness (μ m) = 21.

600 K ≤ Tx = g(Al, B, ..., Fe, ..., Zr) ≤ 800 K

**additional constraint**

Let's follow the first approach

## Two general approaches

- **Train a third model:**

$T_x = g(Al, B, \dots, Zr)$  based on the new data set and incorporate this trained  $T_x$  model as part of the constrained optimization

- Make an assumption about the missing processing conditions

- The property map becomes 3-dimensional spanned by (Tc, Bs, Tx) but look at the 2-dimensional sub-space (Tc, Bs) where  $600 < T_x < 800$  K

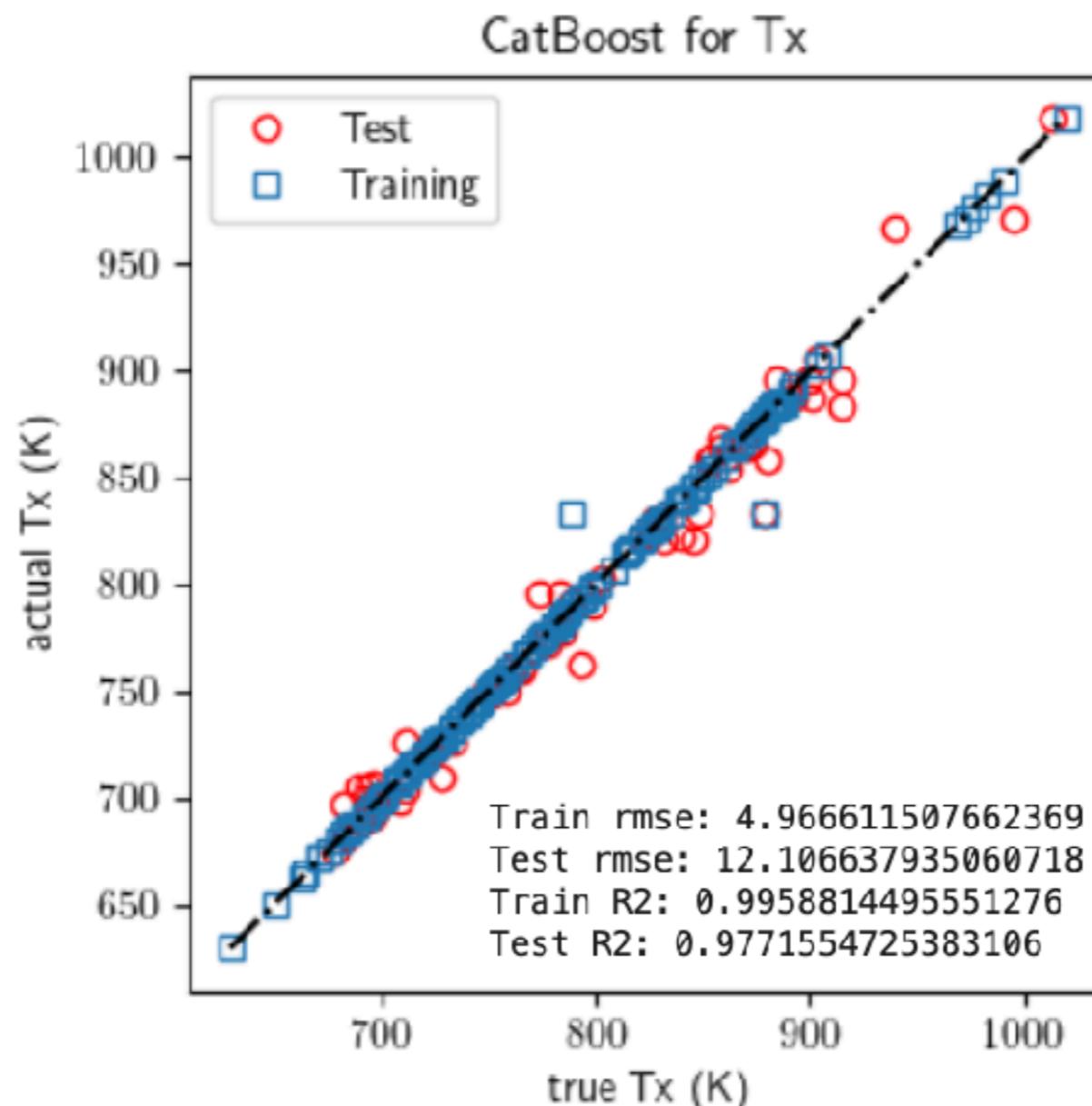
- **Use Tx as additional input feature:**

Re-train  $T_c = f_1(x, T_x)$  and  $B_s = f_2(x, T_x)$  with x being elemental/processing features

- Combine datasets carefully

# Machine Learning

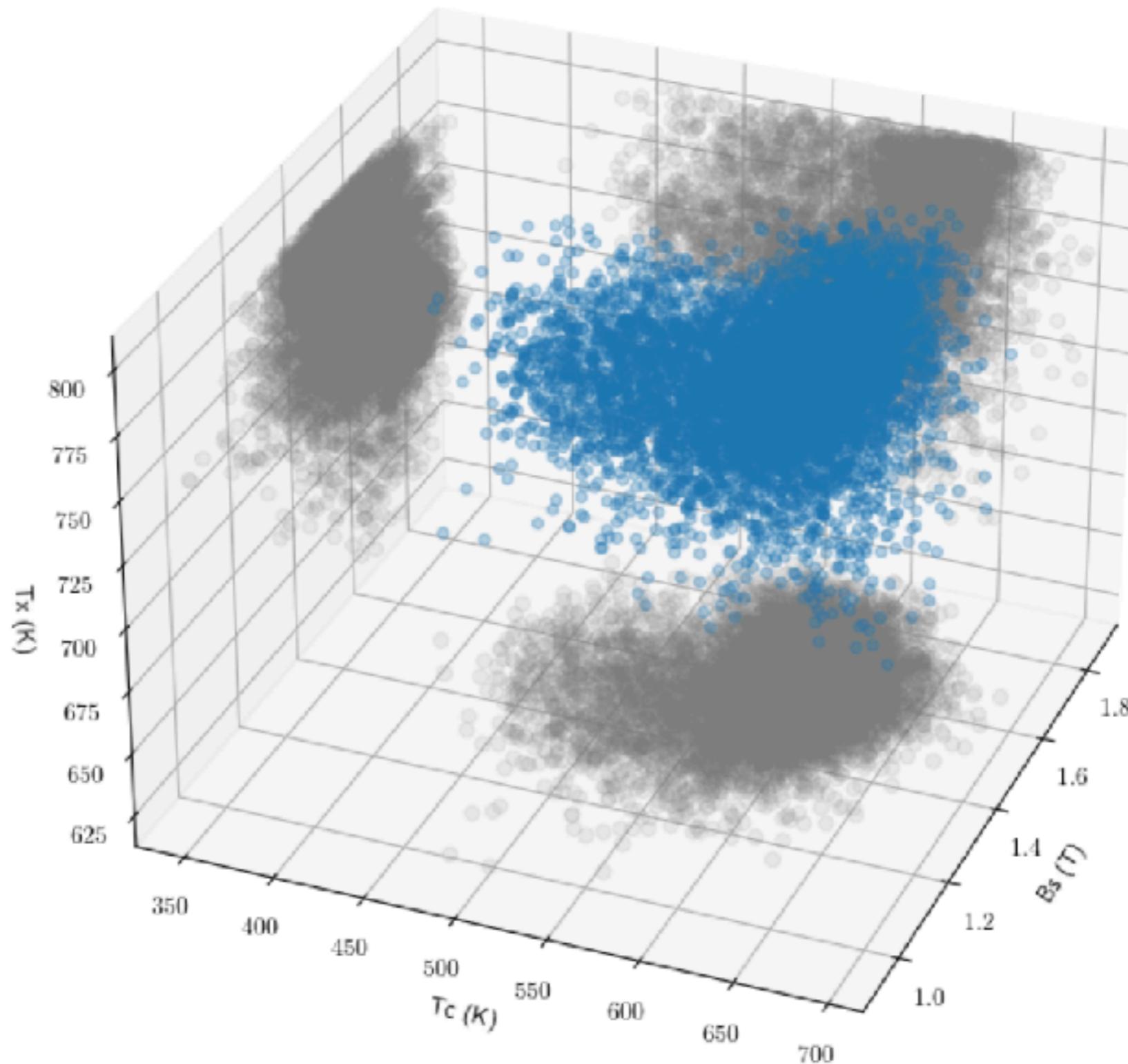
- Models Used: CatBoost
- Hyperparameter Tuning: GridSearchCV, cross-validation
- Training Strategy: Train-test split, standardization, evaluation metrics



# Pareto Front

600<Tx<800 K

Random Search



# Bayesian Optimization

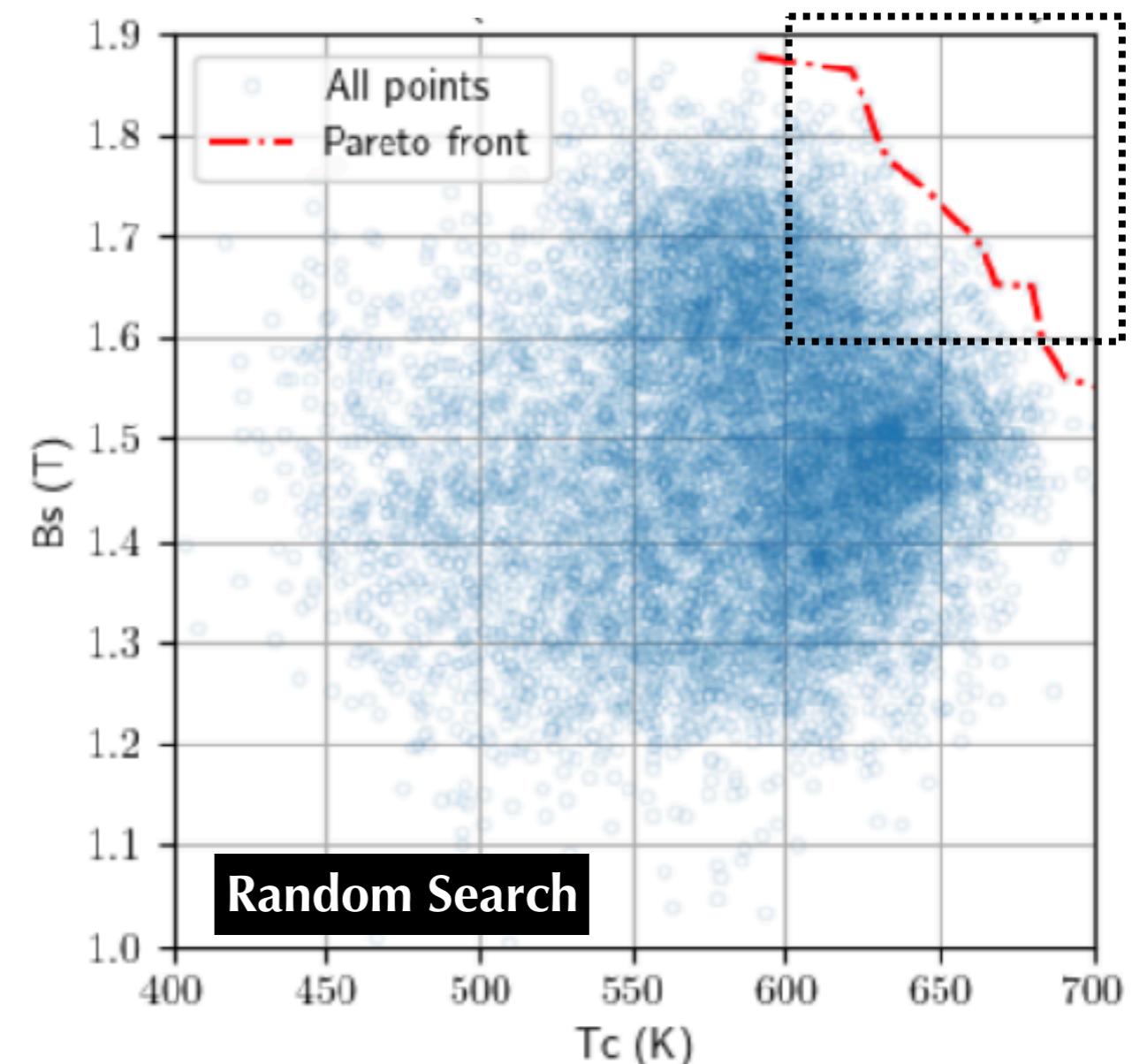
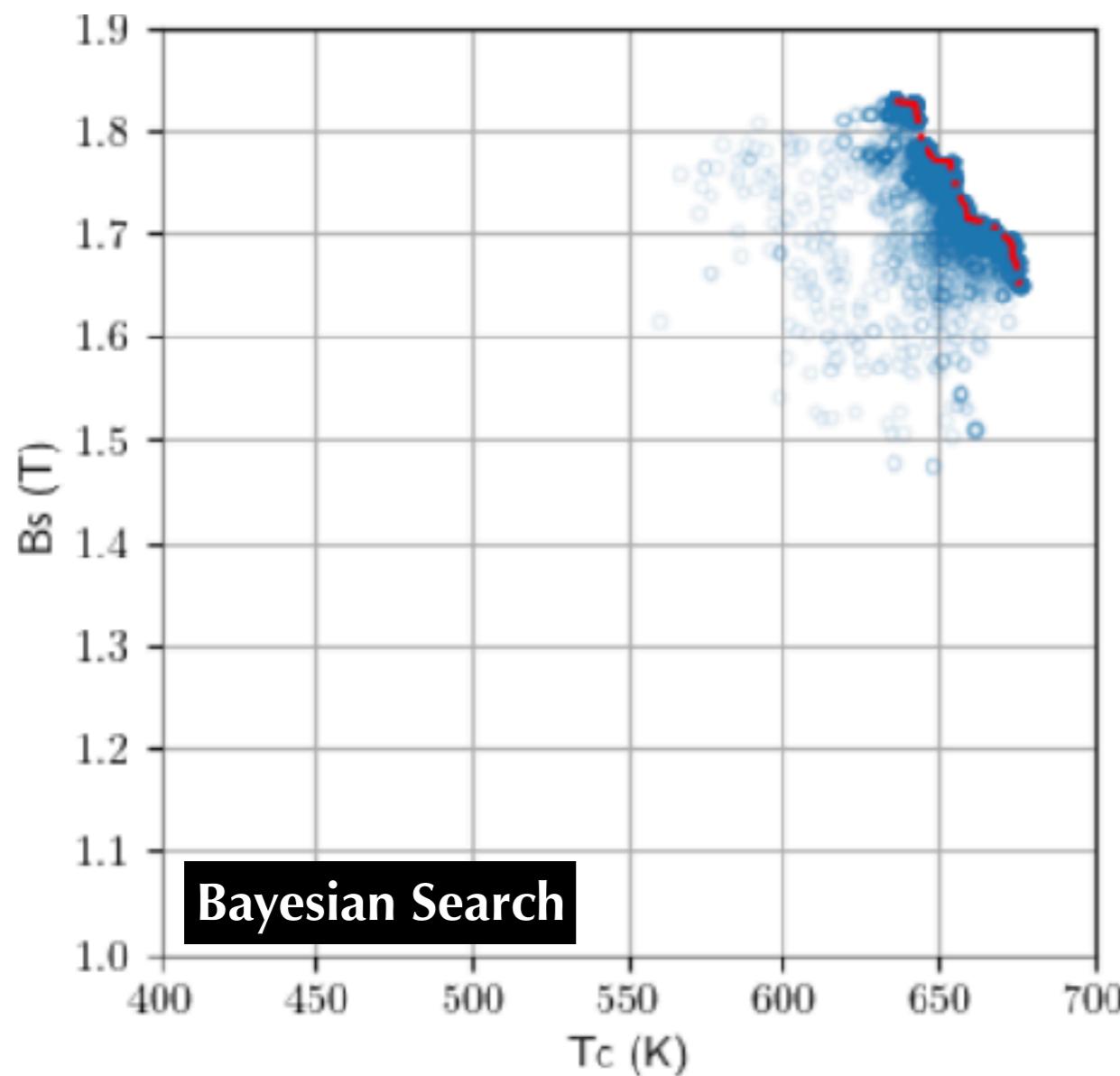
Composition    T<sub>c</sub> (K)    B<sub>s</sub> (T)    T<sub>x</sub> (K)

B11.5Co5.1Fe72.3P5.7Si5.2    687.7    1.5    775.8

B12.0C2.6Co2.0Fe78.3Si5.0    658.8    1.6    784.4

B11.5Co2.1Fe80.4Si5.2    645.7    1.7    753.8

B11.5Co4.8Fe72.4P5.0Si5.0    681.4    1.5    759.9



## Key Findings & Insights:

- **Optimization Results:** The Pareto front analysis excluding the  $T_x$  constraint suggests a trade-off between maximizing  $B_s$  and  $T_c$ . Applying this constraint, it might be feasible to optimize both properties at the same time.
- **Uncertainty Quantification:** Bayesian analysis reveals the impact of fluctuations in Fe composition on the uncertainty of  $B_s$ , highlighting the importance of precise composition control.
- **Additional Data:** Need more comprehensive dataset to capture the interplay between elemental compositions and processing conditions and develop more comprehensive alloy designs.
- **Model Refinement:** Further refinement and fine-tuning of ML models during the optimization process could enhance prediction accuracy.
- **Real-world Validation:** Include experimental validation of the predicted alloy compositions to assess the model's effectiveness in practical applications.