#### Summary of Word Association Mining

- Two basic associations: paradigmatic and syntagmatic
  - Generally applicable to any items in any language (e.g., phrases or entities as units)
- Pure statistical approaches are available for discovering both (can be combined to perform joint analysis).
  - Generally applicable to any text with no human effort
  - Different ways to define "context" and "segment" lead to interesting variations of applications
- Discovered associations can support many other applications.

#### Recommended Reading

- Chris Manning and Hinrich Schütze, Foundations of Statistical Natural Language Processing, MIT Press. Cambridge, MA: May 1999. (Chapter 5 on collocations)
- Chengxiang Zhai, Exploiting context to identify lexical atoms: A statistical view of linguistic context. Proceedings of the International and Interdisciplinary Conference on Modelling and Using Context (CONTEXT-97), Rio de Janeiro, Brazil, Feb. 4-6, 1997. pp. 119-129.
- Shan Jiang and ChengXiang Zhai, Random walks on adjacency graphs for mining lexical relations from big text data. Proceedings of IEEE BigData Conference 2014, pp. 549-554.

## Topic Mining and Analysis: Motivation and Task Definition

ChengXiang "Cheng" Zhai
Department of Computer Science
University of Illinois at Urbana-Champaign



#### **Topic Mining and Analysis:** Motivation and Task Definition

5. Text-based prediction

3. Topic mining and analysis

Real World



Perceive

(Perspective)

Observed World



Express

(English)

Text Data

Natural language processing and text representation

4. Opinion mining and sentiment analysis

2. Word association mining and analysis

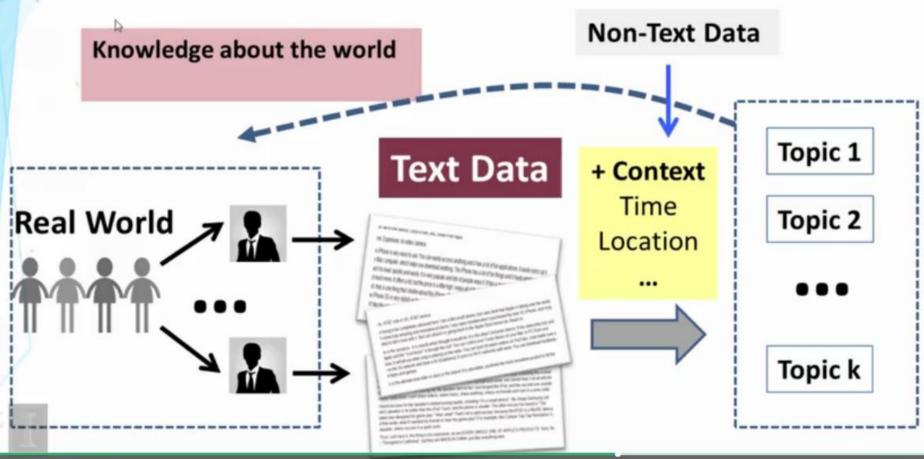


## Topic Mining and Analysis: Motivation

D

- Topic ≈ main idea discussed in text data
  - Theme/subject of a discussion or conversation
  - Different granularities (e.g., topic of a sentence, an article, etc.)
- Many applications require discovery of topics in text
  - What are Twitter users talking about today?
  - What are the current research topics in data mining? How are they different from those 5 years ago?
  - What do people like about the iPhone 6? What do they dislike?
  - What were the major topics debated in 2012 presidential election?

## Topics As Knowledge About the World



## Formal Definition of Topic Mining and Analysis

- Input
  - A collection of N text documents  $C=\{d_1, ..., d_N\}$
  - Number of topics: k
- Output
  - k topics:  $\{\theta_1, ..., \theta_k\}$
  - Coverage of topics in each  $d_i$ : {  $\pi_{i1}$ , ...,  $\pi_{ik}$  }
  - $-\pi_{ij}$  = prob. of  $d_i$  covering topic  $\theta_j$

$$\sum_{j=1}^k \pi_{ij} = 1$$

How to define  $\theta_i$ ?

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## Topic Mining and Analysis: Term as Topic

ChengXiang "Cheng" Zhai
Department of Computer Science
University of Illinois at Urbana-Champaign



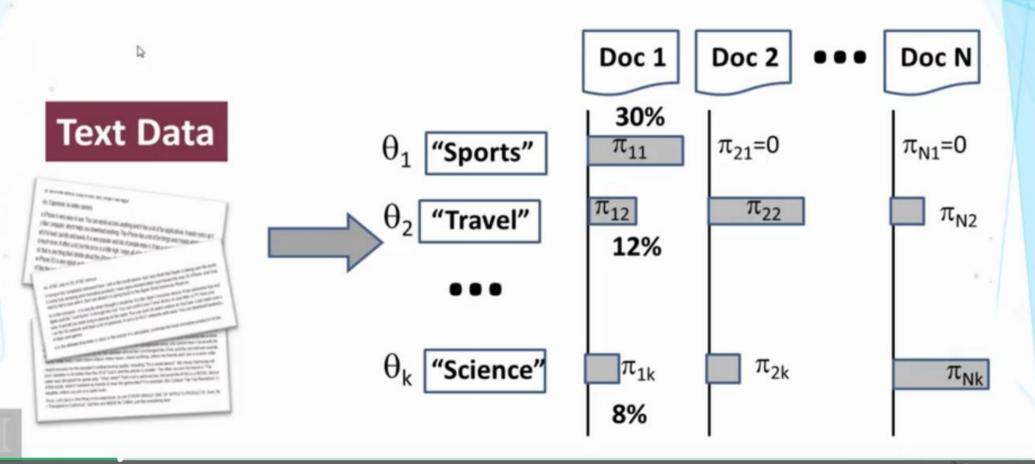
#### Formal Definition of Topic Mining and Analysis

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How to define  $\theta_i$ ?

## Initial Idea: Topic = Term



## Mining k Topical Terms from Collection C

Parse text in C to obtain candidate terms (e.g., term = word).



## Mining k Topical Terms from Collection C

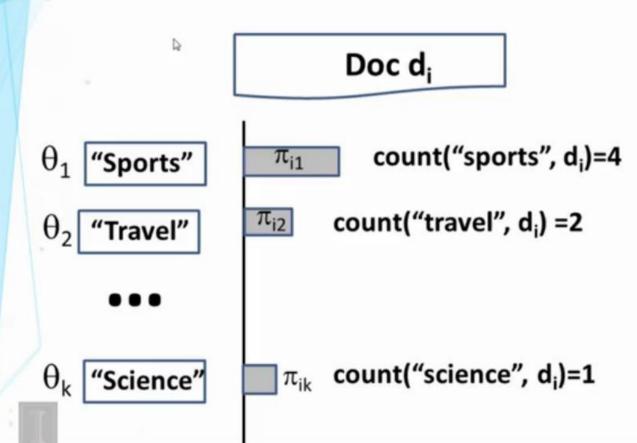
- Parse text in C to obtain candidate terms (e.g., term = word).
- Design a scoring function to measure how good each term is as a topic.
  - Favor a representative term (high frequency is favored)
  - Avoid words that are too frequent (e.g., "the", "a").
  - TF-IDF weighting from retrieval can be very useful.
  - Domain-specific heuristics are possible (e.g., favor title words, hashtags in tweets).



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  - TF-IDF weighting from retrieval can be very useful.
  - Domain-specific heuristics are possible (e.g., favor title words, hashtags in tweets).
- Pick k terms with the highest scores but try to minimize redundancy.
  - If multiple terms are very similar or closely related, pick only one of them and ignore others.

## Computing Topic Coverage: $\pi_{ij}$



$$\pi_{ij} = \frac{count(\theta_j, d_i)}{\sum_{L=1}^{k} count(\theta_L, d_i)}$$

## How Well Does This Approach Work?



Cavaliers vs. Golden State Warriors: NBA playoff finals ... basketball game ... travel to Cleveland ... star ...

$$\theta_1$$
 "Sports"

$$\pi_{i1} \propto c("sports", d_i) = 0 \longleftarrow$$

1. Need to count related words also!

$$\theta_2$$
 "Travel"

$$\pi_{i2} \propto c("travel", d_i) = 1 > 0$$

•••

2. "Star" can be ambiguous (e.g., star in the sky).

$$\theta_k$$
 "Science"

$$\pi_{ik} \propto c("science", d_i) = 0$$

3. Mine complicated topics?

## Problems with "Term as Topic"

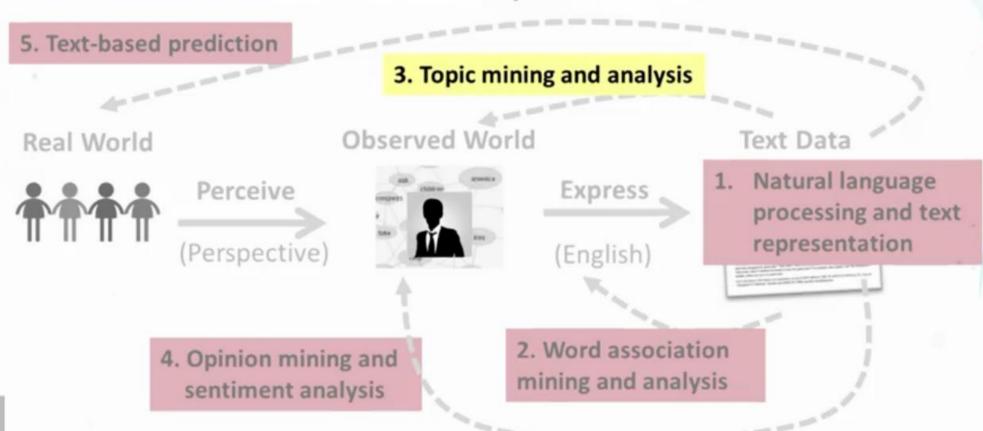
- Lack of expressive power
  - Can only represent simple/general topics
  - Can't represent complicated topics
- Incompleteness in vocabulary coverage
  - Can't capture variations of vocabulary (e.g., related words)
- Word sense ambiguity
  - A topical term or related term can be ambiguous (e.g., basketball star vs. star in the sky)

# Topic Mining and Analysis: Probabilistic Topic Models

ChengXiang "Cheng" Zhai
Department of Computer Science
University of Illinois at Urbana-Champaign



## Topic Mining and Analysis: Probabilistic Topic Models



#### Problems with "Term as Topic"

- Lack of expressive power
- → Topic = {Multiple Words}
- Can only represent simple/general topics
- Can't represent complicated topics
- Incompleteness in vocabulary coverage + weights on words
  - Can't capture variations of vocabulary (e.g., related words)
- Word sense ambiguity → Split an ambiguous word
  - A topical term or related term can be ambiguous (e.g., basketball star vs. star in the sky)

A probabilistic topic model can do all these!

#### Improved Idea: Topic = Word Distribution

```
\theta_1 "Sports"
```

 $P(w|\theta_1)$ 

```
sports 0.02
game 0.01
basketball 0.005
football 0.004
play 0.003
star 0.003
...
nba 0.001
...
travel 0.0005
```

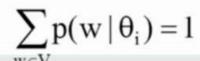
```
\theta_2 "Travel"
```

 $P(w | \theta_2)$ 

```
travel 0.05
attraction 0.03
trip 0.01
flight 0.004
hotel 0.003
island 0.003
...
culture 0.001
...
play 0.0002
...
```

$$\theta_k$$
 "Science"  $P(w | \theta_k)$ 

```
science 0.04
scientist 0.03
spaceship 0.006
telescope 0.004
genomics 0.004
star 0.002
...
genetics 0.001
...
travel 0.00001
```



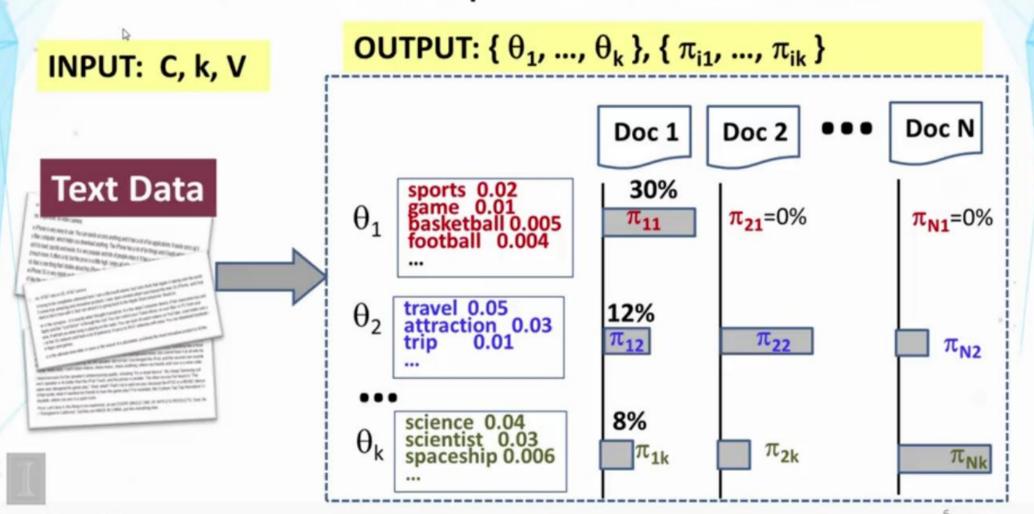
Vocabulary Set: V={w1, w2,....}

## Probabilistic Topic Mining and Analysis

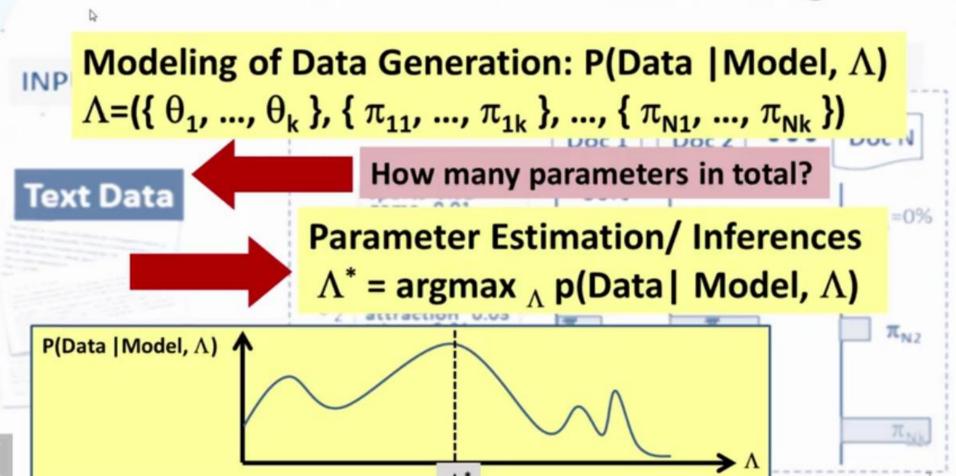
- Input
  - A collection of N text documents  $C=\{d_1, ..., d_N\}$
  - Vocabulary set: V={w<sub>1</sub>, ..., w<sub>M</sub>}
  - Number of topics: k
- Output
  - k topics, each a word distribution:  $\{\theta_1, ..., \theta_k\}$
- $\sum_{w \in V} p(w \mid \theta_i) = 1$
- Coverage of topics in each  $d_i$ : {  $\pi_{i1}$ , ...,  $\pi_{ik}$  }
- $-\pi_{ij}$ =prob. of d<sub>i</sub> covering topic  $\theta_{j}$

$$\sum_{j=1}^k \pi_{ij} = 1$$

#### The Computation Task



#### Generative Model for Text Mining



#### Summary

- Topic represented as word distribution
  - Multiple words: allow for describing a complicated topic
  - Weights on words: model subtle semantic variations of a topic
- Task of topic mining and analysis
  - Input: collection C, number of topics k, vocabulary set V
  - Output: a set of topics, each a word distribution; coverage of all topics in each document

$$\Lambda = (\{ \theta_1, ..., \theta_k \}, \{ \pi_{11}, ..., \pi_{1k} \}, ..., \{ \pi_{N1}, ..., \pi_{Nk} \})$$

$$\forall j \in [1, k], \sum_{w \in V} p(w \mid \theta_j) = 1 \\ \forall i \in [1, N], \sum_{i = 1}^k \pi_{ij} = 1$$

$$\forall i \in [1, N], \ \sum_{j=1}^k \pi_{ij} = 1$$

#### Summary (cont.)

- Generative model for text mining
  - Model data generation with a prob. model: P(Data | Model,  $\Lambda$ )
  - Infer the most likely parameter values  $\Lambda^*$  given a particular data set:  $\Lambda^*$  = argmax  $_{\Lambda}$  p(Data | Model,  $\Lambda$ )
  - Take  $\Lambda^*$  as the "knowledge" to be mined for the text mining problem
  - Adjust the design of the model to discover different knowledge

## Topic Mining and Analysis: Overview of Statistical Language Models

Part 1

ChengXiang "Cheng" Zhai
Department of Computer Science
University of Illinois at Urbana-Champaign



## **Probabilistic Topic Models:** Overview of Statistical Language Models

5. Text-based prediction

4----

3. Topic mining and analysis

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sentiment analysis

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#### What Is a Statistical Language Model (LM)?

- A probability distribution over word sequences
  - -p("Today is Wednesday") ≈ 0.001
  - -p("Today Wednesday is") ≈ 0.000000000001
  - p("The eigenvalue is positive") ≈ 0.00001
- Context-dependent!
- Can also be regarded as a probabilistic mechanism for "generating" text – thus also called a "generative" model





## The Simplest Language Model: Unigram LM

- Generate text by generating each word INDEPENDENTLY
- Thus,  $p(w_1 w_2 ... w_n) = p(w_1)p(w_2)...p(w_n)$
- Parameters:  $\{p(w_i)\}\ p(w_1)+...+p(w_N)=1\ (N \text{ is voc. size})$
- Text = sample drawn according to this word distribution



```
p("today is Wed")
   = p(\text{"today"})p(\text{"is"})p(\text{"Wed"})
   = 0.0002 \times 0.001 \times 0.000015
```

10:25

#### Text Generation with Unigram LM

D

#### Unigram LM $p(w|\theta)$

Sampling

Document d  $p(d|\theta)=?$ 

Topic 1:
Text mining

text 0.2 mining 0.1 association 0.01 clustering 0.02

Text mining paper

food 0.00001

Topic 2: **Health** 

food 0.25 nutrition 0.1 healthy 0.05 diet 0.02



Food nutrition paper

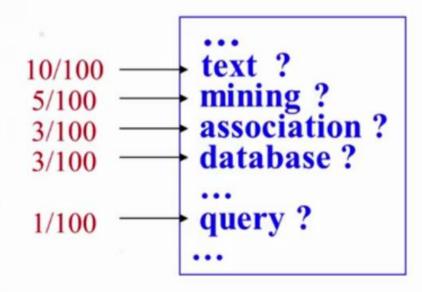
#### Estimation of Unigram LM

Unigram LM  $p(w|\theta)=?$ 



Text Mining Paper d

Total #words=100





text 10
mining 5
association 3
database 3
algorithm 2
...
query 1
efficient 1

Is this our best estimate? How do we define "best"?

## Topic Mining and Analysis: Overview of Statistical Language Models

Part 2

ChengXiang "Cheng" Zhai
Department of Computer Science
University of Illinois at Urbana-Champaign



## Maximum Likelihood vs. Bayesian

- Maximum likelihood estimation
  - "Best" means "data likelihood reaches maximum"

$$\hat{\theta} = \arg \max P(X \mid \theta)$$

- Problem: Small sample
- Bayesian estimation:

Bayes Rule 
$$p(X|Y) = \frac{p(Y|X)p(X)}{p(Y)}$$

- "Best" means being consistent with our "prior" knowledge and explaining data well

$$\hat{\theta} = \text{arg max } P(\theta \mid X) = \text{arg max } P(X \mid \theta)P(\theta)$$

– Problem: How to define prior?



Maximum a Posteriori (MAP) estimate

## Illustration of Bayesian Estimation

Bayesian inference:  $f(\theta)=?$ **Posterior:** Likelihood:  $p(\theta|X) \propto p(X|\theta)p(\theta)$  $\hat{f}(\theta) = \sum f(\theta)p(\theta \mid X)$  $p(X|\theta)$  $X = (x_1, ..., x_N)$  $\hat{\theta} = \sum \theta * p(\theta \mid X)$ **Posterior** Mean Prior:  $p(\theta)$ θ  $\theta_0$ : prior mode

 $\theta_1$ : posterior mode

 $\theta_{ml}$ : ML estimate

#### Summary

- Language Model = probability distribution over text = generative model for text data
- Unigram Language Model = word distribution
- Likelihood function: p(X | θ)
  - Given  $\theta$   $\rightarrow$  which X has a higher likelihood?
  - Given X → which  $\theta$  maximizes  $p(X|\theta)$ ? [ML estimate]
- Bayesian estimation/inference
  - Must define a **prior**:  $p(\theta)$
  - Posterior distribution:  $p(\theta|X) \propto p(X|\theta)p(\theta)$
  - $\rightarrow$  Allows for inferring any "derived value" from  $\theta$ !

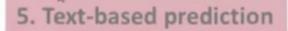


## Topic Mining and Analysis: Mining One Topic

ChengXiang "Cheng" Zhai
Department of Computer Science
University of Illinois at Urbana-Champaign



#### Probabilistic Topic Models: Mining One Topic



4----

3. Topic mining and analysis

Real World



Perceive

(Perspective)

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Express

(English)

Text Data

 Natural language processing and text representation

Salar de controller de la controller de

4. Opinion mining and sentiment analysis

2. Word association mining and analysis







#### Simplest Case of Topic Model: Mining One Topic

INPUT: C={d}, V

#### **Text Data**

fig in displaying the term of the second sec

Spelan guidy in 4853/1525-CRESCOSE. The guider is unply ordinations, when you are cycling exologicals. When water it is define up because you can have of concerns large soundary like of lawsaler. What is for this period of all And And Anne is All And Angland sound you support the field with many policy was for the guider of an And Angland State (and Angland State) and and sound washing of and share whose, the man when you have the foreign as washing of an and and and an analysis.

hand records to the protect reflectioning guidy, including "to a mild describ" the thorp Serving self, and a sotherprocess made. The other second in traction "the sales excepted to protection of the Affiliation of excluding the country of PETC or Affiliation of the country of PETC or Affiliation of the country of the Country of the Affiliation of the

Ros Left Ser C Multing is to represe, as an ESER SREED DE STAPPLES PRODUCTS. Say, for "Despector Calcins" bother an IACE MORAL per like mending site.

Brotton SEES .....

OUTPUT:  $\{\theta\}$ 

 $P(w|\theta)$ 

θ

text ?
mining ?
association ?
database ?

... query

•••

Doc d

100%

#### Language Model Setup

- **Data**: Document  $d = x_1 x_2 ... x_{|d|}$ ,  $x_i \in V = \{w_1, ..., w_M\}$  is a word
- Model: Unigram LM  $\theta$ (=topic) : { $\theta_i$ =p( $w_i \mid \theta$ )}, i=1, ..., M;  $\theta_1+...+\theta_M=1$
- **Likelihood** function:  $p(d \mid \theta) = p(x_1 \mid \theta) \times ... \times p(x_{|d|} \mid \theta)$ =  $p(w_1 | \theta)^{c(w_1,d)} \times ... \times p(w_M | \theta)^{c(w_M,d)}$  $= \prod_{i=1}^{M} p(w_i \mid \theta)^{c(w_i,d)} = \prod_{i=1}^{M} \theta_i^{c(w_i,d)}$
- ML estimate:  $(\hat{\theta}_1, ..., \hat{\theta}_M) = \arg \max_{\theta_1, ..., \theta_M} p(d \mid \theta) = \arg \max_{\theta_1, ..., \theta_M} \prod_{i=1}^{M} \theta_i^{c(w_i, d)}$

#### Computation of Maximum Likelihood Estimate

Maximize 
$$p(d \mid \theta)$$
  $(\hat{\theta}_1, ..., \hat{\theta}_M) = \arg \max_{\theta_1, ..., \theta_M} p(d \mid \theta) = \arg \max_{\theta_1, ..., \theta_M} \prod_{i=1}^M \theta_i^{c(w_i, d)}$ 

$$\textbf{Max. Log-Likelihood} \quad (\hat{\theta}_1, ..., \hat{\theta}_M) = \arg\max_{\theta_1, ..., \theta_M} \log[p(d \mid \theta)] = \arg\max_{\theta_1, ..., \theta_M} \sum_{i=1}^M c(w_i, d) \log \theta_i$$

$$\sum_{i=1}^M \theta_i = 1$$

Subject to constraint:  $\sum_{i=1}^{M} \theta_i = 1$  Use Lagrange multiplier approach

Lagrange function: 
$$f(\theta \mid d) = \sum_{i=1}^{M} c(w_i, d) \log \theta_i + \lambda (\sum_{i=1}^{M} \theta_i - 1)$$

$$\frac{\partial f(\theta \mid d)}{\partial \theta_i} = \frac{c(w_i, d)}{\theta_i} + \lambda = 0 \quad \Rightarrow \quad \theta_i = -\frac{c(w_i, d)}{\lambda}$$

$$\sum_{i=1}^{M} -\frac{c(w_{i}, d)}{\lambda} = 1 \to \lambda = -\sum_{i=1}^{N} c(w_{i}, d) \to \hat{\theta}_{i} = p(w_{i} | \hat{\theta}) = \frac{c(w_{i}, d)}{\sum_{i=1}^{M} c(w_{i}, d)} = \frac{c(w_{i}, d)}{|d|}$$

#### Computation of Maximum Likelihood Estimate

Maximize 
$$p(d \mid \theta)$$
  $(\hat{\theta}_1, ..., \hat{\theta}_M) = \arg \max_{\theta_1, ..., \theta_M} p(d \mid \theta) = \arg \max_{\theta_1, ..., \theta_M} \prod_{i=1}^M \theta_i^{c(w_i, d)}$ 

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Normalized Counts

$$\frac{\partial f(\theta \mid d)}{\partial \theta_i} = \frac{c(w_i, d)}{\theta_i} + \lambda = 0 \quad \to \quad \theta_i = -\frac{c(w_i, d)}{\lambda}$$

$$\sum_{i=1}^{M} -\frac{c(w_i, d)}{\lambda} = 1 \to \lambda = -\sum_{i=1}^{N} c(w_i, d) \to \hat{\theta}_i = p(w_i | \hat{\theta}) = \frac{c(w_i, d)}{\sum_{i=1}^{M} c(w_i, d)} = \frac{c(w_i, d)}{|d|}$$

#### What Does the Topic Look Like?

