STAT390: Homework 2

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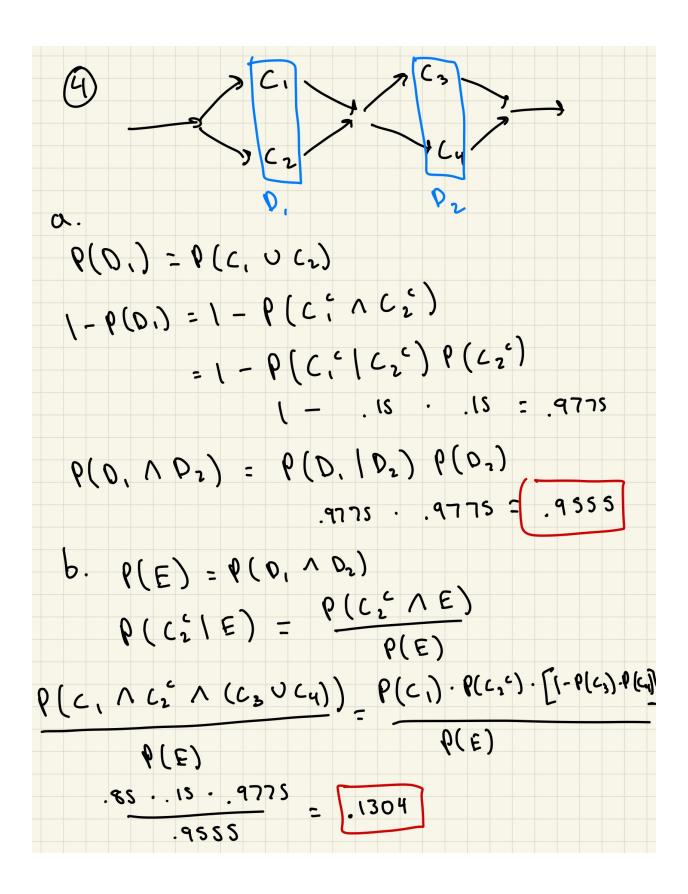
Howework 2

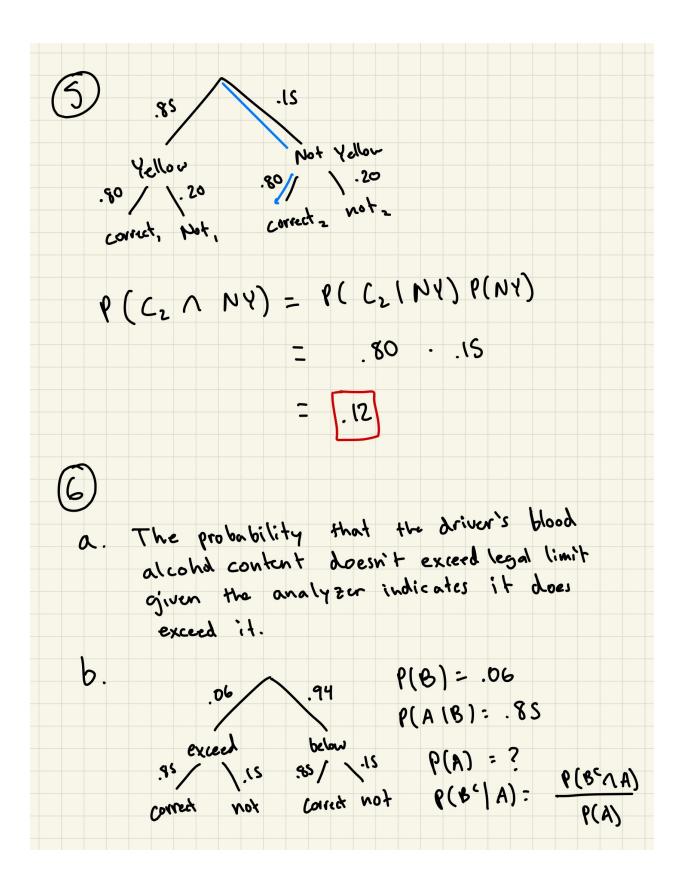
(a)
$$\rho(Bz \mid Bi) + \rho(Bz \mid Bi^c) = \rho(Bz)$$
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$$P(A) = .06 \cdot .85 + .94 \cdot .15 = .192$$

$$P(B^{c}) P(A | B^{c}) = .94 \cdot .15 = .734$$

$$P(B | A) = .95$$

$$.95 = \frac{P(B) P(B)}{P(A)}$$

$$.9$$

Question 7

```
pSP500 <- sp500[,7]
pSP500 <- rev(pSP500)
rSP500 <- diff(log(pSP500))*100
ndays <- length(rSP500)
sum(rSP500 < 0)/ndays</pre>
```

[1] 0.4684298

is the probability that the log-returns are negative.

```
numCons <- sum(rSP500[1:(ndays-1)]<0 & rSP500[2:ndays]<0)
numPrev <- sum(rSP500[1:(ndays-1)]<0)
numCons/numPrev</pre>
```

```
## [1] 0.43257
```

is the probability that it will be down two consecutive days. I would say they are because the probability isn't very high to make us believe that having a down day leads the next day to be down as well.

```
c <- sum(rSP500[1:ndays] >= 1.5)
c/ndays
```

[1] 0.07290922

is the probability that the absolute value of the log-returns is at least 1.5%.

Looking for P("following day log-return abs value >= 1.5%" | "abs val log-return of selected day >= 1%").

```
oneP <- sum(rSP500[1:ndays] >= 1)
following <- sum(rSP500[2:ndays] >= 1.5 & rSP500[1:ndays-1] >= 1)
following/oneP
```

```
## [1] 0.08866995
```

is the probability that the following day has an absolute value log-return of at least 1.5% given that the current day is at least 1%.