Lecture 3: Machine Learning Fundamentals

UBC 2022 Summer

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Imports

```
In [1]:
        # import the libraries
        import os
        import sys
        import graphviz
        import IPython
        import matplotlib.pyplot as plt
         import numpy as np
        import pandas as pd
        from IPython.display import HTML
        from sklearn.model_selection import train_test_split
        sys.path.append("code/.")
        from plotting_functions import *
        # # Classifiers
        from sklearn.tree import DecisionTreeClassifier, export_graphviz
        from utils import *
        %matplotlib inline
        pd.set_option("display.max_colwidth", 200)
```

Learning outcomes

From this lecture, you will be able to

- explain how decision boundaries change with the max_depth hyperparameter;
- explain the concept of generalization;
- appropriately split a dataset into train and test sets using train_test_split function;
- explain the difference between train, validation, test, and "deployment" data;
- identify the difference between training error, validation error, and test error;
- explain cross-validation and use cross_val_score and cross_validate to calculate cross-validation error;
- recognize overfitting and/or underfitting by looking at train and test scores;
- explain why it is generally not possible to get a perfect test score (zero test error) on a supervised learning problem;
- describe the fundamental tradeoff between training score and the train-test gap;

- state the golden rule;
- start to build a standard recipe for supervised learning: train/test split, hyperparameter tuning with cross-validation, test on test set.

Generalization [video]

Big picture and motivation

In machine learning, we want to glean information from labeled data so that we can label **new unlabeled** data. For example, suppose we want to build a spam filtering system. We will take a large number of spam/non-spam messages from the past, learn patterns associated with spam/non-spam from them, and predict whether **a new incoming message** in someone's inbox is spam or non-spam based on these patterns.

So we want to learn from the past but ultimately we want to apply it on the future email messages.

How can we generalize from what we've seen to what we haven't seen?

In this lecture, we'll see how machine learning tackles this question.

Model complexity and training error

In the last lecture, we looked at **decision boundaries**, a way to visualize what sort of examples will be classified as positive and negative.

Let's examine how does the decision boundary change for different tree depths.

```
In [2]: # Toy quiz2 grade data
  classification_df = pd.read_csv("data/quiz2-grade-toy-classification.csv")
  classification_df.head(10)
```

```
Out[2]:
              ml_experience class_attendance lab1 lab2 lab3 lab4
                                                                         quiz1
                                                                                  quiz2
          0
                          1
                                                  92
                                                        93
                                                              84
                                                                     91
                                                                            92
                                            1
                                                                                    A+
          1
                          1
                                            0
                                                  94
                                                        90
                                                              80
                                                                     83
                                                                            91
                                                                                not A+
          2
                          0
                                            0
                                                  78
                                                        85
                                                              83
                                                                     80
                                                                            80
                                                                                not A+
                          0
          3
                                            1
                                                  91
                                                        94
                                                              92
                                                                     91
                                                                            89
                                                                                    A+
          4
                          0
                                            1
                                                        83
                                                              90
                                                                     92
                                                  77
                                                                            85
                                                                                    A+
          5
                          1
                                                  70
                                                        73
                                                              68
                                                                     74
                                                                            71
                                                                                not A+
          6
                          1
                                            0
                                                  80
                                                        88
                                                              89
                                                                     88
                                                                            91
                                                                                    A+
          7
                          0
                                                  95
                                                        93
                                                              69
                                                                     79
                                                                            75
                                                                                not A+
                          0
          8
                                            0
                                                  97
                                                        90
                                                              94
                                                                     99
                                                                            80
                                                                                not A+
          9
                                                  95
                                                        95
                                                              94
                                                                               not A+
```

```
In [3]: X = classification_df.drop(["quiz2"], axis=1)
y = classification_df["quiz2"]

In [4]: X_subset = X[["lab4", "quiz1"]] # Let's consider a subset of the data for visualization
X_subset.head()
```

```
Out[4]:
             lab4 quiz1
          0
               91
                      92
          1
               83
                       91
          2
               80
                      80
          3
               91
                       89
          4
               92
                      85
```

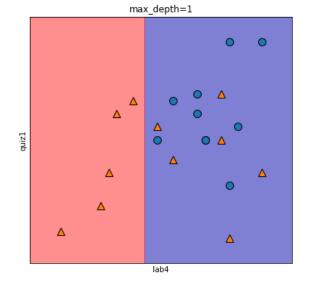
In the following model, this decision boundary is created by asking one question.

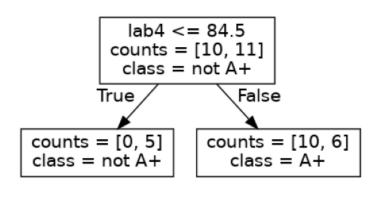
```
In [5]: depth = 1
    model = DecisionTreeClassifier(max_depth=depth)
    model.fit(X_subset, y)
    print("Accuracy: %0.3f" % model.score(X_subset, y))
    print("Error: %0.3f" % (1 - model.score(X_subset, y)))

Accuracy: 0.714
    Error: 0.286

In [6]: plot_tree_decision_boundary_and_tree(
          model, X_subset, y, x_label="lab4", y_label="quiz1"
    )
```

/home/moveisi/miniconda3/envs/cpsc330/lib/python3.10/site-packages/sklearn/base.py:450: UserWarn ing: X does not have valid feature names, but DecisionTreeClassifier was fitted with feature names warnings.warn(





In the following model, this decision boundary is created by asking two questions.

```
In [7]: depth = 2
    model = DecisionTreeClassifier(max_depth=depth)
    model.fit(X_subset, y)
    print("Accuracy: %0.3f" % model.score(X_subset, y))
    print("Error: %0.3f" % (1 - model.score(X_subset, y)))

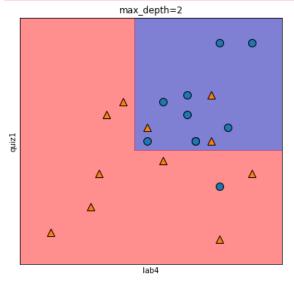
Accuracy: 0.810
    Error: 0.190

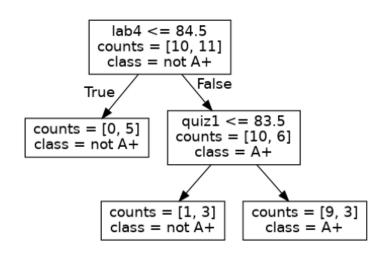
In [8]: plot_tree_decision_boundary_and_tree(
          model, X_subset, y, x_label="lab4", y_label="quiz1"
    )

/home/moveisi/miniconda3/envs/cpsc330/lib/python3.10/site-packages/sklearn/base.py:450: UserWarn
```

/home/moveisi/miniconda3/envs/cpsc330/lib/python3.10/site-packages/sklearn/base.py:450: UserWarn ing: X does not have valid feature names, but DecisionTreeClassifier was fitted with feature names

warnings.warn(





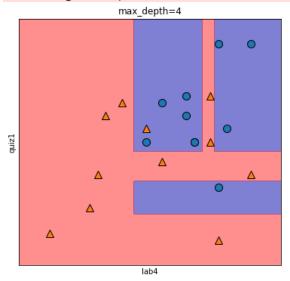
Let's look at the decision boundary with depth = 4.

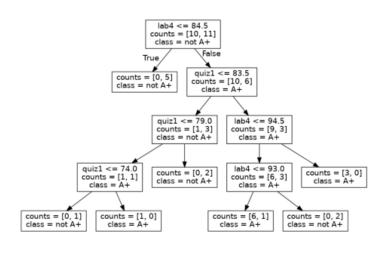
```
In [9]: depth = 4
    model = DecisionTreeClassifier(max_depth=depth)
    model.fit(X_subset, y)
    print("Accuracy: %0.3f" % model.score(X_subset, y))
    print("Error: %0.3f" % (1 - model.score(X_subset, y)))
```

Accuracy: 0.952 Error: 0.048

/home/moveisi/miniconda3/envs/cpsc330/lib/python3.10/site-packages/sklearn/base.py:450: UserWarn ing: X does not have valid feature names, but DecisionTreeClassifier was fitted with feature names

warnings.warn(





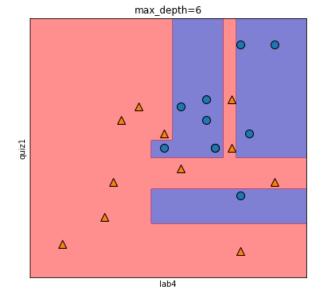
Let's look at the decision boundary with depth = 6.

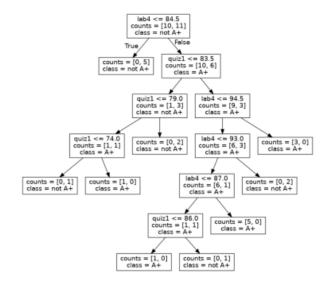
```
In [11]: depth = 6
    model = DecisionTreeClassifier(max_depth=depth)
    model.fit(X_subset, y)
    print("Accuracy: %0.3f" % model.score(X_subset, y))
    print("Error: %0.3f" % (1 - model.score(X_subset, y)))
```

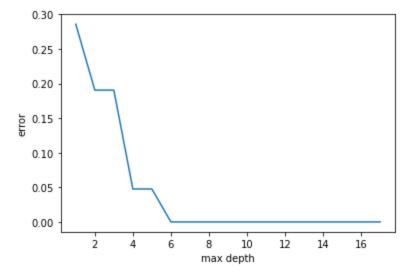
Accuracy: 1.000 Error: 0.000

/home/moveisi/miniconda3/envs/cpsc330/lib/python3.10/site-packages/sklearn/base.py:450: UserWarn ing: X does not have valid feature names, but DecisionTreeClassifier was fitted with feature names

warnings.warn(



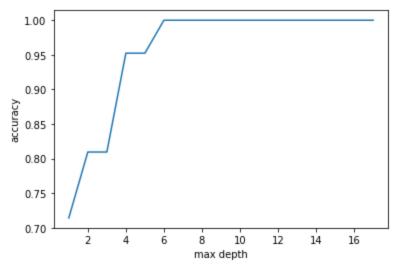




- Our model has 0% error for depths >= 6!!
- But it's also becoming more and more specific and sensitive to the training data.
- Is it good or bad?

Note Although the plot above (complexity hyperparameter vs error) is more popular, we could also look at the same plot flip the \$y\$-axis, i.e., consider accuracy instead of error.

```
plt.plot(max_depths, accuracies)
plt.xlabel("max depth")
plt.ylabel("accuracy");
```



Eva's questions

At this point Eva is wondering about the following questions.

- How to pick the best depth?
- How can we make sure that the model we have built would do reasonably well on new data in the wild when it's deployed?
- Which of the following rules learned by the decision tree algorithm are likely to generalize better to new data?

```
Rule 1: If class_attendance == 1 then grade is A+.

Rule 2: If lab3 > 83.5 and quiz1 <= 83.5 and lab2 <= 88 then quiz2 grade is A+
```

To better understand the material in the next sections, think about these questions on your own or discuss them with your friend/neighbour before proceeding.

Generalization: Fundamental goal of ML

To generalize beyond what we see in the training examples

We only have access to limited amount of training data and we want to learn a mapping function which would predict targets reasonably well for examples beyond this training data.

Example: Imagine that a learner sees the following images and corresponding labels.

Generalizing to unseen data

- Now the learner is presented with new images (1 to 4) for prediction.
- What prediction would you expect for each image?
- Goal: We want the learner to be able to generalize beyond what it has seen in the training data.
- But these new examples should be representative of the training data. That is they should have the same characteristics as the training data.
- In this example, we would like the leaner to be able to predict labels for test examples 1, 2, and 3 accurately. Although 2, 3 don't exactly occur in the training data, they are very much similar to the images in the training data. That said, is it fair to expect the learner to label image 4 correctly?

Training error vs. Generalization error

- Given a model \$M\$, in ML, people usually talk about two kinds of errors of \$M\$.
 - 1. Error on the training data: \$error_{training}(M)\$
 - 2. Error on the entire distribution \$D\$ of data: \$error_{D}(M)\$
- We are interested in the error on the entire distribution
 - ... But we do not have access to the entire distribution



How to approximate generalization error?

A common way is **data splitting**.

- Keep aside some randomly selected portion from the training data.
- fit (train) a model on the training portion only.
- score (assess) the trained model on this set aside data to get a sense of how well the model would be able to generalize.
- Pretend that the kept aside data is representative of the real distribution \$D\$ of data.

```
In [15]: # scikit-learn train_test_split
url = "https://scikit-learn.org/stable/modules/generated/sklearn.model_selection.train_test_split
HTML("<iframe src=%s width=1000 height=800></iframe>" % url)
```

/home/moveisi/miniconda3/envs/cpsc330/lib/python3.10/site-packages/IPython/core/display.py:41
9: UserWarning: Consider using IPython.display.IFrame instead
warnings.warn("Consider using IPython.display.IFrame instead")

sklearn.model selection.train_tes

sklearn.model_selection.train_test_split(*arrays, test_size=None, train_size=None, stratify=None)

Split arrays or matrices into random train and test subsets.

Quick utility that wraps input validation and next(ShuffleSplit().split(X, y)) and applications splitting (and optionally subsampling) data in a oneliner.

Read more in the **User Guide**.

Parameters:

*arrays: sequence of indexables with same length / shape[0]

Allowed inputs are lists, numpy arrays, scipy-sparse matrices or pandas dataframes.

test_size : float or int, default=None

If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to it the absolute number of test samples. If None, the value is set to the complement of the will be set to 0.25.

train_size : float or int, default=None

If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to it the absolute number of train samples. If None, the value is automatically set to the cor

random_state : int, RandomState instance or None, default=None

Controls the shuffling applied to the data before applying the split. Pass an int for repressalls. See <u>Glossary</u>.

shuffle : bool, default=True

Toggle Menu r or not to shu

r or not to shuffle the data before splitting. If shuffle=False then stratify must be

- We can pass X and y or a dataframe with both X and y in it.
- We can also specify the train or test split sizes.

Simple train/test split

- The picture shows an 80%-20% split of a toy dataset with 10 examples.
- The data is shuffled before splitting.

• Usually when we do machine learning we split the data before doing anything and put the test data in an imaginary chest lock.

```
# Let's demonstrate this with the canada usa cities data
In [16]:
          # The data is available in the data directory
          df = pd.read_csv("data/canada_usa_cities.csv")
          X = df.drop(columns=["country"])
          y = df["country"]
In [17]:
Out[17]:
               longitude latitude
            0 -130.0437
                         55.9773
            1 -134.4197
                         58.3019
            2 -123.0780
                        48.9854
            3 -122.7436 48.9881
               -122.2691
                        48.9951
          204
                -72.7218
                        45.3990
          205
                        45.9664
                -66.6458
          206
                -79.2506 42.9931
          207
                -72.9406 45.6275
          208
                -79.4608 46.3092
         209 rows × 2 columns
In [18]:
                    USA
Out[18]:
          1
                    USA
          2
                    USA
          3
                    USA
          4
                    USA
                  . . .
          204
                 Canada
          205
                 Canada
          206
                 Canada
          207
                 Canada
          208
                 Canada
          Name: country, Length: 209, dtype: object
In [19]:
          from sklearn.model_selection import train_test_split
          X_train, X_test, y_train, y_test = train_test_split(
              X, y, test_size=0.2, random_state=123
          ) # 80%-20% train test split on X and y
          # Print shapes
          shape_dict = {
              "Data portion": ["X", "y", "X_train", "y_train", "X_test", "y_test"],
```

"Shape": [
X.shape,

```
y.shape,
X_train.shape,
y_train.shape,
X_test.shape,
y_test.shape,
],
}
shape_df = pd.DataFrame(shape_dict)
HTML(shape_df.to_html(index=False))
```

```
Out[19]: Data portion Shape
```

```
X (209, 2)
y (209,)
X_train (167, 2)
y_train (167,)
X_test (42, 2)
y_test (42,)
```

Creating train_df and test_df

• Sometimes we want to keep the target in the train split for EDA or for visualization.

Out[20]: longitude latitude country

```
      160
      -76.4813
      44.2307
      Canada

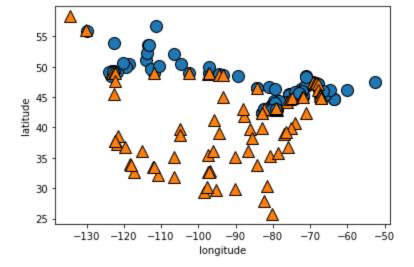
      127
      -81.2496
      42.9837
      Canada

      169
      -66.0580
      45.2788
      Canada

      188
      -73.2533
      45.3057
      Canada

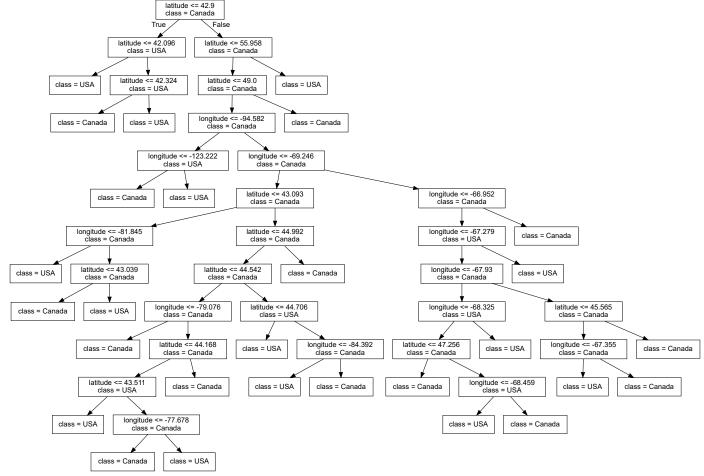
      187
      -67.9245
      47.1652
      Canada
```

```
In [21]: mglearn.discrete_scatter(X.iloc[:, 0], X.iloc[:, 1], y, s=12)
    plt.xlabel("longitude")
    plt.ylabel("latitude");
```



```
In [22]: model = DecisionTreeClassifier()
  model.fit(X_train, y_train)
  display_tree(X_train.columns, model)
```

Out[22]:



Let's examine the train and test accuracies with the split now.

```
In [23]: print("Train accuracy: %0.3f" % model.score(X_train, y_train))
    print("Test accuracy: %0.3f" % model.score(X_test, y_test))

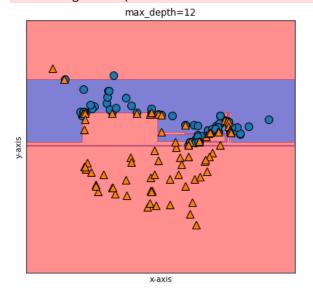
Train accuracy: 1.000
    Test accuracy: 0.714

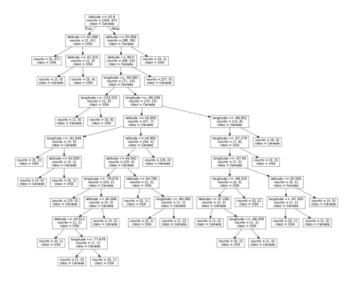
In [24]: plot_tree_decision_boundary_and_tree(model, X, y, height=6, width=16, eps=10)
```

/home/moveisi/miniconda3/envs/cpsc330/lib/python3.10/site-packages/sklearn/base.py:450: UserWarn ing: X does not have valid feature names, but DecisionTreeClassifier was fitted with feature names

warnings.warn(

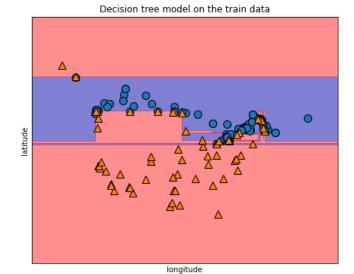
warnings.warn(

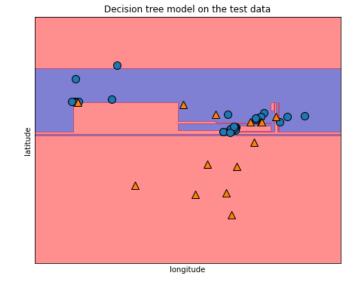




```
fig, ax = plt.subplots(1, 2, figsize=(16, 6), subplot_kw={"xticks": (), "yticks": ()})
In [25]:
          plot_tree_decision_boundary(
              model,
              X_train,
              y_train,
              eps=10,
              x_label="longitude",
              y_label="latitude",
              ax=ax[0],
              title="Decision tree model on the train data",
          plot_tree_decision_boundary(
              model,
              X_test,
              y_test,
              eps=10,
              x_label="longitude",
              y_label="latitude",
              ax=ax[1],
              title="Decision tree model on the test data",
          )
```

/home/moveisi/miniconda3/envs/cpsc330/lib/python3.10/site-packages/sklearn/base.py:450: UserWarn ing: X does not have valid feature names, but DecisionTreeClassifier was fitted with feature names warnings.warn(
/home/moveisi/miniconda3/envs/cpsc330/lib/python3.10/site-packages/sklearn/base.py:450: UserWarn ing: X does not have valid feature names, but DecisionTreeClassifier was fitted with feature names





- Useful arguments of train_test_split :
 - test_size
 - train_size
 - random_state

test_size, train_size arguments

- Let's us specify how we want to split the data.
- We can specify either of the two. See the documentation here.
- There is no hard and fast rule on what split sizes should we use.
 - It depends upon how much data is available to you.
- Some common splits are 90/10, 80/20, 70/30 (training/test).
- In the above example, we used 80/20 split.

random_state argument

- The data is shuffled before splitting which is crucial step. (You will explore this in the lab.)
- The random_state argument controls this shuffling.
- In the example above we used random_state=123 . If you run this notebook with the same random_state it should give you exactly the same split.
 - Useful when you want reproducible results.

Train/validation/test split

- Some of you may have heard of "validation" data.
- Sometimes it's a good idea to have a separate data for **hyperparameter tuning**.
- We will try to use "validation" to refer to data where we have access to the target values.
 - But, unlike the training data,
 - we only use this for hyperparameter tuning and model assessment;
 - we don't pass these into fit .

- We will try to use "test" to refer to data where we have access to the target values
 - But, unlike training and validation data,
 - we neither use it in training nor hyperparameter optimization.
 - We only use it once to evaluate the performance of the best performing model on the validation
 - We lock it in a "vault" until we're ready to evaluate.

Note that there isn't good concensus on the terminology of what is validation and what is test.

Note Validation data is also referred to as **development data** or **dev set** for short.

"Deployment" data

- After we build and finalize a model, we deploy it, and then the model deals with the data in the wild.
- We will use "deployment" to refer to this data, where we do **not** have access to the target values.
- Deployment error is what we *really* care about.
- We use validation and test errors as proxies for deployment error, and we hope they are similar.
- So, if our model does well on the validation and test data, we hope it will do well on deployment data.

Summary of train, validation, test, and deployment data

	fit	score	predict
Train	✓	✓	✓
Validation		✓	✓
Test		once	once
Deployment			✓

You can typically expect \$E_{train} < E_{validation} < E_{test} < E_{deployment}\$.

?? Questions on generalization and data splitting

Exercise 3.1: True or False

- 1. A decision tree model with no depth is likely to perform very well on the deployment data.
- 2. Data splitting helps us generalize our model better.
- 3. Deployment data is used at the very end and only scored once.
- 4. Validation data could be used for hyperparameter optimization.

Exercise 3.1: Solution

- 1. False
- 2. False. Data splitting helps us assess how well our model would generalize.
- 3. False. You cannot score on the deployment data as there are no labels available.
- 4. True

Exercise 3.2: Questions for discussion

1. Why you can typically expect $E_{\text{rain}} < E_{\text{on}} < E_{\text{test}} < E_{\text{deployment}}$ \$.

2. Discuss the consequences of not shuffling before splitting the data in train_test_split.

Cross-validation [video]

Problems with single train/validation split

- Only using a portion of your data for training and only a portion for validation.
- If your dataset is small you might end up with a tiny training and/or validation set.
- You might be unlucky with your splits such that they don't align well or don't well represent your test data.

Cross-validation to the rescue!!

- Cross-validation provides a solution to this problem.
- Split the data into \$k\$ folds (\$k>2\$, often \$k=10\$). In the picture below \$k=4\$.
- Each "fold" gets a turn at being the validation set.
- Note that cross-validation doesn't shuffle the data; it's done in train_test_split.
- Each fold gives a score and we usually average our \$k\$ results.

from sklearn.model_selection import cross_val_score, cross_validate

- It's better to examine the variation in the scores across folds.
- Gives a more **robust** measure of error on unseen data.

Cross-validation using scikit-learn

Average cross-validation score = 0.84

Under the hood

Standard deviation of cross-validation score = 0.09

In [26]:

- It creates cv folds on the data.
- In each fold, it fits the model on the training portion and scores on the validation portion.
- The output is a list of validation scores in each fold.

cross_validate

- Similar to cross_val_score but more powerful.
- Let's us access training and validation scores.

```
In [29]: scores = cross_validate(
    model, X_train, y_train, cv=10, return_train_score=True)

pd.DataFrame(scores)
```

Out[29]: fit time score_time test_score train_score 0 0.005024 0.003402 0.764706 0.913333 **1** 0.004111 0.001857 0.823529 0.906667 **2** 0.002359 0.001834 0.705882 0.906667 **3** 0.005365 0.003011 0.941176 0.900000 **4** 0.002439 0.002123 0.906667 0.823529 **5** 0.003261 0.001877 0.823529 0.913333 **6** 0.003830 0.002324 0.705882 0.920000 **7** 0.002746 0.001652 0.937500 0.900662 0.003531 0.001948 0.937500 0.900662 9 0.003350 0.002111 0.937500 0.900662

```
In [30]: pd.DataFrame(pd.DataFrame(scores).mean())
```

Out[30]: 0 fit_time 0.003602

test_score 0.840074 **train score** 0.906865

score_time 0.002214

Keep in mind that cross-validation does not return a model. It is not a way to build a model that can be applied to new data. The purpose of cross-validation is to **evaluate** how well the model will generalize to unseen data.

Note that both <code>cross_val_score</code> and <code>cross_validate</code> functions do not shuffle the data. Check out <code>StratifiedKFold</code>, where proportions of classes is the same in each fold as they are in the whole dataset. By default, <code>sklearn</code> uses <code>StratifiedKFold</code> when carrying out cross-validation for classification problems.

```
In [31]: mglearn.plots.plot_cross_validation()
```

Data points

Our typical supervised learning set up is as follows:

- We are **given** training data with features X and target y
- We **split** the data into train and test portions: X_train, y_train, X_test, y_test
- We carry out **hyperparameter optimization** using cross-validation on the train portion: X_train and y_train.
- We assess our best performing model on the test portion: X_test and y_test.
- What we care about is the *test error*, which tells us how well our model can be **generalized**.
- If this test error is "reasonable" we deploy the model which will be used on new unseen examples.

```
In [32]: X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=42)
model = DecisionTreeClassifier(max_depth=10)
scores = cross_validate(model, X_train, y_train, cv=10, return_train_score=True)
pd.DataFrame(scores)
```

Out[32]:		fit_time	score_time	test_score	train_score
	0	0.005208	0.002126	0.875000	1.000000
	1	0.004690	0.002903	0.875000	0.992857
	2	0.002567	0.001885	0.875000	1.000000
	3	0.007660	0.003621	0.687500	1.000000
	4	0.004101	0.003407	0.812500	1.000000
	5	0.005708	0.002980	0.812500	1.000000
	6	0.003248	0.002322	0.866667	0.985816
	7	0.004195	0.003055	0.600000	1.000000
	8	0.002877	0.001634	0.666667	1.000000
	9	0.002927	0.003188	0.733333	1.000000

Note the *unfortunate naming* above: test_score, which should have been *validation score*. We usually leave this as is, but if you insist to be consistent, you could rename by, for example, replacing the key test_score with val_score in the scores dictionary, or by renaming the dataframe columns as follows:

```
In [33]: pd.DataFrame(scores).rename({'test_score': 'val_score'}, axis='columns')
```

Out[33]:		fit_time	score_time	val_score	train_score
	0	0.005208	0.002126	0.875000	1.000000
	1	0.004690	0.002903	0.875000	0.992857
	2	0.002567	0.001885	0.875000	1.000000
	3	0.007660	0.003621	0.687500	1.000000
	4	0.004101	0.003407	0.812500	1.000000
	5	0.005708	0.002980	0.812500	1.000000
	6	0.003248	0.002322	0.866667	0.985816
	7	0.004195	0.003055	0.600000	1.000000
	8	0.002877	0.001634	0.666667	1.000000
	9	0.002927	0.003188	0.733333	1.000000

In [34]:

But given that we need to use <code>cross_validate</code> function over and over in different places, it's better to just keep in mind this naming problem, and decide to rename on a case by case basis.

```
Returns mean and std of cross validation
"""

scores = cross_validate(model, X_train, y_train, **kwargs)

mean_scores = pd.DataFrame(scores).mean()
std_scores = pd.DataFrame(scores).std()
out_col = []

for i in range(len(mean_scores)):
    out_col.append((f"%0.3f (+/- %0.3f)" % (mean_scores[i], std_scores[i])))

return pd.Series(data=out_col, index=mean_scores.index)

In [35]:
results = {}
results["Decision tree"] = mean_std_cross_val_scores(
    model, X_train, y_train, return_train_score=True
)
pd.DataFrame(results).T
```

Out[35]: fit_time score_time test_score train_score

Decision tree 0.005 (+/- 0.002) 0.003 (+/- 0.001) 0.782 (+/- 0.059) 0.992 (+/- 0.014)

def mean_std_cross_val_scores(model, X_train, y_train, **kwargs):

How do we know whether this test score (validation score) is reasonable?

?? Questions on cross-validation

Exercise 3.3: Cross-validation

- 1. \$k\$-fold cross-validation calls fit \$k\$. True or False?
- 2. We use cross-validation to improve model performance. True or False?
- 3. Discuss advantages and disadvantages of cross-validation.

- 1. True
- 2. False. We can use it to assess model performance.

Break (5 min)

Underfitting, overfitting, the fundamental trade-off, the golden rule [video]

Types of errors

Imagine that your train and validation errors do not align with each other. How do you diagnose the problem?

We're going to think about 4 types of errors:

- \$E_\textrm{train}\ \$ is your training error (or mean train error from cross-validation).
- \$E_\textrm{valid}\ \$ is your validation error (or mean validation error from cross-validation).
- \$E_\textrm{test}\ \$ is your test error.
- \$E_\textrm{best}\ \$ is the best possible error you could get for a given problem (often unknown, but desired).

Underfitting

```
In [36]: model = DecisionTreeClassifier(max_depth=1) # decision stump
    scores = cross_validate(model, X_train, y_train, cv=10, return_train_score=True)
    print("Train error: %0.3f" % (1 - np.mean(scores["train_score"])))
    print("Validation error: %0.3f" % (1 - np.mean(scores["test_score"])))
```

Train error: 0.188
Validation error: 0.212

- If your **model** is **too simple**, like DummyClassifier or DecisionTreeClassifier with max_depth=1, it's not going to pick up on some random quirks in the data but it won't even capture useful patterns in the training data.
- The model won't be very good in general. Both train and validation errors would be high. This is **underfitting**.
- The gap between train and validation error is going to be lower.
- \$E_\textrm{best} \lt E_\textrm{train} \lesssim E_\textrm{valid}\$

Overfitting

```
In [37]: model = DecisionTreeClassifier(max_depth=None)
    scores = cross_validate(model, X_train, y_train, cv=10, return_train_score=True)
    print("Train error: %0.3f" % (1 - np.mean(scores["train_score"])))
    print("Validation error: %0.3f" % (1 - np.mean(scores["test_score"])))
```

Train error: 0.000 Validation error: 0.207

- If your **model is very complex**, like a DecisionTreeClassifier(max_depth=None), then you will learn unreliable patterns in order to get every single training example correct.
- The training error is going to be very low but there will be a big gap between the training error and the validation error. This is **overfitting**.
- In overfitting scenario, usually we'll see: \$E_\textrm{train} \lt E_\textrm{best} \lt E_\textrm{valid}\$
- In general, if \$E_\textrm{train}\ \$ is low, we are likely to be in the overfitting scenario. It is fairly common to have at least a bit of this.
- So the validation error does not necessarily decrease with the training error.

```
X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=1)
In [38]:
         results_dict = {
             "depth": [],
             "mean_train_error": [],
             "mean_cv_error": [],
             "std_cv_error": [],
             "std_train_error": [],
         param_grid = {"max_depth": np.arange(1, 16)}
         for depth in param_grid["max_depth"]:
             model = DecisionTreeClassifier(max_depth=depth)
             scores = cross_validate(model, X_train, y_train, cv=10, return_train_score=True)
             results dict["depth"].append(depth)
             results_dict["mean_cv_error"].append(1 - np.mean(scores["test_score"]))
             results_dict["mean_train_error"].append(1 - np.mean(scores["train_score"]))
             results_dict["std_cv_error"].append(scores["test_score"].std())
             results_dict["std_train_error"].append(scores["train_score"].std())
         results_df = pd.DataFrame(results_dict)
         results_df = results_df.set_index("depth")
```

In [39]: results_df

	mean_train_error	mean_cv_error	std_cv_error	std_train_error
depth				
1	0.171657	0.211250	0.048378	0.006805
2	0.160258	0.223750	0.062723	0.007316
3	0.142467	0.204583	0.053763	0.022848
4	0.092604	0.204167	0.070907	0.006531
5	0.083338	0.185000	0.064205	0.010650
6	0.066251	0.191250	0.072707	0.012019
7	0.044873	0.204167	0.088329	0.009059
8	0.029909	0.210000	0.092331	0.009422
9	0.020653	0.190833	0.096426	0.010294
10	0.009260	0.215833	0.092229	0.005563
11	0.005699	0.229167	0.093782	0.004264
12	0.002143	0.248333	0.089485	0.003273
13	0.000000	0.235833	0.092687	0.000000
14	0.000000	0.248333	0.089485	0.000000

0.235833

Out[39]:

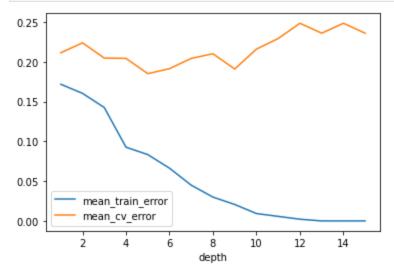
15

0.000000



0.092687

0.000000



- Here, for larger depths we observe that the training error is close to 0 but validation error goes up and down.
- As we make **more complex models we start encoding random quirks** in the data, which are not grounded in reality.
- These random quirks do not generalize well to new data.
- This problem of failing to be able to generalize to the validation data or test data is called **overfitting**.

The "fundamental tradeoff" of supervised learning:

As you increase model complexity, $E_{\text{train}}\$ tends to go down but $E_{\text{train}}\$ tends to go up.

Bias vs variance tradeoff

• The fundamental trade-off is also called the bias/variance tradeoff in supervised machine learning.

Bias: the tendency to consistently learn the same wrong thing (high bias corresponds to underfitting)

Variance: the tendency to learn random things irrespective of the real signal (high variance corresponds to overfitting)

Check out this article by Pedro Domingos for some approachable explanation on machine learning fundamentals and bias-variance tradeoff.

How to pick a model that would generalize better?

- We want to avoid both underfitting and overfitting.
- We want to be consistent with the training data but we don't want to rely too much on it.

source

• There are many subtleties here, and there is no perfect answer, but a common practice is to pick the model with minimum cross-validation error.

```
In [41]:

def cross_validate_std(*args, **kwargs):
    """Like cross_validate, except also gives the standard deviation of the score""
    res = pd.DataFrame(cross_validate(*args, **kwargs))
    res_mean = res.mean()
    res_mean["std_test_score"] = res["test_score"].std()
    if "train_score" in res:
        res_mean["std_train_score"] = res["train_score"].std()
    return res_mean
```

This function makes it more convenient to produce the same results that we already had above:

```
In [42]: results_df
```

depth				
1	0.171657	0.211250	0.048378	0.006805
2	0.160258	0.223750	0.062723	0.007316
3	0.142467	0.204583	0.053763	0.022848
4	0.092604	0.204167	0.070907	0.006531
5	0.083338	0.185000	0.064205	0.010650
6	0.066251	0.191250	0.072707	0.012019
7	0.044873	0.204167	0.088329	0.009059
8	0.029909	0.210000	0.092331	0.009422
9	0.020653	0.190833	0.096426	0.010294
10	0.009260	0.215833	0.092229	0.005563
11	0.005699	0.229167	0.093782	0.004264
12	0.002143	0.248333	0.089485	0.003273
13	0.000000	0.235833	0.092687	0.000000
14	0.000000	0.248333	0.089485	0.000000
15	0.000000	0.235833	0.092687	0.000000

mean_train_error mean_cv_error std_cv_error std_train_error

Out[42]:

test score vs. cross-validation score

The minimum validation error is 0.185 at max_depth = 5

• Let's make a decision tree model with max_depth = 5 and try this model on the test set.

```
In [44]: model = DecisionTreeClassifier(max_depth=best_depth)
    model.fit(X_train, y_train)
    print("Error on test set is %0.3f " % (1 - model.score(X_test, y_test)))
    print("The minimum validation error is %0.3f " % best_depth_error)
```

Error on test set is 0.189
The minimum validation error is 0.185

- The test error is comparable with the cross-validation error.
- Do we feel confident that this model would give similar performace when deployed?

The golden rule

Even though we care the most about test error THE TEST DATA CANNOT INFLUENCE THE TRAINING
 PHASE IN ANY WAY.

- We have to be very careful not to violate it while developing our ML pipeline.
- Even experts end up breaking it sometimes which leads to misleading results and lack of generalization on the real data.

Golden rule violation: Example 1

... He attempted to reproduce the research, and found a major flaw: there was some overlap in the data used to both train and test the model.

Golden rule violation: Example 2

... The Challenge rules state that you must only test your code twice a week, because there's an element of chance to the results. Baidu has admitted that it used multiple email accounts to test its code roughly 200 times in just under six months – over four times what the rules allow.

How can we avoid violating golden rule?

• Recall that when we split data, we put our test set in an imaginary vault.

Here is the workflow we'll generally follow.

- **Splitting**: Before doing anything, split the data X and y into X_train, X_test, y_train, y_test or train_df and test_df using train_test_split.
- Select the best model using cross-validation: Use cross_validate with return_train_score = True so that we can get access to training scores in each fold. (If we want to plot train vs validation error plots, for instance.)
- Scoring on test data: Finally score on the test data with the chosen hyperparameters to examine the
 generalization performance.

Again, there are many subtleties here we'll discuss the golden rule multiple times throughout the course and in the program.

?? Questions for you

- 1. If the mean train accuracy is much higher than the mean cross-validation accuracy.
- 2. If the mean train accuracy and the mean cross-validation accuracy are both low and relatively similar in value
- 3. Decision tree with no limit on the depth.
- 4. Decision stump on a complicated classification problem.

Exercise 3.4: Solution

- 1. Overfitting
- 2. Underfitting
- 3. Overfitting
- 4. Underfitting

Exercise 3.5

State whether True/False.

- 1. In supervised learning, the training error is always lower than the validation error.
- 2. The fundamental tradeoff of ML states that as training error goes down, validation error goes up.
- 3. More "complicated" models are more likely to overfit than "simple" ones.
- 4. If we had an infinite amount of training data, overfitting would not be a problem.
- 5. If our training error is extremely low, we are likely to be overfitting.

Exercise 3.5: Solution

- 1. False
- 2. False
- 3. True
- 4. True
- 5. True

What did we learn today?

- Importance of generalization in supervised machine learning
- Data splitting as a way to approximate generalization error
- Train, test, validation, deployment data
- Cross-validation
- A typical sequence of steps to train supervised machine learning models
 - training the model on the train split
 - tuning hyperparamters using the validation split
 - checking the generalization performance on the test split
- Overfitting, underfitting, the fundamental tradeoff, and the golden rule.

Coming up ...

- KNNs, SVM RBFs
- Preprocessing
 - Imputation
 - Scaling

- One-hot encoding
- sklearn pipelines