$$H_n(x) = \frac{2^n \int_{-\infty}^{\infty} \frac{(x+it)^n}{e^{t^2}} dt}{\sqrt{\pi}}$$