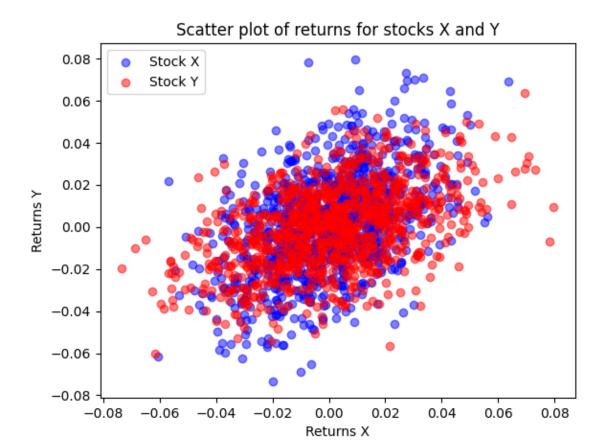
## September 30, 2024

- 2. The daily returns of two correlated stocks, X and Y , follow a joint lognormal distribution with the following parameters:  $X=0.001,\ Y=0.002,\ X=0.02,\ Y=0.03,\ X,Y=0.8$
- (c) (4 points) Simulate 1,000 days of returns for both stocks using the joint lognormal distribution. Plot the scatter plot and calculate the empirical correlation.

```
[17]: import matplotlib.pyplot as plt
     import numpy as np
     mu_X = 0.001 # Expected return of stock X
     sigma_X = 0.02 # Standard deviation of return of stock X
     mu_Y = 0.0015  # Expected return of stock Y
     sigma_Y = 0.025 # Standard deviation of return of stock Y
     rho XY = 0.5 # Correlation coefficient between returns of stock X and Y
     num_days = 1000  # Number of days to simulate returns for both stocks
     \# Simulate 1,000 days of returns for both stocks using the joint lognormal \sqcup
      \rightarrow distribution
     np.random.seed(42) # For reproducibility
     mean = [mu_X, mu_Y]
     cov_matrix = [[sigma_X**2, rho_XY * sigma_X * sigma_Y], [rho_XY * sigma_X *_

sigma_Y, sigma_Y**2]]
     returns = np.random.multivariate_normal(mean, cov_matrix, num_days)
     returns_X = returns[:, 0]
     returns Y = returns[:, 1]
     # Plot the scatter plot with different colors for each stock
     plt.scatter(returns_X, returns_Y, alpha=0.5, c='blue', label='Stock X')
     plt.scatter(returns_Y, returns_X, alpha=0.5, c='red', label='Stock Y')
     plt.xlabel('Returns X')
     plt.ylabel('Returns Y')
     plt.title('Scatter plot of returns for stocks X and Y')
     plt.legend()
     plt.show()
     print("The empirical correlation coefficient between the returns of stock X and \Box
```



The empirical correlation coefficient between the returns of stock X and Y is: 0.462009489994836

(d) (2 points) Using the simulated data, calculate the percentage of days where both stocks have positive returns. Compare this to the theoretical correlation.

```
[18]: # Calculate the percentage of days where both stocks have positive returns positive_returns_both = np.sum((returns_X > 0) & (returns_Y > 0)) percentage_positive_returns_both = (positive_returns_both / num_days) * 100

print(f"The percentage of days where both stocks have positive returns is:

-{percentage_positive_returns_both:.2f}%")
```

The percentage of days where both stocks have positive returns is: 33.70%

[]: