q4

April 18, 2025

1 Clustering Human Activity using Inertial Sensors Data

1.1 Note:

- Use the next cell to download the data directly, if that didn't work. you can download it manually (available at UCI archive) a copy will also be available on Piazza.
- Don't change the part of the code that labels #Do not change
- Attach this notebook to your answer sheet with all outputs visible.
- make sure you have pytorch, scikit learn, pandas in your environment

1.2 Imports

```
[1]: import numpy as np
[2]: #### Download the dataset
     import urllib.request
     import zipfile
     import os
     dataset_url = "https://archive.ics.uci.edu/static/public/240/
      →human+activity+recognition+using+smartphones.zip"
     zip_file_path = "Dataset.zip"
     extracted_downloaded_folder = "Dataset"
     extracted_data_folder = "UCI HAR Dataset"
     if not os.path.exists(zip_file_path):
         print("Downloading the dataset...")
         urllib.request.urlretrieve(dataset_url, zip_file_path)
     if not os.path.exists(extracted_downloaded_folder):
         print("Extracting the dataset...")
         with zipfile.ZipFile(zip_file_path, 'r') as zip_ref:
             zip_ref.extractall(".")
     if not os.path.exists(extracted_data_folder):
         print("Extracting the dataset...")
```

```
with zipfile.ZipFile(extracted_data_folder +'.zip', 'r') as zip_ref:
    zip_ref.extractall(".")
print("Dataset is ready.")
```

Downloading the dataset... Extracting the dataset... Extracting the dataset... Dataset is ready.

1.2.1 Load the data into a dataframe

The X_train dataframe contains all extracted features from the smartphone dataset - 561 features for each of the 30 individuals single activity

The Y_train contains the labels of each rows - of all this 561 single features, this is the activity they were performing

```
[3]: # Import necessary libraries
    import pandas as pd
    import matplotlib.pyplot as plt
    import warnings
    warnings.filterwarnings('ignore', category=FutureWarning)
     # Define paths to data files
    train path = "UCI HAR Dataset/train/"
    test_path = "UCI HAR Dataset/test/"
    activity_mapper_path = "UCI HAR Dataset/activity_labels.txt"
     # Load training and testing data
    X_train, y_train = pd.read_csv(train_path + "X_train.txt",
      delim_whitespace=True, header=None), pd.read_csv(train_path + "y_train.txt",
      →delim_whitespace=True, header=None)
    X_test, y_test = pd.read_csv(test_path + "X_test.txt", delim_whitespace=True, u
      ⇔header=None), pd.read_csv(test_path + "y_test.txt", delim_whitespace=True,
      →header=None)
    # Display the first 5 rows of the training dataframe
    print("First 5 rows of training feature dataframe:")
    X_train.head() # DO NOT CHANGE
```

First 5 rows of training feature dataframe:

```
[3]: 0 1 2 3 4 5 6 \
0 0.288585 -0.020294 -0.132905 -0.995279 -0.983111 -0.913526 -0.995112
1 0.278419 -0.016411 -0.123520 -0.998245 -0.975300 -0.960322 -0.998807
2 0.279653 -0.019467 -0.113462 -0.995380 -0.967187 -0.978944 -0.996520
```

```
3 0.279174 -0.026201 -0.123283 -0.996091 -0.983403 -0.990675 -0.997099
4 0.276629 -0.016570 -0.115362 -0.998139 -0.980817 -0.990482 -0.998321
                                          551
                                                    552
                                                               553
                                                                         554 \
0 -0.983185 -0.923527 -0.934724 ... -0.074323 -0.298676 -0.710304 -0.112754
1 \ -0.974914 \ -0.957686 \ -0.943068 \ \dots \ 0.158075 \ -0.595051 \ -0.861499 \ 0.053477
2 -0.963668 -0.977469 -0.938692 ... 0.414503 -0.390748 -0.760104 -0.118559
3 -0.982750 -0.989302 -0.938692 ... 0.404573 -0.117290 -0.482845 -0.036788
4 -0.979672 -0.990441 -0.942469 ... 0.087753 -0.351471 -0.699205 0.123320
        555
                  556
                            557
                                       558
                                                 559
                                                           560
0 0.030400 -0.464761 -0.018446 -0.841247 0.179941 -0.058627
1 - 0.007435 - 0.732626 \quad 0.703511 - 0.844788 \quad 0.180289 - 0.054317
2 0.177899 0.100699 0.808529 -0.848933 0.180637 -0.049118
3 -0.012892 0.640011 -0.485366 -0.848649 0.181935 -0.047663
4 0.122542 0.693578 -0.615971 -0.847865 0.185151 -0.043892
```

scaling the data and PCA

[5 rows x 561 columns]

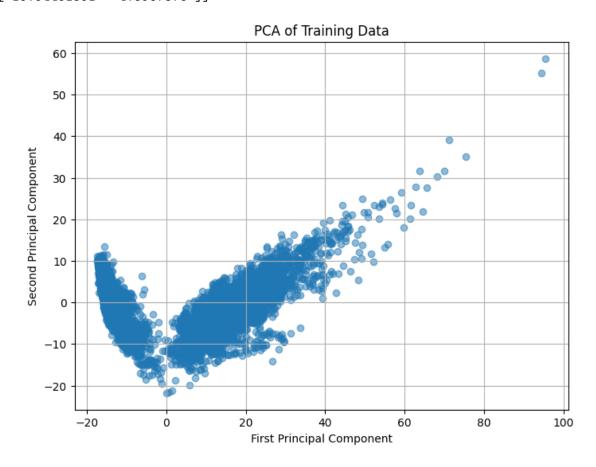
```
[4]: from sklearn.preprocessing import StandardScaler
     # TODO: Scale X train
     scaler = StandardScaler()
     # Scale X_train
     X_train_scaled = scaler.fit_transform(X_train)
     # Scale X test
     X_test_scaled = scaler.transform(X_test)
     # Convert scaled arrays back to DataFrames
     X_train = pd.DataFrame(X_train_scaled, columns=X_train.columns)
     X_test = pd.DataFrame(X_test_scaled, columns=X_test.columns)
     # Add 'Activity' column to create training_df and testing_df
     # TODO: Combine X train and y train into a single DataFrame named training df.
     training_df = pd.concat([X_train, y_train], axis=1)
     # TODO: Combine X_test and y_test into a single DataFrame named testing_df.
     testing_df = pd.concat([X_test, y_test], axis=1)
     # Display the first 5 rows of the training feature dataframe
     print("First 5 rows of training feature dataframe:")
```

```
training_df.head() # DO NOT CHANGE
    First 5 rows of training feature dataframe:
[4]:
     0 .200642 -0.063683 -0.419628 -0.868814 -0.939441 -0.737529 -0.859817
     1 \quad 0.055948 \quad 0.031486 \quad -0.253908 \quad -0.875426 \quad -0.923902 \quad -0.849304 \quad -0.868531
     2 0.073515 -0.043416 -0.076295 -0.869039 -0.907760 -0.893785 -0.863137
     3 0.066696 -0.208422 -0.249712 -0.870626 -0.940022 -0.921805 -0.864503
     4 0.030469 0.027587 -0.109848 -0.875188 -0.934878 -0.921343 -0.867384
             7
                       8
                                               552
                                                         553
                                                                   554
                                                                             555 \
     0 -0.939019 -0.766437 -0.856036 ... 0.025960 -0.276399 -0.360603 0.062940
     1 -0.921998 -0.848928 -0.871359
                                      ... -0.897357 -0.767990 0.133011 -0.021461
     2 -0.898854 -0.896701 -0.863323 ... -0.260878 -0.438316 -0.377840 0.391976
     3 -0.938124 -0.925279 -0.863323 ... 0.591045 0.463155 -0.135025 -0.033637
     4 -0.931789 -0.928028 -0.870260 ... -0.138515 -0.240313 0.340406 0.268486
             556
                       557
                                 558
                                           559
                                                      560
     0 -0.778427 -0.026080 -0.687219 0.407946 -0.007568
                                                             5
     1 -1.218805 1.484470 -0.694138 0.409117 0.007875
                                                             5
     2 0.151207 1.704201 -0.702239 0.410288 0.026502
                                                             5
     3 1.037851 -1.003019 -0.701684 0.414650 0.031714
                                                             5
     4 1.125918 -1.276282 -0.700152 0.425463 0.045225
                                                             5
     [5 rows x 562 columns]
[5]: from sklearn.decomposition import PCA
     # TODO perform PCA on the train data and get the first 2 PC
     pca = PCA(n_components=2)
     X_train_pca = pca.fit_transform(X_train)
     print("PCA shape: ", X_train_pca.shape) # DO NOT CHANGE
     # print the first two principal components
     print("First two principal components: ")
     print(X_train_pca[:5]) # DO NOT CHANGE
     # Plot the first two principal components
     plt.figure(figsize=(8, 6))
     plt.scatter(X_train_pca[:, 0], X_train_pca[:, 1], alpha=0.5)
     plt.title("PCA of Training Data")
     plt.xlabel("First Principal Component")
     plt.ylabel("Second Principal Component")
     plt.grid()
     plt.show()
    PCA shape: (7352, 2)
    First two principal components:
    [[-16.13854371
                     2.15202247]
```

[-15.2961943

1.38714362]

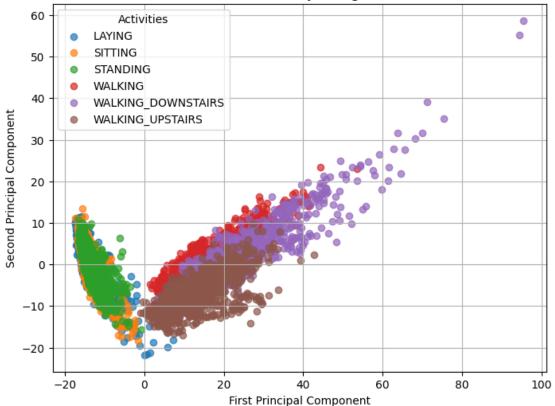
[-15.13701861 2.47335052] [-15.35088376 3.91568149] [-15.54481351 4.5987378]]



Visualize the data import numpy as np # Visualize training data using PCA # Use the feature decoder to create Activity Name column # Load activity labels activity_labels = pd.read_csv(activity_mapper_path, header=None, sep=r'\s+',u names=['id', 'activity_name']) # Create mapping dictionary {1: "WALKING", 2: "WALKING_UPSTAIRS", ...} activity_mapping = dict(zip(activity_labels['id'],u activity_labels['activity_name'])) # TODO use the mapping to decode the Activities labels # Since y_train is a DataFrame, we need to access the values differently

```
y_values = y_train.iloc[:, 0].values # Get the first column as values
Activity_Name = np.array([activity_mapping[int(label)] for label in y_values])
# TODO: Create a scatter plot using the X_train_pca and the Activity Names
plt.figure(figsize=(8, 6))
# Create scatter plot with different colors for each activity
unique_activities = np.unique(Activity_Name)
for activity in unique_activities:
    indices = np.where(Activity_Name == activity)[0]
   plt.scatter(X_train_pca[indices, 0], X_train_pca[indices, 1],
                label=activity, alpha=0.7)
plt.title("PCA of Human Activity Recognition Data")
plt.xlabel("First Principal Component")
plt.ylabel("Second Principal Component")
plt.legend(title="Activities")
plt.grid(True)
plt.savefig("PCA_activities.png", dpi=300, bbox_inches='tight')
plt.show()
```





```
[7]: # Print the unique values in y_train
    print("Unique values in y_train:", np.unique(y_train))

# Print the activity mapping to see what keys are available
    print("Keys in activity_mapping:", list(activity_mapping.keys()))

# Print some sample values to understand their format
    print("Sample y_train values:", y_train[:5])
    print("Sample y_train type:", type(y_train), "element type:", type(y_train[0]))

# Check if any values in y_train are not in the mapping
    missing_keys = []
    for label in np.unique(y_train):
        if label not in activity_mapping:
            missing_keys.append(label)

print("Labels not found in mapping:", missing_keys)
```

```
Unique values in y_train: [1 2 3 4 5 6]
Keys in activity_mapping: [1, 2, 3, 4, 5, 6]
Sample y_train values: 0
0 5
1 5
2 5
3 5
4 5
Sample y_train type: <class 'pandas.core.frame.DataFrame'> element type: <class 'pandas.core.series.Series'>
Labels not found in mapping: []
```

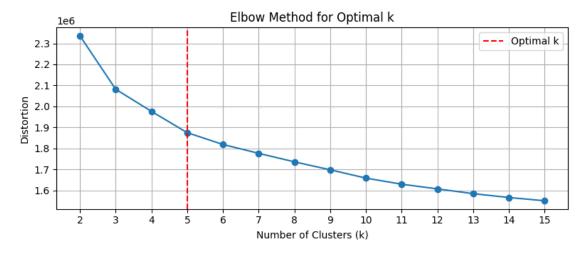
1.3 Kmeans Clustering and The Optimal Number of Clusters

1. Elbow Method

```
[8]: from sklearn.cluster import KMeans
# Elbow Method
distortion_values = []
for k in range(2, 16):
    kmeans = KMeans(n_clusters=k, random_state=42)
    kmeans.fit(X_train_scaled)
    distortion = kmeans.inertia_
    distortion_values.append(distortion)

# Plotting the Elbow Method
plt.figure(figsize=(8, 3.5))
plt.plot(range(2, 16), distortion_values, marker='o')
plt.title("Elbow Method for Optimal k")
```

```
plt.xlabel("Number of Clusters (k)")
plt.ylabel("Distortion")
plt.xticks(range(2, 16))
plt.grid()
plt.axvline(x=5, color='r', linestyle='--', label='Optimal k')
plt.legend()
plt.tight_layout()
plt.show()
```



```
[9]: !pip install kneed
from kneed import KneeLocator

k = range(2, 16)

knee = KneeLocator(k, distortion_values, curve='convex',
direction='decreasing').knee

print("Optimal k:", knee)
```

Collecting kneed

Downloading kneed-0.8.5-py3-none-any.whl.metadata (5.5 kB)

Requirement already satisfied: numpy>=1.14.2 in /usr/local/lib/python3.11/dist-packages (from kneed) (1.26.4)

Requirement already satisfied: scipy>=1.0.0 in /usr/local/lib/python3.11/dist-packages (from kneed) (1.15.2)

Requirement already satisfied: mkl_fft in /usr/local/lib/python3.11/dist-packages (from numpy>=1.14.2->kneed) (1.3.8)

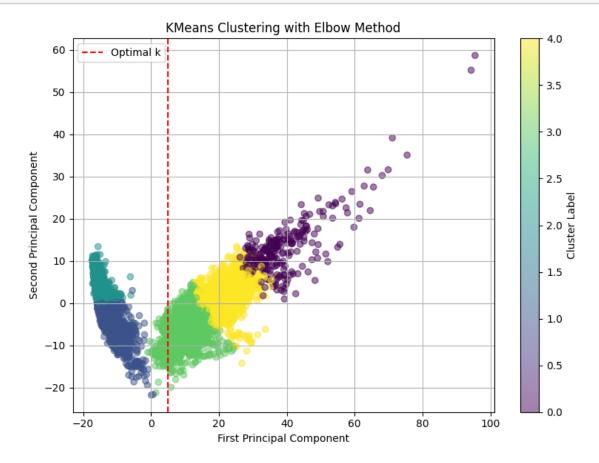
Requirement already satisfied: mkl_random in /usr/local/lib/python3.11/dist-packages (from numpy>=1.14.2->kneed) (1.2.4)

Requirement already satisfied: mkl_umath in /usr/local/lib/python3.11/dist-packages (from numpy>=1.14.2->kneed) (0.1.1)

```
(from numpy>=1.14.2->kneed) (2025.1.0)
     Requirement already satisfied: tbb4py in /usr/local/lib/python3.11/dist-packages
     (from numpy>=1.14.2->kneed) (2022.1.0)
     Requirement already satisfied: mkl-service in /usr/local/lib/python3.11/dist-
     packages (from numpy>=1.14.2->kneed) (2.4.1)
     Requirement already satisfied: intel-openmp<2026,>=2024 in
     /usr/local/lib/python3.11/dist-packages (from mkl->numpy>=1.14.2->kneed)
     (2024.2.0)
     Requirement already satisfied: tbb==2022.* in /usr/local/lib/python3.11/dist-
     packages (from mkl->numpy>=1.14.2->kneed) (2022.1.0)
     Requirement already satisfied: tcmlib==1.* in /usr/local/lib/python3.11/dist-
     packages (from tbb==2022.*->mkl->numpy>=1.14.2->kneed) (1.2.0)
     Requirement already satisfied: intel-cmplr-lib-rt in
     /usr/local/lib/python3.11/dist-packages (from mkl_umath->numpy>=1.14.2->kneed)
     (2024.2.0)
     Requirement already satisfied: intel-cmplr-lib-ur==2024.2.0 in
     /usr/local/lib/python3.11/dist-packages (from intel-
     openmp<2026,>=2024->mkl->numpy>=1.14.2->kneed) (2024.2.0)
     Downloading kneed-0.8.5-py3-none-any.whl (10 kB)
     Installing collected packages: kneed
     Successfully installed kneed-0.8.5
     Optimal k: 5
[10]: # Choose k based on the elbow method
      elbow k = 5
      kmeans elbow = KMeans(n clusters=elbow k, random state=42, n init=10)
      clusters_elbow = kmeans_elbow.fit_predict(X_train)
      # TODO: PCA for visualization
      pca = PCA(n_components=2)
      X_train_pca_elbow = pca.fit_transform(X_train)
      # Plotting the clusters
      plt.figure(figsize=(8, 6))
      # TODO <--code below-->
      plt.scatter(X_train_pca_elbow[:, 0], X_train_pca_elbow[:, 1], c=clusters_elbow,__
       ⇔cmap='viridis', alpha=0.5)
      plt.title("KMeans Clustering with Elbow Method")
      plt.xlabel("First Principal Component")
      plt.ylabel("Second Principal Component")
      plt.colorbar(label='Cluster Label')
      plt.grid()
      plt.axvline(x=knee, color='r', linestyle='--', label='Optimal k')
      plt.legend()
      plt.tight_layout()
```

Requirement already satisfied: mkl in /usr/local/lib/python3.11/dist-packages

plt.show()

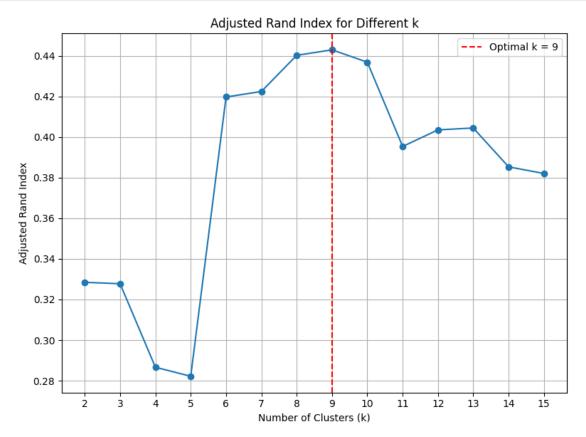


1.3.1 Observing Distortion with Increasing k

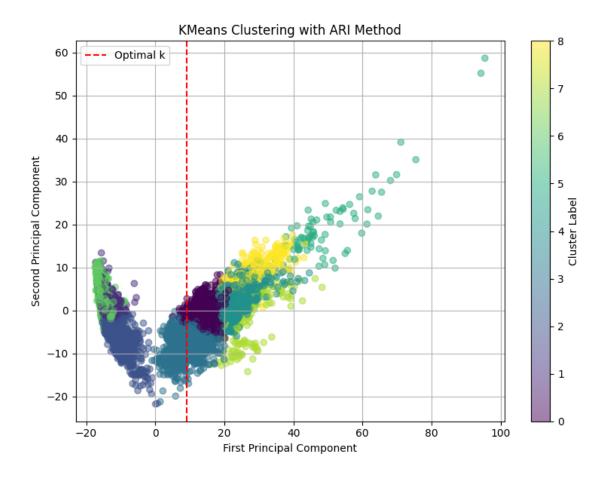
The distortion, which measures the sum of squared distances between data points and their assigned cluster centroids, decreases as the number of clusters (k) increases. This is because adding more clusters allows the centroids to better fit the data, reducing the distance between points and their nearest centroid. However, the rate of decrease in distortion diminishes as k becomes larger, leading to the "elbow" point, where adding more clusters provides diminishing returns in reducing distortion.

2. Adjusted Rand Index (ARI)

```
kmeans = KMeans(n_clusters=k, random_state=42)
    clusters = kmeans.fit_predict(X_train_scaled)
    ari = adjusted_rand_score(y_train.values.ravel(), clusters)
    ari_scores.append(ari)
# Plotting ARI Scores
plt.figure(figsize=(8, 6))
plt.plot(k_values, ari_scores, marker='o')
plt.title("Adjusted Rand Index for Different k")
plt.xlabel("Number of Clusters (k)")
plt.ylabel("Adjusted Rand Index")
plt.xticks(k_values)
plt.grid(True)
\# Optional: Automatically highlight the best k
best_k = k_values[np.argmax(ari_scores)]
plt.axvline(x=best_k, color='r', linestyle='--', label=f'Optimal k = {best_k}')
plt.legend()
plt.tight_layout()
plt.show()
```



```
[12]: from sklearn.metrics import adjusted_rand_score
      from sklearn.cluster import KMeans
      # Choose k based on ARI
      best_ari_k = best_k
      kmeans_ari = KMeans(n_clusters=best_ari_k, random_state=42, n_init=10)
      clusters_ari = kmeans_ari.fit_predict(X_train)
      # PCA for visualization
      pca = PCA(n_components=2)
      X_train_pca_ari = pca.fit_transform(X_train)
      # Plotting the clusters
      plt.figure(figsize=(8, 6))
      # TODO <--code below-->
      plt.scatter(X_train_pca_ari[:, 0], X_train_pca_ari[:, 1], c=clusters_ari,__
       ⇔cmap='viridis', alpha=0.5)
      plt.title("KMeans Clustering with ARI Method")
      plt.xlabel("First Principal Component")
      plt.ylabel("Second Principal Component")
      plt.colorbar(label='Cluster Label')
      plt.grid()
      plt.axvline(x=best_k, color='r', linestyle='--', label='Optimal k')
      plt.legend()
      plt.tight_layout()
     plt.show()
```



1.3.2 Adjusted Rand Index (ARI) Analysis with Increasing k

The Adjusted Rand Index (ARI) measures the similarity between the clustering results and the ground truth labels. As the number of clusters (k) increases, the ARI values exhibit the following behavior:

- 1. **Fluctuations**: As k increases, the ARI fluctuates due to overfitting or the creation of clusters that do not correspond well to the actual data distribution.
- 2. Optimal k: The ARI reaches its peak at an optimal value of k, where the clustering best matches the ground truth labels. In this case, the optimal k is observed at k=9, where the ARI achieves its maximum value of approximately 0.4533.
- 3. **Decline or Plateau**: Beyond the optimal k, the ARI declines or plateau as the clustering becomes too granular, leading to over-segmentation and reduced alignment with the ground truth.

1.4 Prototype Selection using K-means Clustering.

1.4.1 1. Random Selection

```
[13]: import numpy as np
      import pandas as pd
      from sklearn.linear_model import LogisticRegression
      from sklearn.metrics import accuracy_score
      import warnings
      from sklearn.exceptions import DataConversionWarning
      warnings.filterwarnings(action='ignore', category=DataConversionWarning)
      def random_prototype_selection(X, y, n_samples):
          Selects a random subset from the data. train a logistic regression model
          on the selected data.
          Arqs:
              X (pd.DataFrame): The input features.
              y (pd.Series): The target labels.
              n_samples(int): The number of samples to select from each class.
          Returns:
              tuple: A tuple containing the selected features (X_selected) and labels_{\sqcup}
       \hookrightarrow (y selected).
          # Step 1: Initialize lists to store selected features and labels
          X_selected = []
          y_selected = []
          # Step 2: Iterate over each unique class label in the target labels
          for label in np.unique(y.values.ravel()):
              # Filter the data for the current class
              X_class = X[y.values.ravel() == label]
              y_class = y[y.values.ravel() == label]
              # Randomly select n_samples data points from the current class
              indices = np.random.choice(len(X_class), n_samples, replace=False)
              X_selected.append(X_class.iloc[indices])
              y_selected.append(y_class.iloc[indices])
          # Step 3: Concatenate the selected data points from all classes
          X_selected = pd.concat(X_selected, axis=0)
```

```
y_selected = pd.concat(y_selected, axis=0)
   return X_selected, y_selected
n_repetitions = 10
accuracies = []
n \text{ samples} = 120
# TODO caculate the accracy for the randomly selected prototype for 10_{\square}
\rightarrow expermenteds
# TODO <--code below-->
for _ in range(n_repetitions):
    # Select prototypes
   X_selected, y_selected = random_prototype_selection(X_train, y_train, u
 ⇔n_samples)
    # Train Logistic Regression model
   logistic_regression = LogisticRegression(random_state=42, max_iter=1000)
   logistic_regression.fit(X_selected, y_selected)
   # Make predictions and calculate accuracy
   y_pred = logistic_regression.predict(X_test)
   accuracy = accuracy_score(y_test, y_pred)
   accuracies.append(accuracy)
average_accuracy = np.mean(accuracies)
print(f"Average Accuracy with Random Selection over {n_repetitions} repetitions:
```

Average Accuracy with Random Selection over 10 repetitions: 0.9206

1.4.2 2. K-means Clustering by Class

```
[14]: # 2. K-means Clustering by Class

def kmeans_prototype_selection(X, y, n_prototypes_per_class):
    """

    Selects prototypes using K-means clustering for each class.

Args:
    X (pd.DataFrame): The input features.
    y (pd.Series): The target labels.
    n_prototypes_per_class (int): The number of prototypes to select from ← each class.

→ each class.
```

```
Returns:
       pd.DataFrame: The selected prototypes.
       pd. Series: The selected labels.
   #Initialize lists to store selected prototypes and labels
   X_selected = [] # List to store selected feature subsets for each class
   y_selected = [] # List to store selected labels for each class
   # TODO:
      # Step 1: Iterate over each unique class label in the target labels
      # Step 2: for each class cluster its points using k = 1
 →n_prototypes_per_class
      # Step 3: Find the closest points to each centroid
   # TODO <--code below-->
   for label in np.unique(y.values.ravel()):
        # Step 1: Filter the data for the current class
       X_class = X[y.values.ravel() == label]
       y_class = y[y.values.ravel() == label]
        # Step 2: Apply K-means clustering to the current class
       kmeans = KMeans(n_clusters=n_prototypes_per_class, random_state=42)
       kmeans.fit(X_class)
        # Step 3: Find the closest points to each centroid
       centroids = kmeans.cluster_centers_
       closest_indices = []
       for centroid in centroids:
            distances = np.linalg.norm(X_class - centroid, axis=1)
            closest index = np.argmin(distances)
            closest_indices.append(closest_index)
        # Append the selected prototypes and their corresponding labels
       X_selected.append(X_class.iloc[closest_indices])
       y_selected.append(y_class.iloc[closest_indices])
    # Step 4: Concatenate the selected prototypes from all classes
   X_selected = pd.concat(X_selected, axis=0)
   y_selected = pd.concat(y_selected, axis=0)
   # Step 5: Return the selected prototypes and labels
   return X_selected, y_selected
# Select prototypes using K-means
```

Accuracy with K-means Selection: 0.8931

1.4.3 Comparison of Model Accuracy with Random Selection vs. K-means Clustering for Prototype Selection

The accuracy of the model trained using random prototype selection is average_accuracy = 0.9019, while the accuracy of the model trained using K-means clustering for prototype selection is accuracy_kmeans = 0.8931.

Observations:

1. Random Prototype Selection:

- Achieved a higher average accuracy of 90.19%.
- This method relies on randomly selecting prototypes, which may capture diverse samples from each class.

2. K-means Clustering for Prototype Selection:

- Achieved a slightly lower accuracy of 89.31%.
- This method selects prototypes based on clustering, which ensures that the selected samples are representative of the cluster centroids. However, it may miss some outlier or diverse samples.

Using clustering for prototype selection slightly reduces the model's performance compared to random selection. This could be due to the loss of diversity in the selected prototypes, as clustering focuses on centroids rather than capturing the full variability of the data.

1.5 Autoencoder for Features Learning.

####1. Data Preparation:

```
[15]: import glob
import numpy as np

# Load data with proper tensor formatting
def load_inertial_data(path):
    files = glob.glob(path)
    data_dict = {}
    for f in files:
```

```
name = f.split('/')[-1][:-4]
              # Read as numpy array and convert to float32
              data_dict[name] = pd.read_csv(f, sep='\s+', header=None).values.
       ⇒astype(np.float32)
          return data_dict
      # Load training data
      train_data = load_inertial_data("/kaggle/working/UCI HAR Dataset/train/Inertial_u
       ⇔Signals/*.txt")
      train_labels = pd.read_csv("/kaggle/working/UCI_HAR_Dataset/train/y_train.txt", __
       ⇔header=None) [0].values
      # Load Test data
      test_data = load_inertial_data("/kaggle/working/UCI_HAR_Dataset/test/Inertial_
       ⇔Signals/*.txt")
      test_labels = pd.read_csv("/kaggle/working/UCI HAR Dataset/test/y_test.txt",__
       ⇔header=None)[0].values
      print(f"Train Data Dictionary keys: {list(train_data.keys())}")
      print(f"For each sensor the Data shape: {train_data['body_acc_x_train'].shape}")
     Train Data Dictionary keys: ['body_acc_z_train', 'body_gyro_y_train',
     'body_gyro_z_train', 'body_acc_x_train', 'total_acc_z_train',
     'body_acc_y_train', 'total_acc_y_train', 'body_gyro_x_train',
     'total_acc_x_train']
     For each sensor the Data shape: (7352, 128)
[16]: import torch
      from torch.utils.data import Dataset, DataLoader
      # Create PyTorch Dataset
      class SensorsDataset(Dataset):
          def __init__(self, data_dict, labels):
              # Stack all signals along the feature dimension Shape: (num_samples, ____
       →128, num_features)
              self.data = torch.stack([torch.tensor(data_dict[key]) for key in_
       ⇒sorted(data dict.keys())], dim=1)
              self.labels = torch.tensor(labels)
          def __len__(self):
              return len(self.data)
          def __getitem__(self, idx):
              return self.data[idx], self.labels[idx]
      # Create dataset and dataloader
      train_dataset = SensorsDataset(train_data, train_labels)
```

```
# TODO: create pytorch dataloader with Batch sie 32, and shuffle
train_loader = DataLoader(train_dataset, batch_size=32, shuffle=True)

# Verify shapes
sample, label = next(iter(train_loader))
print(f"Input shape: {sample.shape}") # Should be (batch_size, 128, 9)
print(f"Label shape: {label.shape}") # Should be (batch_size)
```

Input shape: torch.Size([32, 9, 128])
Label shape: torch.Size([32])

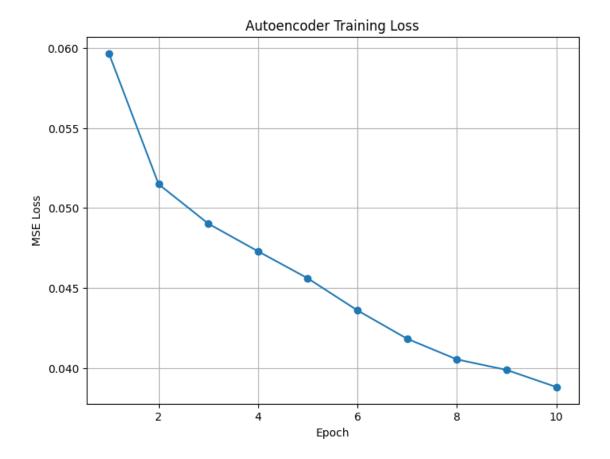
2. Autoencoder Implementation

```
[17]: import torch.nn as nn
      import torch.optim as optim
      import matplotlib.pyplot as plt
      class TimeSeriesAE(nn.Module):
          def __init__(self, input_size=9, seq_length=128, hidden_size=64,__
       ⇔encoding dim=64):
              super().__init__()
              # Transpose the input before feeding to GRU
              self.input_size = input_size
              self.seq_length = seq_length
              # Encoder
              self.encoder = nn.GRU(input_size=input_size,
                                    hidden_size=hidden_size,
                                    batch first=True,
                                    bidirectional=True)
              self.enc_fc = nn.Linear(hidden_size * 2, encoding_dim) # *2 for_
       \hookrightarrow bidirectional
              # Decoder
              self.dec_fc = nn.Linear(encoding_dim, hidden_size)
              self.decoder = nn.GRU(input_size=hidden_size,
                                    hidden_size=hidden_size,
                                    batch first=True,
                                    bidirectional=True)
              self.output_layer = nn.Linear(hidden_size * 2, input_size) # Output_
       ⇔matches input features
          def forward(self, x):
              # x shape: [batch_size, num_features, seq_length]
              # Need to transpose to [batch_size, seq_length, num_features]
              x = x.transpose(1, 2)
```

```
# Encoding
        _, hidden = self.encoder(x)
        hidden = torch.cat([hidden[-2], hidden[-1]], dim=1) # Combine_
 \hookrightarrow bidirectional
        encoded = self.enc_fc(hidden)
        # Decoding
        decoded = self.dec_fc(encoded).unsqueeze(1).repeat(1, x.size(1), 1)
        out, _ = self.decoder(decoded)
        reconstructed = self.output_layer(out)
        # Transpose back to original format [batch_size, num_features,_
 ⇔seq_length]
        reconstructed = reconstructed.transpose(1, 2)
        return reconstructed, encoded
# Instantiate the model
input_size = 9 # Number of features
seq_length = 128  # Time steps
hidden_size = 64
encoding_dim = 64
device = torch.device("cuda" if torch.cuda.is_available() else "cpu")
model = TimeSeriesAE(input_size=input_size, seq_length=seq_length,_
 →hidden_size=hidden_size, encoding_dim=encoding_dim).to(device)
# Define loss function and optimizer
criterion = nn.MSELoss()
optimizer = optim.Adam(model.parameters(), lr=0.001)
# Train loop for the autoencoder
num_epochs = 10
loss_history = []
for epoch in range(num_epochs):
   model.train()
    total loss = 0
    for batch_X, _ in train_loader:
        # Move batch to device
        batch_X = batch_X.to(device)
        # Forward pass
        reconstructed, _ = model(batch_X)
        loss = criterion(reconstructed, batch_X)
```

```
# Backward pass and optimization
        optimizer.zero_grad()
        loss.backward()
        optimizer.step()
        total_loss += loss.item()
    # Calculate average loss for the epoch
    avg_loss = total_loss / len(train_loader)
    loss_history.append(avg_loss)
    print(f"Epoch {epoch+1}/{num_epochs}, Loss: {avg_loss:.4f}")
# Plotting the loss vs epoch
plt.figure(figsize=(8, 6))
plt.plot(range(1, num_epochs+1), loss_history, marker='o')
plt.title('Autoencoder Training Loss')
plt.xlabel('Epoch')
plt.ylabel('MSE Loss')
plt.grid(True)
plt.savefig('autoencoder_training_loss.pdf', format='pdf', dpi=300, __
  ⇔bbox_inches='tight')
plt.show()
Epoch 1/10, Loss: 0.0597
Epoch 2/10, Loss: 0.0515
```

Epoch 1/10, Loss: 0.0597
Epoch 2/10, Loss: 0.0515
Epoch 3/10, Loss: 0.0490
Epoch 4/10, Loss: 0.0473
Epoch 5/10, Loss: 0.0456
Epoch 6/10, Loss: 0.0436
Epoch 7/10, Loss: 0.0418
Epoch 8/10, Loss: 0.0405
Epoch 9/10, Loss: 0.0399
Epoch 10/10, Loss: 0.0388



```
[18]: # 3. Embedding Extraction and Visualization
import numpy as np

ae_loader = DataLoader(train_dataset, batch_size=32, shuffle=False)

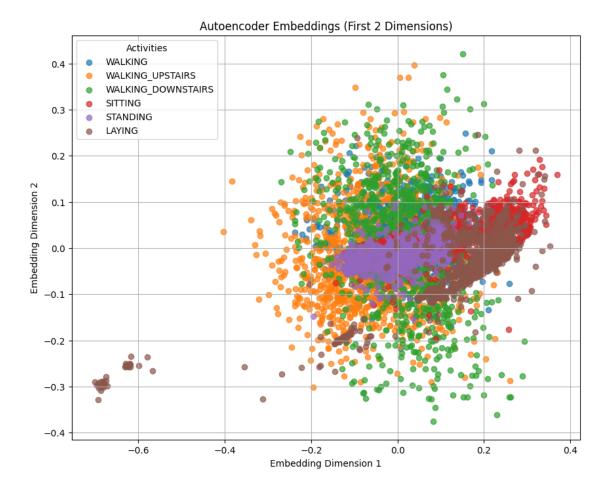
# Extract embeddings for the training data
model.eval()
embeddings = []
labels_list = []

with torch.no_grad():
    for batch_X, batch_y in ae_loader:
        # Move batch to device
        batch_X = batch_X.to(device)

# Pass through the model to get embeddings
        _, encoded = model(batch_X)

# Move embeddings to CPU and convert to numpy
embeddings.append(encoded.cpu().numpy())
```

```
labels_list.append(batch_y.numpy())
# Concatenate all batches
embeddings = np.concatenate(embeddings, axis=0)
labels = np.concatenate(labels_list, axis=0)
# Create a scatter plot of the 2D embeddings (first 2 dimensions)
plt.figure(figsize=(10, 8))
# Load activity labels for better visualization
activity_labels = pd.read_csv("UCI HAR Dataset/activity_labels.txt",
                              header=None, sep=r'\s+',
                              names=['id', 'activity_name'])
activity_mapping = dict(zip(activity_labels['id'],__
 →activity_labels['activity_name']))
# Create scatter plot with different colors for each activity
unique_activities = np.unique(labels)
for activity in unique_activities:
   indices = np.where(labels == activity)[0]
   plt.scatter(embeddings[indices, 0], embeddings[indices, 1],
                label=activity_mapping[activity], alpha=0.7)
plt.title("Autoencoder Embeddings (First 2 Dimensions)")
plt.xlabel("Embedding Dimension 1")
plt.ylabel("Embedding Dimension 2")
plt.legend(title="Activities")
plt.grid(True)
plt.savefig('autoencoder_embeddings.pdf', format='pdf', dpi=300,__
 ⇔bbox_inches='tight')
plt.show()
```



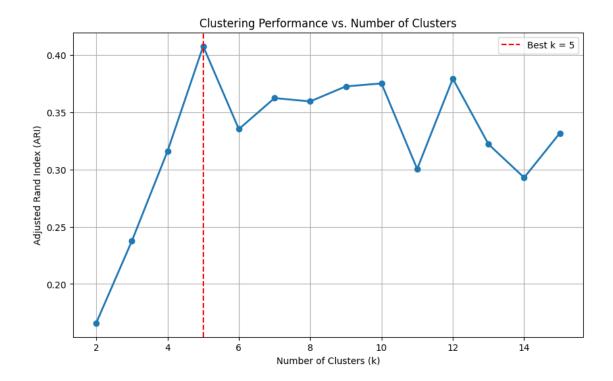
```
[19]: # Adjusted Rand Index (ARI) for the embeddings
from sklearn.cluster import KMeans
from sklearn.metrics import adjusted_rand_score
import numpy as np
import matplotlib.pyplot as plt

ari_scores = []
for k in range(2, 16):
    # Perform K-means clustering
    kmeans = KMeans(n_clusters=k, random_state=42, n_init=10)
    cluster_labels = kmeans.fit_predict(embeddings)

# Calculate ARI
ari = adjusted_rand_score(labels, cluster_labels)
ari_scores.append(ari)
print(f"Number of clusters: {k}, ARI: {ari:.4f}")

# Find the best k
```

```
best_k = np.argmax(ari_scores) + 2 # +2 because we started from k=2
print(f"Best number of clusters: {best_k} with ARI: {ari_scores[best_k-2]:.4f}")
# Plotting ARI Scores
plt.figure(figsize=(10, 6))
plt.plot(range(2, 16), ari_scores, marker='o', linestyle='-', linewidth=2)
plt.axvline(x=best_k, color='r', linestyle='--', label=f'Best k = {best_k}')
plt.grid(True)
plt.xlabel('Number of Clusters (k)')
plt.ylabel('Adjusted Rand Index (ARI)')
plt.title('Clustering Performance vs. Number of Clusters')
plt.legend()
plt.savefig('ari_scores.pdf', format='pdf', dpi=300, bbox_inches='tight')
plt.show()
# Perform clustering with the best k
best_kmeans = KMeans(n_clusters=best_k, random_state=42, n_init=10)
best_cluster_labels = best_kmeans.fit_predict(embeddings)
# Get the final ARI score
final_ari = adjusted_rand_score(labels, best_cluster_labels)
print(f"Final ARI with {best_k} clusters: {final_ari:.4f}")
# Compare with previous ARI from hand-engineered features
# Assuming you have a previous ARI score from part 4.2
# print(f"Previous ARI from hand-engineered features: {previous ari:.4f}")
# print(f"Difference: {final_ari - previous_ari:.4f}")
Number of clusters: 2, ARI: 0.1658
Number of clusters: 3, ARI: 0.2375
Number of clusters: 4, ARI: 0.3160
Number of clusters: 5, ARI: 0.4078
Number of clusters: 6, ARI: 0.3353
Number of clusters: 7, ARI: 0.3624
Number of clusters: 8, ARI: 0.3596
Number of clusters: 9, ARI: 0.3727
Number of clusters: 10, ARI: 0.3753
Number of clusters: 11, ARI: 0.3005
Number of clusters: 12, ARI: 0.3794
Number of clusters: 13, ARI: 0.3221
Number of clusters: 14, ARI: 0.2930
Number of clusters: 15, ARI: 0.3318
Best number of clusters: 5 with ARI: 0.4078
```



Final ARI with 5 clusters: 0.4078

```
[20]: # Choose k based on ARI
     best_embedd_ari_k = 6  # Setting to 6 for the 6 activity classes
     kmeans_ari = KMeans(n_clusters=best_embedd_ari_k, random_state=42, n_init=10)
     clusters_ari = kmeans_ari.fit_predict(embeddings) # Using the embeddings, not_
       \hookrightarrow X train
     # PCA for visualization
     pca = PCA(n_components=2)
     X_train_pca_ari = pca.fit_transform(embeddings) # Apply PCA to embeddings
     # Plotting the clusters
     plt.figure(figsize=(8, 6))
     scatter = plt.scatter(X_train_pca_ari[:, 0], X_train_pca_ari[:, 1],
                          c=clusters_ari, cmap='viridis', alpha=0.7)
     plt.colorbar(scatter, label='Cluster')
     plt.title(f'K-means Clustering of Autoencoder Embeddings
       plt.xlabel('Principal Component 1')
     plt.ylabel('Principal Component 2')
     plt.grid(True)
     plt.show()
```

