

examperformance

October 26, 2024

1 STEPS FOR SIMULATION AND ANALYSIS

We aim to simulate an examination process where two groups of students are compared: one group uses cheat sheets, and the other does not. We will perform a z-test and adjust parameters interactively to observe their impact.

1.1 STEP 1

The parameters to simulate the exam process are: 1. Mean score of students using cheat sheets (1): range [85, 95], step size: 1 2. Mean score of students not using cheat sheets (2): range [80, 90], step size: 1 3. Standard deviation of students using cheat sheets (1): range [1, 5], step size: 0.1 4. Standard deviation of students not using cheat sheets (2): range [1, 5], step size: 0.1 5. Sample size for both groups (n1, n2): range [20, 200], step size: 10

```
[2]: import numpy as np
      from scipy import stats

      # Define the parameters
      mu1_range_cheatsheet = np.arange(85, 96, 1)
      mu2_range_no_cheatsheet = np.arange(80, 91, 1)
      std_range_cheatsheet = np.arange(1, 5.1, 0.1)
      std_range_no_cheatsheet = np.arange(1, 5.1, 0.1)
      sample_size_n_range = np.arange(20, 201, 10)

      # Example: Simulate for specific values
      mean_score_cheatsheet = 88
      mean_score_no_cheatsheet = 85
      std_cheatsheet = 3
      std_no_cheatsheet = 2
      initial_sample_size_cheat_sheet = 45
      initial_no_sample_size_cheat_sheet = 55

      # # Generate random samples
      # np.random.seed(0) # For reproducibility
      # group1_scores = np.random.normal(mu1, sigma1, n1)
      # group2_scores = np.random.normal(mu2, sigma2, n2)

      # # Perform z-test
```

```
# z_stat, p_value = stats.ttest_ind(group1_scores, group2_scores)

# print(f"Z-statistic: {z_stat}, P-value: {p_value}")
```

After running the simulation with default parameters, what are the z-statistic and p-value? What do these values indicate about the performance difference between the two groups

Step 2: Calculate Pooled Standard Deviation and Standard Error

Using the provided formulas, calculate the pooled standard deviation (S_p) and standard error (SE) for each set of parameter values.

Step 3: Perform Z-test

For each set of simulated parameters, calculate the z-score as:

$$z = \frac{\bar{X}_1 - \bar{X}_2}{SE}$$

Compare the z-score to the critical value for a one-tailed test ($z_{crit} = 1.645$ for $\alpha = 0.05$).

1.2 INITIALIZATION OF THE DEFAULT PARAMETERS

```
[3]: import numpy as np

# Example: Simulate for specific values
mean_score_cheatsheet = 88
mean_score_no_cheatsheet = 85
std_cheatsheet = 3
std_no_cheatsheet = 2
initial_sample_size_cheat_sheet = 45
initial_no_sample_size_cheat_sheet = 55
```

calculating z-score and p-value

```
[4]: # Calculate the pooled standard deviation
pooled_variance = ((initial_sample_size_cheat_sheet - 1) * std_cheatsheet**2 +
    ↳ (initial_no_sample_size_cheat_sheet - 1) * std_no_cheatsheet**2) /
    ↳ (initial_sample_size_cheat_sheet + initial_no_sample_size_cheat_sheet - 2)
pooled_std = np.sqrt(pooled_variance)
print(f"Pooled standard deviation: {pooled_std}")

# Calculate the standard error
standard_error = pooled_std * np.sqrt(1 / initial_sample_size_cheat_sheet + 1 /
    ↳ initial_no_sample_size_cheat_sheet)
print(f"Standard error: {standard_error}")

# Calculate the z-score
z_score = (mean_score_cheatsheet - mean_score_no_cheatsheet) / standard_error
```

```
# Calculate the p-value for a one tailed test
p_value = stats.norm.cdf(z_score)

print(f"Z-score: {z_score}, P-value: {p_value}")
```

Pooled standard deviation: 2.498979383505129
Standard error: 0.5023137559951615
Z-score: 5.972362819442471, P-value: 0.9999999988307913

Z-score of 5.9723 tells that there is a 1.2 magnitude difference in performance relative to pooled variance in data.

1.3 Step 3: Perform Z-test

For each set of simulated parameters, calculate the z-score as, Compare the z-score to the critical value for a one-tailed test ($z_{crit} = 1.645$ for $\alpha = 0.05$).

1.4 Step 4: Compare Z-score to Critical Value

For a one-tailed test with a significance level of $\alpha = 0.05$, the critical value (z_{crit}) is 1.645. We compare the calculated z-score to this critical value to determine if we reject the null hypothesis.

- **Z-score (calculated):** 10.874361055604869
- **Critical value (z_{crit}):** 1.645

Since the calculated z-score is greater than the critical value, we reject the null hypothesis. This indicates that there is a statistically significant difference between the two groups.

1.5 Step 4: Plot Results Using Bar Plots

Plot the z-scores and p-values as the parameters vary. Use interactive sliders to dynamically adjust the mean, standard deviation, and sample size.

We are going to run a simulation for different values and plot a graph

Step 4: Plot Results Using Bar Plots Plot the z-scores and p-values as the parameters vary. Use interactive sliders to dynamically adjust the mean, standard deviation, and sample size.

```
[5]: import ipywidgets as widgets
from ipywidgets import interact
import matplotlib.pyplot as plt

# Define the simulation function
def simulation(std_cheatsheet, std_no_cheatsheet, mean_cheatsheet,
    mean_no_cheatsheet, sample_size_cheatsheet, sample_size_no_cheatsheet):
    # Calculate the pooled standard deviation
    pooled_variance = ((sample_size_cheatsheet - 1) * std_cheatsheet**2 +
    (sample_size_no_cheatsheet - 1) * std_no_cheatsheet**2) /
    (sample_size_cheatsheet + sample_size_no_cheatsheet - 2)
    pooled_std = np.sqrt(pooled_variance)
```

```

    # Calculate the standard error
    standard_error = pooled_std * np.sqrt(1 / sample_size_cheatsheet + 1 /
↪sample_size_no_cheatsheet)

    # Calculate the z-score
    z_score = (mean_cheatsheet - mean_no_cheatsheet) / standard_error

    # Calculate the p-value for a one tailed test
    p_value = stats.norm.cdf(z_score)

    return z_score, p_value

# Define the plotting function
def plot_simulation(mean_cheatsheet, mean_no_cheatsheet, std_cheatsheet,
↪std_no_cheatsheet, sample_size_cheatsheet, sample_size_no_cheatsheet):
    z_score, p_value = simulation(std_cheatsheet, std_no_cheatsheet,
↪mean_cheatsheet, mean_no_cheatsheet, sample_size_cheatsheet,
↪sample_size_no_cheatsheet)

    fig, ax = plt.subplots(1, 2, figsize=(12, 5))

    ax[0].bar(['Z-score'], [z_score], color='blue')
    ax[0].set_ylim([0, 10])
    ax[0].set_title('Z-score')

    ax[1].bar(['P-value'], [p_value], color='red')
    ax[1].set_ylim([0, 1])
    ax[1].set_title('P-value')

    plt.show()

# Create interactive sliders
interact(plot_simulation,
        mean_cheatsheet=widgets.FloatSlider(min=85, max=95, step=1, value=88,
↪description='Mean Cheat Sheet'),
        mean_no_cheatsheet=widgets.FloatSlider(min=80, max=90, step=1,
↪value=85, description='Mean No Cheat Sheet'),
        std_cheatsheet=widgets.FloatSlider(min=1, max=5, step=0.1, value=3,
↪description='Std Cheat Sheet'),
        std_no_cheatsheet=widgets.FloatSlider(min=1, max=5, step=0.1, value=2,
↪description='Std No Cheat Sheet'),
        sample_size_cheatsheet=widgets.IntSlider(min=20, max=200, step=10,
↪value=45, description='Sample Size Cheat Sheet'),
        sample_size_no_cheatsheet=widgets.IntSlider(min=20, max=200, step=10,
↪value=55, description='Sample Size No Cheat Sheet'))

```

```
interactive(children=(FloatSlider(value=88.0, description='Mean Cheat Sheet',  
    max=95.0, min=85.0, step=1.0), F...
```

```
[5]: <function __main__.plot_simulation(mean_cheatsheet, mean_no_cheatsheet,  
    std_cheatsheet, std_no_cheatsheet, sample_size_cheatsheet,  
    sample_size_no_cheatsheet)>
```

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[ ]:
```