

B07-9058. 材料力学

1-a.

$$f(z) = \frac{1}{\sqrt{2\pi}} e^{-\frac{z^2}{2}}$$

1-b

$$P(-1 \leq Z \leq 1) \approx 0.6826$$

$$\text{st. norm. cdf}(1, \mu, \sigma) - \text{st. norm. cdf}(-1, \mu, \sigma)$$

1-c.

$$P(-x \leq Z \leq x) = 95\%, x \approx 1.9599$$

$$px = (1 - 0.95)/2$$

$$x = \text{st. norm. pdf}(0.95 + px, \mu, \sigma)$$

x.

1-d

$$f(z) = \frac{1}{\sqrt{2\pi}} e^{-\frac{z^2}{2}}, -\infty < z < \infty$$

$$f(z) = \frac{1}{\sqrt{2\pi}} e^{-\frac{z^2}{2}} \cdot \frac{1}{|J|} \cdot \frac{1}{\sqrt{2\pi}} e^{-\frac{z^2}{2}} (J)$$

$$= \frac{1}{\sqrt{2\pi}} e^{-\frac{z^2}{2}} \frac{1}{\sqrt{Q}}$$



1-e

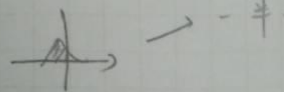
$$\mu = \alpha \beta$$

$$\mu = 1.$$

平方 → 设下 $\sigma^2 \rightarrow 2\sigma^2$ 开根号

1-f

$$\text{std}[Q] = \sqrt{2}$$



1-g

$$P(Z \leq 1) = 0.5$$

2-a

$$f_T(t) = 1e^{-t}$$

2-b

$$\mu = 1$$

2-c

$$\sigma = 1$$

2-d $P(T > 1) = e^{-1} \approx 0.37$

2-e

$$P(1) = 1, \alpha = 3, \beta = 1, T(2) = 1!$$

$$T(3) = 2!$$

$$f(t) = \frac{1}{2} t^2 e^{-t}$$

2-f

$$E[T_3] = 3 \times 1 = 3$$

2-g

$$\text{std}(T_3) = \sqrt{3 \cdot 1^2} = \sqrt{3}$$

2-h

$$P(T_3 > 3) = \frac{1}{2} \cdot 9 \cdot e^{-3} \approx 0.22$$

2-i

$$P(T_3 > 7) = \frac{1}{2} \cdot 49 \cdot e^{-7} \approx 0.0023$$

↓
有機會發生，可接受