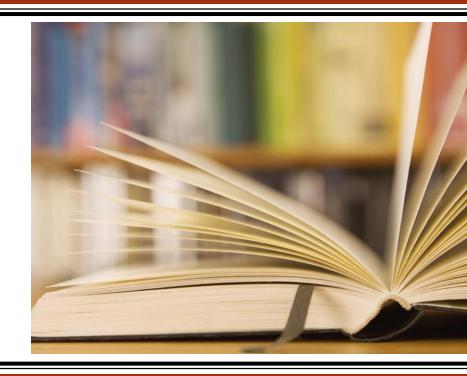
CSCI235 – Database Systems

Normalization In Practice

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A relational schema R = (A, B, C)Functional dependencies: $AB \rightarrow C$

A relational schema R = (A, B, C)

Functional dependencies: $AB \rightarrow C$

- If $AB \rightarrow C$ is valid in R and it covers the entire relational schema, then its left hand side, (A,B), is a minimal super key.
- There is no other minimal super key in R.
- Hence the minimal super key of R is (A, B).

A relational schema R = (A, B, C)Functional dependencies: $AB \rightarrow C$

A relational schema R = (A, B, C)

Functional dependencies: $AB \rightarrow C$

- There is NO partial dependency in R. Hence, the relational schema R is in 2NF.
- There is NO transitive dependency in R. Hence, the relational schema R is in 3NF.
- There is NO non-trivial dependency in R. Hence, the relational schema R has no BCNF violation.
- \therefore The relational schema R is in **BCNF**.

A relational schema R = (A, B, C)Functional dependencies: $AB \rightarrow C, C \rightarrow B$

A relational schema R = (A, B, C)

Functional dependencies: $AB \rightarrow C, C \rightarrow B$

- If $AB \rightarrow C$ is valid in R and it covers the entire relational schema, then its left hand side, (A, B), is a minimal super key.
- If $C \to B$, then through augmentation rule, $AC \to AB$.
- If AC → AB is valid in R and it covers the entire relational schema, then its left hand side, (A, C), is a minimal super key.
- \therefore the minimal super keys of R are (A, B) and (A, C).

A relational schema R = (A, B, C)Functional dependencies: $AB \rightarrow C, C \rightarrow B$

A relational schema R = (A, B, C)Functional dependencies: $AB \rightarrow C, C \rightarrow B$

What is the normal form? (Scenario 1)

- Since (A, B) is a minimal super key, there is NO partial dependency and NO transitive dependency, but there exist non-trivial dependency C→B. Existence of non-trivial dependency is a violation of BCNF requirement. Hence, the relational schema CANNOT be in BCNF.
- : the relational schema R = (A, B, C) is in 3NF.

A relational schema R = (A, B, C)Functional dependencies: $AB \rightarrow C, C \rightarrow B$

What is the normal form? (Scenario 2)

- Since (A, C) is a minimal super key, there exist a partial dependency $C \to B$, a violation of 2NF requirement. There is NO transitive dependency, and there is NO non-trivial dependency.
- : the relational schema R = (A, B, C) is in 1NF.
- Question: Why the relational schema is not in 3NF or BCNF?

A relational schema R = (A, B, C)

Functional dependencies: $AB \rightarrow C, C \rightarrow B$

How to transform the relational schema R into BCNF? (Scenario 1)

A relational schema R = (A, B, C)

Functional dependencies: $AB \rightarrow C, C \rightarrow B$

How to transform the relational schema R into BCNF? (Scenario 1)

- Remove the non-trivial dependency $C \rightarrow B$ from the relational schema R, and decompose it into two relational schema, R1 = (A, B) and R2 = (C, B).
- In relational schema R1, the minimal super key is (A, B).
 - There is NO partial dependency, NO transitive dependency, and NO non-trivial dependency. Hence, the relational schema R1 is in BCNF.

A relational schema R = (A, B, C)

Functional dependencies: $AB \rightarrow C, C \rightarrow B$

How to transform the relational schema R into BCNF? (Scenario 1)

- Remove the non-trivial dependency $C \rightarrow B$ from the relational schema R, and decompose it into two relational schema, R1 = (A, B) and R2 = (C, B).
- In relational schema R2, the minimal super key is
 (C).
 - There is NO partial dependency, NO transitive dependency, and NO non-trivial dependency. Hence, the relational schema R2 is in BCNF.

A relational schema R = (A, B, C)

Functional dependencies: $AB \rightarrow C, C \rightarrow B$

How to transform the relational schema R into BCNF? (Scenario 2)

A relational schema R = (A, B, C)

Functional dependencies: $AB \rightarrow C, C \rightarrow B$

How to transform the relational schema R into BCNF? (Scenario 2)

- In scenario 2, $AC \rightarrow AB$. Remove the partial dependency $C \rightarrow B$ from the relational schema R, and decompose it into two relational schema, R1 = (A, C) and R2 = (C, B).
- In relational schema R1, the minimal super key is (AC).
 - There is NO partial dependency, NO transitive dependency, and NO non-trivial dependency. Hence, the relational schema R1 is in BCNF.

A relational schema R = (A, B, C)

Functional dependencies: $AB \rightarrow C, C \rightarrow B$

How to transform the relational schema R into BCNF? (Scenario 2)

- In scenario 2, $AC \rightarrow AB$. Remove the partial dependency $C \rightarrow B$ from the relational schema R, and decompose it into two relational schema, R1 = (A, C) and R2 = (C, B).
- In relational schema R2, the minimal super key is (C).
 - There is NO partial dependency, NO transitive dependency, and NO non-trivial dependency. Hence, the relational schema R2 is in BCNF.

A relational schema R = (A, B, C)Functional dependencies: $AB \rightarrow C$, $C \rightarrow B$, $C \rightarrow A$

A relational schema R = (A, B, C)

Functional dependencies: $AB \rightarrow C$, $C \rightarrow B$, $C \rightarrow A$

- If $AB \rightarrow C$ is valid in R, and it covers the entire relational schema, then the left hand side of the functional dependency, (A, B) is a minimal super key.
- If $C \to B$ and $C \to A$, then through union rule $C \to AB$.
- If C → AB is valid in R and it covers the entire relational schema, then the left hand side of the functional dependency, C is a minimal super key.
- Hence, the minimal super keys of the relational schema R are (A, B) and (C).

A relational schema R = (A, B, C)

Functional dependencies: $AB \rightarrow C$, $C \rightarrow B$, $C \rightarrow A$

A relational schema R = (A, B, C)

Functional dependencies: $AB \rightarrow C$, $C \rightarrow B$, $C \rightarrow A$

- There is NO partial dependency in the relational schema R. Hence, the relational schema R is in 2NF.
- There is NO transitive dependency in the relational schema R. Hence, the relational schema R is in 3NF.
- There is NO non-trivial dependency in the relational schema R. Hence the relational schema R does not have BCNF violation.
- \therefore The relational schema R is in **BCNF**.

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$

- If $A \rightarrow B$ is valid in R, then through augmentation rule, $AC \rightarrow BC$.
- If $AC \rightarrow BC$ is valid in R and it covers the entire relational schema then the left hand side of the functional dependency (A, C) is a minimal key.
- Hence, the minimal super keys of the relational schema R is (A, C).

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$

- Since (A, C) is a minimal super key, and $A \rightarrow B$, there exist a partial dependency. Hence, the relational schema R CANNOT be in 2NF.
- There is NO transitive dependency and NO non-trivial dependency in the relational schema R.
- Hence, the highest normal form of the relational schema R is in 1NF.

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$

How to transform the relational schema R into BCNF?

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$

How to transform the relational schema R into BCNF?

• Since there exists a partial dependency in the relational schema R, to transform the relational schema to BCNF, we need to remove the partial dependency, and split it into two relational schemas R1 = (A, C) and R2 = (A, B).

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$

How to transform the relational schema R into BCNF?

- In the relational schema R1 = (A, C), the minimal super key is (A, C).
 - There is NO partial dependency nor transitive dependency in the relational schema R1. In addition, there is also NO non-trivial dependency exist. Hence, the relational schema R1 is in BCNF.
- In the relational schema R2 = (A, B), the minimal super key is (A).

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$

How to transform the relational schema R into BCNF?

- In the relational schema R2 = (A, B), the minimal super key is (A).
 - There is NO partial dependency nor transitive dependency. In addition there is also NO nontrivial dependency. Hence, the relational schema R2 is in BCNF.

A relational schema R = (A, B, C)Functional dependencies: $A \rightarrow B$, $B \rightarrow A$

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$, $B \rightarrow A$

- If $A \rightarrow B$ then through augmentation rule, $AC \rightarrow BC$.
- If $AC \rightarrow BC$ is valid in R and it covers the entire relational schema, then the left-hand-side of the functional dependency (AC) is a minimal super key.
- If $B \rightarrow A$ then through augmentation rule, $BC \rightarrow AC$.
- If $BC \rightarrow AC$ is valid in R and it covers the entire relational schema, then the left-hand-side of the functional dependency (BC) is a minimal super key.

A relational schema R = (A, B, C)Functional dependencies: $A \rightarrow B$, $B \rightarrow A$

A relational schema R = (A, B, C)Functional dependencies: $A \rightarrow B$, $B \rightarrow A$

What is the normal form?

Since (A, C) is a minimal super key, and A → B, there exist a partial dependency (violate 2NF requirement). In addition, the functional dependency B → A, the determinant B is not a minimal super key and A is part of a minimal super key (A, C), this forms a non-trivial dependency (violate BCNF requirement). Hence, the relational schema is in 1NF.

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$, $B \rightarrow A$

- Similarly, if (B, C) is a minimal super key, then B → A forms a partial dependency (this violates 2NF requirement). Hence, the relational schema CANNOT be in 2NF. In addition, the functional dependency A → B, the determinant A is not a minimal super key and B is part of a minimal super key (B, C), this forms a non-trivial dependency (violate BCNF requirement). Hence, the relational schema is in 1NF.
- Hence, the relational schema R = (A, B, C) is in 1NF.

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$, $B \rightarrow A$

How to transform the relational schema R into BCNF?

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$, $B \rightarrow A$

How to transform the relational schema R into BCNF?

• Since there exists a partial dependency in the relational schema R, to transform the relational schema to BCNF, we need to remove the partial dependency, and split it into two relational schemas R1 = (A, C) and R2 = (A, B).

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$, $B \rightarrow A$

How to transform the relational schema R into BCNF?

- In the relational schema R1 = (A, C), the minimal super key is (A, C).
 - There is NO partial dependency (No violation of 2NF).
 - There is NO transitive dependency (No violation of 3NF).
 - There is NO non-trivial dependency (No violation of BCNF).
 - \therefore the relational schema R1 is in BCNF.

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$, $B \rightarrow A$

- In the relational schema R2 = (A, B), the minimal super key can be (A) or (B).
 - There is NO partial dependency (No violation of 2NF).
 - There is NO transitive dependency (No violation of 3NF).
 - There is NO non-trivial dependency (No violation of BCNF).
 - \therefore the relational schema R2 is in BCNF.

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$, $B \rightarrow C$.

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$, $B \rightarrow C$.

- If $A \rightarrow B$ and $B \rightarrow C$ then through transitivity rule, $A \rightarrow C$.
- If $A \rightarrow B$ and $A \rightarrow C$ then through union rule, $A \rightarrow BC$
- If A → BC is valid in R and it covers the entire relational schema then, the left-hand-side of the functional dependency (A) is a minimal super key.

A relational schema R = (A, B, C)Functional dependencies: $A \rightarrow B$, $B \rightarrow C$.

A relational schema R = (A, B, C)Functional dependencies: $A \rightarrow B$, $B \rightarrow C$.

- With the functional dependency A → BC, there is NO partial dependency.
- However, there exist a transitive dependency $B \rightarrow C$ (a violation of 3NF requirement), hence, the relational schema R = (A, B, C) is in 2NF.

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$, $B \rightarrow C$.

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$, $B \rightarrow C$.

- With the functional dependency $A \rightarrow BC$, there exist a transitive dependency $B \rightarrow C$ (a violation of 3NF requirement).
- To transform the relational schema R to BCNF, we need to remove the transitive dependency violation and decompose the relational schema R into two relational schemas R1 = (A, B) and R2 = (B, C).

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$, $B \rightarrow C$.

How to transform the relational schema *R* into BCNF?

• In the relational schema R1 = (A, B), the minimal super key is (A) and there is NO partial dependency, transitive dependency, and non-transitive dependency, the relational schema R1 is in BCNF.

A relational schema R = (A, B, C)

Functional dependencies: $A \rightarrow B$, $B \rightarrow C$.

How to transform the relational schema *R* into BCNF?

• In the relational schema R2 = (B, C), the minimal super key is (B) and there is NO partial dependency, transitive dependency, and non-transitive dependency, the relational schema R2 is also in BCNF.

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, A \rightarrow C, B \rightarrow D$

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, A \rightarrow C, B \rightarrow D$

- If $A \to B$ and $A \to C$ then through union rule $A \to BC$.
- If $A \rightarrow B$ and $B \rightarrow D$ then through **transitivity rule** $A \rightarrow D$.
- If $A \rightarrow BC$ and $A \rightarrow D$ then through union rule $A \rightarrow BCD$.
- If $A \rightarrow BCD$ is valid in R and it covers the entire relational schema, then the left-hand-side of the functional dependency (A) is a minimal super key.

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, A \rightarrow C, B \rightarrow D$

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, A \rightarrow C, B \rightarrow D$

- In the functional dependency $A \rightarrow BCD$, there is NO partial dependency. However, there is a transitive dependency $B \rightarrow D$ (a violation of 3NF.)
- : the relational schema R = (A, B, C, D) is in 2NF.

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, A \rightarrow C, B \rightarrow D$

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, A \rightarrow C, B \rightarrow D$

How to transform the relational schema R into BCNF?

• With the functional dependency $A \rightarrow BCD$, there is no partial dependency, but there exists a transitive dependency $B \rightarrow D$ (a violation of 3NF.) To transform the relational schema to BCNF, we need to remove the transitive dependency and split the relational schema R into two schemas R1 = (A, B, C) and R2 = (B, D).

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, A \rightarrow C, B \rightarrow D$

- In R1 = (A, B, C), the minimal super key is (A) and there are NO partial dependency, transitive dependency, and non-trivial dependency violations. Hence, the relational schema R1 = (A, B, C) is in BCNF.
- In R2 = (B, D), the minimal super key is (B) and there are NO partial dependency, transitive dependency, and non-trivial dependency violations. Hence, the relational schema R2 = (B, D) is in BCNF.

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, B \rightarrow D, C \rightarrow B$

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow D, C \rightarrow B$

- If $A \rightarrow B$ and $B \rightarrow D$ then through **transitivity rule** $A \rightarrow D$.
- If $A \rightarrow D$ and $A \rightarrow B$ then through union rule $A \rightarrow BD$.
- If $A \rightarrow BD$ then through augmentation rule $AC \rightarrow BCD$.
- If $AC \rightarrow BCD$ is valid in R and it covers the entire relational schema, then the left-hand-side of the functional dependency (AC) is a minimal super key.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow D, C \rightarrow B$

- If $C \rightarrow B$ and $B \rightarrow D$ then through **transitivity rule** $C \rightarrow D$.
- If $C \to D$ and $C \to B$ then through union rule $C \to BD$.
- If $C \rightarrow BD$ then through augmentation rule $AC \rightarrow ABD$.
- If AC → ABD is valid in R and it covers the entire relational schema, then the left-hand-side of the functional dependency (AC) is a minimal super key.

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, B \rightarrow D, C \rightarrow B$

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, B \rightarrow D, C \rightarrow B$

- In $AC \rightarrow BCD$, there exists a partial dependency $A \rightarrow B$ and $C \rightarrow B$, hence, a violation of 2NF requirement.
- There exists also a transitive dependency $B \rightarrow D$, hence, a violation of 3NF requirement.
- \therefore the relational schema is in 1NF.

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, B \rightarrow D, C \rightarrow B$

- In $AC \rightarrow ABD$, there exists a partial dependency $A \rightarrow B$ and $C \rightarrow B$, hence, a violation of 2NF requirement.
- There exists also a transitive dependency $B \rightarrow D$, hence, a violation of 3NF requirement.
- \therefore the relational schema is in 1NF.

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, B \rightarrow D, C \rightarrow B$

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, B \rightarrow D, C \rightarrow B$

- In $AC \rightarrow BCD$, there exists a partial dependency $A \rightarrow B$ and $C \rightarrow B$, hence, a violation of 2NF requirement.
- There exists also a transitive dependency $B \rightarrow D$, hence, a violation of 3NF requirement.
- To transform the relational schema to BCNF, we need to first remove all partial dependencies from the relational schema $AC \rightarrow BCD$, and we have R1 = (A, B, D), R2 = (C, B), R3 = (A, C).

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, B \rightarrow D, C \rightarrow B$

- In the relational schema R1 = (A, B, D), (A) is the minimal super key. There is NO partial dependency, but there exist a transitive dependency $B \rightarrow D$, (a violation of 3NF.)
- To transform the relational schema R1 = (A, B, D) to BCNF, we need to remove the transitive dependency $B \rightarrow D$ by splitting R1 into R1 = (A, B) and R4 = (B, D).

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, B \rightarrow D, C \rightarrow B$

- In relational schema R1 = (A, B), the minimal super key is (A). There are NO partial dependency, no transitive dependency, and no non-trivial dependency. Hence, R1 = (A, B) is in BCNF.
- In relational schema R4 = (B, D), the minimal super key is (B). There are NO partial dependency, no transitive dependency, and no non-trivial dependency. Hence, R4 = (B, D) is in BCNF.

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, B \rightarrow D, C \rightarrow B$

- In relational schema, R2 = (C, B), the minimal super key is (C). There are NO partial dependency, no transitive dependency, and no non-trivial dependency. Hence, R2 = (C, B) is in BCNF.
- In relational schema, R3 = (A, C), the minimal super key is (AC). There are NO partial dependency, no transitive dependency, and no non-trivial dependency. Hence, R3 = (A, C) is in BCNF.

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, A \rightarrow C, B \rightarrow A, B \rightarrow C$

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, A \rightarrow C, B \rightarrow A, B \rightarrow C$

- If $A \rightarrow B$ and $A \rightarrow C$, then through union rule, $A \rightarrow BC$
- If $A \rightarrow BC$ then through augmentation rule $AD \rightarrow BCD$.
- If $AD \rightarrow BCD$ is valid in R and it covers the entire relational schema, then the left-hand-side of the functional dependency (A, D) is a minimal super key.

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, A \rightarrow C, B \rightarrow A, B \rightarrow C$

- If $B \to A$ and $B \to C$, then through union rule, $B \to AC$
- If $B \rightarrow AC$ then through augmentation rule $BD \rightarrow ACD$.
- If $BD \rightarrow ACD$ is valid in R and it covers the entire relational schema, then the left-hand-side of the functional dependency (B,D) is a minimal super key.

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, A \rightarrow C, B \rightarrow A, B \rightarrow C$

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, A \rightarrow C, B \rightarrow A, B \rightarrow C$

- In the functional dependency $AD \rightarrow BCD$, there exist:
 - Partial dependencies A → B and A → C. These partial dependencies are a violation of 2NF requirement.
 - Transitive dependency $B \rightarrow C$. This transitive dependency is a violation of 3NF requirement.
 - Non-trivial dependency $B \rightarrow A$. This non-trivial dependency is a violation of BCNF.
- Hence, the relational schema R is in 1NF.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, A \rightarrow C, B \rightarrow A, B \rightarrow C$

- In the functional dependency $BD \rightarrow ACD$, there exist:
 - Partial dependencies $B \rightarrow A$ and $B \rightarrow C$. These partial dependencies are a violation of 2NF requirement.
 - Transitive dependency A → C. This transitive dependency is a violation of 3NF requirement.
 - Non-trivial dependency $B \rightarrow A$. This non-trivial dependency is a violation of BCNF.
- Hence, the relational schema R is in 1NF.

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, A \rightarrow C, B \rightarrow A, B \rightarrow C$

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, A \rightarrow C, B \rightarrow A, B \rightarrow C$

- With $AD \rightarrow BCD$, we need to remove the partial dependencies $A \rightarrow BC$ and split the relational schema R into two relational schemas R1 = (A, D) and R2 = (A, B, C)
 - In relational schema R1 = (A, D), the minimal super key is (A), and the relational schema has NO partial dependency, NO transitive dependency, and NO non-trivial dependency. Hence, the relational schema R1 is in BCNF.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, A \rightarrow C, B \rightarrow A, B \rightarrow C$

How to transform the relational schema R into BCNF?

• In relational schema R2 = (A, B, C), the minimal super key is (A), and the relational schema has NO partial dependency, but there exists a transitive dependency $B \rightarrow C$, and a non-trivial dependency $B \rightarrow A$. To transform the relational schema to BCNF, we need to remove both the transitive dependency $B \rightarrow C$, and the non-trivial dependency $B \rightarrow A$. Split the relational schema R2 into R3 = (A, B), and R4 = (B, C).

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B$, $A \rightarrow C$, $B \rightarrow A$, $B \rightarrow C$

How to transform the relational schema R into BCNF?

- In relational schema R3 = (A, B), the minimal super key is (A), and the relational schema has NO partial dependency, NO transitive dependency and NO non-trivial dependency. Hence the relational schema R3 is in BCNF.
- In relational schema R4 = (B, C), the minimal super key is (B), and the relational schema has NO partial dependency, NO transitive dependency and NO non-trivial dependency. Hence the relational schema R4 is in BCNF.

A relational schema R = (A, B, C, D)

Functional dependencies: $AB \rightarrow C, C \rightarrow D, D \rightarrow A, D \rightarrow B$

What is the minimal super key? (Scenario 1)

A relational schema R = (A, B, C, D)Functional dependencies: $AB \rightarrow C, C \rightarrow D, D \rightarrow A, D \rightarrow B$

What is the minimal super key? (Scenario 1)

- If $AB \rightarrow C$ and $C \rightarrow D$ then through **transitivity** rule, $AB \rightarrow D$.
- If $AB \rightarrow D$ and $AB \rightarrow C$ then through union rule, $AB \rightarrow CD$.
- If $AB \rightarrow CD$ is valid in R and it covers the entire relational schema then the left-hand-side of the functional dependency (A, B) is a minimal key.

A relational schema R = (A, B, C, D)Functional dependencies: $AB \rightarrow C, C \rightarrow D, D \rightarrow A, D \rightarrow B$

What is the minimal super key? (Scenario 2)

- If $D \rightarrow A$ and $D \rightarrow B$ then through union rule, $D \rightarrow AB$.
- If $D \rightarrow AB$ and $AB \rightarrow C$ then through transitivity rule, $D \rightarrow C$.
- If $D \rightarrow C$ and $D \rightarrow AB$ then $D \rightarrow ABC$.
- If $D \rightarrow ABC$ is valid in R and it covers the entire relational schema then the left-hand-side of the functional dependency (D) is a minimal key.

A relational schema R = (A, B, C, D)

Functional dependencies: $AB \rightarrow C, C \rightarrow D, D \rightarrow A, D \rightarrow B$

What is the minimal super key? (Scenario 3)

- If $C \rightarrow D$ and $D \rightarrow AB$ then through **transitivity** rule, $C \rightarrow AB$.
- If $C \rightarrow D$ and $C \rightarrow AB$ then through union rule, $C \rightarrow ABD$.
- If $C \rightarrow ABD$ is valid in R and it covers the entire relational schema then the left-hand-side of the functional dependency (C) is a minimal key.

A relational schema R = (A, B, C, D)

Functional dependencies: $AB \rightarrow C, C \rightarrow D, D \rightarrow A, D \rightarrow B$

What is the normal form? (Scenario 1)

A relational schema R = (A, B, C, D)

Functional dependencies: $AB \rightarrow C, C \rightarrow D, D \rightarrow A, D \rightarrow B$

What is the normal form? (Scenario 1)

- In the functional dependency $AB \rightarrow CD$, there is NO partial dependency, but there exist a transitive dependency $C \rightarrow D$. A transitive dependency is a violation of 3NF requirement.
- : the relational schema R = (A, B, C, D) is in 2NF.

A relational schema R = (A, B, C, D)

Functional dependencies: $AB \rightarrow C, C \rightarrow D, D \rightarrow A, D \rightarrow B$

What is the normal form? (Scenario 2)

- In the functional dependency $D \rightarrow ABC$, there is NO partial dependency, but there exist a transitive dependency $AB \rightarrow C$. A transitive dependency is a violation of 3NF requirement.
- : the relational schema R = (A, B, C, D) is in 2NF.

A relational schema R = (A, B, C, D)

Functional dependencies: $AB \rightarrow C, C \rightarrow D, D \rightarrow A, D \rightarrow B$

What is the normal form? (Scenario 3)

- In the functional dependency $C \rightarrow DAB$, there is NO partial dependency, but there exist a transitive dependency $D \rightarrow AB$. A transitive dependency is a violation of 3NF requirement.
- : the relational schema R = (A, B, C, D) is in 2NF.

A relational schema R = (A, B, C, D)

Functional dependencies: $AB \rightarrow C, C \rightarrow D, D \rightarrow A, D \rightarrow B$

A relational schema R = (A, B, C, D)Functional dependencies: $AB \rightarrow C, C \rightarrow D, D \rightarrow A, D \rightarrow B$

- In the functional dependency $AB \rightarrow CD$, we need to remove the transitive dependency $C \rightarrow D$ and split the relational schema R into two relational schemas R1 = (A, B, C) and R2 = (C, D).
 - In relational schema R1 = (A, B, C), the minimal super key is (A, B), and the relational schema has NO partial dependency, NO transitive dependency and NO non-trivial dependency. Hence the relational schema R1 is in BCNF.

A relational schema R = (A, B, C, D)Functional dependencies: $AB \rightarrow C, C \rightarrow D, D \rightarrow A, D \rightarrow B$

How to transform the relational schema R into BCNF? (Scenario 1)

 In relational schema R2 = (C, D), the minimal super key is (C), and the relational schema has NO partial dependency, NO transitive dependency and NO non-trivial dependency. Hence the relational schema R2 is in BCNF.

A relational schema R = (A, B, C, D)

Functional dependencies: $AB \rightarrow C, C \rightarrow D, D \rightarrow A, D \rightarrow B$

- In the functional dependency $D \to ABC$, we need to remove the transitive dependency $AB \to C$ and split the relational schema R into two relational schemas R3 = (D, A, B) and R4 = (A, B, C).
 - In relational schema R3 = (D, A, B), the minimal super key is (D), and the relational schema has NO partial dependency, NO transitive dependency and NO nontrivial dependency. Hence the relational schema R3 is in BCNF.

A relational schema R = (A, B, C, D)

Functional dependencies: $AB \rightarrow C, C \rightarrow D, D \rightarrow A, D \rightarrow B$

- In the functional dependency $D \to ABC$, we need to remove the transitive dependency $AB \to C$ and split the relational schema R into two relational schemas R3 = (D, A, B) and R4 = (A, B, C).
 - In relational schema R4 = (A, B, C), the minimal super key is (A, B), and the relational schema has NO partial dependency, NO transitive dependency and NO nontrivial dependency. Hence the relational schema R4 is in BCNF.

A relational schema R = (A, B, C, D)

Functional dependencies: $AB \rightarrow C, C \rightarrow D, D \rightarrow A, D \rightarrow B$

- In the functional dependency $C \to DAB$, we need to remove the transitive dependency $D \to AB$ and split the relational schema R into two relational schemas R5 = (C, D) and R6 = (D, A, B).
 - In relational schema R5 = (C, D), the minimal super key is (C), and the relational schema has NO partial dependency, NO transitive dependency and NO nontrivial dependency. Hence the relational schema R5 is in BCNF.

A relational schema R = (A, B, C, D)

Functional dependencies: $AB \rightarrow C, C \rightarrow D, D \rightarrow A, D \rightarrow B$

- In the functional dependency $C \rightarrow DAB$, we need to remove the transitive dependency $D \rightarrow AB$ and split the relational schema R into two relational schemas R5 = (C, D) and R6 = (D, A, B).
 - In relational schema R6 = (D, A, B), the minimal super key is (D), and the relational schema has NO partial dependency, NO transitive dependency and NO nontrivial dependency. Hence the relational schema R6 is in BCNF.

 Note: In the Example 10, the transformation of the relational schema to BCNF is needed (done) only using one of the three possible scenario.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

What is the minimal super key? (Scenario 1)

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

What is the minimal super key? (Scenario 1)

- If $A \rightarrow B$ and $B \rightarrow C$ then through **transitivity rule**, $A \rightarrow C$.
- If $A \rightarrow C$ and $C \rightarrow D$ then through **transitivity rule**, $A \rightarrow D$.
- If $A \rightarrow B$ and $A \rightarrow D$ then through union rule $A \rightarrow BCD$.
- If A → BCD is valid in R and it covers the entire relational schema then the left-hand-side of the functional dependency (A) is a minimal super key.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

What is the minimal super key? (Scenario 2)

- If $B \to C$ and $C \to D$ then through transitivity rule, $B \to D$.
- If $B \to D$ and $D \to A$ then through transitivity rule, $B \to A$.
- If $B \to C$ and $B \to D$ and $B \to A$ then through union rule $B \to ACD$.
- If B → ACD is valid in R and it covers the entire relational schema then the left-hand-side of the functional dependency (B) is a minimal super key.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

What is the minimal super key? (Scenario 3)

- If $C \to D$ and $D \to A$ then through transitivity rule, $C \to A$.
- If $C \to A$ and $A \to B$ then through **transitivity rule**, $C \to B$.
- If $C \rightarrow A$ and $C \rightarrow B$ and $C \rightarrow D$ then through union rule $C \rightarrow ABD$.
- If C → ABD is valid in R and it covers the entire relational schema then the left-hand-side of the functional dependency (C) is a minimal super key.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

What is the normal form? (Scenario 1)

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

What is the normal form? (Scenario 1)

- In the functional dependency $A \rightarrow BCD$, there is NO partial dependency, but there exist transitive dependencies $B \rightarrow C$ and $C \rightarrow D$. Existence of transitive dependency is a violation of 3NF requirement. In addition, there also exist a non-trivial dependency $D \rightarrow A$. Existence of non-trivial dependency is a violation of BCNF requirement.
- : the relational schema R = (A, B, C, D) is in 2NF.

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

What is the normal form? (Scenario 2)

- In the functional dependency $B \rightarrow ACD$, there is NO partial dependency, but there exist transitive dependencies $C \rightarrow D$ and $D \rightarrow A$. Existence of transitive dependency is a violation of 3NF requirement. In addition, there also exist a non-trivial dependency $A \rightarrow B$. Existence of non-trivial dependency is a violation of BCNF requirement.
- : the relational schema R = (A, B, C, D) is in 2NF.

A relational schema R = (A, B, C, D)Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

What is the normal form? (Scenario 3)

- In the functional dependency C → ABD, there is NO partial dependency, but there exist transitive dependencies D → A and A → B. Existence of transitive dependency is a violation of 3NF requirement. In addition, there also exist a non-trivial dependency B → C. Existence of non-trivial dependency is a violation of BCNF requirement.
- : the relational schema R = (A, B, C, D) is in 2NF.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

- In the functional dependency $A \rightarrow BCD$, we need to remove the transitive dependencies $B \rightarrow C$ and $C \rightarrow D$, and the non-trivial dependency $D \rightarrow A$. Split the relational schema R into four relational schemas R1 = (A, B), R2 = (B, C), R3 = (C, D), and R4 = (D, A).
 - In relational schema R1 = (A, B), the minimal super key is
 (A), and the relational schema has NO partial dependency,
 NO transitive dependency and NO non-trivial dependency.
 ∴ the relational schema R1 is in BCNF.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

- In the functional dependency $A \rightarrow BCD$, we need to remove the transitive dependencies $B \rightarrow C$ and $C \rightarrow D$, and the non-trivial dependency $D \rightarrow A$. Split the relational schema R into four relational schemas R1 = (A, B), R2 = (B, C), R3 = (C, D), and R4 = (D, A).
 - In relational schema R2 = (B, C), the minimal super key is (B), and the relational schema has NO partial dependency, NO transitive dependency and NO non-trivial dependency.
 ∴ the relational schema R2 is in BCNF.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

- In the functional dependency $A \rightarrow BCD$, we need to remove the transitive dependencies $B \rightarrow C$ and $C \rightarrow D$, and the non-trivial dependency $D \rightarrow A$. Split the relational schema R into four relational schemas R1 = (A, B), R2 = (B, C), R3 = (C, D), and R4 = (D, A).
 - In relational schema R3 = (C, D), the minimal super key is (C), and the relational schema has NO partial dependency, NO transitive dependency and NO non-trivial dependency.
 ∴ the relational schema R3 is in BCNF.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

- In the functional dependency $A \rightarrow BCD$, we need to remove the transitive dependencies $B \rightarrow C$ and $C \rightarrow D$, and the non-trivial dependency $D \rightarrow A$. Split the relational schema R into four relational schemas R1 = (A, B), R2 = (B, C), R3 = (C, D), and R4 = (D, A).
 - In relational schema R4 = (D, A), the minimal super key is (D), and the relational schema has NO partial dependency, NO transitive dependency and NO non-trivial dependency.
 ∴ the relational schema R4 is in BCNF.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

- In the functional dependency $B \to ACD$, we need to remove the transitive dependencies $C \to D$ and $D \to A$, and the non-trivial dependency $D \to B$. Split the relational schema R into four relational schemas R1 = (B,C), R2 = (C,D), R3 = (D,A), and R4 = (D,B).
 - In relational schema R1 = (B, C), the minimal super key is (B), and the relational schema has NO partial dependency, NO transitive dependency and NO non-trivial dependency.
 ∴ the relational schema R1 is in BCNF.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

- In the functional dependency $B \to ACD$, we need to remove the transitive dependencies $C \to D$ and $D \to A$, and the non-trivial dependency $A \to B$. Split the relational schema R into four relational schemas R1 = (B, C), R2 = (C, D), R3 = (D, A), and R4 = (A, B).
 - In relational schema R2 = (C, D), the minimal super key is (C), and the relational schema has NO partial dependency, NO transitive dependency and NO non-trivial dependency.
 - \therefore the relational schema R2 is in BCNF.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

- In the functional dependency $B \to ACD$, we need to remove the transitive dependencies $C \to D$ and $D \to A$, and the non-trivial dependency $D \to B$. Split the relational schema R into four relational schemas R1 = (B,C), R2 = (C,D), R3 = (D,A), and R4 = (D,B).
 - In relational schema R3 = (D,A), the minimal super key is (D), and the relational schema has NO partial dependency, NO transitive dependency and NO non-trivial dependency.
 ∴ the relational schema R3 is in BCNF.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

- In the functional dependency $B \to ACD$, we need to remove the transitive dependencies $C \to D$ and $D \to A$, and the non-trivial dependency $D \to B$. Split the relational schema R into four relational schemas R1 = (B,C), R2 = (C,D), R3 = (D,A), and R4 = (D,B).
 - In relational schema R4 = (D, B), the minimal super key is (D), and the relational schema has NO partial dependency, NO transitive dependency and NO non-trivial dependency.
 ∴ the relational schema R4 is in BCNF.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

- In the functional dependency $C \to DAB$, we need to remove the transitive dependencies $D \to A$ and $A \to B$, and the non-trivial dependency $B \to C$. Split the relational schema R into four relational schemas R1 = (C, D), R2 = (D, A), R3 = (A, B), and R4 = (B, C).
 - In relational schema R1 = (C, D), the minimal super key is (C), and the relational schema has NO partial dependency, NO transitive dependency and NO non-trivial dependency.
 ∴ the relational schema R1 is in BCNF.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

- In the functional dependency $C \to DAB$, we need to remove the transitive dependencies $D \to A$ and $A \to B$, and the non-trivial dependency $B \to C$. Split the relational schema R into four relational schemas R1 = (C, D), R2 = (D, A), R3 = (A, B), and R4 = (B, C).
 - In relational schema R2 = (D, A), the minimal super key is (D), and the relational schema has NO partial dependency, NO transitive dependency and NO non-trivial dependency.
 - \therefore the relational schema R2 is in BCNF.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

- In the functional dependency $C \to DAB$, we need to remove the transitive dependencies $D \to A$ and $A \to B$, and the non-trivial dependency $B \to C$. Split the relational schema R into four relational schemas R1 = (C, D), R2 = (D, A), R3 = (A, B), and R4 = (B, C).
 - In relational schema R3 = (A, B), the minimal super key is (A), and the relational schema has NO partial dependency, NO transitive dependency and NO non-trivial dependency.
 - \therefore the relational schema R3 is in BCNF.

A relational schema R = (A, B, C, D)

Functional dependencies: $A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A$

- In the functional dependency $C \to DAB$, we need to remove the transitive dependencies $D \to A$ and $A \to B$, and the non-trivial dependency $B \to C$. Split the relational schema R into four relational schemas R1 = (C, D), R2 = (D, A), R3 = (A, B), and R4 = (B, C).
 - In relational schema R4 = (B, C), the minimal super key is (B), and the relational schema has NO partial dependency, NO transitive dependency and NO non-trivial dependency.
 ∴ the relational schema R4 is in BCNF.

 Note: In the Example 11, the transformation of the relational schema to BCNF is needed (done) only using one of the three possible scenario.

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