

# Collision Detection

# Overview

- Collision detection
  - Coarse collision detection
    - Bounding volumes
    - Hierarchies
    - Spatial data structures
  - Fine collision detection
    - Contact generation
  - Collision queries

# Collision Detection

- Collisions
  - Simulating collisions consists of
    - Collision detection (programming problem)
      - To detect whether a collision has occurred
    - Collision response (physics problem)
      - How objects react when they collide
  - Games without physics still use collision
    - For example
      - Ray casts: select objects, shoot at things, distance to the ground
      - To move interpenetrating objects apart
      - To query the surroundings, e.g., explosions, entities within range
      - Triggers: pick up items, trigger events, activate AI

# Collision Detection

- Collision detection system
  - Determining whether objects come into *contact*
    - More than just true/false
    - Information about the nature of each contact
  - Responsible for finding
    - Pairs of colliding objects
    - Single objects that are colliding with immovable objects
  - Needs to take geometry into account
    - Geometric shapes can be simple or complex
    - Collision representation can differ from visual representation

# Collision Detection

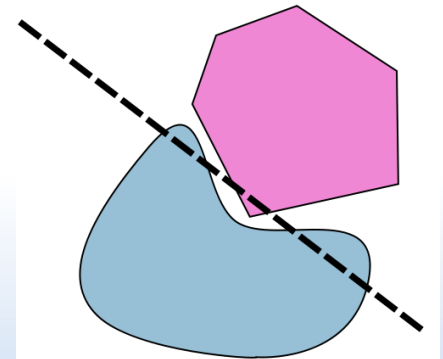
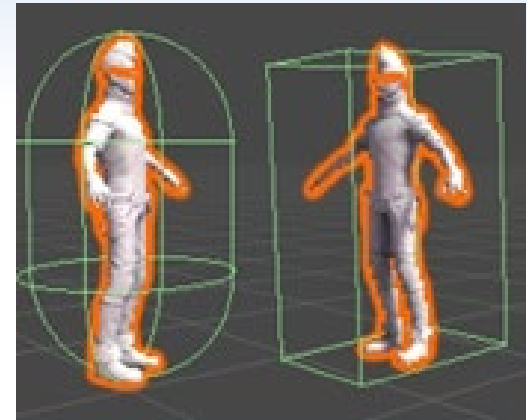
- Unity

- Collider

- Base class for all colliders, e.g.,
      - BoxCollider, SphereCollider, CapsuleCollider, MeshCollider
    - If an object with a Collider needs to be moved during gameplay, should attach a Rigidbody component
      - The Rigidbody can be set to be kinematic if you don't want the object to have physical interaction with other objects
    - Some properties and methods
      - `isTrigger`: specifies if the collider used as a trigger
      - `OnCollisionEnter`: called when this collider touches another collider

# Collision Detection

- Unity
  - Collision detection often not carried out directly on meshes
  - Primitive colliders
    - Box, sphere and capsule
      - Relatively simple collision detection algorithms
  - Mesh collider
    - Very computationally expensive
    - Only convex mesh colliders supported
    - Collision between two mesh colliders may not always be detected



# Collision Detection

- Complex problem

- Can be very time-consuming

- Each object in the game may be colliding with any other object
- Each pair has to be checked
- Each object may have different geometry
- Number of possible collisions:

$$N_c = \frac{n!}{2(n-2)!}$$

| Number of objects | Number of possible collisions |
|-------------------|-------------------------------|
| 2                 | 1                             |
| 4                 | 6                             |
| 10                | 45                            |
| 100               | 4950                          |
| 1000              | 499,500                       |
| 10000             | 49,995,000                    |

# Collision Detection

- Computational complexity
  - Key problems
    - Too many possible collisions
    - Expensive checks
  - To reduce the number of checks
    - Phase 1: Coarse collision detection (broad phase)
      - Find sets of objects *likely* to be in contact
    - Phase 2: Fine collision detection (narrow phase)
      - Check whether candidate collisions (from broad phase) are actually in contact
      - If so, obtain contact information (contact generation)



# Collision Detection

- Coarse collision detection

- Key features

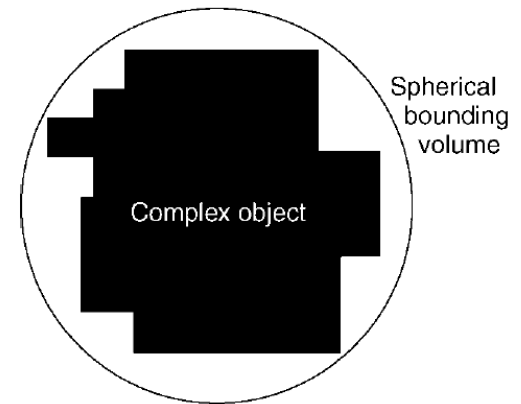
- As fast as possible
    - Should be conservative
      - Allowed to generate checks that end up not being actual collisions ('false positives' to be discarded in phase 2)
    - At the same time, should minimise number of false positives to reduce computational overheads in phase 2

- Common approaches

- Bounding volume and hierarchies
    - Spatial data structures
      - Same structure can be used elsewhere in the game engine, e.g., in the rendering systems

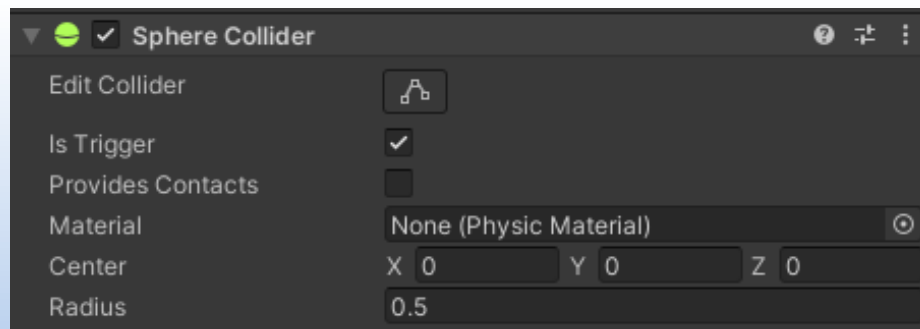
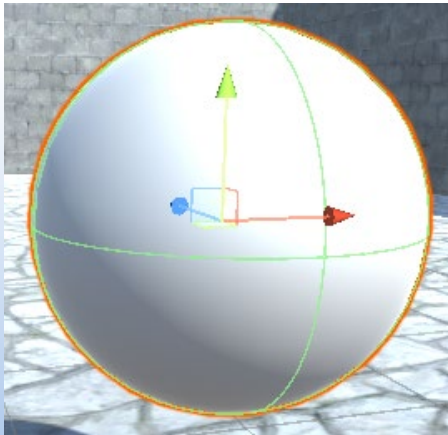
# Bounding Volumes

- Bounding volumes
  - An area of space known to contain the object
  - Large enough for the object to be inside
    - Ideally, as close fitting as possible
  - Simple shape used
    - Simplifies collision tests
    - Simplifies repositioning
    - Minimises data storage overheads
  - Concept
    - If the bounding volumes of two objects do not touch
      - The objects inside them cannot be in contact



# Bounding Volumes

- Bounding sphere
  - Easy to represent, only needs
    - Centre and radius
  - Invariant under rotation
    - When moving, only its position needs to be updated
  - Easy to check whether two spheres overlap
  - Unity: SphereCollider

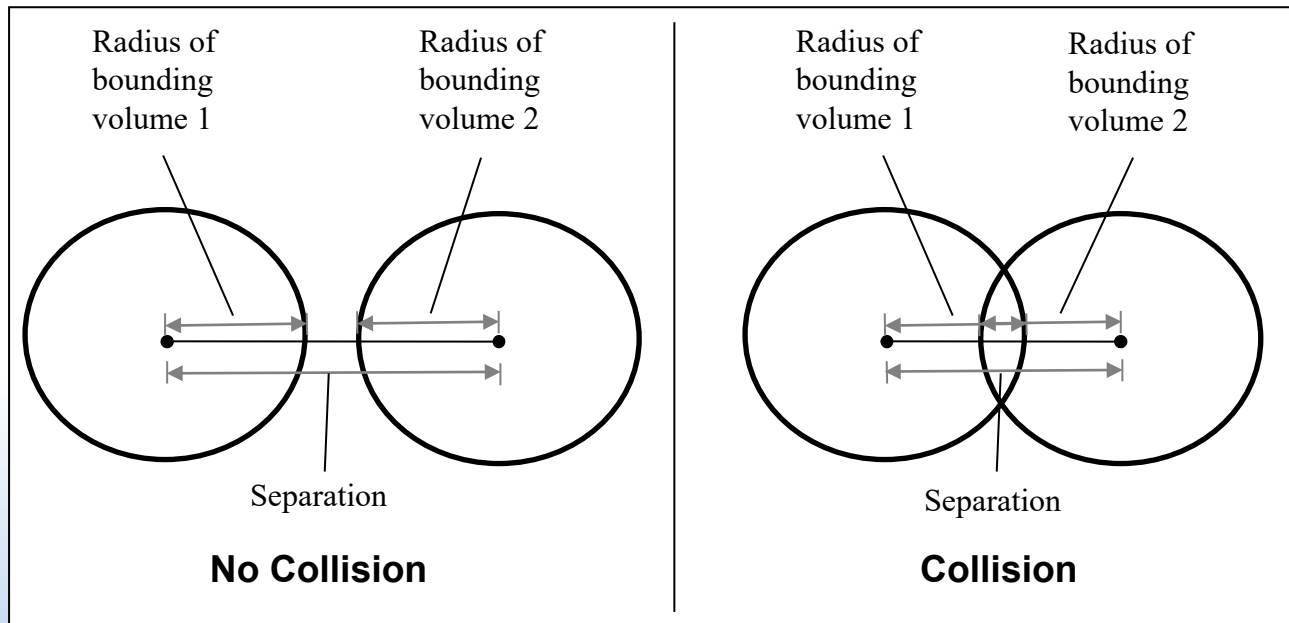


# Bounding Volumes

## ➤ Simple collision check

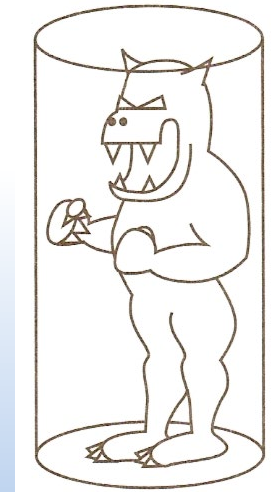
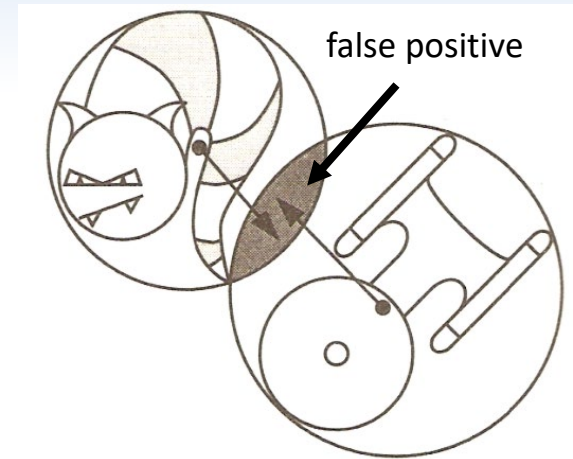
- Overlap if distances between centres less than sum of radii

`if(separationDistance < radius1 + radius2)`



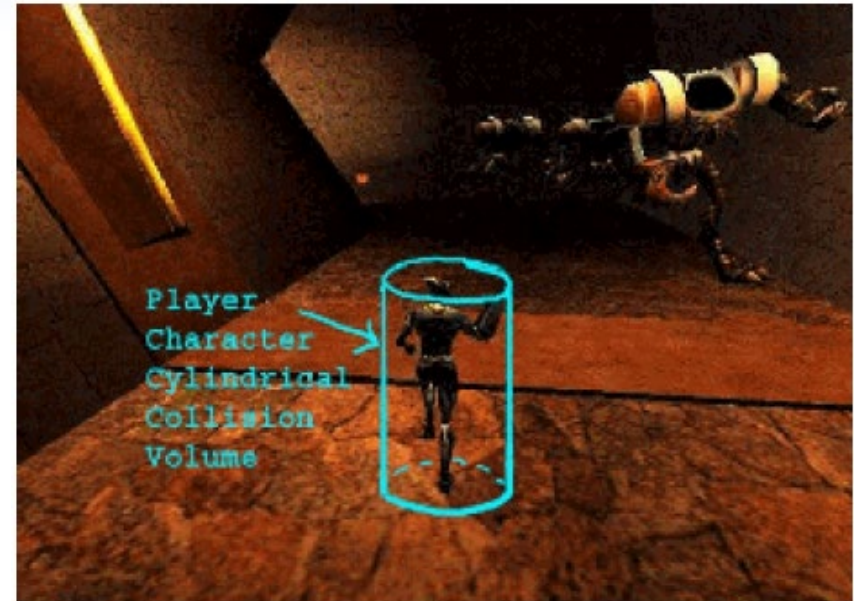
# Bounding Volumes

- Bounding cylinders
  - Problem with spheres
    - Good for objects that spread out in a number of directions
    - But not good for tall and thin objects
  - Work well for games where most objects orientated about the same way toward some surface



# Bounding Volumes

- In many games
  - Characters stay orientated in same direction with respect to the floor
- If always aligned to floor
  - When moving only need to update position
  - No need to rotate

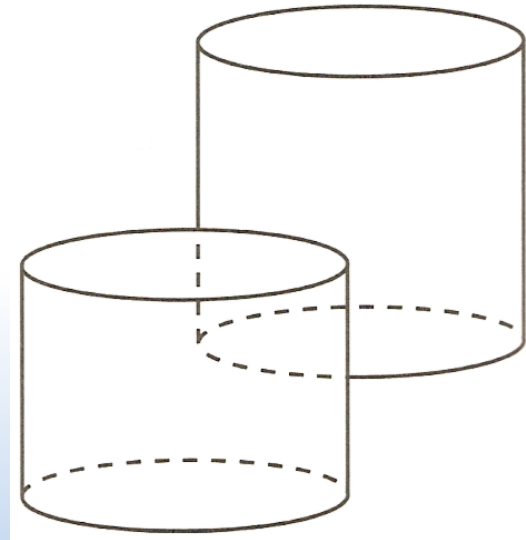
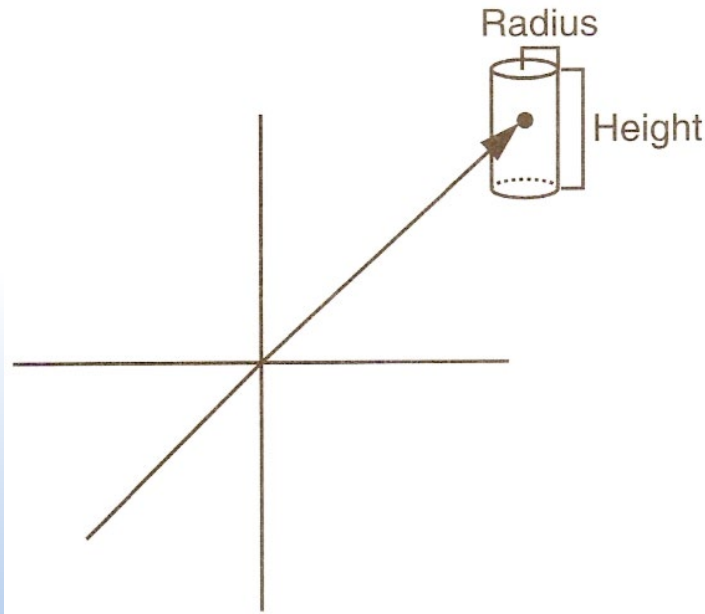


**In *MDK2* we used a cylinder model for the character-to-environment collision detection.**

# Bounding Volumes

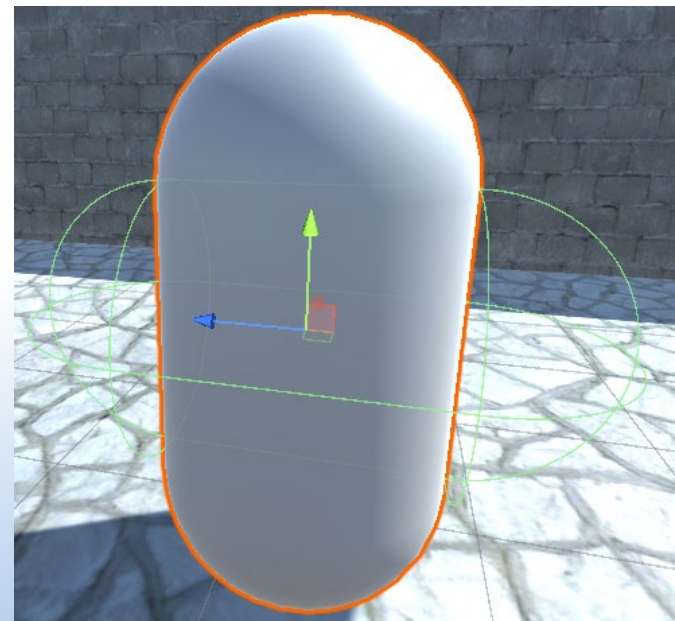
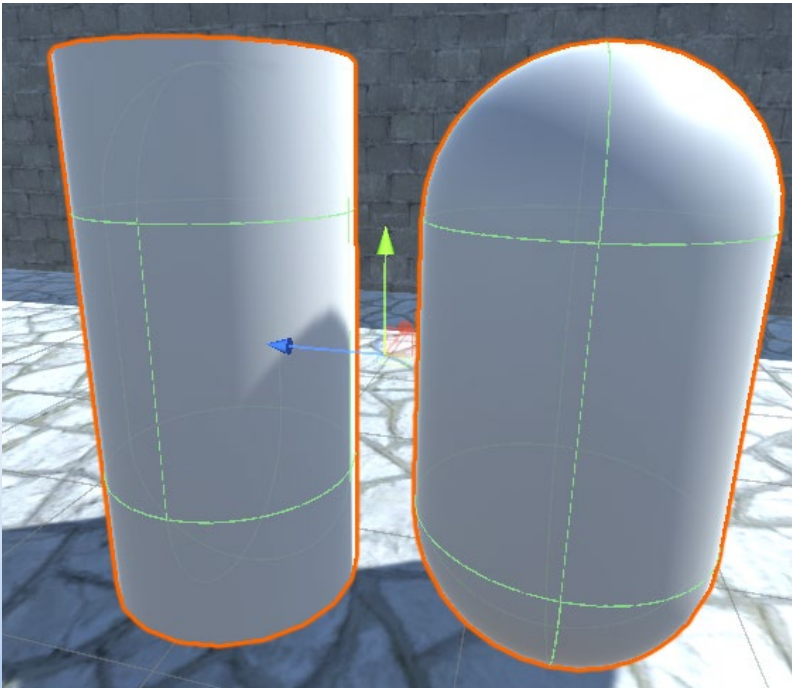
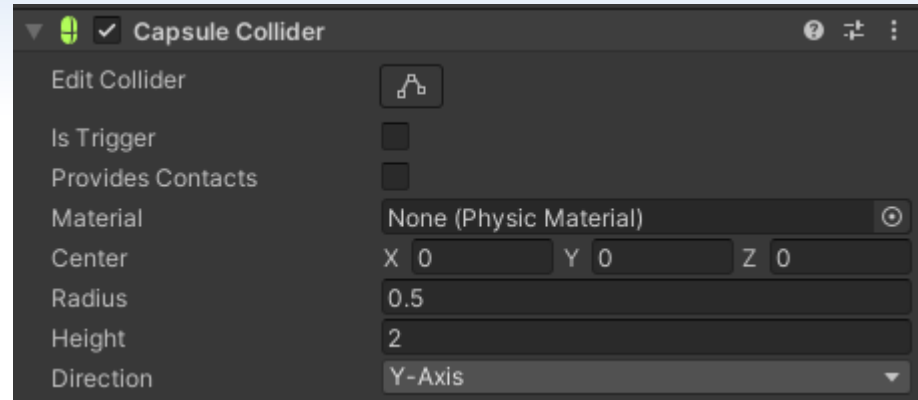
## ➤ Collision check

- Two-steps process
  - Check radius (the same method as spheres)
  - If the radii overlap
    - » Check whether heights of the cylinders overlap



# Bounding Volumes

- Unity
  - CapsuleCollider
    - Used for cylinders as well
    - Can set Direction





# Bounding Volumes

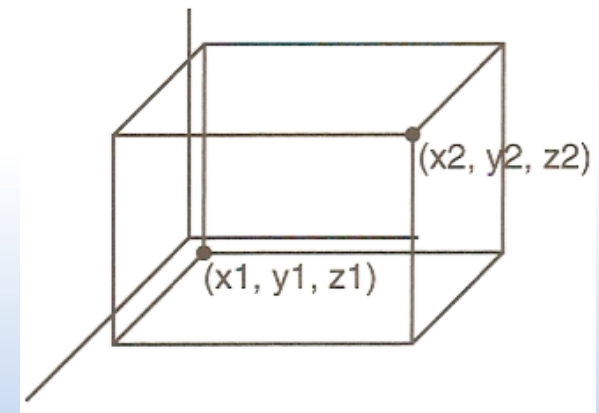
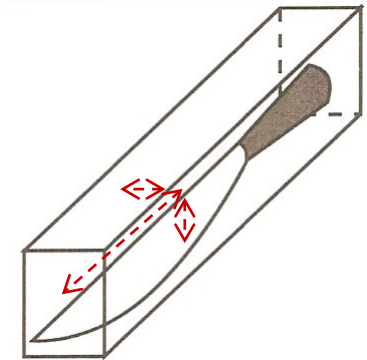
- Bounding boxes
  - Good for rectangular objects
  - Can be represented as
    - Central point and a set of dimensions, one for each direction
      - E.g., distance from the central point to its sides in x, y and z directions (half the overall box size, 'half-size')
- Other representations are also possible

```
Vector3 centre;
```

```
Vector3 halfSize;
```

```
Vector3 maxVertex;
```

```
Vector3 minVertex;
```

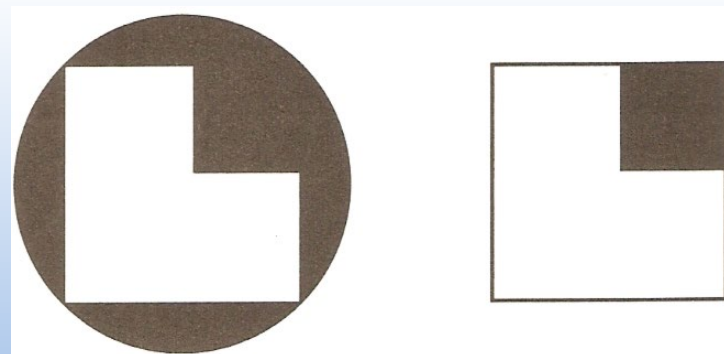
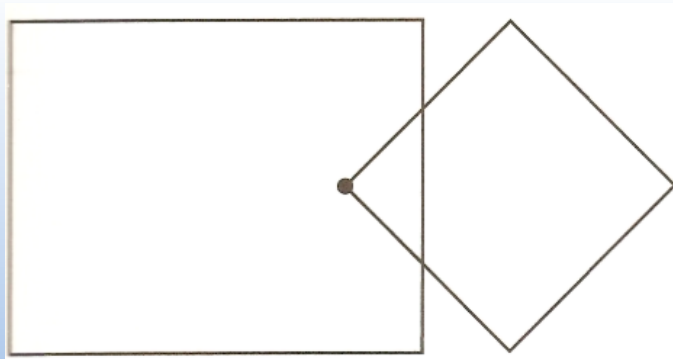
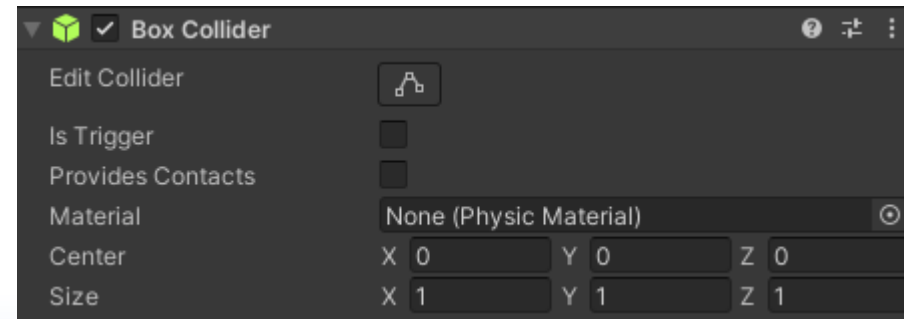
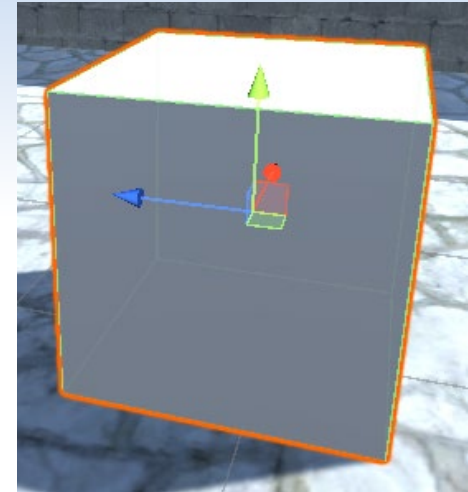


# Bounding Volumes

## ➤ Collision check

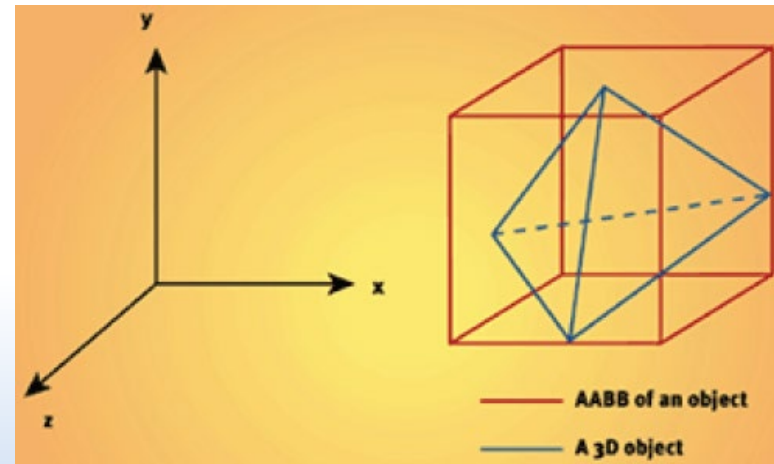
- More complex than spheres or cylinders
- Two bounding boxes are colliding if the vertex of one is inside the other
- Requires more computation compared to spheres or cylinders

## ➤ Unity: BoxCollider



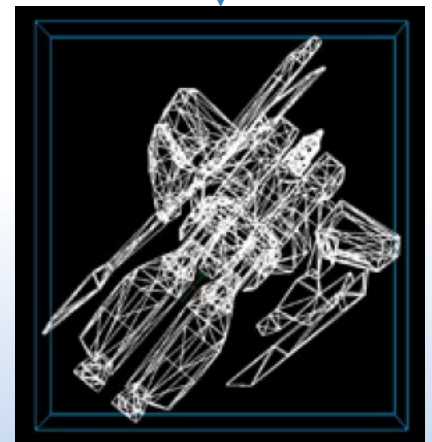
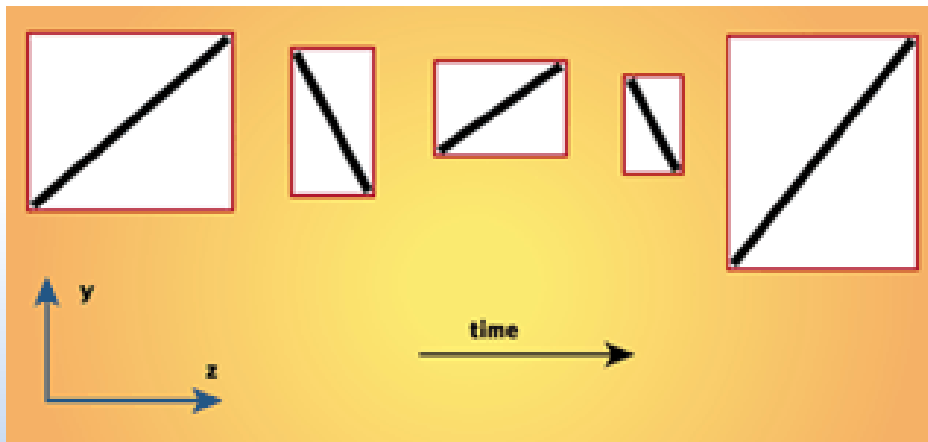
# Bounding Volumes

- Two types of bounding boxes in game engines
  - Axis-Aligned Bounding Boxes (AABBs)
  - Orientated Bounding Boxes (OBBs)
- AABBs
  - Aligned to world axes
  - Each box face perpendicular to one coordinate axis
  - AABBs do not rotate
  - Good for static objects that are aligned to axes and do not rotate



# Bounding Volumes

- When object rotates, need to re-compute bounds
- Assumption
  - Faster than rotating the bounding box, but more empty space, i.e. more false positives
  - Trade-off between speed and accuracy



# Bounding Volumes

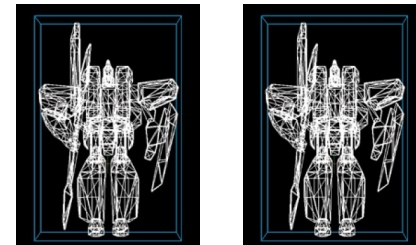
## ➤ Collision check

- Two AABBs do not collide if their projections on a plane do not overlap

## • Unity

### ➤ Bounds

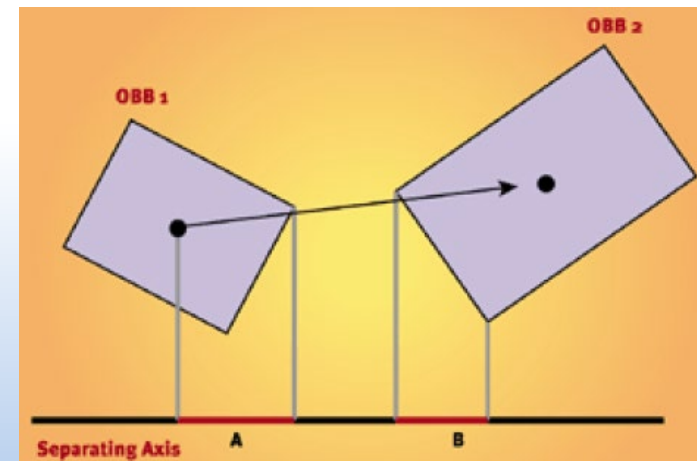
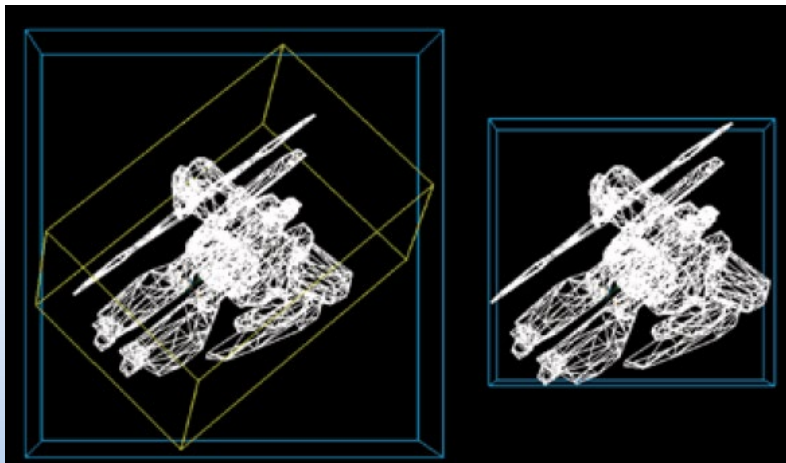
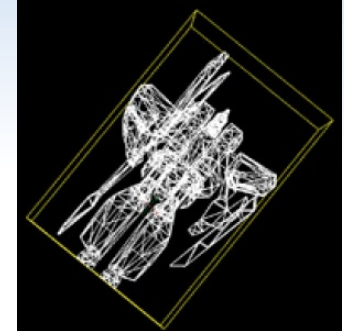
- Represents an AABB
- Some properties
  - `center`
  - `extents`: half sizes
  - `max`: `center + extents`
  - `min`: `center - extents`



# Bounding Volumes

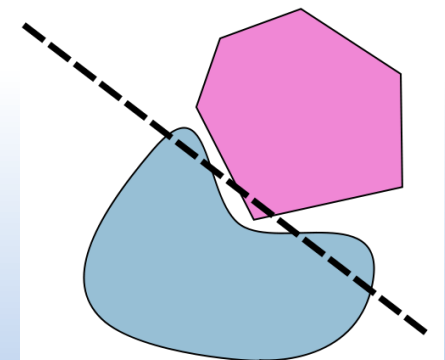
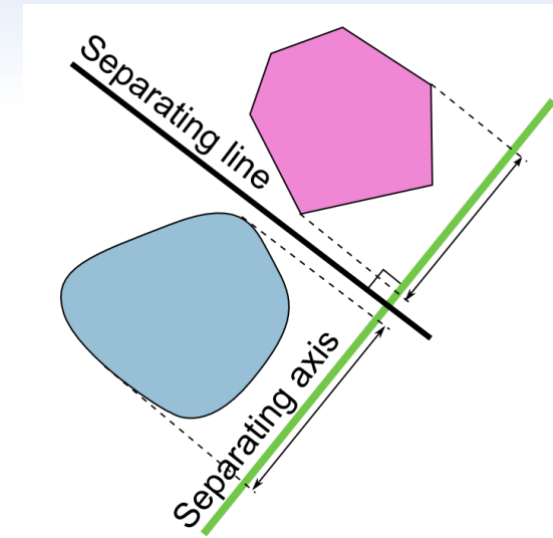
- OBB

- Aligned to the object's coordinates
  - Rotates with the object
- Less empty space, but more difficult to implement and slower
- Can convert OBB to AABB, but not tight fitting



# Bounding Volumes

- Separating axis theorem
  - Two **convex** shapes do not intersect
    - If an axis can be found along which the projection of the shapes do not overlap
    - If such an axis does not exist and shapes are convex then they intersect
  - Used in most collision detection systems
    - Only applies to convex shapes



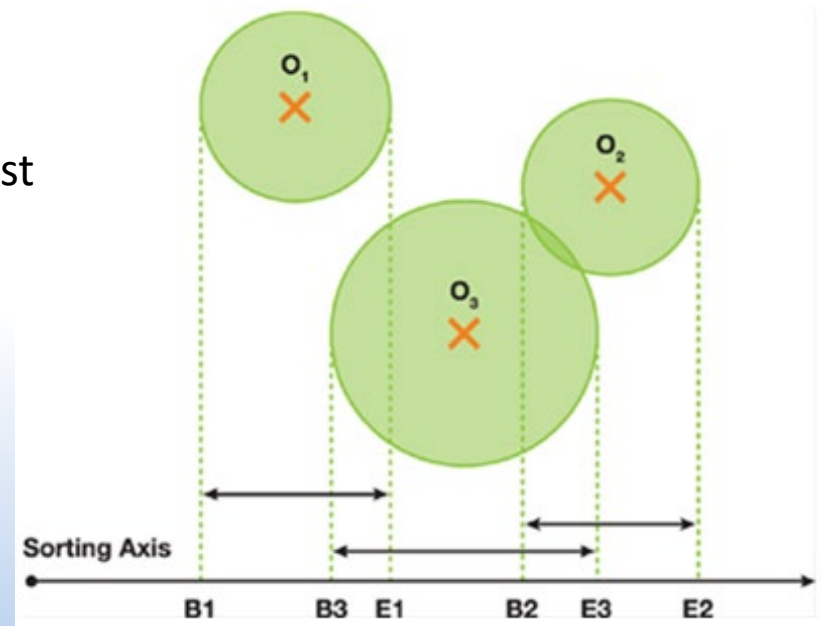
Not convex

# Bounding Volumes

- PhysX's sort and sweep algorithm

- Sphere example

- Each sphere is projected onto  $x$ ,  $y$ , or  $z$  axis
- Interval  $[b_i, e_i]$  for each projection of each object is added to a list
- The list is sorted
- If  $b_{i+1}$  is greater than  $e_i$ 
  - Object  $i$  is removed from the list

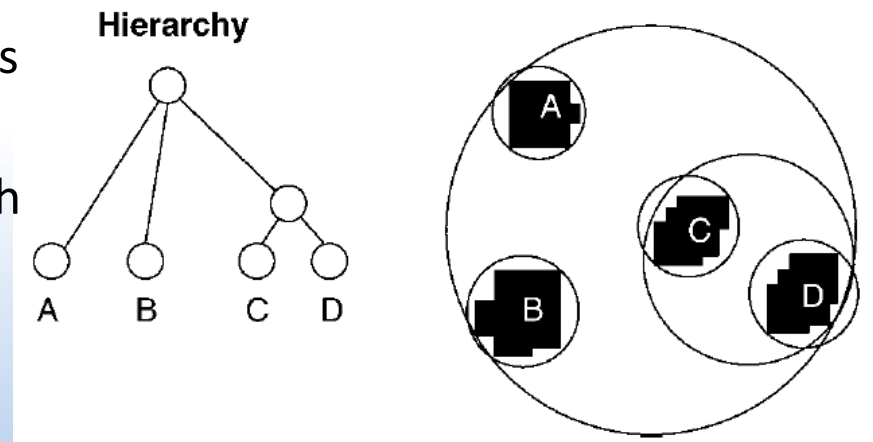




# Bounding Volume Hierarchies

- Bounding volumes alone
  - Still involves checking every pair of objects
- Bounding volume hierarchy (BVH)
  - Helps to avoid checking every object pair
  - Each object (in its bounding volume) is a leaf of a tree data structure
    - These connect to parent nodes
    - Each parent has its own bounding volume large enough to enclose all descendents

$$N_c = \frac{n!}{2(n-2)!}$$



# Bounding Volume Hierarchies

## ➤ Concept

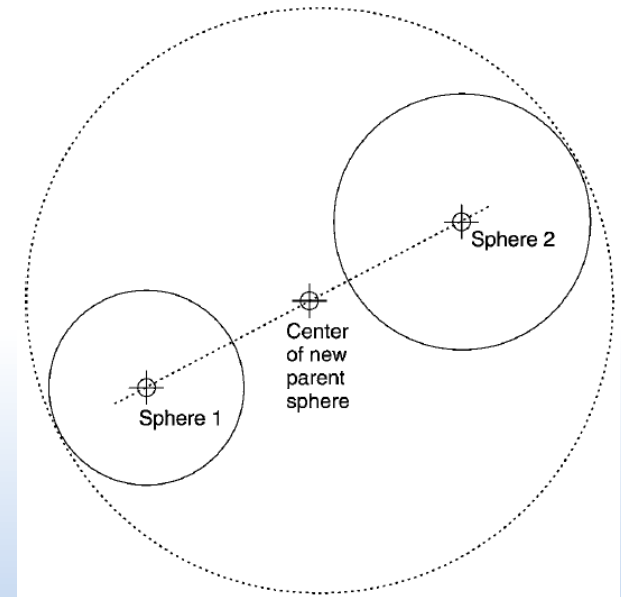
- If bounding volumes of two nodes in the tree do not touch
  - None of their descendants can possibly be in contact

## ➤ Different bounding volumes for each object and parent

- Gives best fit

## ➤ Simpler implementation

- Use spheres
- Large parent bounding volumes
  - But fast calculations



# Bounding Volume Hierarchies

- Building the hierarchy

- Static environments

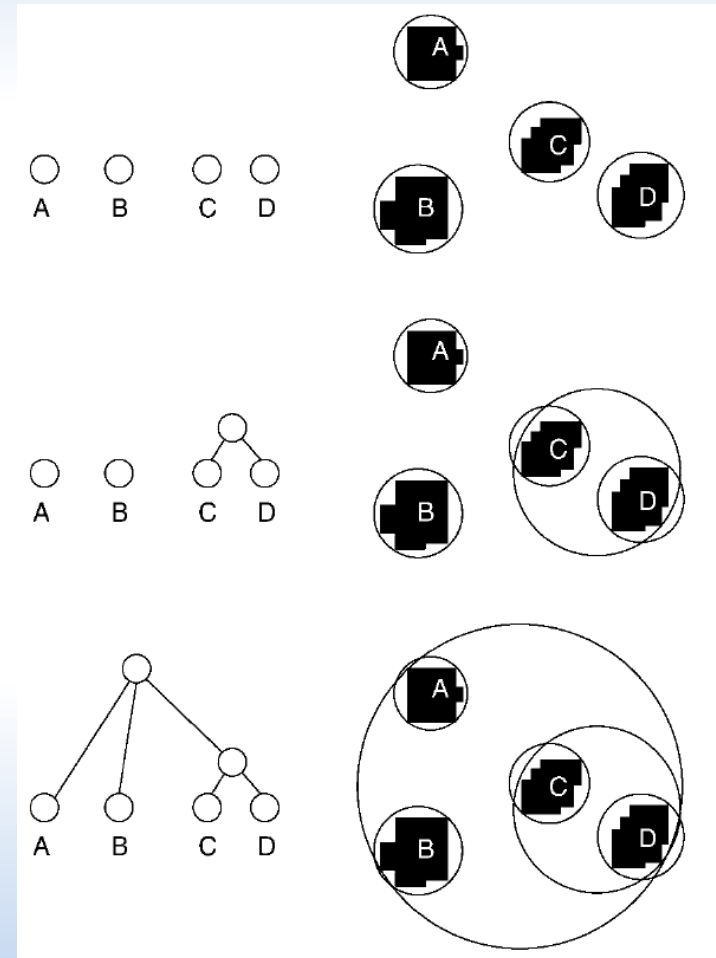
- Hierarchies can be constructed offline

- Dynamic environments

- Hierarchies need to be recalculated in game

- Bottom-up

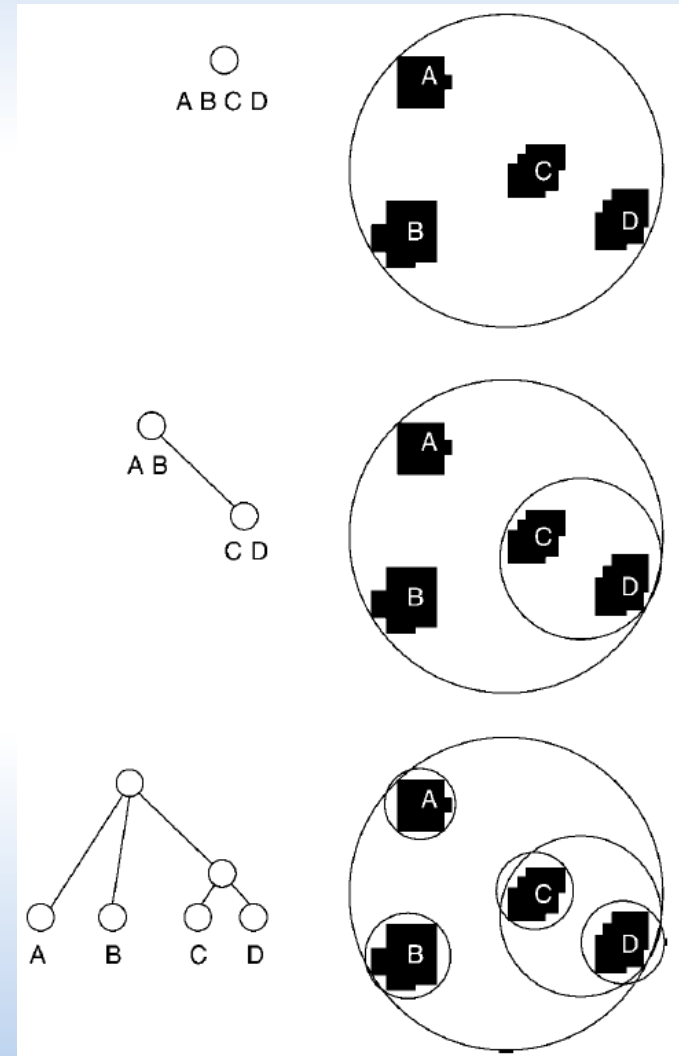
- Starts with bounding volumes of individual objects
    - Parents added
    - Continue until only one node left in the list



# Bounding Volume Hierarchies

## ➤ Top-down

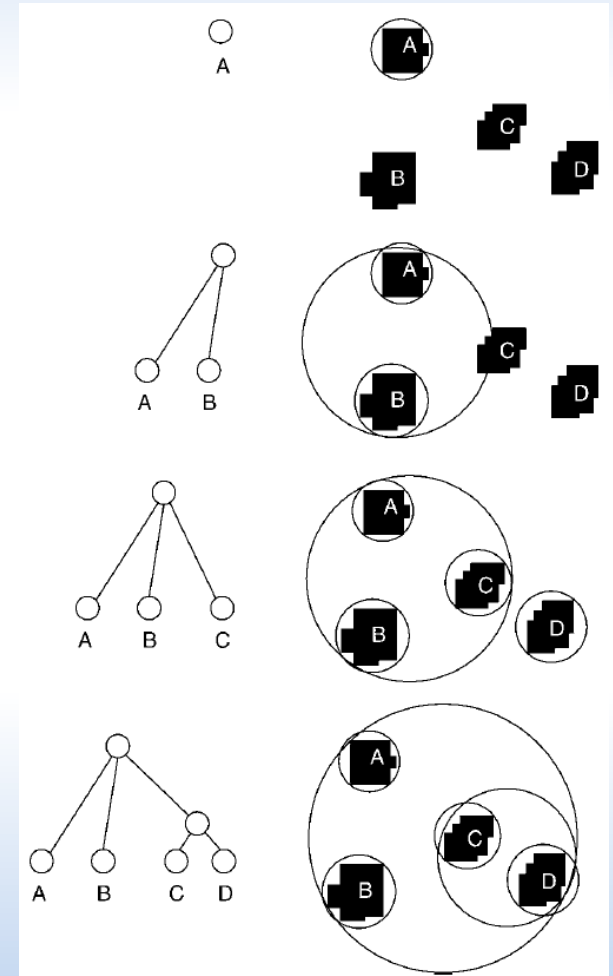
- Also starts with bounding volumes of individual objects
- Each iteration, objects in each group separated into two groups
- Continue until only one object in each group



# Bounding Volume Hierarchies

## ➤ Insertion

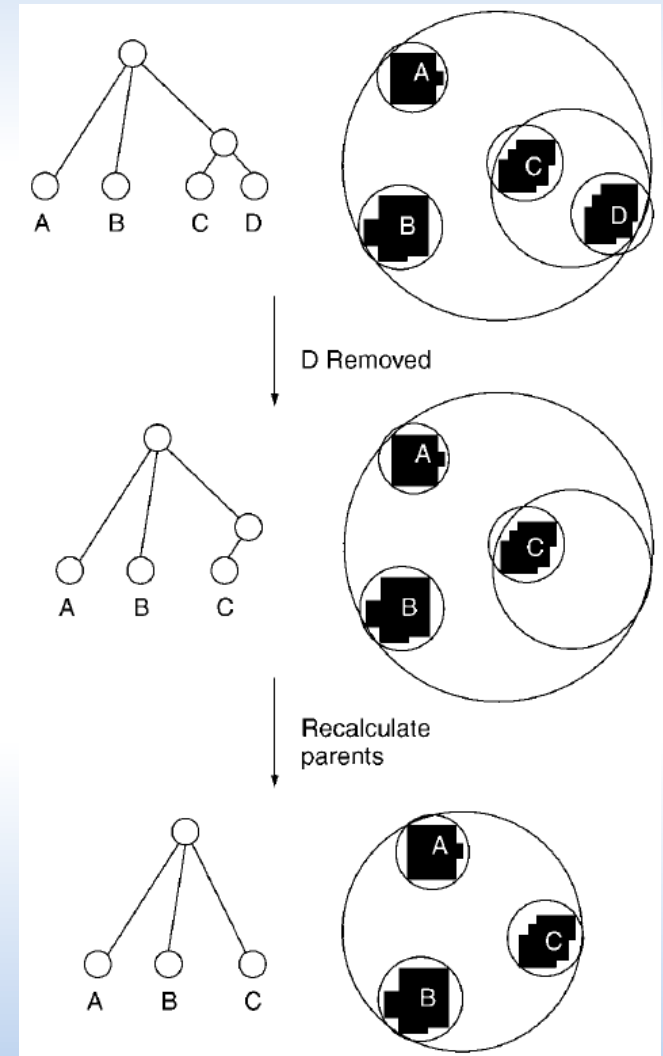
- Only approach suitable for use during the game
- Can adjust hierarchy without having to rebuild it completely
- Starts with existing tree (or empty tree)
- Objects added/inserted into the tree



# Bounding Volume Hierarchies

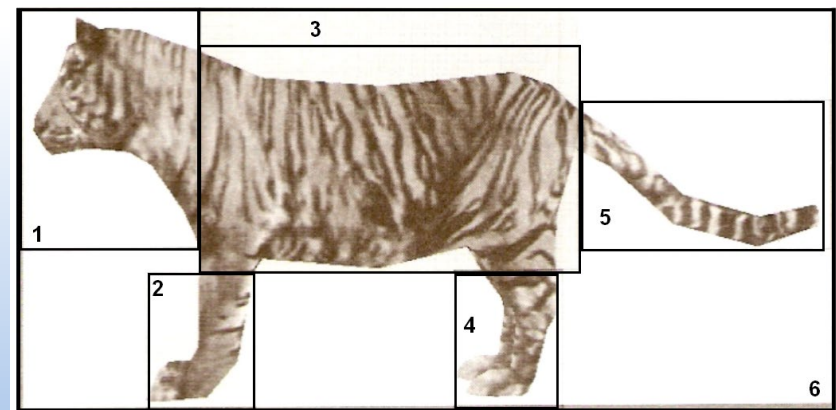
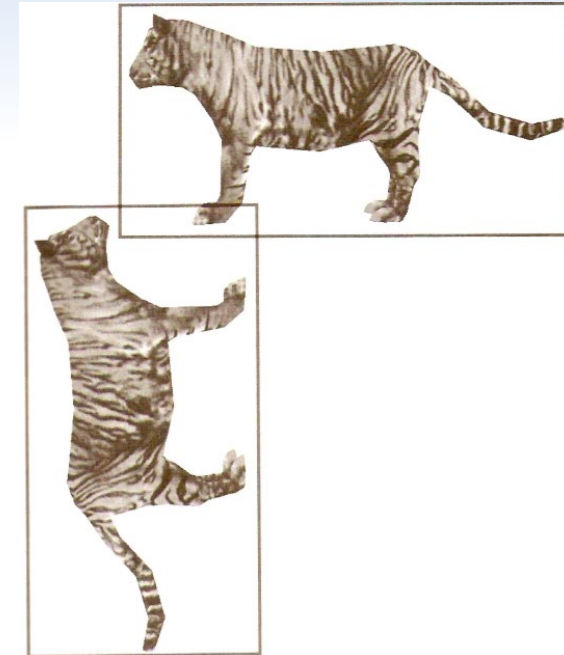
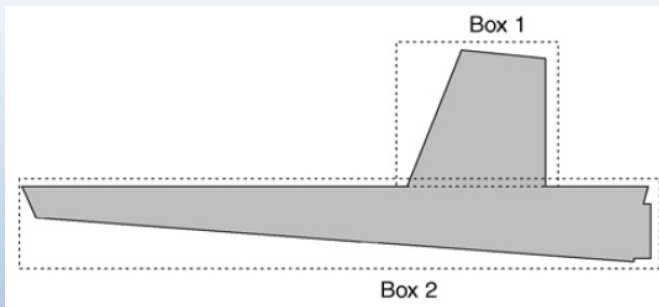
## ➤ Removing objects

- Cannot simply remove an object
- Potentially
  - Need to replace or remove parent nodes
  - Need to recalculate the bounding volumes further up the hierarchy



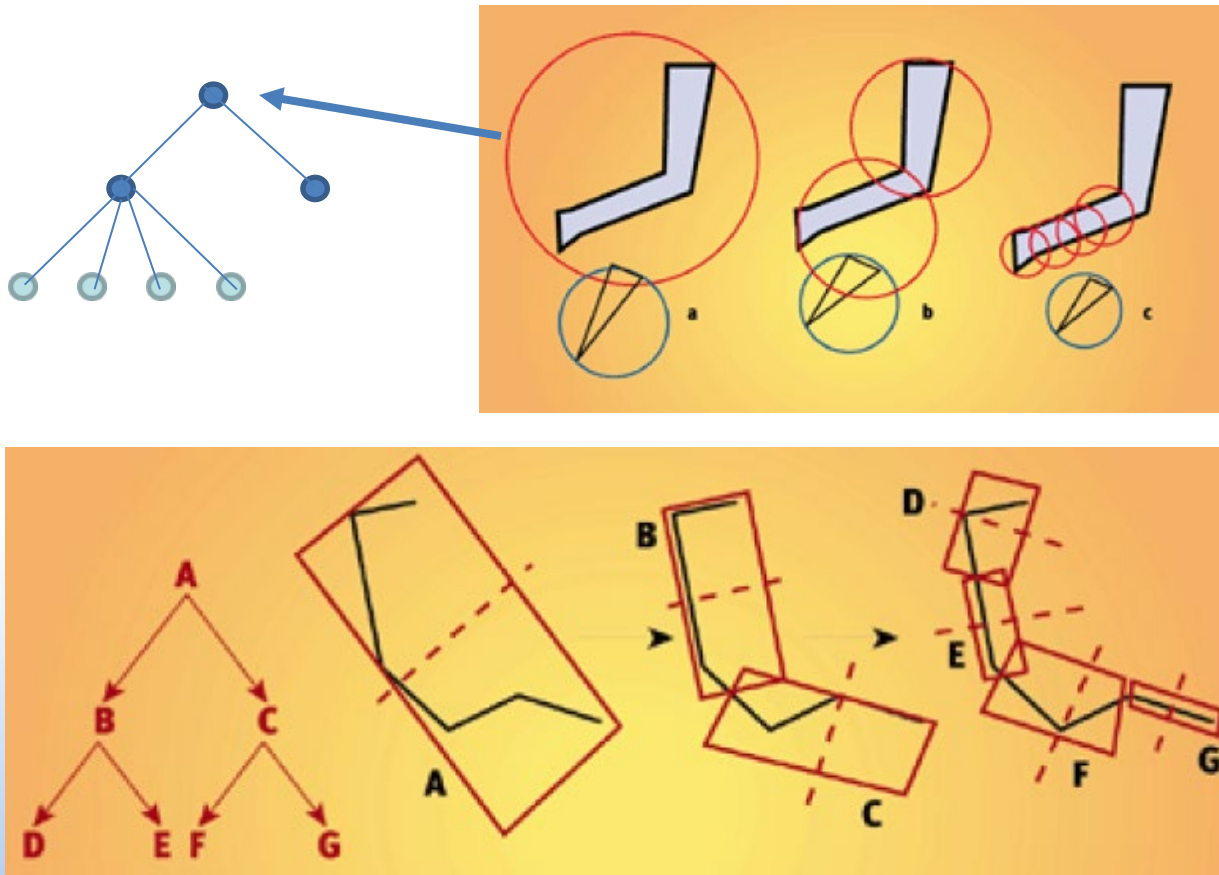
# Sub-object Hierarchies

- Sub-object hierarchies
  - Objects with awkward shapes
    - Difficult to fit within simple bounding volumes
    - Results in inaccurate collision detection
  - Solution
    - Use multiple bounding volumes arranged in a hierarchy for the object
      - Gives tighter fit



# Sub-object Hierarchies

- Sub-object hierarchies





# Spatial Data Structures

- Bounding volume hierarchy
  - Groups objects based on relative positions and sizes
  - If objects move, the hierarchy needs to be recalculated
- Spatial data structure
  - Locked to the world
  - Structure doesn't change with regard to objects
  - Common structures found in games
    - Binary Space Partitioning (BSP)
    - Octree or quadtree
    - Grids

# Spatial Data Structures

- BSP tree
  - First proposed in 1980!! But only gained popularity when 3D games started using it
    - Original purpose was to solve the visibility determination problem in computer graphics
  - Often seen in First-Person-Shooter (FPS) game engines
    - Doom was the first game that used this as part of the rendering pipeline for back-face culling, partial z-ordering, hidden surface removal
  - Also used to accelerate rendering and other things like shadow generation, collision detection

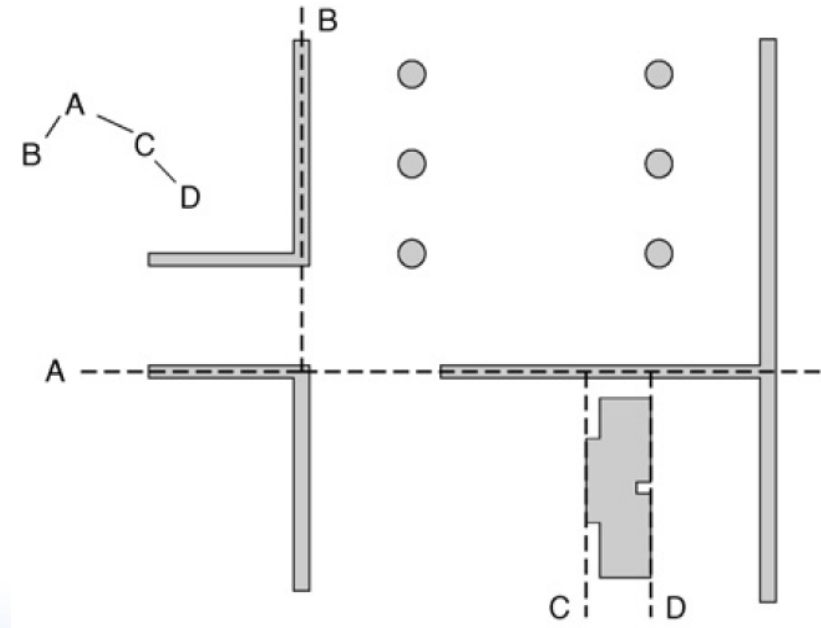
# Spatial Data Structures

## ➤ Binary tree

- Built by recursively subdividing objects or polygons in a scene using planes
- Unlike BVH, each node uses a plane to divide space
- Each parent only has a maximum of two children

## ➤ Two phases

- Building the BSP tree
  - Can be done offline
- Traversing the BSP tree
  - At run-time



# Spatial Data Structures

## ➤ Concept

- Properties of partitioning a scene using planes
  - Objects on one side of a plane can never collide with objects on the other side
  - Given a viewpoint in the scene space, objects on the same side as the viewer are nearer than any objects on the other side

## ➤ Works well for static objects in scenes

- Useful for indoor scenes in games
  - Boundaries are often static planes, e.g., walls, floor

## ➤ Many different variations to BSP trees

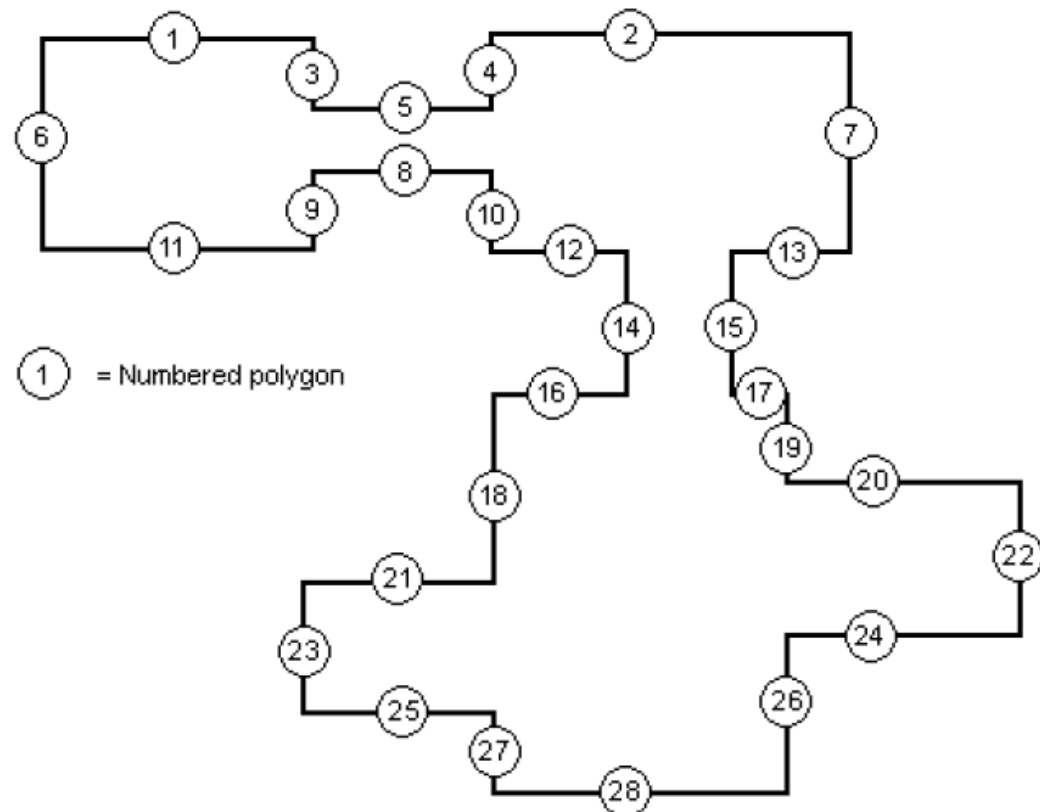
- Can even put BVHs at the leaves of BSP tree

# Spatial Data Structures

- Constructing the tree is no trivial task, among things to consider
  - How to choose partition planes
    - Best to get a balanced tree
  - If an object crosses a partitioning plane
    - Split object? (expensive)
    - Place in parent node
    - Place in closest child node
    - Place in both child nodes
  - When to stop partitioning space

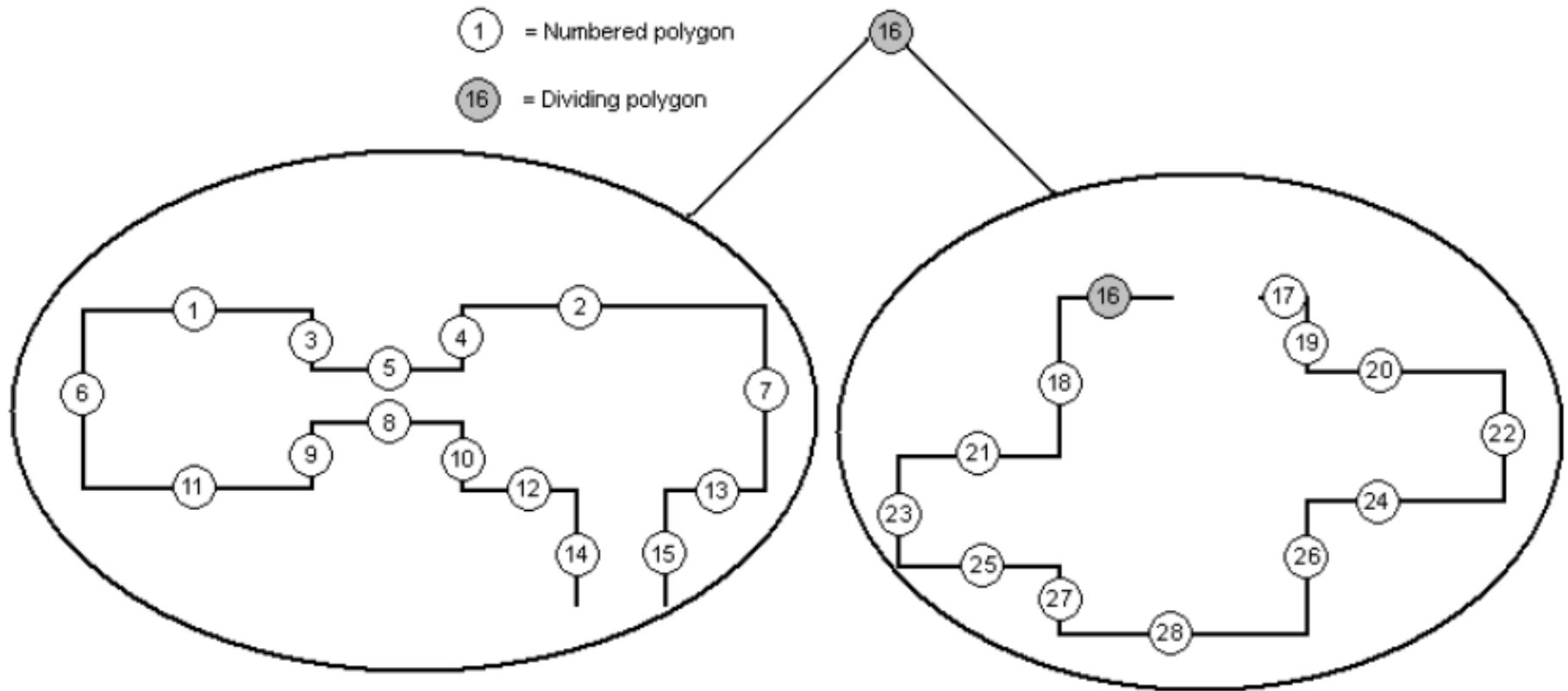
# Spatial Data Structures

- BSP tree example



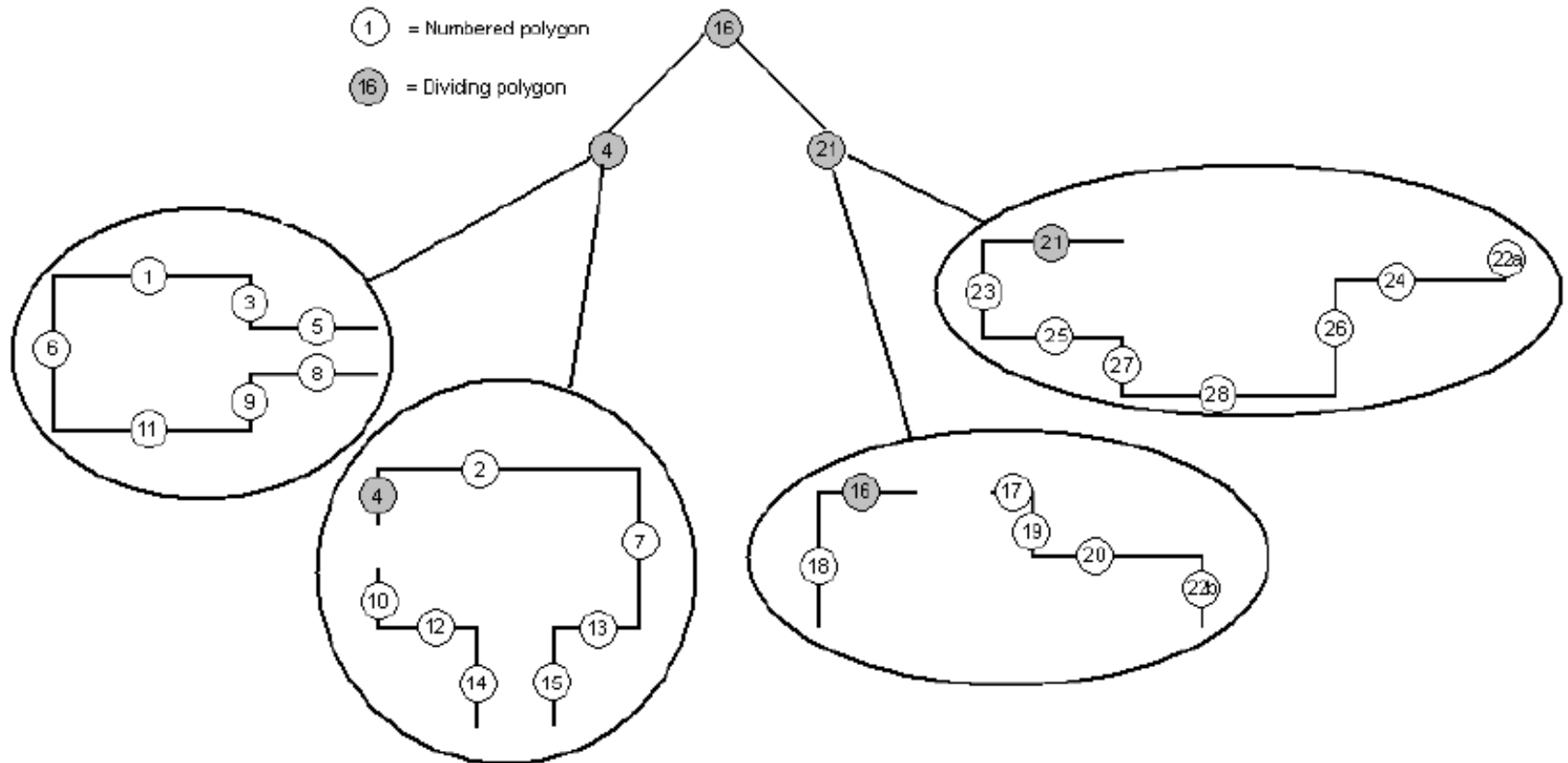
# Spatial Data Structures

- BSP tree example



# Spatial Data Structures

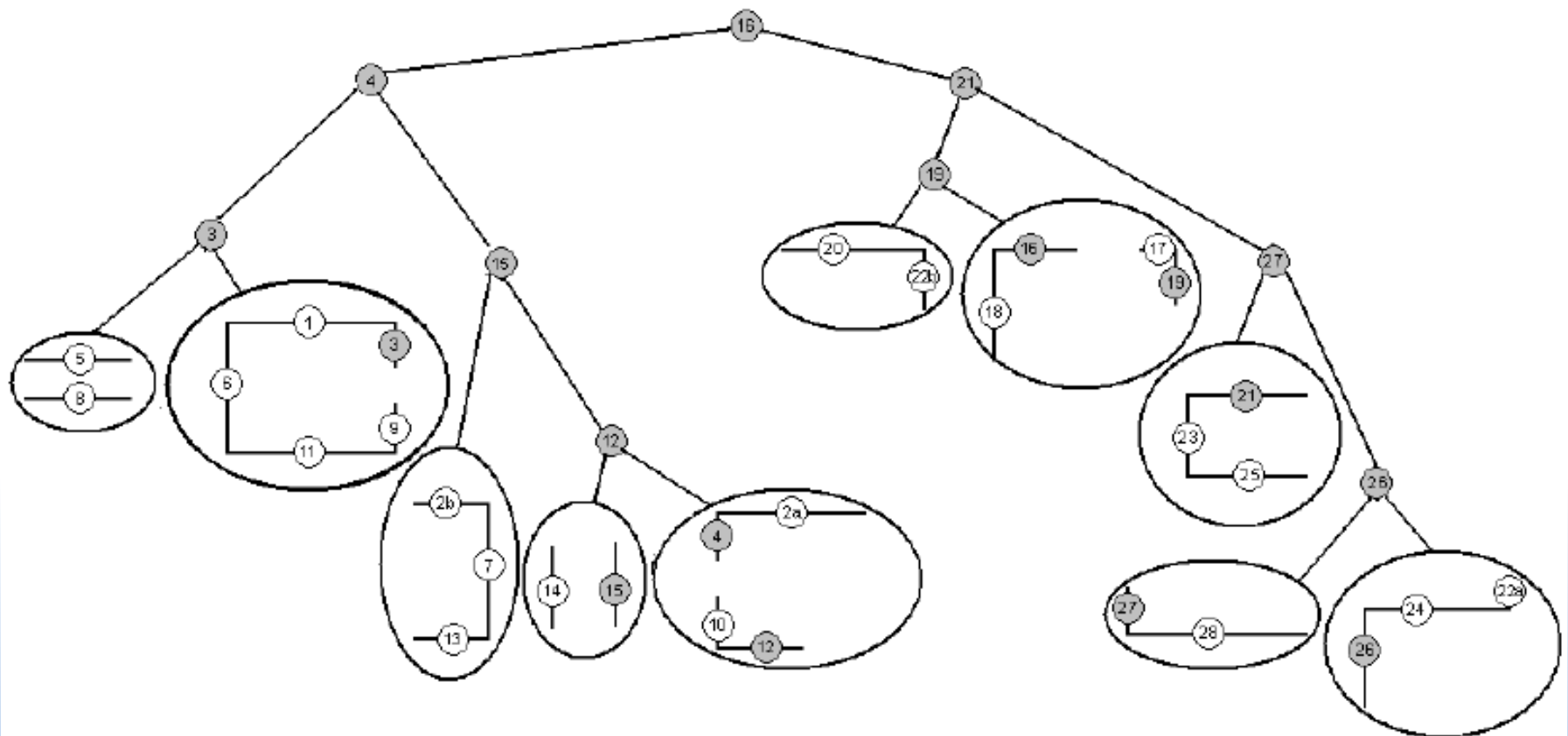
- BSP tree example





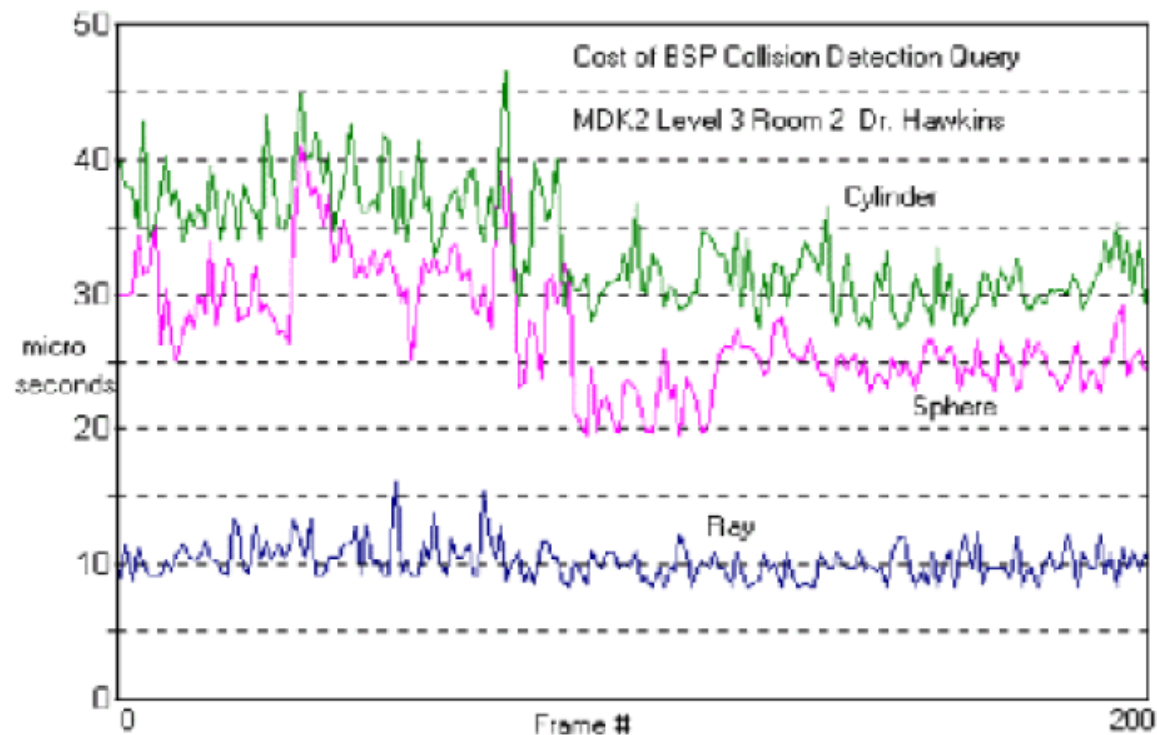
# Spatial Data Structures

- BSP tree example



# Spatial Data Structures

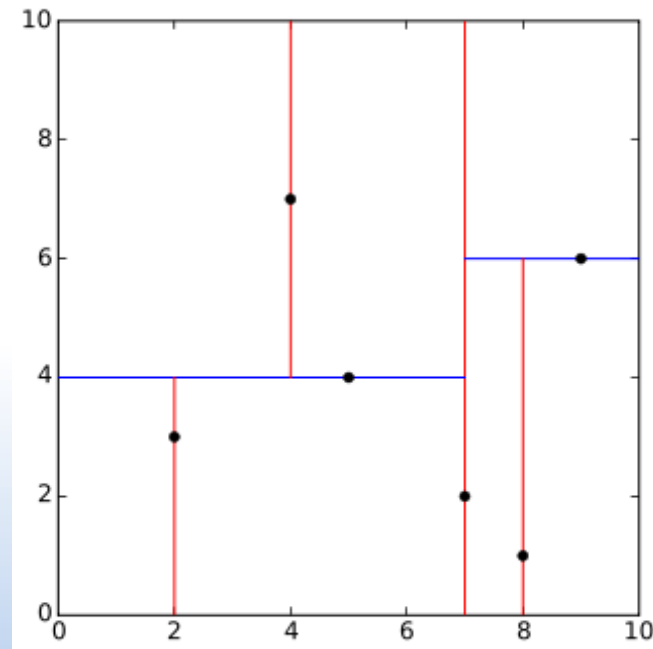
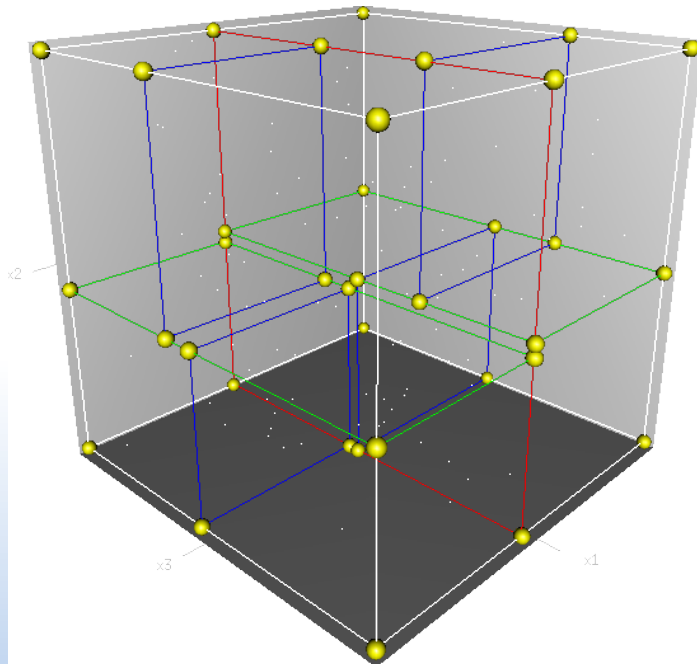
- BSP tree example



**Comparison of three methods of collision detection: regular BSP collision (labeled Ray), spherical offset, and cylindrical offset.**

# Spatial Data Structures

- $k$ -dimensional tree ( $kd$ -tree)
  - A special case of BSP tree
    - Partition planes perpendicular to one of the coordinate axes



# Spatial Data Structures

- Octrees and quadtrees

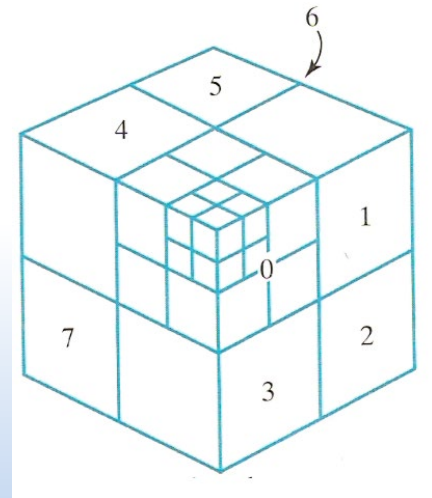
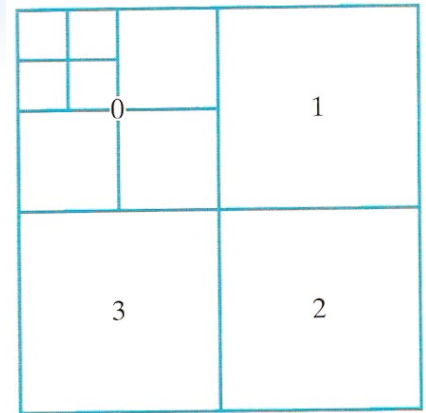
- Quadtree

- Splits space into four areas
  - Each node can have up to four children
- Can also be used in 3D games
  - Where most objects stuck to the ground
  - Takes up less memory than an octree

- Octree

- Splits space into eight areas
  - Each node can have up to eight children

- Do not have to store empty nodes



# Spatial Data Structures

## ➤ Subdivide space

- Until a termination criterion is reached
  - E.g., contains less than a predefined number of objects

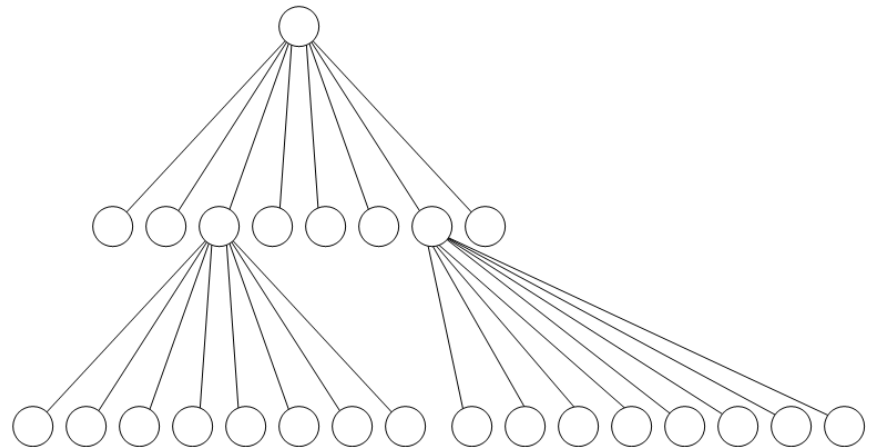
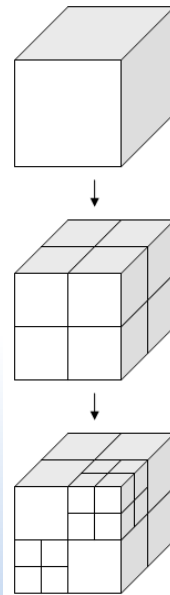
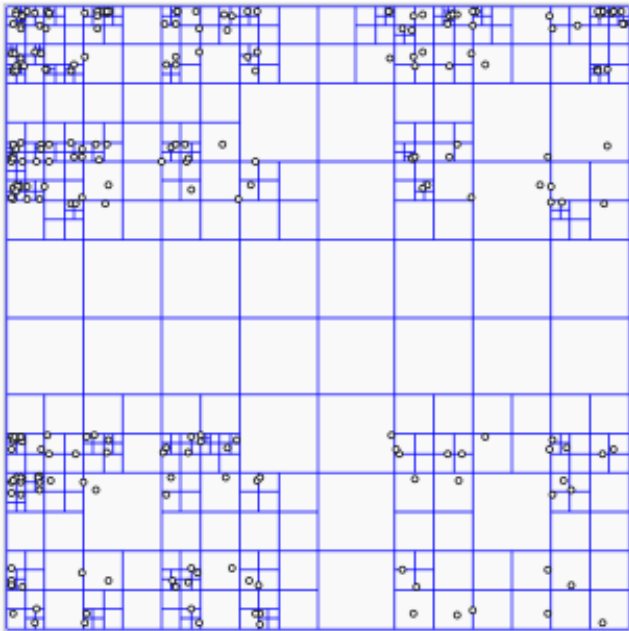
## ➤ Each level does not require space to be divided into boxes/cubes of the same sizes

- However, two advantages
  - Do not have to store the position of the nodes (can infer from the hierarchy level and node number)
    - » Saves memory
  - Do not need to perform calculations to find the best location to divide into nodes
    - » Faster to build

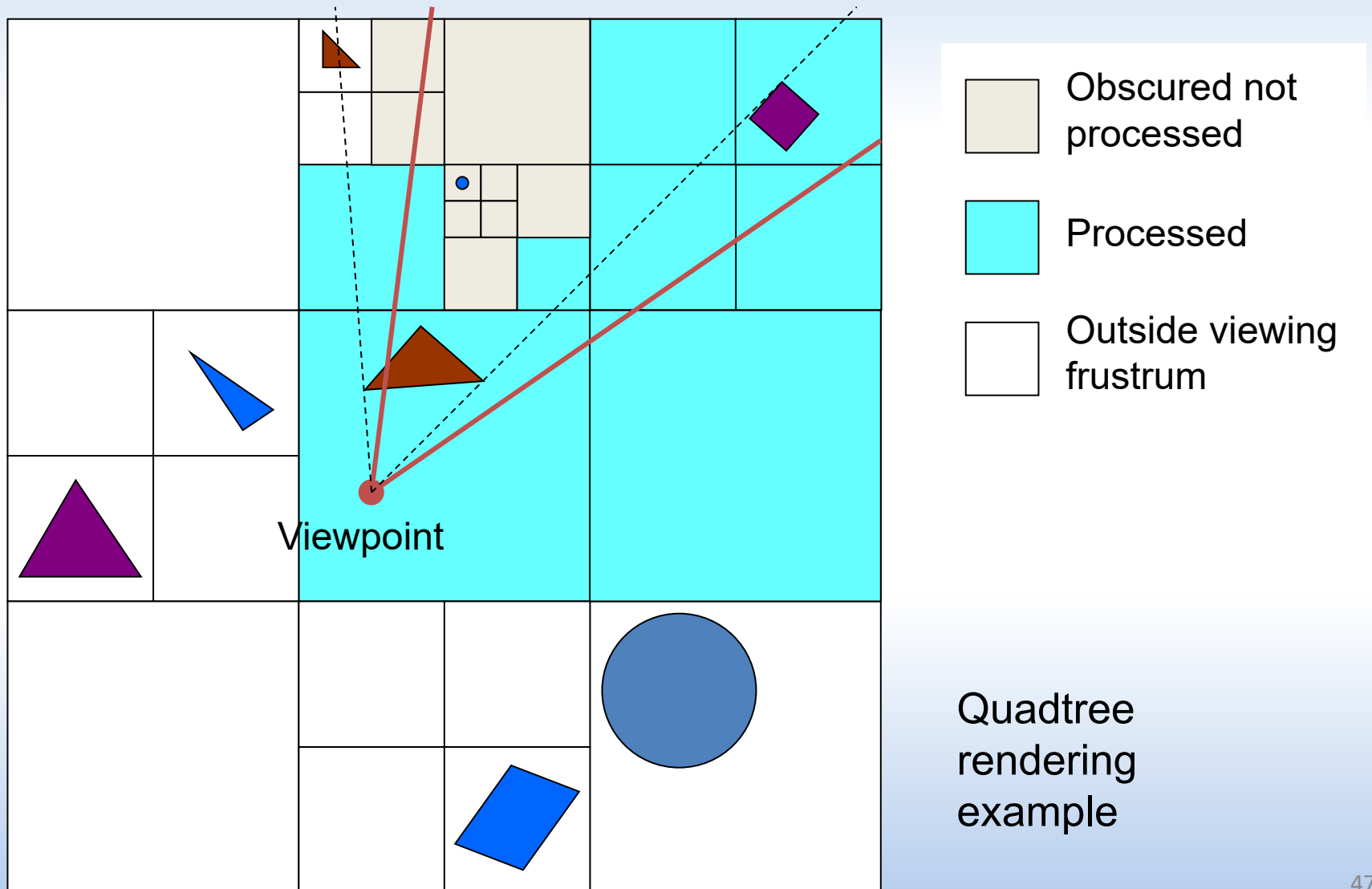
# Spatial Data Structures

## ➤ Particularly useful for

- Outdoor scenes in games where most objects are on the ground
- Less for indoor games
  - Cannot easily use to detect collisions with walls



# Spatial Data Structures



# Spatial Data Structures

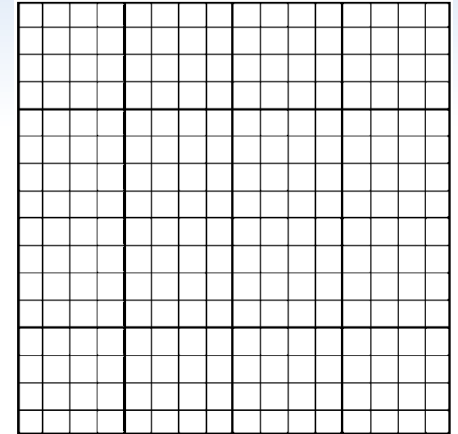
- Grids

- Unlike quadtree/octree

- Does not use a tree data structure
      - Just a regular grid array

- Advantages over tree-based approaches

- An object's location in the grid
      - Can be determined directly from the object's position
      - Once found just check for collision with other objects in that cell
      - Faster as do not have to traverse a tree structure
    - Can be defined and built without requiring any information about objects in the environment





# Spatial Data Structures

- Tradeoff in selecting cell size
  - Large cells, may need to check lots of objects
  - Small cells, may have to keep multiple records of objects

## ➤ Disadvantages

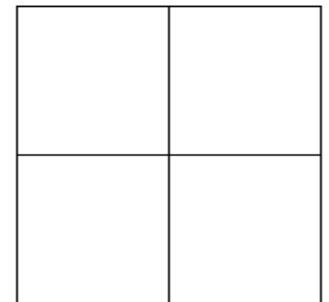
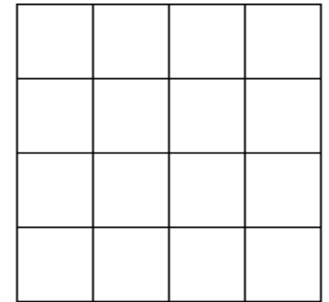
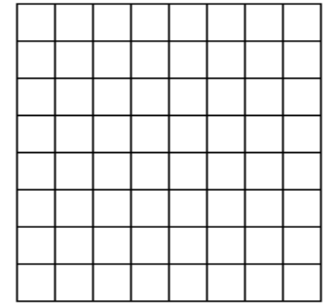
- Each cell can contain any number of objects
  - Quadtrees/Octrees typically have a maximum number of objects per node
- Cells exist even if space is empty
  - Sparse environments can have lots of empty space
  - Wastes memory
- Still have to check empty cells
  - Check whether they contain objects
  - Wasted effort

# Spatial Data Structures

- Large objects span multiple cells
  - Tree structure: large objects can be placed higher in the tree (i.e. in parent nodes)
  - Grids: each cell must store the object, wastes memory
  - To remove a large object, must remove from all cells

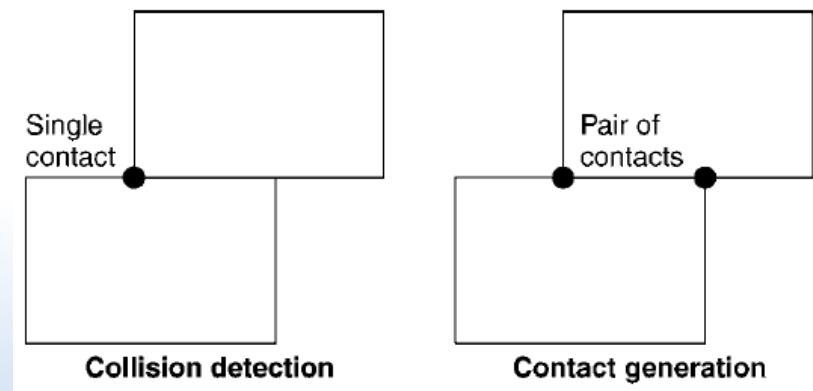
## ➤ Multi-resolution grids

- A set of grids with increasing cell sizes
  - Usually four times the size of previous level, so grids align
- Objects added into one of the grids only
  - Based on the size of the object
    - » i.e. smallest cells that can contain object



# Fine Collision Detection

- Fine collision detection
  - Coarse collision detection produces a list of object pairs that may have collided
    - Need to check whether there are contacts to generate
  - More complex than single-intersection collision detection
    - Collision may have multiple contact points
    - Single point may not be enough to generate realistic response
    - Takes more processor time to complete



# Fine Collision Detection

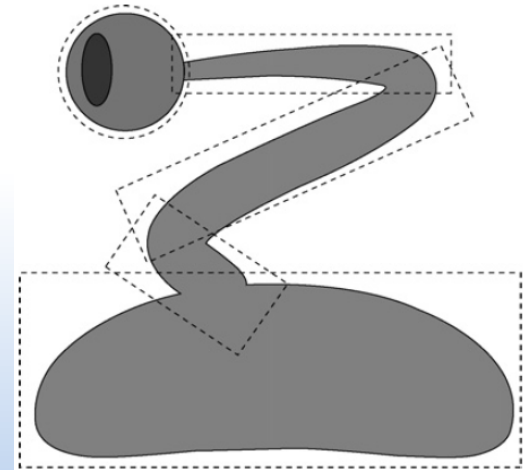
- Contact generation

- Work out the set of contact points

- Not just whether objects are touching or overlapping
    - Need to find contact data before can determine collision response
    - Needs to be fast
      - Improve speed by performing against simplified geometry rather than rendering geometry

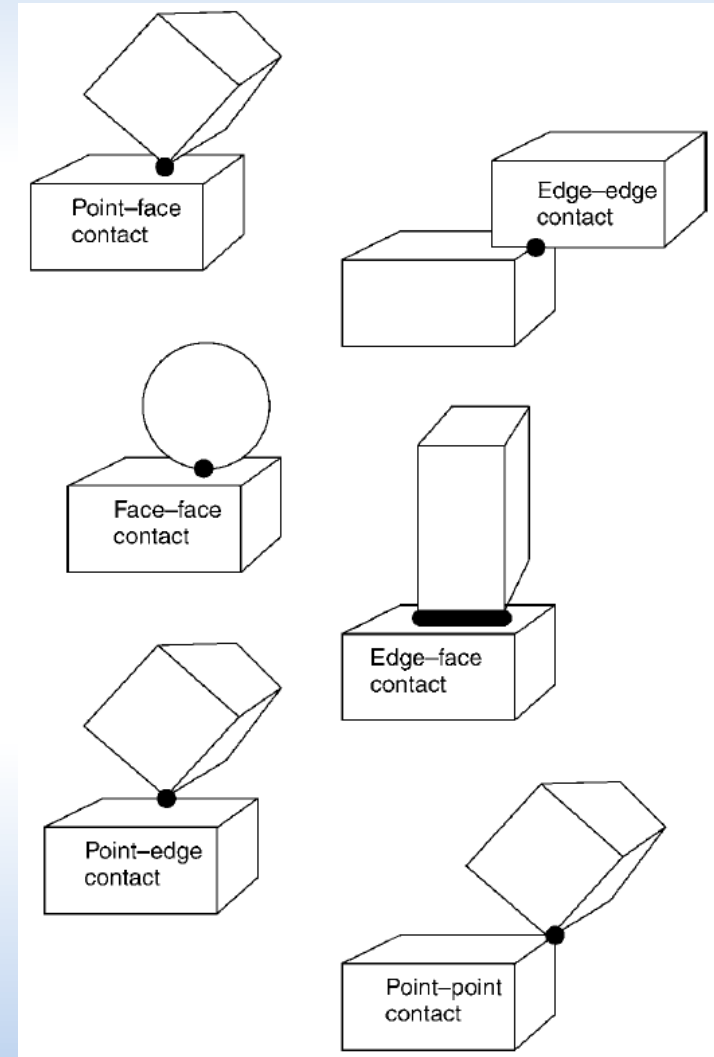
- Compound bodies

- Assemblies of primitive objects
    - Each primitive typically has a transformation matrix to offset it from the object's origin
    - To collide two assemblies, find collisions between all pairs of primitives for each object



# Fine Collision Detection

- Contact generation
  - A limited set of contact situations used to approximate contacts
    - Accuracy is sufficient for video games
    - Face-face collision is only used when one object has a curved surface
      - Otherwise use edge-face
    - Edge-face can be approximated by a pair of contact points
    - Point-point contacts are so rare that are ignored by some physics engines



# Fine Collision Detection

- Contact data

- Collision point

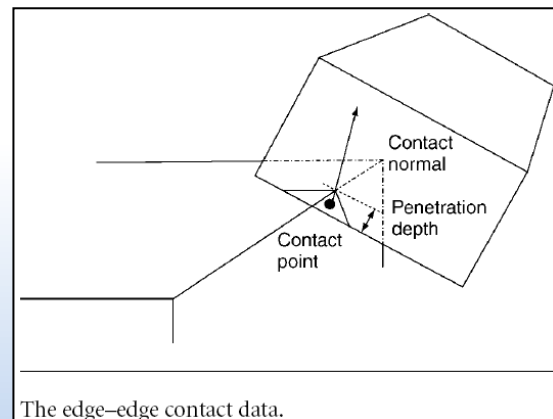
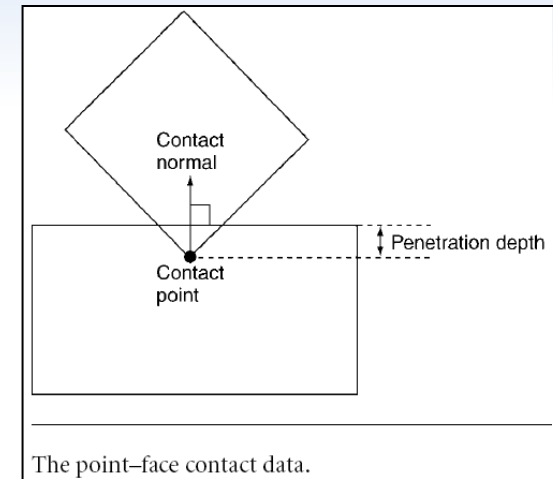
- Point of contact between two objects
    - Objects will be interpenetrating somewhat, may be a number of possible points

- Collision normal

- Direction in which impact impulse will be felt between two objects

- Penetration depth

- The amount that two objects are interpenetrating
    - Measured along the direction of the collision normal passing through the collision point



# Fine Collision Detection

- Unity

- Collision

- Describes a collision and passed to the following event methods:
      - `OnCollisionEnter()`
      - `OnCollisionStay()`
      - `OnCollisionExit()`
    - Some properties
      - `contactCount`: number of contacts for this collision
      - `relativeVelocity`: the relative linear velocity of the two colliding objects
      - `gameObject`: the `GameObject` whose collider you are colliding with
    - Public method
      - `GetContacts()`: retrieves all contact points for this collision

# Fine Collision Detection

- Unity

- `ContactPoint`

- Describes a contact point where the collision occurs
    - Properties
      - `impulse`: impulse applied for collision resolution
      - `normal`: normal of the contact point
      - `point`: point of contact
      - `separation`: distance between colliders at the point of contact
      - `thisCollider` : the first collider in contact at the point
      - `otherCollider` : the other collider

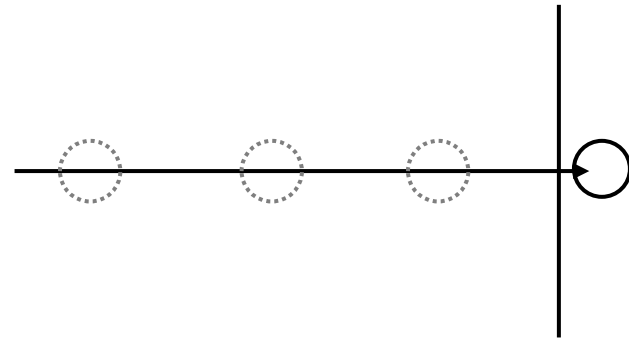
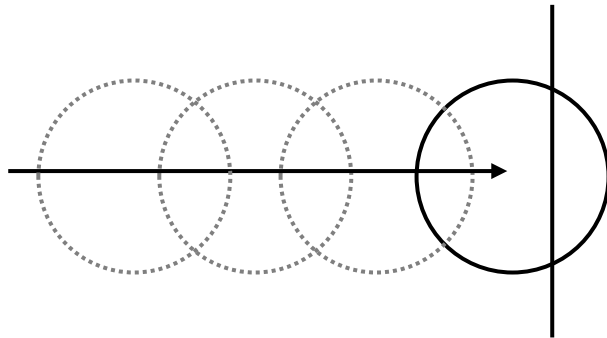


# Collision Detection

- Discrete collision detection

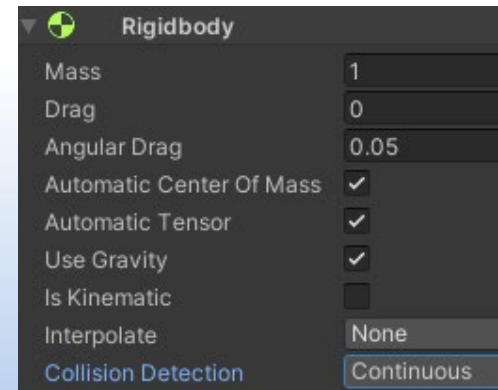
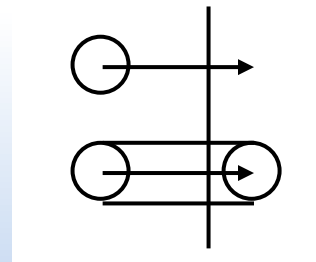
- 'Tunneling' problem

- Potential problem for small objects moving at high speeds



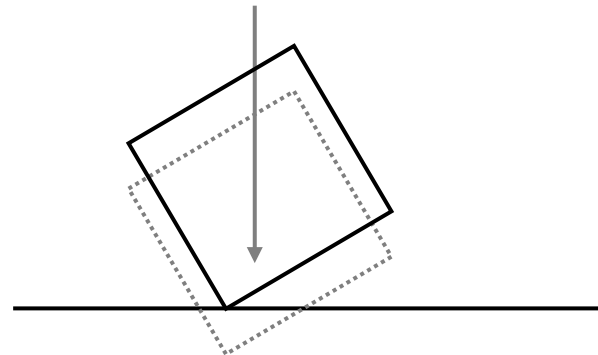
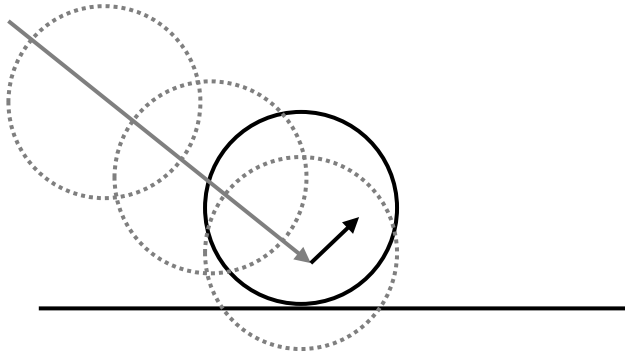
- Solution

- Ray casting
    - Sweep shapes
    - Continuous collision detection
      - Predict time of impact along current path

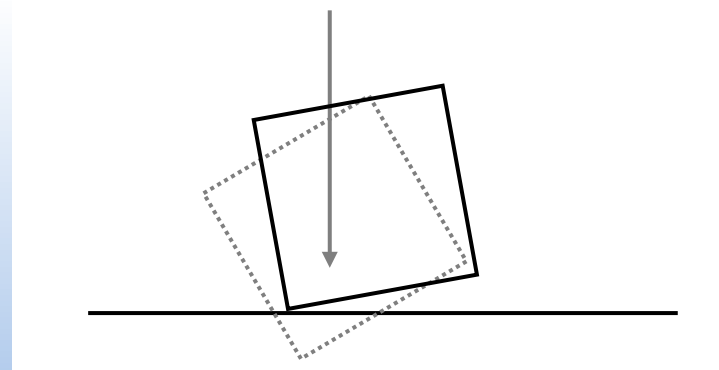
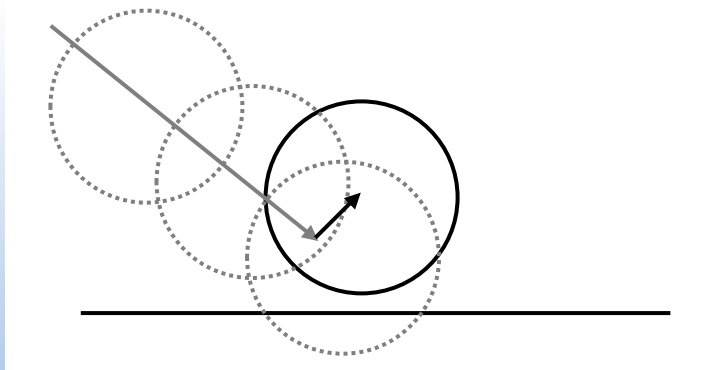


# Collision Detection

- Resolving penetration
  - Simple but inaccurate approximation



- More accurate method



# Collision Queries

- Ray cast

- Cast a directed line segment

- From a starting point to an endpoint
      - Some game engines do not support infinite rays
    - Line segment tested against collidable objects
      - Returns contact point(s)
      - Typically want the closest intersection point
      - Spatial data structures speed up collision tests

- Example applications

- Weapons, direct line of sight, movement queries, distance to ground

# Collision Queries

- Unity

- `Physics.Raycast`

- For example

```
bool Raycast(Vector3 origin, Vector3 direction,  
    out RaycastHit hitInfo,  
    float maxDistance, // these have default values  
    int layerMask,  
    QueryTriggerInteraction queryTriggerInteraction);
```

- Has a number of variants
      - Returns true if the ray intersects with a Collider
      - Casts a ray against all colliders in the Scene and returns detailed information on what was hit

# Collision Queries

- Unity

- `RaycastHit`

- Structure used to get information back from a raycast
    - Some properties
      - `point`: impact point in world space where the ray hit a Collider
      - `distance`: Distance from ray's origin to impact point
      - `normal`: normal of the surface that was hit
      - `collider`: Collider that was hit
      - `rigidbody`: Rigidbody of the Collider that was hit
      - `transform`: Transform of the Collider/Rigidbody that was hit

# Collision Queries

- Shape cast
  - Casting a shape along a directed line segment
    - Shape usually a sphere
  - Example applications
    - Sliding a character forward on uneven terrain
    - Determining whether an object can move between obstacles
    - Virtual camera collision
- Volume queries
  - Determine which collidable objects lie within some specific (invisible) volume
    - Like a zero distance shape cast, but unlike casts can be persistent and takes advantage of temporal coherence

# Collision Queries

- Unity

- `Physics.SphereCast`

- For example

```
bool SphereCast(Vector3 origin, float radius,  
    Vector3 direction, out RaycastHit hitInfo,  
    float maxDistance, // these have default values  
    int layerMask,  
    QueryTriggerInteraction queryTriggerInteraction);
```

- Returns true if the sphere sweep intersects any Collider
      - Casts a sphere along a ray and returns detailed information on what was hit
      - Useful when a Raycast does not give enough precision

# Collision Queries

- Unity

- `Physics.OverlapSphere`

- Returns an array with all Colliders touching or inside the sphere

```
Collider[] OverlapSphere(Vector3 position, float radius,  
    int layerMask, // these have default values  
    QueryTriggerInteraction queryTriggerInteraction);
```



# Collision Detection

- Unity

- Interaction between Colliders

- Static Collider

- A GameObject that has a Collider but not a Rigidbody component
      - Does not move when a Rigidbody collides with it

- Rigidbody Collider

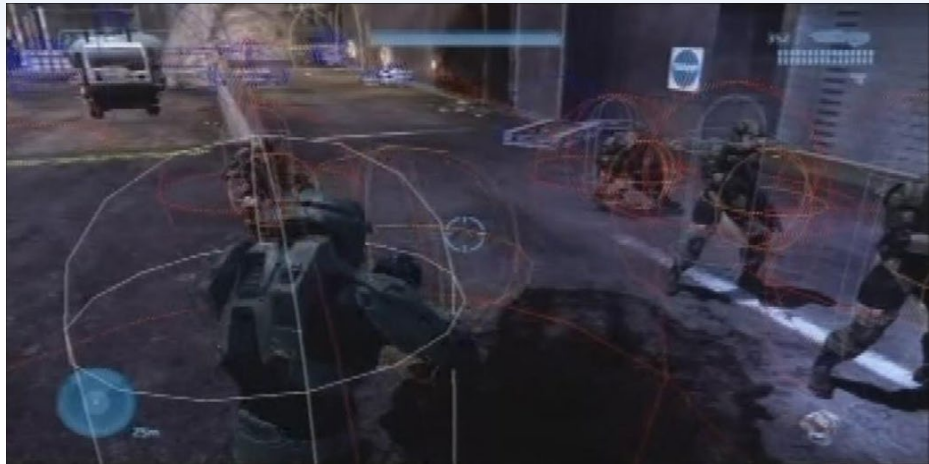
- Fully simulated by the physics engine and can react to collisions and forces

- Kinematic Rigidbody Collider

- Rigidbody with isKinematic property enabled
      - Reacts to Rigidbody Colliders but not affected by forces and collisions
      - Does not react to other kinematic Colliders and static Colliders

- Bounciness and surface friction set using physics material

# Collision Detection



# References

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