

Question 1A

Problem Definition/Specification

A program is needed that will raise a specified number to a specified power. For this implementation of the program, iteration must be used to accomplish this task. See Exercise 5.16 for details.

Problem Analysis

The program is to raise a given number to a given power, and this must be accomplished using loops rather than recursive functions. The number of appropriate iterations of a loop to get the desired output must be determined based on the input exponent value.

Program Inputs

- A base integer
- An exponent integer

Program Outputs

- The result of the base number raised to the input exponent

Formula or Relations

Raising a base number to a power is the same as multiplying the base number by itself the amount of times of its power number.

Algorithm Design

Initial Algorithm

1. Read in the base number from the user
2. Read in the exponent number from the user
3. If the exponent less than or equal to zero display an error message. Otherwise continue
4. Create an integer to keep track of the result and set it equal to base number
5. Loop an amount of times determined by exponent and multiply the result by the base number on each iteration of the loop.
6. Display the result number

Refinement

1. Read in the base as an integer using the scanf command
2. Read in the exponent as an integer using the scanf command
3. Use an if statement to determine whether the exponent is less than or equal to zero and if necessary, display error message: `Invalid input: Exponent must be a positive nonzero integer`

4. Initialize a new integer at the top of the method called “result” and set it equal to the input base number
5. Using a while loop, continue to iterate while exponent > 1. In each iteration, multiply the result by the base integer, and decrement the exponent integer
6. Print out the result number using a printf line

Desk Checking/Test Plan

This program will first be tested using a positive nonzero integer for both the base and the exponent, and they should not cause any errors to occur. A second test will be performed using a number less than or equal to zero for the exponent, which should display an error message if the program is working correctly. A third test will be performed with a number less than or equal to zero for the base, which should NOT cause an error in the program.

Implementation

```

1  /*
2  * Programmer: Kollin Labowski
3  * Date Completed: September 27, 2020
4  * Course: CS 350
5  * Description: This program includes a function integerPower(int a, int b) and the main method to test this function. The program prompts the
6  * user for two inputs, a base number and an exponent to raise the base number to. This program accomplished the task using loops instead of
7  * using recursion.
8  */
9
10 # include <stdio.h>
11
12 //Function prototype
13 int integerPower(int a, int b);
14
15 //Main method
16 void main()
17 {
18     int x, y;
19
20     printf("What is your base number?\n");
21     scanf("%d", &x);
22
23     printf("What is your exponent?\n");
24     scanf("%d", &y);
25
26     int answer = integerPower(x, y);
27
28     printf("The result of %d^%d is %d", x, y, answer);
29 }
30
31 /*
32 * This method accepts 2 parameters, a base number and an exponent, and raises the base number to the exponent using a while loop. It returns a
33 * value of type integer, and returns a -1 when there is an invalid input
34 */
35 int integerPower(int base, int exponent)
36 {
37     if(exponent <= 0)
38     {
39         printf("Invalid input: Exponent must be a positive nonzero integer");
40         return -1;
41     }
42
43     int counter = exponent;
44     int result = base;
45     while(counter > 1)
46     {
47         result = result * base;
48         counter--;
49     }
50
51     return result;
52 }
```

Testing

Test 1:

```
What is your base number?  
8  
What is your exponent?  
4  
The result of 8^4 is 4096
```

Test 2:

```
What is your base number?  
6  
What is your exponent?  
-3  
Invalid input: Exponent must be a positive nonzero integer
```

Test 3:

```
What is your base number?  
-3  
What is your exponent?  
5  
The result of -3^5 is -243
```

The tests showed that the program behaved as was expected

Question 1B

Problem Definition/Specification

A program is needed that will raise a specified number to a specified power. For this implementation of the program, recursion must be used to accomplish this task. See Exercise 5.34 for details.

Problem Analysis

The program is to raise a given number to a given power, and this must be accomplished using a recursive function. The appropriate base case for the recursive function must be determined so that the correct output is produced.

Program Inputs

- A base integer
- An exponent integer

Program Outputs

- The result of the base number raised to the input exponent

Formula or Relations

Raising a base number to a power is the same as multiplying the base number by itself the amount of times of its power number.

Algorithm Design

Initial Algorithm

1. Read in the base number from the user
2. Read in the exponent number from the user
3. If the exponent less than or equal to zero display an error message. Otherwise continue
4. In the function, create base case to determine when to stop recursion
5. Return the recursive result
6. Display the result number

Refinement

1. Read in the base as an integer using the `scanf` command
2. Read in the exponent as an integer using the `scanf` command
3. Use an if statement to determine whether the exponent is less than or equal to zero and if necessary, display error message: `Invalid input: Exponent must be a positive nonzero integer`

4. Create an if statement to act as a base case, ending the recursion when the exponent is ≤ 0
5. Return the base number * a recursive call to the function, so that each time the function is called the base is multiplied again. Decrement exponent in the method so that the base case is eventually reached
6. Print out the result number using a printf line

Desk Checking/Test Plan

This program will first be tested using a positive nonzero integer for both the base and the exponent, and they should not cause any errors to occur. A second test will be performed using a number less than or equal to zero for the exponent, which should display an error message if the program is working correctly. A third test will be performed with a number less than or equal to zero for the base, which should NOT cause an error in the program.

Implementation

```

1  /*
2   * Programmer: Kollin Labowski
3   * Date Completed: September 27, 2020
4   * Course: CS 350
5   * Description: This program includes a function integerPower(int a, int b) and the main method to test this function. The program prompts the
6   * user for two inputs, a base number and an exponent to raise the base number to. This program accomplished the task using a recursive function.
7   */
8
9 #include <stdio.h>
10
11 //Function prototype
12 int integerPower(int a, int b);
13
14 //Main method
15 void main()
16 {
17     int x, y;
18
19     printf("What is your base number?\n");
20     scanf("%d", &x);
21
22     printf("What is your exponent?\n");
23     scanf("%d", &y);
24
25     int answer = -1;
26     if(y <= 0)
27         printf("Invalid input: Exponent must be a positive nonzero integer");
28     else
29         answer = integerPower(x, y);
30
31     if(answer != -1)
32         printf("The result of %d^%d is %d", x, y, answer);
33 }
34
35 /*
36 * This method accepts 2 parameters, a base number and an exponent, and raises the base number to the exponent using recursion. It returns a
37 * value of type integer.
38 */
39 int integerPower(int base, int exponent)
40 {
41     if(exponent <= 0)
42         return 1;
43
44     return base * integerPower(base, exponent - 1);
45 }
```

Testing

Test 1:

```
What is your base number?  
6  
What is your exponent?  
4  
The result of 6^4 is 1296
```

Test 2:

```
What is your base number?  
4  
What is your exponent?  
0  
Invalid input: Exponent must be a positive nonzero integer
```

Test 3:

```
What is your base number?  
-7  
What is your exponent?  
3  
The result of -7^3 is -343
```

The tests showed that the program behaved as was expected

Question 2A1

Answer to Questions on Assignment (Question 2)

Q: How many of these 10,000 numbers do you really have to test before making sure you have found all the primes?

A: Rather than test all $n = 10,000$ numbers, it is only necessary to test $\sqrt{n} = 100$ numbers. In fact, because you can immediately determine that any even number other than 2 is not a prime number, you only need to test the odd numbers from 1 – 100, or in other words $\sqrt{n}/2$. For even larger values of n , this will be significant in reducing the runtime of the program.

Problem Definition/Specification

A program is needed that will be able to generate all the prime numbers from 1 – 10,000 in an efficient manner. See Exercise 5.27 for more details.

Problem Analysis

The program is to use a function that will determine whether a number is a prime number to print out every number from 1-10,000 that is a prime number. First, it must be considered what makes a number prime and how to determine whether a given number is prime. An efficient way to make this determination is necessary to ensure that the program can run relatively quickly. For this specific implementation of the algorithm, each number that is checked will be checked from 1 to $n/2$, as specified in the assignment.

Program Inputs

- This program has no inputs

Program Outputs

- Every prime number within the range 1-10,000

Formula or Relations

A prime number is defined as a number which is greater than 1 and which has no factors other than 1 and itself. In addition, because every even number is divisible by 2, 2 is the only even number that is considered a prime number.

Algorithm Design

Initial Algorithm

1. Loop from 1 to 10,000 and test each of the numbers on the function which determines whether a number is prime.

2. Within the function, first test whether the input is a 1, which is nonprime
3. Within the function, test whether the input is a 2, which is prime
4. Within the function, test whether the input is an even number, which is nonprime
5. Within the function, loop through all odd numbers from 3 to the input/2 and test whether the input is divisible by each number, returning the appropriate determination.
6. Within the main method, each number that evaluates as prime will be printed to the screen

Refinement

1. Use a for loop from $i = 1$ to a constant integer on 10,000 and increment i by 1 in each iteration. Within the loop, use an if statement and call the method int isPrime(int test) on the current value of i .
2. Within the function isPrime(int test), use an if statement with $test == 1$ to determine if the input is 1, and return 0 (false) if it is.
3. Within the function isPrime(int test), use an if statement with $test == 2$ to determine if the input is 2, and return 1 (true) if it is.
4. Within the function, use an if statement with $test \% 2 == 0$ to determine whether the number is even (divisible by 2), and return 0 (false) if it is.
5. Within the function, use a for loop that starts at $i = 3$ and iterates while $i <= test/2$. Increment i by 2 each iteration, and use an if statement each loop to determine whether the test number is divisible by the current value of i . Return 0 (false) if this is the case, and 1 (true) if the end of the loop is reached and the if statement has not evaluated as true.
6. In the main method, whenever the if statement in step 1 evaluates as true, print out the current value of i to the screen.

Desk Checking/Test Plan

Because there are no inputs to this program, a single run will be enough to determine whether the program works as intended. If the program output all the prime numbers from 1 to 10,000, then it can be determined that the program works correctly. However, an additional test was added that shows the amount of time the program takes to run (using function from the time.h include statement in C). This was important for comparing this program to the other 2 in question 2 of this assignment, and a table comparing the runtimes of the three programs can be seen below all programs in question 2.

Implementation

```
1  /*
2  * Programmer: Kollin Labowski
3  * Date Completed: September 27, 2020
4  * Course: CS 350
5  * Description: This program includes a function isPrime(int a) that determines whether a number is prime or not (more description below), and a main method
6  * which tests this function on the numbers 1-10000, printing out all of the numbers for which the function evaluates as true. This specific version uses an
7  * upper bound to check primes of n/2, as stated in the programming assignment.
8  */
9
10 //Include statements
11 #include <stdio.h>
12 #include <math.h>
13 #include <time.h>
14
15 //Function prototype
16 int isPrime(int a);
17
18 //Main method
19 void main()
20 {
21     clock_t start = clock(); //Used for timing the program
22
23     //Variables (including constant 10000 which specifies amount of iterations)
24     int format = 0; //Used to format the printed values
25     const int LOOPS = 10000;
26
27     for(int i = 1; i <= LOOPS; i++)
28     {
29         if(isPrime(i))
30         {
31             printf("%d ", i);
32             if(format % 10 == 0)
33                 printf("\n");
34             format++;
35         }
36     }
37
38     //These methods determine the elapsed time and print it to the terminal
39     clock_t end = clock();
40     double time = (double)(end - start) / CLOCKS_PER_SEC;
41     printf("\n\nTime elapsed: %lf", time);
42 }
```



```
43 /*
44 * This function determines whether a number is prime or not by using loops. It first checks and evaluates the unique cases of 1 and 2 individually. It also
45 * is able to determine immediately that a number is not prime by checking if it is even. Otherwise, the function will loop and determine whether the input
46 * value is divisible by each odd integer that is <= the square root of the input number. This function uses a loop that terminates at n/2.
47 */
48 int isPrime(int test)
49 {
50     //1 evaluates as nonprime
51     if(test == 1)
52     {
53         return 0;
54     }
55     //2 evaluates as prime
56     if(test == 2)
57     {
58         return 1;
59     }
60     //All other even numbers evaluate as nonprime
61     if(test % 2 == 0)
62     {
63         return 0;
64     }
65     //Loop used to determine whether the number is prime if not even or an extraneous case
66     for(int i = 3; i <= test/2; i+=2) //The loop checks until n/2 is reached
67     {
68         if(test % i == 0)
69         {
70             return 0;
71         }
72     }
73     return 1;
74 }
```

Testing

Test 1:

2
3 5 7 11 13 17 19 23 29 31
37 41 43 47 53 59 61 67 71 73
79 83 89 97 101 103 107 109 113 127
131 137 139 149 151 157 163 167 173 179
181 191 193 197 199 211 223 227 229 233
239 241 251 257 263 269 271 277 281 283
293 307 311 313 317 331 337 347 349 353
359 367 373 379 383 389 397 401 409 419
421 431 433 439 443 449 457 461 463 467
479 487 491 499 503 509 521 523 541 547
557 563 569 571 577 587 593 599 601 607
613 617 619 631 641 643 647 653 659 661
673 677 683 691 701 709 719 727 733 739
743 751 757 761 769 773 787 797 809 811
821 823 827 829 839 853 857 859 863 877
881 883 887 907 911 919 929 937 941 947
953 967 971 977 983 991 997 1009 1013 1019
1021 1031 1033 1039 1049 1051 1061 1063 1069 1087
1091 1093 1097 1103 1109 1117 1123 1129 1151 1153
1163 1171 1181 1187 1193 1201 1213 1217 1223 1229
1231 1237 1249 1259 1277 1279 1283 1289 1291 1297
1301 1303 1307 1319 1321 1327 1361 1367 1373 1381
1399 1409 1423 1427 1429 1433 1439 1447 1451 1453
1459 1471 1481 1483 1487 1489 1493 1499 1511 1523
1531 1543 1549 1553 1559 1567 1571 1579 1583 1597
1601 1607 1609 1613 1619 1621 1627 1637 1657 1663
1667 1669 1693 1697 1699 1709 1721 1723 1733 1741
1747 1753 1759 1777 1783 1787 1789 1801 1811 1823
1831 1847 1861 1867 1871 1873 1877 1879 1889 1901
1907 1913 1931 1933 1949 1951 1973 1979 1987 1993
1997 1999 2003 2011 2017 2027 2029 2039 2053 2063
2069 2081 2083 2087 2089 2099 2111 2113 2129 2131
2137 2141 2143 2153 2161 2179 2203 2207 2213 2221
2237 2239 2243 2251 2267 2269 2273 2281 2287 2293
2297 2309 2311 2333 2339 2341 2347 2351 2357 2371
2377 2381 2383 2389 2393 2399 2411 2417 2423 2437
2441 2447 2459 2467 2473 2477 2503 2521 2531 2539
2543 2549 2551 2557 2579 2591 2593 2609 2617 2621
2633 2647 2657 2659 2663 2671 2677 2683 2687 2689
2693 2699 2707 2711 2713 2719 2729 2731 2741 2749
2753 2767 2777 2789 2791 2797 2801 2803 2819 2833
2837 2843 2851 2857 2861 2879 2887 2897 2903 2909
2917 2927 2939 2953 2957 2963 2969 2971 2999 3001
3011 3019 3023 3037 3041 3049 3061 3067 3079 3083
3089 3109 3119 3121 3137 3163 3167 3169 3181 3187
3191 3203 3209 3217 3221 3229 3251 3253 3257 3259
3271 3299 3301 3307 3313 3319 3323 3329 3331 3343

3347	3359	3361	3371	3373	3389	3391	3407	3413	3433
3449	3457	3461	3463	3467	3469	3491	3499	3511	3517
3527	3529	3533	3539	3541	3547	3557	3559	3571	3581
3583	3593	3607	3613	3617	3623	3631	3637	3643	3659
3671	3673	3677	3691	3697	3701	3709	3719	3727	3733
3739	3761	3767	3769	3779	3793	3797	3803	3821	3823
3833	3847	3851	3853	3863	3877	3881	3889	3907	3911
3917	3919	3923	3929	3931	3943	3947	3967	3989	4001
4003	4007	4013	4019	4021	4027	4049	4051	4057	4073
4079	4091	4093	4099	4111	4127	4129	4133	4139	4153
4157	4159	4177	4201	4211	4217	4219	4229	4231	4241
4243	4253	4259	4261	4271	4273	4283	4289	4297	4327
4337	4339	4349	4357	4363	4373	4391	4397	4409	4421
4423	4441	4447	4451	4457	4463	4481	4483	4493	4507
4513	4517	4519	4523	4547	4549	4561	4567	4583	4591
4597	4603	4621	4637	4639	4643	4649	4651	4657	4663
4673	4679	4691	4703	4721	4723	4729	4733	4751	4759
4783	4787	4789	4793	4799	4801	4813	4817	4831	4861
4871	4877	4889	4903	4909	4919	4931	4933	4937	4943
4951	4957	4967	4969	4973	4987	4993	4999	5003	5009
5011	5021	5023	5039	5051	5059	5077	5081	5087	5099
5101	5107	5113	5119	5147	5153	5167	5171	5179	5189
5197	5209	5227	5231	5233	5237	5261	5273	5279	5281
5297	5303	5309	5323	5333	5347	5351	5381	5387	5393
5399	5407	5413	5417	5419	5431	5437	5441	5443	5449
5471	5477	5479	5483	5501	5503	5507	5519	5521	5527
5531	5557	5563	5569	5573	5581	5591	5623	5639	5641
5647	5651	5653	5657	5659	5669	5683	5689	5693	5701
5711	5717	5737	5741	5743	5749	5779	5783	5791	5801
5807	5813	5821	5827	5839	5843	5849	5851	5857	5861
5867	5869	5879	5881	5897	5903	5923	5927	5939	5953
5981	5987	6007	6011	6029	6037	6043	6047	6053	6067
6073	6079	6089	6091	6101	6113	6121	6131	6133	6143
6151	6163	6173	6197	6199	6203	6211	6217	6221	6229
6247	6257	6263	6269	6271	6277	6287	6299	6301	6311
6317	6323	6329	6337	6343	6353	6359	6361	6367	6373
6379	6389	6397	6421	6427	6449	6451	6469	6473	6481
6491	6521	6529	6547	6551	6553	6563	6569	6571	6577
6581	6599	6607	6619	6637	6653	6659	6661	6673	6679
6689	6691	6701	6703	6709	6719	6733	6737	6761	6763
6779	6781	6791	6793	6803	6823	6827	6829	6833	6841
6857	6863	6869	6871	6883	6899	6907	6911	6917	6947
6949	6959	6961	6967	6971	6977	6983	6991	6997	7001
7013	7019	7027	7039	7043	7057	7069	7079	7103	7109
7121	7127	7129	7151	7159	7177	7187	7193	7207	7211
7213	7219	7229	7237	7243	7247	7253	7283	7297	7307
7309	7321	7331	7333	7349	7351	7369	7393	7411	7417
7433	7451	7457	7459	7477	7481	7487	7489	7499	7507

```
7517 7523 7529 7537 7541 7547 7549 7559 7561 7573  
7577 7583 7589 7591 7603 7607 7621 7639 7643 7649  
7669 7673 7681 7687 7691 7699 7703 7717 7723 7727  
7741 7753 7757 7759 7789 7793 7817 7823 7829 7841  
7853 7867 7873 7877 7879 7883 7901 7907 7919 7927  
7933 7937 7949 7951 7963 7993 8009 8011 8017 8039  
8053 8059 8069 8081 8087 8089 8093 8101 8111 8117  
8123 8147 8161 8167 8171 8179 8191 8209 8219 8221  
8231 8233 8237 8243 8263 8269 8273 8287 8291 8293  
8297 8311 8317 8329 8353 8363 8369 8377 8387 8389  
8419 8423 8429 8431 8443 8447 8461 8467 8501 8513  
8521 8527 8537 8539 8543 8563 8573 8581 8597 8599  
8609 8623 8627 8629 8641 8647 8663 8669 8677 8681  
8689 8693 8699 8707 8713 8719 8731 8737 8741 8747  
8753 8761 8779 8783 8803 8807 8819 8821 8831 8837  
8839 8849 8861 8863 8867 8887 8893 8923 8929 8933  
8941 8951 8963 8969 8971 8999 9001 9007 9011 9013  
9029 9041 9043 9049 9059 9067 9091 9103 9109 9127  
9133 9137 9151 9157 9161 9173 9181 9187 9199 9203  
9209 9221 9227 9239 9241 9257 9277 9281 9283 9293  
9311 9319 9323 9337 9341 9343 9349 9371 9377 9391  
9397 9403 9413 9419 9421 9431 9433 9437 9439 9461  
9463 9467 9473 9479 9491 9497 9511 9521 9533 9539  
9547 9551 9587 9601 9613 9619 9623 9629 9631 9643  
9649 9661 9677 9679 9689 9697 9719 9721 9733 9739  
9743 9749 9767 9769 9781 9787 9791 9803 9811 9817  
9829 9833 9839 9851 9857 9859 9871 9883 9887 9901  
9907 9923 9929 9931 9941 9949 9967 9973
```

```
Time elapsed: 0.178000
```

Test with size 100,000:

```
99409 99431 99439 99469 99487 99497 99523 99527 99529 99551  
99559 99563 99571 99577 99581 99607 99611 99623 99643 99661  
99667 99679 99689 99707 99709 99713 99719 99721 99733 99761  
99767 99787 99793 99809 99817 99823 99829 99833 99839 99859  
99871 99877 99881 99901 99907 99923 99929 99961 99971 99989  
99991
```

```
Time elapsed: 1.169000
```

Question 2A2

Problem Definition/Specification

A program is needed that will be able to generate all the prime numbers from 1 – 10,000 in an efficient manner. See Exercise 5.27 for more details. This program differs from the previous in that the loop in the function must terminate at $\text{sqrt}(n)$ rather than $n/2$.

Problem Analysis

The program is to use a function that will determine whether a number is a prime number to print out every number from 1-10,000 that is a prime number. First, it must be considered what makes a number prime and how to determine whether a given number is prime. An efficient way to make this determination is necessary to ensure that the program can run relatively quickly. For this specific implementation of the algorithm, each number that is checked will be checked from 1 to $\text{sqrt}(n)$, as specified in the assignment.

Program Inputs

- This program has no inputs

Program Outputs

- Every prime number within the range 1-10,000

Formula or Relations

A prime number is defined as a number which is greater than 1 and which has no factors other than 1 and itself. In addition, because every even number is divisible by 2, 2 is the only even number that is considered a prime number.

Algorithm Design

Initial Algorithm

1. Loop from 1 to 10,000 and test each of the numbers on the function which determines whether a number is prime.
2. Within the function, first test whether the input is a 1, which is nonprime
3. Within the function, test whether the input is a 2, which is prime
4. Within the function, test whether the input is an even number, which is nonprime
5. Within the function, loop through all odd numbers from 3 to the $\text{sqrt}(\text{input})$ and test whether the input is divisible by each number, returning the appropriate determination.
6. Within the main method, each number that evaluates as prime will be printed to the screen

Refinement

1. Use a for loop from $i = 1$ to a constant integer on 10,000 and increment i by 1 in each iteration. Within the loop, use an if statement and call the method int isPrime(int test) on the current value of i .
2. Within the function isPrime(int test), use an if statement with $test == 1$ to determine if the input is 1, and return 0 (false) if it is.
3. Within the function isPrime(int test), use an if statement with $test == 2$ to determine if the input is 2, and return 1 (true) if it is.
4. Within the function, use an if statement with $test \% 2 == 0$ to determine whether the number is even (divisible by 2), and return 0 (false) if it is.
5. Within the function, use a for loop that starts at $i = 3$ and iterates while $i \leq \sqrt{test}$. Increment i by 2 each iteration, and use an if statement each loop to determine whether the test number is divisible by the current value of i . Return 0 (false) if this is the case, and 1 (true) if the end of the loop is reached and the if statement has not evaluated as true.
6. In the main method, whenever the if statement in step 1 evaluates as true, print out the current value of i to the screen.

Desk Checking/Test Plan

Because there are no inputs to this program, a single run will be enough to determine whether the program works as intended. If the program output all the prime numbers from 1 to 10,000, then it can be determined that the program works correctly. However, an additional test was added that shows the amount of time the program takes to run (using function from the time.h include statement in C). This was important for comparing this program to the other 2 in question 2 of this assignment, and a table comparing the runtimes of the three programs can be seen below all programs in question 2.

Implementation

```
1  /*
2  * Programmer: Kolin Labowski
3  * Date Completed: September 27, 2020
4  * Course: CS 350
5  * Description: This program includes a function isPrime(int a) that determines whether a number is prime or not (more description below), and a main method
6  * which tests this function on the numbers 1-10000, printing out all of the numbers for which the function evaluates as true. This particular version of the
7  * program uses a loop with size sqrt(n) instead of n/2, which was stated in the problem assignment.
8  */
9
10 //Include statements
11 #include <stdio.h>
12 #include <math.h>
13 #include <time.h>
14
15 //Function prototype
16 int isPrime(int a);
17
18 //Main method
19 void main()
20 {
21     clock_t start = clock(); //Used for timing the program
22
23     //Variables (including constant 10000 which specifies amount of iterations)
24     int format = 0; //Used to format the printed values
25     const int LOOPS = 10000;
26
27     for(int i = 1; i <= LOOPS; i++)
28     {
29         if(isPrime(i))
30         {
31             printf("%d ", i);
32             if(format % 10 == 0)
33                 printf("\n");
34             format++;
35         }
36     }
37
38     //These methods determine the elapsed time and print it to the terminal
39     clock_t end = clock();
40     double time = (double)(end - start) / CLOCKS_PER_SEC;
41     printf("\n\nTime elapsed: %lf", time);
42 }
```



```
43 /*
44 * This function determines whether a number is prime or not by using loops. It first checks and evaluates the unique cases of 1 and 2 individually. It also
45 * is able to determine immediately that a number is not prime by checking if it is even. Otherwise, the function will loop and determine whether the input
46 * value is divisible by each odd integer that is <= the square root of the input number. This function uses a loop that terminates at sqrt(n) instead of n/2.
47 */
48 int isPrime(int test)
49 {
50     //1 evaluates as nonprime
51     if(test == 1)
52     {
53         return 0;
54     }
55     //2 evaluates as prime
56     if(test == 2)
57     {
58         return 1;
59     }
60     //All other even numbers evaluate as nonprime
61     if(test % 2 == 0)
62     {
63         return 0;
64     }
65     //Loop used to determine whether the number is prime if not even or an extraneous case
66     for(int i = 3; i <= sqrt(test); i+=2) //The loop checks until sqrt(n) is reached (NOT n/2)
67     {
68         if(test % i == 0)
69         {
70             return 0;
71         }
72     }
73     return 1;
74 }
```

Testing

Test 1:

```
2
3 5 7 11 13 17 19 23 29 31
37 41 43 47 53 59 61 67 71 73
79 83 89 97 101 103 107 109 113 127
131 137 139 149 151 157 163 167 173 179
181 191 193 197 199 211 223 227 229 233
239 241 251 257 263 269 271 277 281 283
293 307 311 313 317 331 337 347 349 353
359 367 373 379 383 389 397 401 409 419
421 431 433 439 443 449 457 461 463 467
479 487 491 499 503 509 521 523 541 547
557 563 569 571 577 587 593 599 601 607
613 617 619 631 641 643 647 653 659 661
673 677 683 691 701 709 719 727 733 739
743 751 757 761 769 773 787 797 809 811
821 823 827 829 839 853 857 859 863 877
881 883 887 907 911 919 929 937 941 947
953 967 971 977 983 991 997 1009 1013 1019
1021 1031 1033 1039 1049 1051 1061 1063 1069 1087
1091 1093 1097 1103 1109 1117 1123 1129 1151 1153
1163 1171 1181 1187 1193 1201 1213 1217 1223 1229
1231 1237 1249 1259 1277 1279 1283 1289 1291 1297
1301 1303 1307 1319 1321 1327 1361 1367 1373 1381
1399 1409 1423 1427 1429 1433 1439 1447 1451 1453
1459 1471 1481 1483 1487 1489 1493 1499 1511 1523
1531 1543 1549 1553 1559 1567 1571 1579 1583 1597
1601 1607 1609 1613 1619 1621 1627 1637 1657 1663
1667 1669 1693 1697 1699 1709 1721 1723 1733 1741
1747 1753 1759 1777 1783 1787 1789 1801 1811 1823
1831 1847 1861 1867 1871 1873 1877 1879 1889 1901
1907 1913 1931 1933 1949 1951 1973 1979 1987 1993
1997 1999 2003 2011 2017 2027 2029 2039 2053 2063
2069 2081 2083 2087 2089 2099 2111 2113 2129 2131
2137 2141 2143 2153 2161 2179 2203 2207 2213 2221
2237 2239 2243 2251 2267 2269 2273 2281 2287 2293
2297 2309 2311 2333 2339 2341 2347 2351 2357 2371
2377 2381 2383 2389 2393 2399 2411 2417 2423 2437
2441 2447 2459 2467 2473 2477 2503 2521 2531 2539
2543 2549 2551 2557 2579 2591 2593 2609 2617 2621
2633 2647 2657 2659 2663 2671 2677 2683 2687 2689
2693 2699 2707 2711 2713 2719 2729 2731 2741 2749
2753 2767 2777 2789 2791 2797 2801 2803 2819 2833
2837 2843 2851 2857 2861 2879 2887 2897 2903 2909
2917 2927 2939 2953 2957 2963 2969 2971 2999 3001
3011 3019 3023 3037 3041 3049 3061 3067 3079 3083
3089 3109 3119 3121 3137 3163 3167 3169 3181 3187
3191 3203 3209 3217 3221 3229 3251 3253 3257 3259
3271 3299 3301 3307 3313 3319 3323 3329 3331 3343
```

3347	3359	3361	3371	3373	3389	3391	3407	3413	3433
3449	3457	3461	3463	3467	3469	3491	3499	3511	3517
3527	3529	3533	3539	3541	3547	3557	3559	3571	3581
3583	3593	3607	3613	3617	3623	3631	3637	3643	3659
3671	3673	3677	3691	3697	3701	3709	3719	3727	3733
3739	3761	3767	3769	3779	3793	3797	3803	3821	3823
3833	3847	3851	3853	3863	3877	3881	3889	3907	3911
3917	3919	3923	3929	3931	3943	3947	3967	3989	4001
4003	4007	4013	4019	4021	4027	4049	4051	4057	4073
4079	4091	4093	4099	4111	4127	4129	4133	4139	4153
4157	4159	4177	4201	4211	4217	4219	4229	4231	4241
4243	4253	4259	4261	4271	4273	4283	4289	4297	4327
4337	4339	4349	4357	4363	4373	4391	4397	4409	4421
4423	4441	4447	4451	4457	4463	4481	4483	4493	4507
4513	4517	4519	4523	4547	4549	4561	4567	4583	4591
4597	4603	4621	4637	4639	4643	4649	4651	4657	4663
4673	4679	4691	4703	4721	4723	4729	4733	4751	4759
4783	4787	4789	4793	4799	4801	4813	4817	4831	4861
4871	4877	4889	4903	4909	4919	4931	4933	4937	4943
4951	4957	4967	4969	4973	4987	4993	4999	5003	5009
5011	5021	5023	5039	5051	5059	5077	5081	5087	5099
5101	5107	5113	5119	5147	5153	5167	5171	5179	5189
5197	5209	5227	5231	5233	5237	5261	5273	5279	5281
5297	5303	5309	5323	5333	5347	5351	5381	5387	5393
5399	5407	5413	5417	5419	5431	5437	5441	5443	5449
5471	5477	5479	5483	5501	5503	5507	5519	5521	5527
5531	5557	5563	5569	5573	5581	5591	5623	5639	5641
5647	5651	5653	5657	5659	5669	5683	5689	5693	5701
5711	5717	5737	5741	5743	5749	5779	5783	5791	5801
5807	5813	5821	5827	5839	5843	5849	5851	5857	5861
5867	5869	5879	5881	5897	5903	5923	5927	5939	5953
5981	5987	6007	6011	6029	6037	6043	6047	6053	6067
6073	6079	6089	6091	6101	6113	6121	6131	6133	6143
6151	6163	6173	6197	6199	6203	6211	6217	6221	6229
6247	6257	6263	6269	6271	6277	6287	6299	6301	6311
6317	6323	6329	6337	6343	6353	6359	6361	6367	6373
6379	6389	6397	6421	6427	6449	6451	6469	6473	6481
6491	6521	6529	6547	6551	6553	6563	6569	6571	6577
6581	6599	6607	6619	6637	6653	6659	6661	6673	6679
6689	6691	6701	6703	6709	6719	6733	6737	6761	6763
6779	6781	6791	6793	6803	6823	6827	6829	6833	6841
6857	6863	6869	6871	6883	6899	6907	6911	6917	6947
6949	6959	6961	6967	6971	6977	6983	6991	6997	7001
7013	7019	7027	7039	7043	7057	7069	7079	7103	7109
7121	7127	7129	7151	7159	7177	7187	7193	7207	7211
7213	7219	7229	7237	7243	7247	7253	7283	7297	7307
7309	7321	7331	7333	7349	7351	7369	7393	7411	7417
7433	7451	7457	7459	7477	7481	7487	7489	7499	7507

```
7517 7523 7529 7537 7541 7547 7549 7559 7561 7573  
7577 7583 7589 7591 7603 7607 7621 7639 7643 7649  
7669 7673 7681 7687 7691 7699 7703 7717 7723 7727  
7741 7753 7757 7759 7789 7793 7817 7823 7829 7841  
7853 7867 7873 7877 7879 7883 7901 7907 7919 7927  
7933 7937 7949 7951 7963 7993 8009 8011 8017 8039  
8053 8059 8069 8081 8087 8089 8093 8101 8111 8117  
8123 8147 8161 8167 8171 8179 8191 8209 8219 8221  
8231 8233 8237 8243 8263 8269 8273 8287 8291 8293  
8297 8311 8317 8329 8353 8363 8369 8377 8387 8389  
8419 8423 8429 8431 8443 8447 8461 8467 8501 8513  
8521 8527 8537 8539 8543 8563 8573 8581 8597 8599  
8609 8623 8627 8629 8641 8647 8663 8669 8677 8681  
8689 8693 8699 8707 8713 8719 8731 8737 8741 8747  
8753 8761 8779 8783 8803 8807 8819 8821 8831 8837  
8839 8849 8861 8863 8867 8887 8893 8923 8929 8933  
8941 8951 8963 8969 8971 8999 9001 9007 9011 9013  
9029 9041 9043 9049 9059 9067 9091 9103 9109 9127  
9133 9137 9151 9157 9161 9173 9181 9187 9199 9203  
9209 9221 9227 9239 9241 9257 9277 9281 9283 9293  
9311 9319 9323 9337 9341 9343 9349 9371 9377 9391  
9397 9403 9413 9419 9421 9431 9433 9437 9439 9461  
9463 9467 9473 9479 9491 9497 9511 9521 9533 9539  
9547 9551 9587 9601 9613 9619 9623 9629 9631 9643  
9649 9661 9677 9679 9689 9697 9719 9721 9733 9739  
9743 9749 9767 9769 9781 9787 9791 9803 9811 9817  
9829 9833 9839 9851 9857 9859 9871 9883 9887 9901  
9907 9923 9929 9931 9941 9949 9967 9973
```

```
Time elapsed: 0.170000
```

Test time with size 100,000:

```
99559 99563 99571 99577 99581 99607 99611 99623 99643 99661  
99667 99679 99689 99707 99709 99713 99719 99721 99733 99761  
99767 99787 99793 99809 99817 99823 99829 99833 99839 99859  
99871 99877 99881 99901 99907 99923 99929 99961 99971 99989  
99991
```

```
Time elapsed: 0.744000
```

Question 2B

Problem Definition/Specification

A program is needed that will be able to generate all the prime numbers from 1 – 10,000 in an efficient manner using a method called “The Sieve of Eratosthenes”. See Exercise 6.30 for more details. This program accomplishes the same task as the previous 2 but in a slightly different way that takes advantage of the helpful properties of arrays.

Problem Analysis

The program is to use a function that will determine whether a number is a prime number to print out every number from 1-10,000 that is a prime number. First, it must be considered what makes a number prime and how to determine whether a given number is prime. An efficient way to make this determination is necessary to ensure that the program can run relatively quickly. For this specific implementation of the algorithm, an array is to be created of size 10,000 and each of its entries are to be set to 1. Entries will be set to 0 throughout the program’s runtime, and this will indicate that those specific entries are nonprime.

Program Inputs

- This program has no inputs

Program Outputs

- Every prime number within the range 1-10,000

Formula or Relations

A prime number is defined as a number which is greater than 1 and which has no factors other than 1 and itself.

Algorithm Design

Initial Algorithm

1. Create an array of size 10,000 and set all its entries to 1
2. Begin to loop through the array, beginning at the index corresponding to the number 2, and for every entry in the array that is a 1, print out the number corresponding to that index and proceed to step 3.
3. In the case a 1 is reached while looping through the array, loop through the remainder of the array and set all multiples of that index’s corresponding number to 0.

Refinement

1. Initialize an array as follows: int array[ARRSIZE] where ARRSIZE is a constant integer of size 10,000. Set all entries to 1 by using a for loop and setting each entry at the loop's current index to 1.
2. In a new for loop from 1 to ARRSIZE, check each element to see if it is equal to 1 using an if statement with array[i] == 1. If the if statement evaluates as true, print out the current index of the loop + 1, because in this implementation index 0 corresponds to 1, 1 corresponds to 2, and so on.
3. While the if statement is true, loop through the remainder of the array using a nested for loop from the outer loop's index to the end of the array. Set each multiple of the outer loop's index to 0 by incrementing the inner loop by the outer loop index + 1, again because of the offset for the array indices.

Desk Checking/Test Plan

Because there are no inputs to this program, a single run will be enough to determine whether the program works as intended. If the program output all the prime numbers from 1 to 10,000, then it can be determined that the program works correctly. However, an additional test was added that shows the amount of time the program takes to run (using function from the time.h include statement in C). This was important for comparing this program to the other 2 in question 2 of this assignment, and a table comparing the runtimes of the three programs can be seen below all programs in question 2.

Implementation

```
1  /*
2  * Programmer: Kollin Labowski
3  * Date Completed: September 28, 2020
4  * Course: CS 350
5  * Description: This program generates all of the prime numbers from 1 to 10000 using a method called "The Sieve of Eratosthenes". This method uses an array
6  * of 1s and 0s which are used to indicate whether a number at the specified index is prime or not. It should be noted that each index (0-9999) is actually
7  * used to represent a number that is one greater than it (ie: index 0 corresponds to the number 1), thus giving the range 1-10000.
8  */
9
10 //Include statements
11 #include <stdio.h>
12 #include <time.h>
13
14 //Main method
15 void main()
16 {
17     //Used for timing the program
18     clock_t start = clock();
19
20     //Initialize the array at size set by the user, here is 10000
21     const int ARRSIZE = 10000;
22     int array[ARRSIZE];
23
24     //Set each element of the array to 1 to begin
25     for(int i = 0; i < ARRSIZE; i++)
26     {
27         array[i] = 1;
28     }
29
30     //Loops through all values in the array
31     //When a 1 is found, print the value connected to that index and set the indexes of all multiples of that value to 0 so they are not checked again
32     int format = 0;
33     for(int i = 1; i < ARRSIZE; i++)
34     {
35         if(array[i] == 1)
36         {
37             printf("%d ", i + 1);
38             for(int j = i; j < ARRSIZE; j += (i + 1))
39             {
40                 array[j] = 0;
41             }
42             if(format % 10 == 0)
43                 printf("\n");
44             format++;
45         }
46     }
47
48     //Methods used for measuring the time the program spends running
49     clock_t end = clock();
50     double time = (double)(end - start) / CLOCKS_PER_SEC;
51     printf("\n\nTime elapsed: %lf", time);
52 }
```

Testing

Test 1:

```
2
3 5 7 11 13 17 19 23 29 31
37 41 43 47 53 59 61 67 71 73
79 83 89 97 101 103 107 109 113 127
131 137 139 149 151 157 163 167 173 179
181 191 193 197 199 211 223 227 229 233
239 241 251 257 263 269 271 277 281 283
293 307 311 313 317 331 337 347 349 353
359 367 373 379 383 389 397 401 409 419
421 431 433 439 443 449 457 461 463 467
479 487 491 499 503 509 521 523 541 547
557 563 569 571 577 587 593 599 601 607
613 617 619 631 641 643 647 653 659 661
673 677 683 691 701 709 719 727 733 739
743 751 757 761 769 773 787 797 809 811
821 823 827 829 839 853 857 859 863 877
881 883 887 907 911 919 929 937 941 947
953 967 971 977 983 991 997 1009 1013 1019
1021 1031 1033 1039 1049 1051 1061 1063 1069 1087
1091 1093 1097 1103 1109 1117 1123 1129 1151 1153
1163 1171 1181 1187 1193 1201 1213 1217 1223 1229
1231 1237 1249 1259 1277 1279 1283 1289 1291 1297
1301 1303 1307 1319 1321 1327 1361 1367 1373 1381
1399 1409 1423 1427 1429 1433 1439 1447 1451 1453
1459 1471 1481 1483 1487 1489 1493 1499 1511 1523
1531 1543 1549 1553 1559 1567 1571 1579 1583 1597
1601 1607 1609 1613 1619 1621 1627 1637 1657 1663
1667 1669 1693 1697 1699 1709 1721 1723 1733 1741
1747 1753 1759 1777 1783 1787 1789 1801 1811 1823
1831 1847 1861 1867 1871 1873 1877 1879 1889 1901
1907 1913 1931 1933 1949 1951 1973 1979 1987 1993
1997 1999 2003 2011 2017 2027 2029 2039 2053 2063
2069 2081 2083 2087 2089 2099 2111 2113 2129 2131
2137 2141 2143 2153 2161 2179 2203 2207 2213 2221
2237 2239 2243 2251 2267 2269 2273 2281 2287 2293
2297 2309 2311 2333 2339 2341 2347 2351 2357 2371
2377 2381 2383 2389 2393 2399 2411 2417 2423 2437
2441 2447 2459 2467 2473 2477 2503 2521 2531 2539
2543 2549 2551 2557 2579 2591 2593 2609 2617 2621
2633 2647 2657 2659 2663 2671 2677 2683 2687 2689
2693 2699 2707 2711 2713 2719 2729 2731 2741 2749
2753 2767 2777 2789 2791 2797 2801 2803 2819 2833
2837 2843 2851 2857 2861 2879 2887 2897 2903 2909
2917 2927 2939 2953 2957 2963 2969 2971 2999 3001
3011 3019 3023 3037 3041 3049 3061 3067 3079 3083
3089 3109 3119 3121 3137 3163 3167 3169 3181 3187
```

3191	3203	3209	3217	3221	3229	3251	3253	3257	3259
3271	3299	3301	3307	3313	3319	3323	3329	3331	3343
3347	3359	3361	3371	3373	3389	3391	3407	3413	3433
3449	3457	3461	3463	3467	3469	3491	3499	3511	3517
3527	3529	3533	3539	3541	3547	3557	3559	3571	3581
3583	3593	3607	3613	3617	3623	3631	3637	3643	3659
3671	3673	3677	3691	3697	3701	3709	3719	3727	3733
3739	3761	3767	3769	3779	3793	3797	3803	3821	3823
3833	3847	3851	3853	3863	3877	3881	3889	3907	3911
3917	3919	3923	3929	3931	3943	3947	3967	3989	4001
4003	4007	4013	4019	4021	4027	4049	4051	4057	4073
4079	4091	4093	4099	4111	4127	4129	4133	4139	4153
4157	4159	4177	4201	4211	4217	4219	4229	4231	4241
4243	4253	4259	4261	4271	4273	4283	4289	4297	4327
4337	4339	4349	4357	4363	4373	4391	4397	4409	4421
4423	4441	4447	4451	4457	4463	4481	4483	4493	4507
4513	4517	4519	4523	4547	4549	4561	4567	4583	4591
4597	4603	4621	4637	4639	4643	4649	4651	4657	4663
4673	4679	4691	4703	4721	4723	4729	4733	4751	4759
4783	4787	4789	4793	4799	4801	4813	4817	4831	4861
4871	4877	4889	4903	4909	4919	4931	4933	4937	4943
4951	4957	4967	4969	4973	4987	4993	4999	5003	5009
5011	5021	5023	5039	5051	5059	5077	5081	5087	5099
5101	5107	5113	5119	5147	5153	5167	5171	5179	5189
5197	5209	5227	5231	5233	5237	5261	5273	5279	5281
5297	5303	5309	5323	5333	5347	5351	5381	5387	5393
5399	5407	5413	5417	5419	5431	5437	5441	5443	5449
5471	5477	5479	5483	5501	5503	5507	5519	5521	5527
5531	5557	5563	5569	5573	5581	5591	5623	5639	5641
5647	5651	5653	5657	5659	5669	5683	5689	5693	5701
5711	5717	5737	5741	5743	5749	5779	5783	5791	5801
5807	5813	5821	5827	5839	5843	5849	5851	5857	5861
5867	5869	5879	5881	5897	5903	5923	5927	5939	5953
5981	5987	6007	6011	6029	6037	6043	6047	6053	6067
6073	6079	6089	6091	6101	6113	6121	6131	6133	6143
6151	6163	6173	6197	6199	6203	6211	6217	6221	6229
6247	6257	6263	6269	6271	6277	6287	6299	6301	6311
6317	6323	6329	6337	6343	6353	6359	6361	6367	6373
6379	6389	6397	6421	6427	6449	6451	6469	6473	6481
6491	6521	6529	6547	6551	6553	6563	6569	6571	6577
6581	6599	6607	6619	6637	6653	6659	6661	6673	6679
6689	6691	6701	6703	6709	6719	6733	6737	6761	6763
6779	6781	6791	6793	6803	6823	6827	6829	6833	6841
6857	6863	6869	6871	6883	6899	6907	6911	6917	6947
6949	6959	6961	6967	6971	6977	6983	6991	6997	7001
7013	7019	7027	7039	7043	7057	7069	7079	7103	7109

```
7121 7127 7129 7151 7159 7177 7187 7193 7207 7211  
7213 7219 7229 7237 7243 7247 7253 7283 7297 7307  
7309 7321 7331 7333 7349 7351 7369 7393 7411 7417  
7433 7451 7457 7459 7477 7481 7487 7489 7499 7507  
7517 7523 7529 7537 7541 7547 7549 7559 7561 7573  
7577 7583 7589 7591 7603 7607 7621 7639 7643 7649  
7669 7673 7681 7687 7691 7699 7703 7717 7723 7727  
7741 7753 7757 7759 7789 7793 7817 7823 7829 7841  
7853 7867 7873 7877 7879 7883 7901 7907 7919 7927  
7933 7937 7949 7951 7963 7993 8009 8011 8017 8039  
8053 8059 8069 8081 8087 8089 8093 8101 8111 8117  
8123 8147 8161 8167 8171 8179 8191 8209 8219 8221  
8231 8233 8237 8243 8263 8269 8273 8287 8291 8293  
8297 8311 8317 8329 8353 8363 8369 8377 8387 8389  
8419 8423 8429 8431 8443 8447 8461 8467 8501 8513  
8521 8527 8537 8539 8543 8563 8573 8581 8597 8599  
8609 8623 8627 8629 8641 8647 8663 8669 8677 8681  
8689 8693 8699 8707 8713 8719 8731 8737 8741 8747  
8753 8761 8779 8783 8803 8807 8819 8821 8831 8837  
8839 8849 8861 8863 8867 8887 8893 8923 8929 8933  
8941 8951 8963 8969 8971 8999 9001 9007 9011 9013  
9029 9041 9043 9049 9059 9067 9091 9103 9109 9127  
9133 9137 9151 9157 9161 9173 9181 9187 9199 9203  
9209 9221 9227 9239 9241 9257 9277 9281 9283 9293  
9311 9319 9323 9337 9341 9343 9349 9371 9377 9391  
9397 9403 9413 9419 9421 9431 9433 9437 9439 9461  
9463 9467 9473 9479 9491 9497 9511 9521 9533 9539  
9547 9551 9587 9601 9613 9619 9623 9629 9631 9643  
9649 9661 9677 9679 9689 9697 9719 9721 9733 9739  
9743 9749 9767 9769 9781 9787 9791 9803 9811 9817  
9829 9833 9839 9851 9857 9859 9871 9883 9887 9901  
9907 9923 9929 9931 9941 9949 9967 9973
```

```
Time elapsed: 0.167000
```

Test with size 100,000:

```
99559 99563 99571 99577 99581 99607 99611 99623 99643 99661  
99667 99679 99689 99707 99709 99713 99719 99721 99733 99761  
99767 99787 99793 99809 99817 99823 99829 99833 99839 99859  
99871 99877 99881 99901 99907 99923 99929 99961 99971 99989  
99991
```

```
Time elapsed: 0.698000
```

Results of Testing Programs in Question 2

Algorithm	n	10,000	100,000
n/2		0.178	1.169
sqrt(n)		0.170	0.744
Eratosthenes		0.167	0.698

Note: The numbers above are the times measured in seconds. A second trial of 100,000 was performed because the times for size 10,000 were very quick and it was difficult to differentiate them significantly.

Observations: The slowest of the algorithms was the 1st one, which tested values from 1 to n/2 for each tested in the program. This was expected because the portion of values that were checked from sqrt(n) to n/2 were unnecessary. Because these unnecessary values were not checked in the second program where the loop terminated at sqrt(n), the second program ran faster. The difference in runtime is more pronounced in the 100,000-size test. The Eratosthenes algorithm was consistently faster than the sqrt(n) program, which was expected, but the difference in runtime between these programs was very slight, even in the test size of 100,000. This is likely because the sqrt(n) had certain optimizations implemented into its design, such as only testing odd numbers, and these implementations were not coded into the Eratosthenes design to follow the instructions on the programming assignment. It is likely that the Eratosthenes program would have a more noticeable difference in runtime to the sqrt(n) program if these optimizations were implemented into it.

Question 3

Problem Definition/Specification

A program is needed which will allow the user to control a “turtle” which can draw lines and shapes. The details are outlined in the project assignment page as well as Exercise 6.23.

Problem Analysis

The program is to allow the user to control a “turtle”, which moves through a grid, by inputting numbers to the program which correspond to functions. These functions include the ability to place down a pen, lift the pen up, turn left, turn right, move forward an indicated number of spaces, print out the full grid, and exit the program. The numbers corresponding to each function are shown in the programming assignment handout and are detailed in the Relations section below. Additionally, some additional functions may be implemented to allow for a greater ease of use for the programmer. Two additional functions that will be implemented include a help menu to help keep track of the different possible commands, and the ability to see the current position and direction of the cursor. With all the commands correctly implemented, the user of the program should be able to control the “turtle” on the screen and draw different shapes depending on whether the pen is currently down.

Program Inputs

- An integer command which tells the program what function to perform
- A number of spaces to move forward (only necessary if a move forward command is input)

Program Outputs

- A 20 x 20 grid with portions of the grid that have been “drawn” on labeled with an asterisk (*)
- Statements to indicate whether commands were successfully read and performed

Formula or Relations

- Command 1: Lift pen up
- Command 2: Place pen down
- Command 3: Turn to the right
- Command 4: Turn to the left
- Command 5, #: Move forward a number (#) of spaces
- Command 6: Print the grid
- Command 7: (Added by programmer) Print out a help menu
- Command 8: (Added by programmer) Print the current position and direction
- Command 9: Exit the program

Algorithm Design

Initial Algorithm

1. Initialize a 20x20 array of integers and set each position to 0
2. Read in a command from the user
3. Determine which function to be completed based on the input value
4. Perform the function based on the determination made
5. Allow the user to input a new command and repeat until the exit command is entered

Refinement

1. Create a 20x20 integer array and loop through its rows and column with a for loop to set each position to 0. Additionally, initialize the position to be (0,0) and set the initial direction to east.
2. Use a scanf() line to read in up to 2 integer inputs from the user (the command and the number of spaces to move if the command to move forward is given)
3. Use a series of if-else statements to determine what function should be performed based on the command input. See the previous Relations section to see how the input integers will map to each command
4. Within the if statement, perform the appropriate function, using methods if necessary
 - a. If the pen up command is given, set an integer value penIsDown to 0 (false) and print out a success message
 - b. If the pen down command is given, set an integer value penIsDown to 1 (true) and print out a success message
 - c. If turn right command is given, call the void method rightTurn(), which will update the direction the cursor is facing based on the current direction using a series of if-else statements. Directions will be referred to as north, south, east, and west
 - d. If turn left command is given, call the void method leftTurn(), which will update the direction the cursor is facing based on the current direction using a series of if-else statements. Directions will be referred to as north, south, east, and west
 - e. If the move forward command is given, first use a series of if-else statements to determine the current direction of the cursor. Then, based on this direction, increment the x or y value in the appropriate direction in a loop that last a number of times taken from the user's input. If during this loop a bound of the 20x20 array is reached, immediately exit the function. Regardless of how many spaces were input, output how many spaces were actually moved. All of this takes place in the integer method moveForward(int, int[][], int), which returns the number of spaces successfully moved
 - f. If the print grid command is given, loop through the entire 20x20 array and print an asterisk (*) wherever a 1 is found. Additionally, for ease of use, print out a plus sign (+) wherever the cursor is currently located by using an if statement that checks if the position in the loop is the current position of the cursor
 - g. If the help command is input, output a list of all the commands and their corresponding numbers

- h. If the print position command is given, print the current position and direction of the cursor
 - i. If the exit command is given, print out an end message and break out of the loop
 - j. If none of the above commands are given, display an error message and prompt the user to input a valid command
5. The program will continue to allow the user to input commands in a loop until the exit command is entered

Desk Checking/Test Plan

Ensuring this program works correctly requires more comprehensive testing than the previous programs in this assignment. First, the program will be used to create a shape in the console, including both right and left turns and alternations of the pen being down and up. In order to ensure the bounds have been correctly input, some values that would normally allow the cursor to go beyond the bounds of the grid will be tested. Each of the 9 commands will be tested at least once, with the more complex ones such as the move forward command being tested more often. Additionally, an invalid command will be tested in the program to ensure that it does not cause any unwanted side effects. If the program crashes or fails to print out the expected output, it can be determined that the program was not created correctly.

Implementation

```
1  /*
2  * Programmer: Kollin Labowski
3  * Date Completed: October 1, 2020
4  * Course: CS 350
5  * Description: This program allows the user to control a "turtle" by inputting a variety of commands that allow the
6  * turtle to draw shapes and lines when indicated by the user. Commands include the ability to raise and lower a pen
7  * that is used to draw the lines and shapes, the ability to turn either right or left, the ability to move forward
8  * a number of spaces, the ability to print out the grid, and the ability to exit the program. Additionally, 2 extra
9  * functions were added that were not required in the assignment document, these functions being the ability to display
10 * a help menu and the ability to display the current position and direction of the "turtle".
11 */
12
13 //Include Statements
14 #include <stdio.h>
15
16 //Constants used to indicate direction
17 const int EAST = 0;
18 const int SOUTH = 1;
19 const int WEST = 2;
20 const int NORTH = 3;
21
22 //Constants used to indicate size of grid
23 const int ROW_SIZE = 20;
24 const int COL_SIZE = 20;
25
26 //Function prototypes
27 void rightTurn();
28 void leftTurn();
29 void draw(int[][COL_SIZE]);
30 int moveForward(int numSpaces, int[][COL_SIZE]);
31 void drawGrid(int[][COL_SIZE]);
32
33 //Variables that are modified
34 int penIsDown = 0;
35 int xPos = 0;
36 int yPos = 0;
37 int direction = EAST;
38
39 //Main method
40 void main()
41 {
42     //The grid to be modified throughout the program
43     int grid[ROW_SIZE][COL_SIZE];
44
45     //Initialize the array to have all zeroes
46     for(int i = 0; i < ROW_SIZE; i++)
47         for(int j = 0; j < COL_SIZE; j++)
48             grid[i][j] = 0;
```

```
50     //Loops until a sentinel values is reached, in which case the loop is broken out of
51     while(1)
52     {
53         //Variables to track the input command and number of spaces if command 5 is input
54         int command;
55         int spaces;
56         printf("Please input a command: ");
57         scanf("%d, %d", &command, &spaces);
58
59         //If statements used to ensure the correct command is performed based on the input
60         if(command == 1)
61         {
62             //Brings pen up
63             penIsDown = 0;
64             printf("\nThe pen is now up...\n\n");
65         }
66         else if(command == 2)
67         {
68             //Puts pen down
69             penIsDown = 1;
70             draw(grid);
71             printf("\nThe pen is now down...\n\n");
72         }
73         else if(command == 3)
74         {
75             //Performs a right turn
76             rightTurn();
77             printf("\nTurned to the right...\n\n");
78         }
79         else if(command == 4)
80         {
81             //Performs a left turn
82             leftTurn();
83             printf("\nTurned to the left...\n\n");
84         }
85         else if(command == 5)
86         {
87             //Moves forward a number of spaces if possible
88             if((spaces >= ROW_SIZE && spaces >= COL_SIZE) || spaces < 0)
89                 printf("\nInvalid input for number of spaces...\n\n");
90             else
91             {
92                 int actualMovement = moveForward(spaces, grid);
93                 printf("\nMoved forward %d spaces...\n\n", actualMovement);
94             }
95         }
96     }
97 }
```

```
96     else if(command == 6)
97     {
98         //Prints out the full grid
99         printf("\nPrinting the grid below...\n\n");
100        drawGrid(grid);
101    }
102    else if(command == 7)
103    {
104        //Displays a help menu
105        printf("\n - Input 1 to move pen up");
106        printf("\n - Input 2 to move pen down");
107        printf("\n - Input 3 to turn right");
108        printf("\n - Input 4 to turn left");
109        printf("\n - Input 5 followed be a comma and a # to move a # of spaces forward");
110        printf("\n - Input 6 to print out the grid");
111        printf("\n - Input 7 to print this help menu");
112        printf("\n - Input 8 to print the current location and direction of \"turtle\"");
113        printf("\n - Input 9 to exit the program\n\n");
114    }
115    else if(command == 8)
116    {
117        //Displays the position and direction of the "turtle"
118        printf("\nCurrent position is (%d,%d)", xPos, yPos);
119        if(direction == EAST)
120            printf("\nCurrent direction is EAST\n\n");
121        else if(direction == SOUTH)
122            printf("\nCurrent direction is SOUTH\n\n");
123        else if(direction == WEST)
124            printf("\nCurrent direction is WEST\n\n");
125        else if(direction == NORTH)
126            printf("\nCurrent direction is NORTH\n\n");
127        else
128            printf("\nCurrent direction is UNKNOWN\n\n");
129    }
130    else if(command == 9)
131    {
132        //Exits the program
133        printf("\nExiting the program...\n");
134        break;
135    }
136    else
137    {
138        //Invalid input was received
139        printf("\nPlease enter a valid input (input 7 for help)... \n\n");
140    }
141}
142}
143}
```

```
144  /*
145  * This method allows the "turtle" to turn right by resetting the direction based on the current direction
146  */
147 void rightTurn()
148 {
149     if(direction == EAST)
150     {
151         direction = SOUTH;
152     }
153     else if(direction == SOUTH)
154     {
155         direction = WEST;
156     }
157     else if(direction == WEST)
158     {
159         direction = NORTH;
160     }
161     else if(direction == NORTH)
162     {
163         direction = EAST;
164     }
165 }
166
167 /*
168 * This method allows the "turtle" to turn left by resetting the direction based on the current direction
169 */
170 void leftTurn()
171 {
172     if(direction == EAST)
173     {
174         direction = NORTH;
175     }
176     else if(direction == SOUTH)
177     {
178         direction = EAST;
179     }
180     else if(direction == WEST)
181     {
182         direction = SOUTH;
183     }
184     else if(direction == NORTH)
185     {
186         direction = WEST;
187     }
188 }
```

```
190 /*
191 * This is a simple method which sets a position to 1 based on the current x and y position of the "turtle"
192 */
193 void draw(int grid[ROW_SIZE][COL_SIZE])
194 {
195     grid[yPos][xPos] = 1;
196 }
197 /*
198 * Allows the "turtle" to move forward a number of spaces as input by the user. If the pen is down, also draw along this line
199 */
200 int moveForward(int numSpaces, int grid[ROW_SIZE][COL_SIZE])
201 {
202     //Used to keep track of the amount of spaces ACTUALLY moved, which may differ from numSpaces if a bound is reached
203     int movementCount = 0;
204
205     //If statements used to output based on the current direction
206     if(direction == EAST)
207     {
208         for(int i = 0; i < numSpaces; i++)
209         {
210             if(xPos + 1 >= ROW_SIZE)
211                 return movementCount;
212
213             xPos += 1;
214             if(penIsDown)
215                 draw(grid);
216             movementCount++;
217         }
218     }
219     else if(direction == SOUTH)
220     {
221         for(int i = 0; i < numSpaces; i++)
222         {
223             if(yPos + 1 >= COL_SIZE)
224                 return movementCount;
225
226             yPos += 1;
227             if(penIsDown)
228                 draw(grid);
229             movementCount++;
230         }
231     }
232 }
```

```

233     else if(direction == WEST)
234     {
235         for(int i = 0; i < numSpaces; i++)
236         {
237             if(xPos - 1 < 0)
238                 return movementCount;
239
240             xPos -= 1;
241             if(penIsDown)
242                 draw(grid);
243             movementCount++;
244         }
245     }
246     else if(direction == NORTH)
247     {
248         for(int i = 0; i < numSpaces; i++)
249         {
250             if(yPos - 1 < 0)
251                 return movementCount;
252
253             yPos -= 1;
254             if(penIsDown)
255                 draw(grid);
256             movementCount++;
257         }
258     }
259     return movementCount;
260 }
261

```

```

262 /*
263 * Prints out the entire grid, using * to indicate positions of 1 and + to indicate the current location of the "turtle"
264 */
265 void drawGrid(int grid[ROW_SIZE][COL_SIZE])
266 {
267     for(int i = 0; i < ROW_SIZE; i++)
268     {
269         for(int j = 0; j < COL_SIZE; j++)
270         {
271             if(i == yPos && j == xPos)
272                 printf(" + ");
273             else
274             {
275                 if(grid[i][j] == 1)
276                     printf(" * ");
277                 else
278                     printf("   ");
279             }
280         }
281         printf("\n");
282     }
283 } //End of program

```

Testing

Test 1:

```
Please input a command: 6  
Printing the grid below...
```

```
+
```

```
Please input a command: 5, 4  
Moved forward 4 spaces...  
Please input a command: 6
```

```
Printing the grid below...
```

```
+
```

```
Please input a command: 2  
The pen is now down...
```

Note: The + sign is used to show the position of the cursor, and is not actually part of the array

```
Please input a command: 3
Turned to the right...
Please input a command: 5, 7
Moved forward 7 spaces...
Please input a command: 6
Printing the grid below...
*
*
*
*
*
*
*
+
+
```

```
Please input a command: 4
Turned to the left...
Please input a command: 5, 8
Moved forward 8 spaces...
```

```
Please input a command: 6
Printing the grid below...
*
*
*
*
*
*
*
* * * * * * * * +
```

```
Please input a command: 1
The pen is now up...
Please input a command: 3
Turned to the right...
Please input a command: 5,6
Moved forward 6 spaces...
Please input a command: 6
Printing the grid below...
*
*
*
*
*
*
*
* * * * * * * *
+
+
```

```
Please input a command: 4
Turned to the left...
Please input a command: 4
Turned to the left...
Please input a command: 5, 3
Moved forward 3 spaces...
Please input a command: 6
Printing the grid below...
```

```

*
*
*
*
*
*
*
* * * * * * * * *
```

```
+
```

```
Please input a command: 2
The pen is now down...
Please input a command: 8
Current position is (12,10)
Current direction is NORTH
Please input a command: 4
Turned to the left...
Please input a command: 5, 10
Moved forward 10 spaces...
```

```
Please input a command: 6
Printing the grid below...

*
*
*
*
*
*
*
* * * * * * * * * * *
+
* * * * * * * * * * *
```

```
Please input a command: 3
Turned to the right...
Please input a command: 8
Current position is (2,10)
Current direction is NORTH
Please input a command: 5, 13
Moved forward 10 spaces...
Please input a command: 6
Printing the grid below...

+ *
*
*
*
*
*
*
* * * * * * * * * * *
*
*
* * * * * * * * * * *
```

Note: A distance of 13 was entered, but it only moved a distance of 10. This is expected behavior when the cursor approaches the bounds of the array

```
Please input a command: 1  
The pen is now up...  
Please input a command: 3  
Turned to the right...  
Please input a command: 5, 12  
Moved forward 12 spaces...  
Please input a command: 6  
Printing the grid below...
```

```
* * * * * * * * * * * * * *  
* * * * * * * * * * * * * *  
* * * * * * * * * * * * * *  
* * * * * * * * * * * * * *  
* * * * * * * * * * * * * *  
* * * * * * * * * * * * * *  
* * * * * * * * * * * * * *  
* * * * * * * * * * * * * *  
* * * * * * * * * * * * * *
```

```
Please input a command: 2  
The pen is now down...  
Please input a command: 5, 1  
Moved forward 1 spaces...
```

Please input a command: 6

Printing the grid below...

Please input a command: 3

Turned to the right...

Please input a command: 5, 18

Moved forward 18 spaces...

Please input a command: 6

Printing the grid below...

Please input a command: 3

Turned to the right...

Please input a command: 5, 2

Moved forward 2 spaces...

Please input a command: 6

Printing the grid below...

Please input a command: 3

Turned to the right...

Please input a command: 5, 18

Moved forward 18 spaces...

Please input a command: 6

Printing the grid below...

+ * *

```
Please input a command: 4  
Turned to the left...  
  
Please input a command: 5, 11  
Moved forward 11 spaces...  
  
Please input a command: 6  
Printing the grid below...
```

Please input a command: 8

Current position is (2,0)
Current direction is WEST

Please input a command: 7

- Input 1 to move pen up
 - Input 2 to move pen down
 - Input 3 to turn right
 - Input 4 to turn left
 - Input 5 followed be a comma and a # to move a # of spaces forward
 - Input 6 to print out the grid
 - Input 7 to print this help menu
 - Input 8 to print the current location and direction of "turtle"
 - Input 9 to exit the program

Please input a command: 9

Exiting the program...