

Assignment 5

Kiran Kour

2022-11-05

Formulating the Goal Linear Programming model

Objective Function:

$$\text{Max } Z = 20x_1 + 15x_2 + 25x_3 - 6y_{1-} - 6y_{1+} - 3y_{2-}$$

Subject to :

Employment Level

$$6x_1 + 4x_2 + 5x_3 + y_{1-} - y_{1+} = 50$$

Earnings Next Year

$$8x_1 + 7x_2 + 5x_3 + y_{2-} - y_{2+} = 75$$

Non-negativity constraint

$$x_j \geq 0, \text{ where } j = 1, 2, 3$$

$$y_{i+} \geq 0, \text{ where } i = 1, 2$$

$$y_{i-} \geq 0, \text{ where } i = 1, 2$$

- Defining y1+ and y1- as the amount over (if any) and amount under (if any) the employment level goal.
- Defining y2+ and y2- in the same way for the goal regarding earnings next year.
- Defining x1, x2, and x3 as the production rates of Products 1, 2, and 3, respectively.

```
# Load the Library needed
library(lpSolveAPI)
library(lpSolve)

# Load the data
GP <- read.lp("emax.lp")
GP

## Model name:
##      x1      x2      x3      y1m      y1p      y2m      y2p
## Maximize    20    15    25     -6     -6     -3      0
## R1          6     4     5      1     -1      0      0 = 50
## R2          8     7     5      0      0      1     -1 = 75
## Kind        Std     Std     Std     Std     Std     Std     Std
## Type        Real    Real    Real    Real    Real    Real    Real
## Upper       Inf     Inf     Inf     Inf     Inf     Inf     Inf
## Lower        0      0      0      0      0      0      0

# Solving the Goal Programming
solve(GP)

## [1] 0
```

As we can confirm, the solver is giving 0 which means it is finding a solution.

```
#To get the objective solution
get.objective(GP)

## [1] 225
```

Here, we are maximizing the profit while minimizing other business goals like workforce and earnings. As this value shows, the penalty for not satisfying the goals on the objective function is 225.

```
# To get the variables solution
get.variables(GP)

## [1] 0 0 15 0 25 0 0
```

This order is from how the variables were written in the objective function. In our case, the results are as follows: $x_1 = 0$, $x_2 = 0$, $x_3 = 15$, $y_{1-} = 0$, $y_{1+} = 25$, $y_{2-} = 0$, $y_{2+} = 0$, which means that the earnings (y_2) expectations are fully satisfied. Regarding the workforce, the goal projected is exceeded by 25 and based on the total profit of product 3, it has a negative result on its profit by 15.