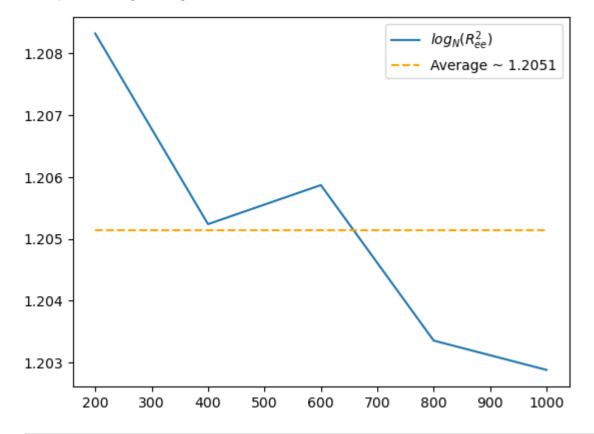
```
In [1]: import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
```

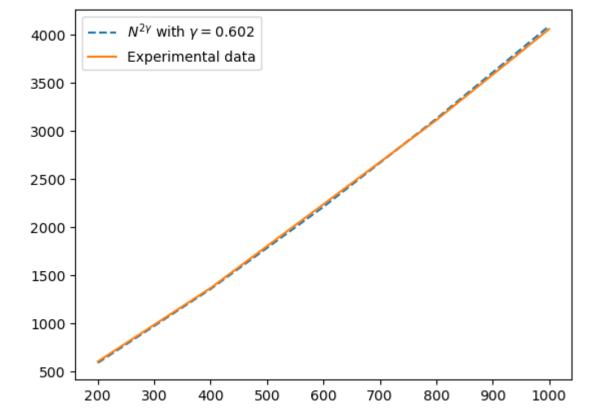
Exercise 2

Out[5]: <matplotlib.legend.Legend at 0x7faa451ea860>



```
In [6]: plt.plot(N, N**1.204, '--', label='$N^{2 \gamma}$ with $\gamma = 0.602$')
    plt.plot(N, R2ee, label='Experimental data')
    plt.legend()
```

Out[6]: <matplotlib.legend.Legend at 0x7faa3c6c7a90>

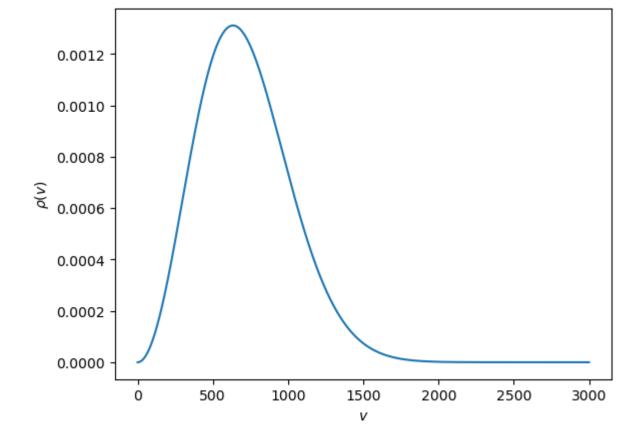


Exercise 4

```
In [7]: from scipy.constants import k, pi, N_A, h

In [8]: M = 60.08e-3 # kg/moL
    m = M / N_A
    T = 1450
    v = np.arange(0, 3e3)
    rho = (m / (2*pi*k*T))**1.5 * 4*pi*v*v*np.exp(-m*v*v/(2*k*T))

In [21]: plt.plot(v, rho)
    plt.xlabel('$v$')
    plt.ylabel('$\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\synt\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sq}
```



b)

Given: $ho(v)=4\pi\Big(rac{c}{2\pi}\Big)^{rac{3}{2}}v^2e^{-rac{cv^2}{2}},$ with $c=rac{m}{k_BT}$, calculate $\langle v
angle=\int_0^\infty v
ho(v)\,\mathrm{d}x.$

$$\Rightarrow \langle v \rangle = \int_0^\infty v \rho(v) \, \mathrm{d}x \tag{1}$$

$$= \int_0^\infty 4\pi \left(\frac{c}{2\pi}\right)^{\frac{3}{2}} f(v)g(v) \,\mathrm{d}x \tag{2}$$

$$=4\pi \left(\frac{c}{2\pi}\right)^{\frac{3}{2}} \int_0^\infty f(v)g(v) \,\mathrm{d}x \tag{3}$$

$$=4\pi \left(\frac{c}{2\pi}\right)^{\frac{3}{2}} \left(\left[f(v)G(v)\right]_0^{\infty} - \int_0^{\infty} 2vG(v) \,\mathrm{d}x\right) \tag{4}$$

$$= 4\pi \left(\frac{c}{2\pi}\right)^{\frac{3}{2}} \left(\underbrace{\left[-v^2 \frac{e^{-\frac{cv^2}{2}}}{c}\right]_0^{\infty}}_{\to 0} + \frac{2}{c} \int_0^{\infty} v^2 e^{-\frac{cv^2}{2}} \, \mathrm{d}x \right)$$
 (5)

$$=4\pi \left(\frac{c}{2\pi}\right)^{\frac{3}{2}} \frac{2}{c} \int_0^\infty v g(v) \, \mathrm{d}x \tag{6}$$

$$=4\pi \left(\frac{c}{2\pi}\right)^{\frac{3}{2}} \frac{2}{c} \left(\underbrace{\left[-v\frac{e^{-\frac{cv^2}{2}}}{c}\right]_0^{\infty}}_{\rightarrow 0} + \frac{1}{c}\underbrace{\int_0^{\infty} e^{-\frac{cv^2}{2}}}_{=1}\right)$$
(7)

$$=4\pi \left(\frac{c}{2\pi}\right)^{\frac{3}{2}}\frac{2}{c^2}\tag{8}$$

$$=2\frac{\pi}{\pi^{\frac{3}{2}}}\frac{\left(\frac{c}{2}\right)^{\frac{3}{2}}}{\left(\frac{c}{2}\right)^{2}}\tag{9}$$

$$=\sqrt{\frac{8}{c\pi}}\tag{10}$$

c)

$$\langle p \rangle = m \langle v \rangle = m \sqrt{\frac{8k_BT}{\pi m}} = \sqrt{\frac{8mk_BT}{\pi}} = \frac{2}{\pi} \sqrt{2\pi m k_BT} = \frac{2}{\pi} p_T$$
 (11)

$$\Rightarrow \lambda = \frac{\pi}{2} \lambda_T \tag{12}$$

d)

In [23]: wl = pi / 2 * h / np.sqrt(2 * pi * m * k * T) # m
bl = 1.6e-10 # m
print(f"The De Broglie wavelength of SiO2 is ~%d%% of the bond length. Therefore we ignore qua

The De Broglie wavelength of SiO2 is \sim 5% of the bond length. Therefore we ignore quantum effect s.