

(8)

- Given that 'm' is the maximum over all vertices, so, by the relax property, we can state that the vertex achieves its shortest path in v.d.
- By the upper-bound property, after m iterations, no d values will ever change.
- Therefore, no d values will change in (m+1) iteration.
- If we make 'm' iterations, we can't terminate the algorithm.
- Hence, we have to make 'm+1' iterations.
- We will set a flag after the Relax() and check if the edge is relaxed and pass w.

So, Relax(u, v, w)

if $v.d > u.d + w(u, v)$

$v.d = u.d + w(u, v)$

$v.prev = u$

visited = true

BELLMAN-FORD (G, w, s)

Initialize-single-source (G, s)

visited = true

while visited == true

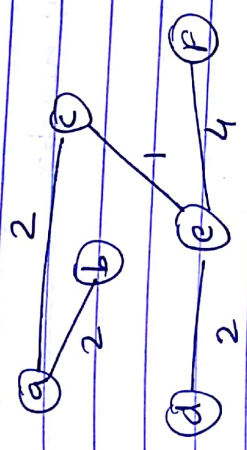
visited = false

for every edge (u, v, w)

Relax(u, v, w)

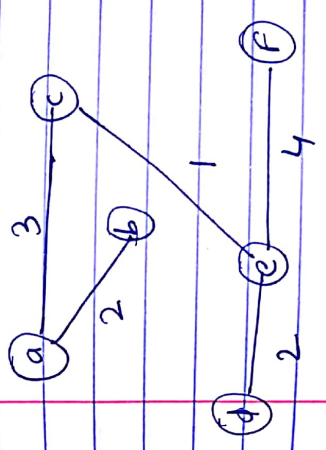
→ To take it out of the while loop (m+1) iterations are made.

for $x=2$

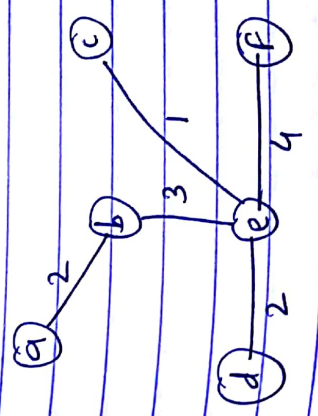


for $x=3$

→ if (a,c) is selected

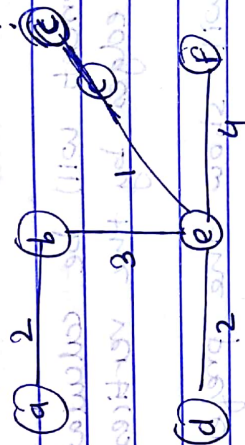


if (a,c) is not selected.



(4)

MST of tree T without considering x will be.

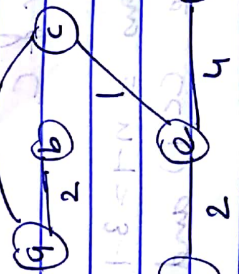


a) Since, all the vertices have been included and we want to keep the MST as T,

if $x > 3$, edge (a,c) won't be selected
 ∴ it will create a cycle for value of 4
 and if $x > 4$, (a,c) won't be selected for MST.

(b) so, if $x \leq 3$ we may get new MST other than T.

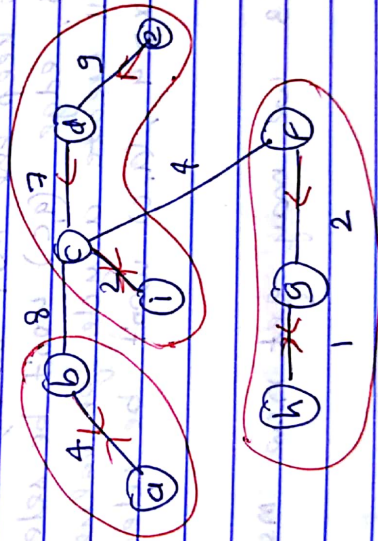
for $x = 1$



5

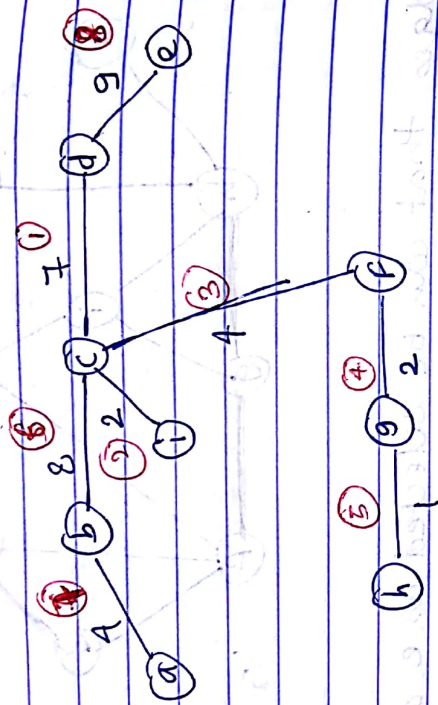
(c) Boruvka's algorithm:

- We need to find number of components for this algorithm.
- These components will be calculated by the selection of edges by the vertices.
- The arrows will show the preference.
- Non-connected components are independent components.



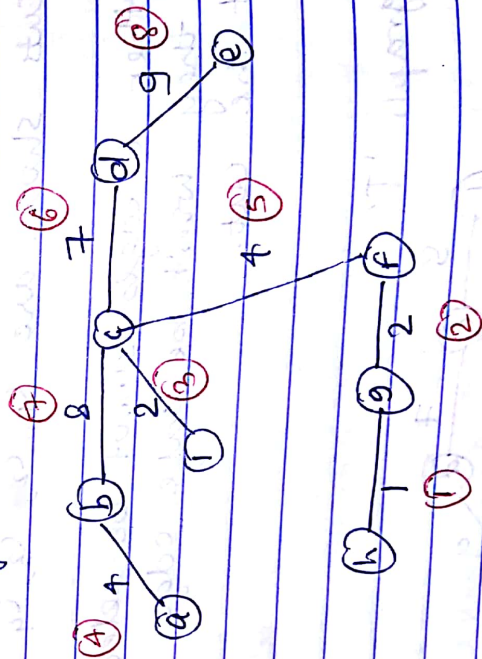
- Now, according to algorithm, find the min-weight (u,v) with $u \in C$ and $v \notin C$.
- Therefore, number of iterations $= n-1 = 3-1 = 2$ and edges found will be (c,f) and (b,c) in two iterations.

(a) Prim's algorithm starting with vertex d

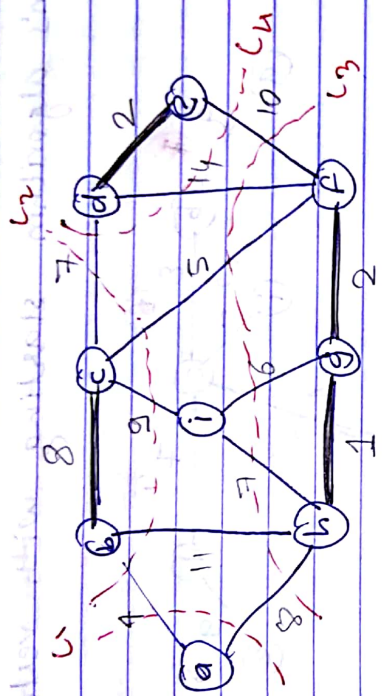


The numbers shown in red color depicts the order of edges selected.

(b) Kruskal's algorithm:



Number depicts the order of edges in which they were selected.



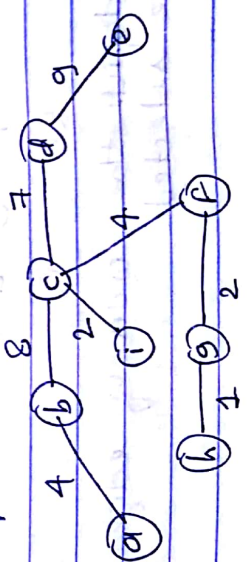
The edges that can be selected as e are:

- a) a-b
- b) c-f
- c) i-g
- d) c-d

The cuts shown are C_1, C_2, C_3, C_4 respectively.

The other 6 edges cannot be selected as 'e' since they won't be safe edge and respect the cut.

(3) Given graph 'T'



$$= 5 - 3 + 3 - 3$$

$$= 2$$

(A, D)

Case 2:

$m = n$, $m = n$, $m = n$, $m = n$

A = MALE, B = LAME

S = LG

$$\text{No. of operations} = m - 2 + n - 2 + 4 - 2$$

i) delete M

ii) delete L

iii) insert M

iv) insert L

Case 3:

$$m < n$$

B = SING, SINGER = A, S = SING, S = SING

$$\text{No. of operations} = m - 4 + n - 4$$

delete (E), delete (R)

1) A Given,

$$A.length = |A| = n$$

$$\text{and } B.length = |B| = m$$

Task: Convert $A \rightarrow B$ using:

- delete () \rightarrow deleting symbol from A.
- insert () \rightarrow inserting symbol at any position in A.

Show that:

minimum number of operations for $A \rightarrow B$ using algo for computing the longest common subsequence.

Let, s be the common longest subsequence of A and B .

Consider three cases:

$$i) m > n$$

$$ii) m = n$$

$$iii) m < n$$

$$(i) m > n$$

= when $m > n$

i.e. $B.length > A.length.$

$$\text{eg. } \underline{MADAM} + \underline{MAM} \quad (S = \underline{MAM} \quad s.length = 3)$$

so, to convert $A \rightarrow B$, we have to use insert()

Here, no. of symbols to be inserted will be.

$$m - s.length + n - s.length$$