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Experiment No.	3

AIM:	Divide and Conquer -Strassen's Matrix Multiplication
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Program 1

PROBLEM STATEMENT :	Use Strassen's Matrix Multiplication to multiply two matrices.
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ALGORITHM:	<p>Here is the procedure :</p> <ol style="list-style-type: none"> 1. Divide a matrix of the order of 2×2 recursively until we get the matrix of order 2×2. 2. To carry out the multiplication of the 2×2 matrix, use Strassen's Multiplication formulas i.e. <ul style="list-style-type: none"> a) $D1 = (a11 + a22) * (b11 + b22)$ b) $D2 = (a21 + a22) * b11$ c) $D3 = (b12 - b22) * a11$ d) $D4 = (b21 - b11) * a22$ e) $D5 = (a11 + a12) * b22$ f) $D6 = (a21 - a11) * (b11 + b12)$ g) $D7 = (a12 - a22) * (b21 + b22)$ <p> $C00 = d1 + d4 - d5 + d7$ $C01 = d3 + d5$ $C10 = d2 + d4$ $C11 = d1 + d3 - d2 - d6$ </p> <p>Here, C00, C01, C10, and C11 are the elements of the 2×2 matrix</p> <ol style="list-style-type: none"> 3. Subtraction is also performed within these seven multiplications and four additions.
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	<p>4. To find the final product or final matrix combine the result of two matrixes.</p>
PROGRAM:	<pre> #include <stdio.h> int main() { int a[2][2],b[2][2],c[2][2],i,j; int m1,m2,m3,m4,m5,m6,m7; // Here we are scanning and printing the first matrix printf("Enter the 4 elements of first matrix: "); for(i=0;i<2;i++) for(j=0;j<2;j++) scanf("%d",&a[i][j]); // Here we are scanning and printing the second matrix printf("Enter the 4 elements of second matrix: "); for(i=0;i<2;i++) for(j=0;j<2;j++) scanf("%d",&b[i][j]); printf("\nThe first matrix is\n"); for(i=0;i<2;i++) { printf("\n"); for(j=0;j<2;j++) printf("%d\t",a[i][j]); } printf("\nThe second matrix is\n"); for(i=0;i<2;i++){ printf("\n"); for(j=0;j<2;j++) printf("%d\t",b[i][j]); } // Here we are applying the above mentioned formulae m1= (a[0][0] + a[1][1])*(b[0][0]+b[1][1]); m2= (a[1][0]+a[1][1])*b[0][0]; m3= a[0][0]*(b[0][1]-b[1][1]); m4= a[1][1]*(b[1][0]-b[0][0]); m5= (a[0][0]+a[0][1])*b[1][1]; </pre>

	<pre> m6= (a[1][0]-a[0][0])*(b[0][0]+b[0][1]); m7= (a[0][1]-a[1][1])*(b[1][0]+b[1][1]); c[0][0]=m1+m4-m5+m7; c[0][1]=m3+m5; c[1][0]=m2+m4; c[1][1]=m1-m2+m3+m6; // As we got the value of the elements, we now print them printf("\n After performing multiplication \n"); for(i=0;i<2;i++){ printf("\n"); for(j=0;j<2;j++) printf("%d\t",c[i][j]); } return 0; } </pre>
OBSERVATION:	<p>In normal matrix multiplication method, the main component for high time complexity is 8 recursive calls. The idea of Strassen's method is to reduce the number of recursive calls to 7. Strassen's method divides matrices to sub-matrices of size $N/2 \times N/2$ and the four sub-matrices of result are calculated using above formulae.</p> <p>The time complexity for Strassen's Multiplication is: $T(N) = 7T(N/2) + O(N^2)$ on solving $O(N^{\log_2 7})$ which is approximately $O(N^{2.8074})$</p> <p>While that using normal method is: $T(N) = 8T(N/2) + O(N^2)$ on solving $O(N^3)$</p>
RESULT:	

```
Enter the 4 elements of first matrix: 2
```

```
4
```

```
3
```

```
8
```

```
Enter the 4 elements of second matrix: 1
```

```
6
```

```
9
```

```
5
```

```
The first matrix is
```

```
2      4
```

```
3      8
```

```
The second matrix is
```

```
1      6
```

```
9      5
```

```
After performing multiplication
```

```
38      32
```

```
75      58
```

```
...Program finished with exit code 0
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```
Press ENTER to exit console. 
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CONCLUSION:

In this experiment, we implemented Strassen's Multiplication.