

# CS114B (Spring 2023) Lab 10 Exercise

## Context-Free Grammars and CKY Algorithm

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You are given a small grammar on the next page. Your task is to use the probabilistic CKY algorithm to fill in the *table* and *back* arrays for the sentence “book that flight”. Please also draw the final tree for the sentence. Note that because the grammar is not in Chomsky normal form (it contains unary rules), you will need to modify the algorithm in Figure C.3 of the Jurafsky and Martin book to handle the unary rules.

```
function PROBABILISTIC-CKY(words,grammar) returns most probable parse
                                         and its probability
for j ← from 1 to LENGTH(words) do
  for all { A | A → words[j] ∈ grammar }
    table[j − 1, j, A] ← P(A → words[j])
  for i ← from j − 2 downto 0 do
    for k ← i + 1 to j − 1 do
      for all { A | A → BC ∈ grammar,
                and table[i, k, B] > 0 and table[k, j, C] > 0 }
        if (table[i, j, A] < P(A → BC) × table[i, k, B] × table[k, j, C]) then
          table[i, j, A] ← P(A → BC) × table[i, k, B] × table[k, j, C]
          back[i, j, A] ← {k, B, C}
  return BUILD_TREE(back[1, LENGTH(words), S], table[1, LENGTH(words), S])
```

**Figure C.3** The probabilistic CKY algorithm for finding the maximum probability parse of a string of *num\_words* words given a PCFG grammar with *num\_rules* rules in Chomsky normal form. *back* is an array of backpointers used to recover the best parse. The *build\_tree* function is left as an exercise to the reader.

## Grammar

Grammar		Lexicon	
$S \rightarrow NP VP$	[.80]	$Det \rightarrow that$ [.10]   $a$ [.30]   $the$ [.60]	
$S \rightarrow Aux NP VP$	[.15]	$Noun \rightarrow book$ [.10]   $trip$ [.30]	
$S \rightarrow VP$	[.05]	$meal$ [.05]   $money$ [.05]	
$NP \rightarrow Pronoun$	[.35]	$flight$ [.40]   $dinner$ [.10]	
$NP \rightarrow Proper-Noun$	[.30]	$Verb \rightarrow book$ [.30]   $include$ [.30]	
$NP \rightarrow Det Nominal$	[.20]	$prefer$ [.40]	
$NP \rightarrow Nominal$	[.15]	$Pronoun \rightarrow I$ [.40]   $she$ [.05]	
$Nominal \rightarrow Noun$	[.75]	$me$ [.15]   $you$ [.40]	
$Nominal \rightarrow Nominal Noun$	[.20]	$Proper-Noun \rightarrow Houston$ [.60]	
$Nominal \rightarrow Nominal PP$	[.05]	$NWA$ [.40]	
$VP \rightarrow Verb$	[.35]	$Aux \rightarrow does$ [.60]   $can$ [.40]	
$VP \rightarrow Verb NP$	[.20]	$Preposition \rightarrow from$ [.30]   $to$ [.30]	
$VP \rightarrow Verb NP PP$	[.10]	$on$ [.20]   $near$ [.15]	
$VP \rightarrow Verb PP$	[.15]	$through$ [.05]	
$VP \rightarrow Verb NP NP$	[.05]		
$VP \rightarrow VP PP$	[.15]		
$PP \rightarrow Preposition NP$	[1.0]		

**Figure C.1** A PCFG that is a probabilistic augmentation of the  $\mathcal{L}_1$  miniature English CFG grammar and lexicon of Fig. ?? . These probabilities were made up for pedagogical purposes and are not based on a corpus (any real corpus would have many more rules, so the true probabilities of each rule would be much smaller).