

# CINEMATICA EN 3D

[HELICE CIRCULAR](#)

[HELICE CONICA](#)

[ESPIRAL CONICA DE PAPUS](#)

[CURVA DE VIVIANI](#)

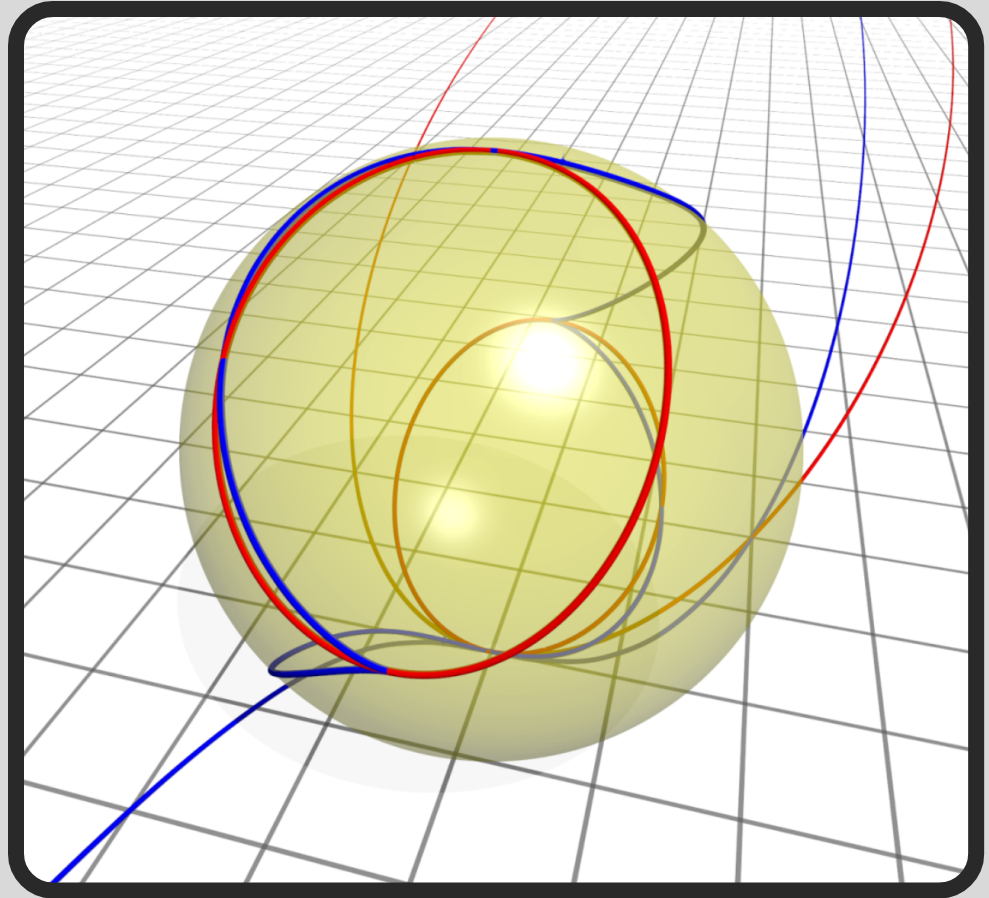
[HOROPTERO](#)

[HIPOPEDE DE EUDOXIO](#)

[CORONA SINUSOIDAL](#)

[CURVA DE ARQUITAS](#)

[CURVA BICILINDRICA](#)



**SALIR**

$a =$

$b =$

$\varepsilon =$

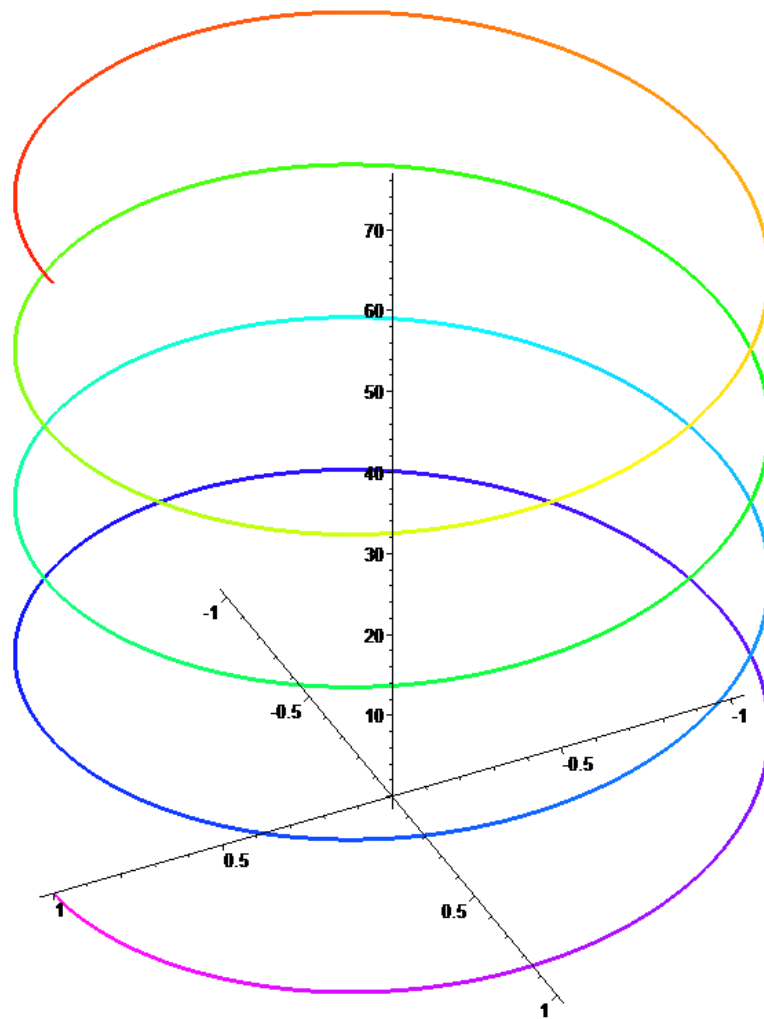
$\omega =$

**GRAFICO**

**CALCULAR**

**VOLVER**

**SALIR**



[POSICION](#)



**VELOCIDAD**

**VELOCIDAD MEDIA**

**ACELERACION**

**ACELERACION MEDIA**

**CURVATURA**

**RADIO DE CURVATURA**

**CENTRO DE CURVATURA**

**TORSION**

**RADIO DE TORSION**

**LONGITUD DE ARCO**

**VOLVER**

**MENU  
PRINCIPAL**

**SALIR**

$$\vec{r}(t) = (x(t), y(t), z(t)) = \begin{cases} x(t) = a \cos(\omega t) \\ y(t) = \varepsilon a \cos(\omega t) \\ z(t) = bt \end{cases} : \begin{cases} \varepsilon = 1 \\ \varepsilon = -1 \end{cases}$$

$$K = \frac{|r'(t) \times r''(t)|}{|r'(t)|^3} = \frac{|a|}{a^2 + b^2} = \frac{1}{\rho}$$

$$R_c = \rho = a + \frac{b^2}{|a|} = \frac{a^2 + b^2}{|a|} = \frac{c^2}{|a|}$$

$$T = \frac{\left( r'(t), r''(t), \frac{d^3 \vec{r}(t)}{dt^3}(t) \right)}{\left[ r'(t) \times r''(t) \right]^3} = \frac{b}{a^2 + b^2}$$

$$C_c = (x_c, y_c, z_c) = \begin{cases} x_c(t) = -\frac{b^2}{a} \cos(\omega t) \\ y_c(t) = -\frac{b^2}{a} \sin(\omega t) \\ z_c(t) = bt \end{cases}$$

$$R_t = \varepsilon \left( b + \frac{a^2}{b} \right) = \varepsilon \frac{c^2}{b}$$

$$L(0, t_0) = \int_0^{t_0} \sqrt{\left[ \frac{dx(t)}{dt} \right]^2 + \left[ \frac{dy(t)}{dt} \right]^2 + \left[ \frac{dz(t)}{dt} \right]^2} = t_0 \sqrt{a^2 + b^2}$$



$a =$

$\alpha =$

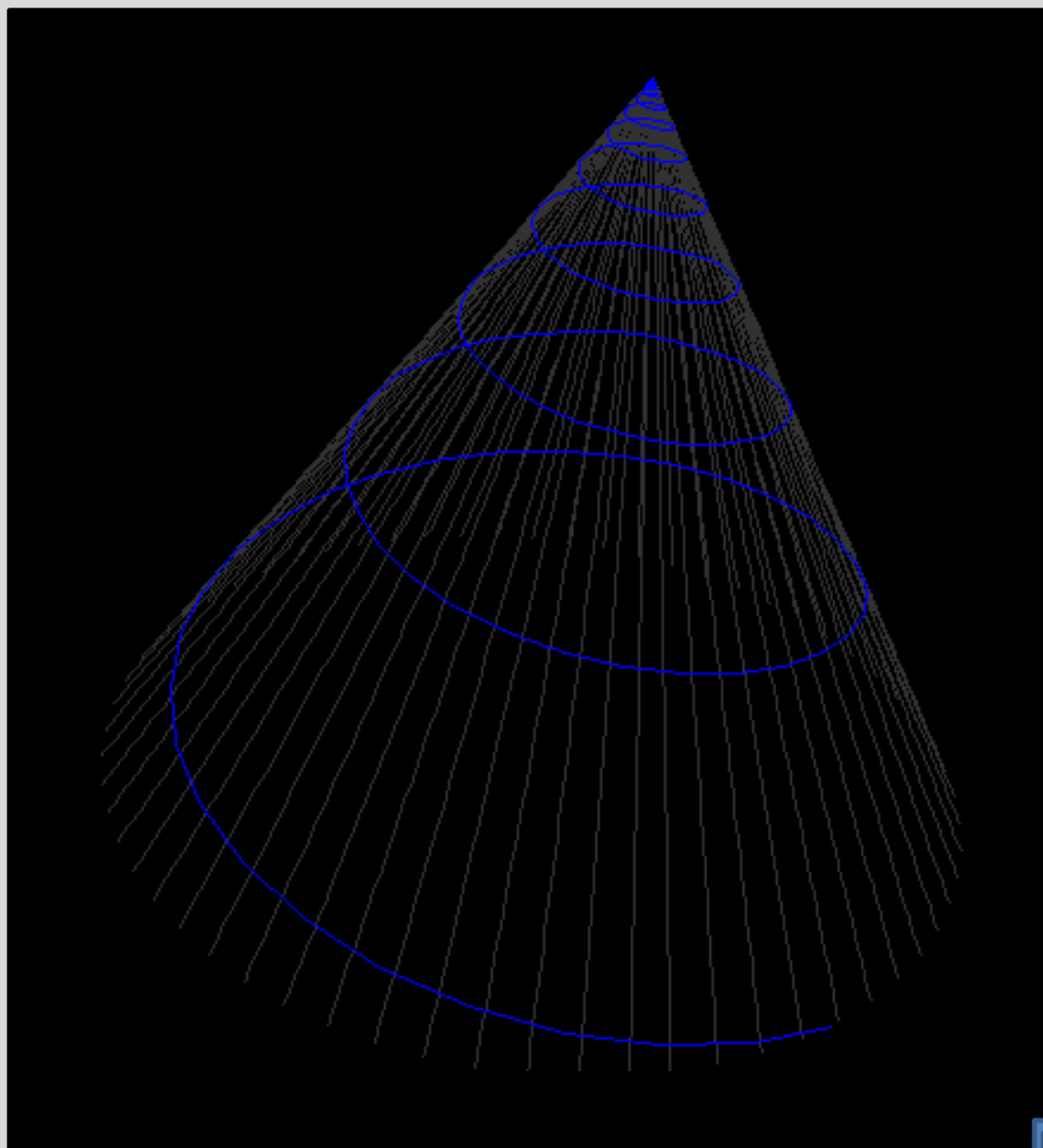
$\beta =$

**GRAFICO**

**CALCULAR**

**VOLVER**

**SALIR**



[POSICION](#)



**VELOCIDAD**

**VELOCIDAD MEDIA**

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$$\vec{r}(t) = (x(t), y(t), z(t)) = \begin{cases} x(t) = ae^{kt}\cos(t) \\ y(t) = ae^{kt}\sin(t) \\ z(t) = ae^{kt}\cot(t) \end{cases} : k = \sin(\alpha)\cot(\beta)$$



$a =$

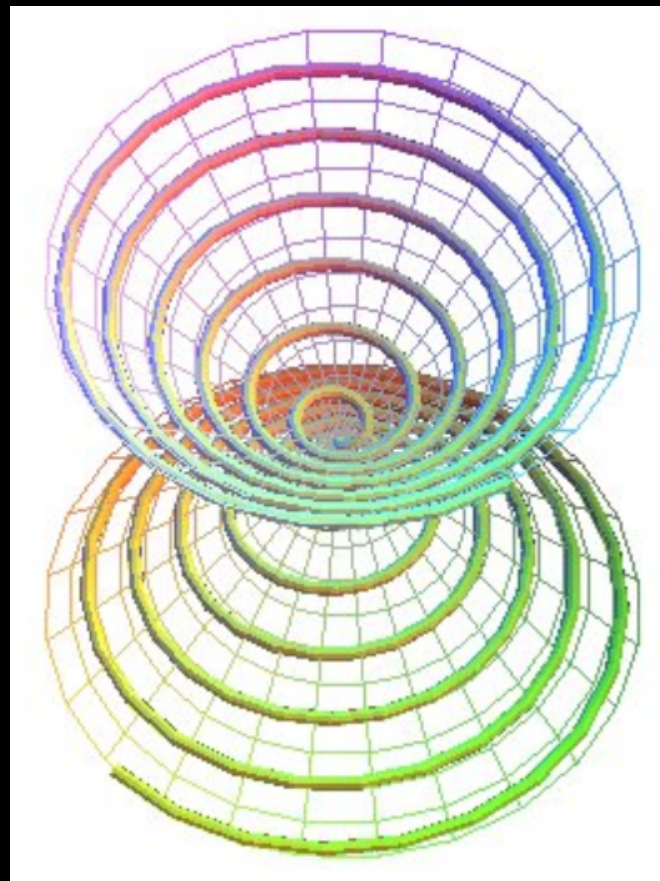
$\alpha =$

**GRAFICO**

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[POSICION](#)



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$$\vec{r}(t) = (x(t), y(t), z(t)) = \begin{cases} x(t) = a(\sin\alpha)t\cos(t) \\ y(t) = a(\sin\alpha)t\sin(t) \\ z(t) = a(\cos\alpha)t \end{cases}$$



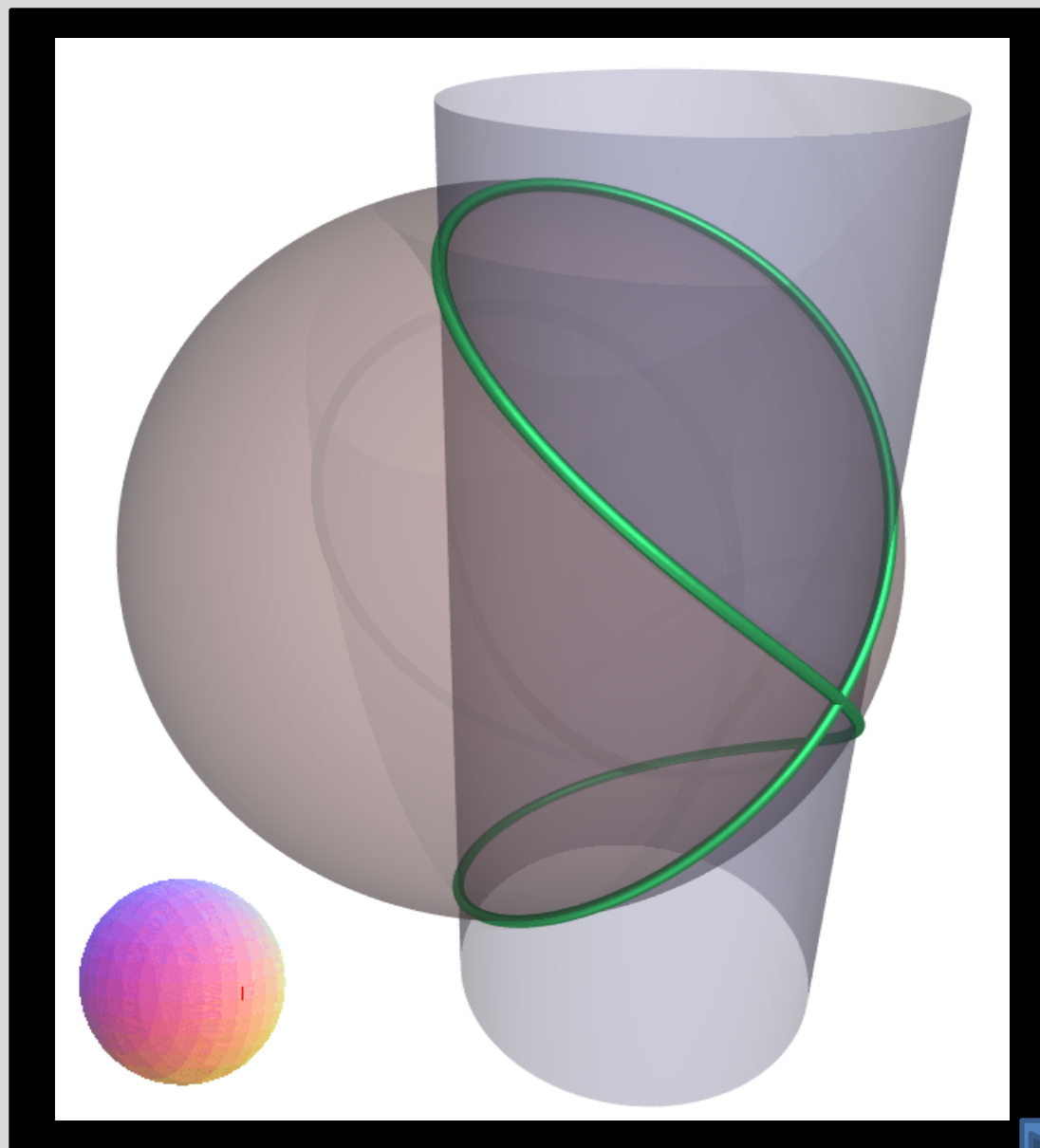
$a =$

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[POSICION](#)



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$$\vec{r}(t) = (x(t), y(t), z(t)) = \begin{cases} x(t) = a + a\cos(t) \\ y(t) = a\sin(t) \\ z(t) = 2a\sin\left(\frac{t}{2}\right) \end{cases}$$

$$R_c = \rho = 2a \frac{\left[1 + \cos^2\left(\frac{t}{2}\right)\right]^{\frac{3}{2}}}{\sqrt{5 + 3\cos^2\left(\frac{t}{2}\right)}}$$

$$R_t = a \left[ \cos\left(\frac{t}{2}\right) + \frac{5}{3} \left( \cos\left(\frac{t}{2}\right) \right)^{-1} \right]$$



$a =$

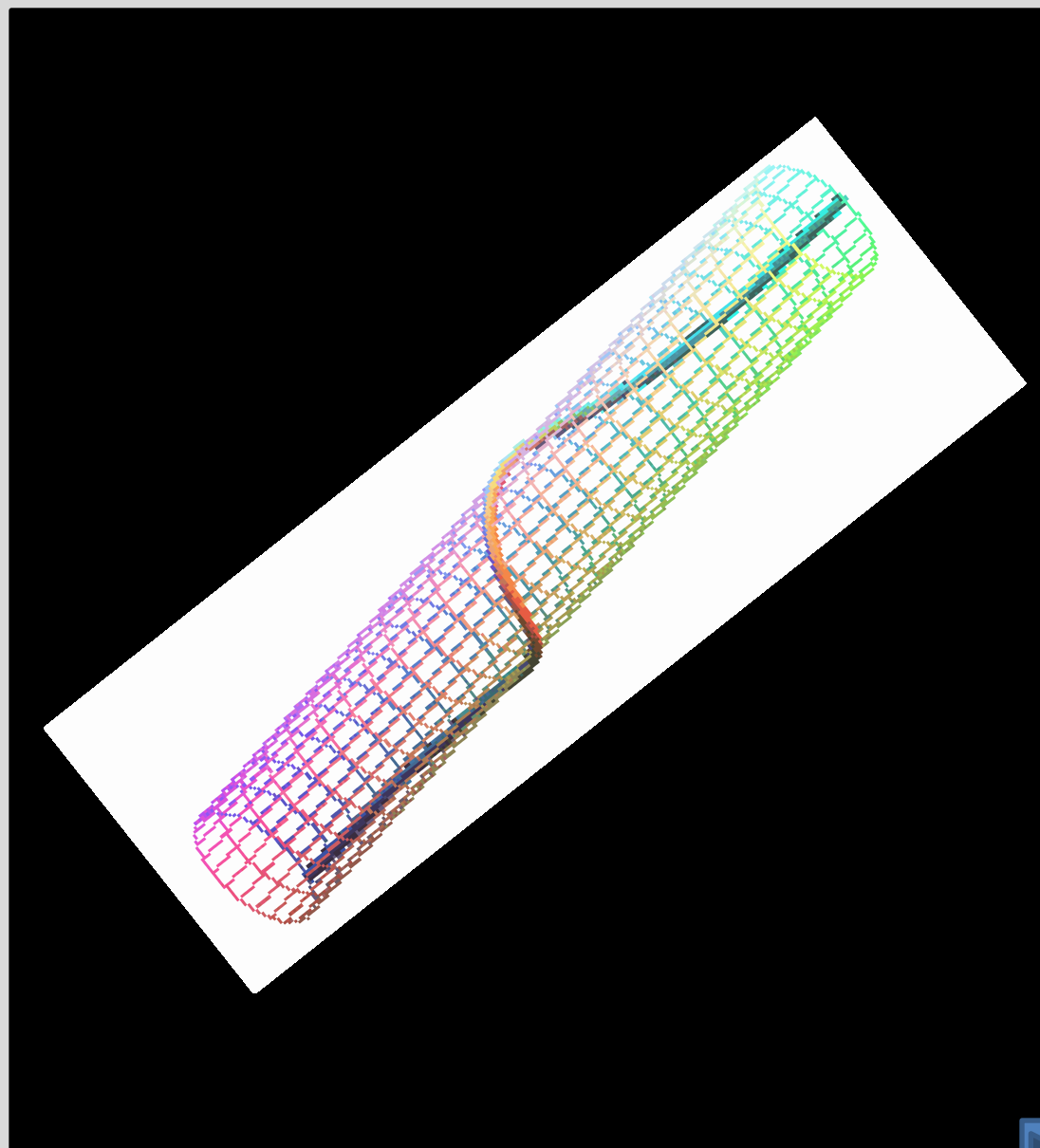
$b =$

**GRAFICO**

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[POSICION](#)



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$$\vec{r}(t) = (x(t), y(t), z(t)) = \begin{cases} x(t) = a + a\cos(t) \\ y(t) = b\tan\left(\frac{t}{2}\right) \\ z(t) = a\sin(t) \end{cases}$$





$a =$

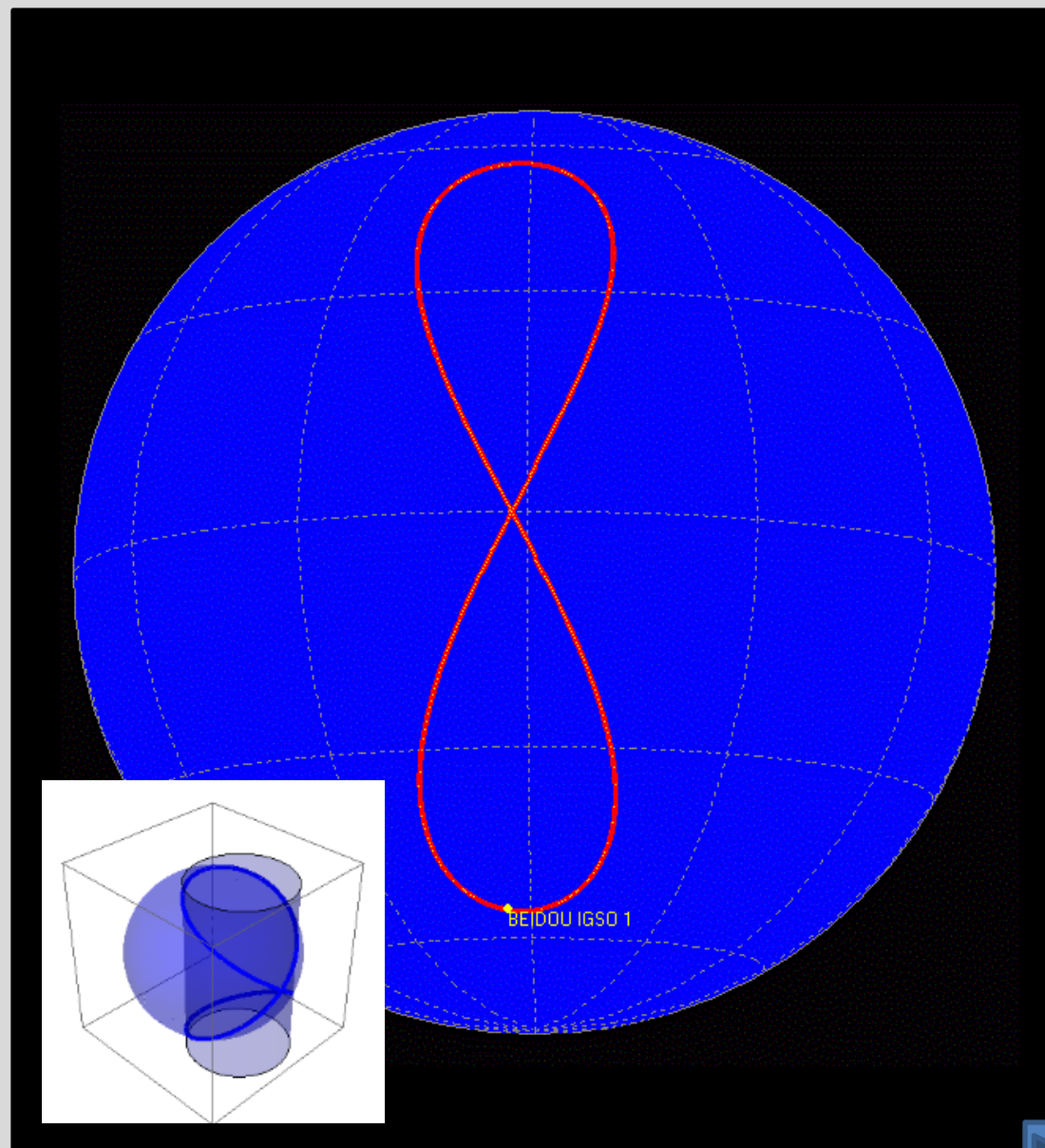
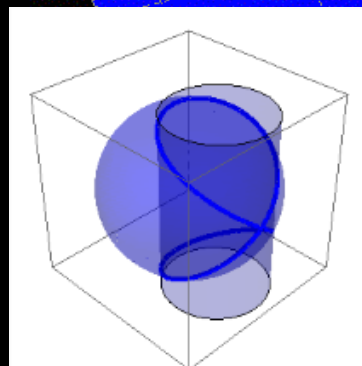
$b =$

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$$\vec{r}(t) = (x(t), y(t), z(t)) = \begin{cases} x(t) = a + (R - a)\cos(t) \\ y(t) = (R - a)\sin(t) \\ z(t) = 2\sqrt{a(R - a)}\sin\left(\frac{t}{2}\right) \end{cases}$$



$a =$

$b =$

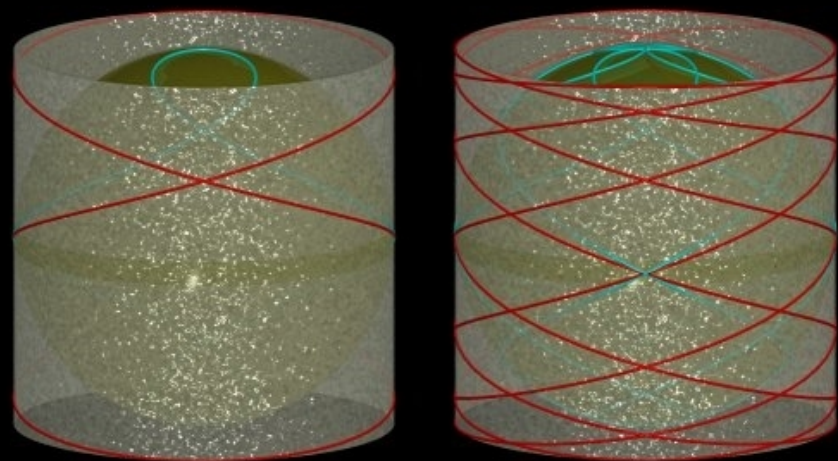
$n =$

GRAFICO

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$$\vec{r}(t) = (x(t), y(t), z(t)) = \begin{cases} x(t) = a \cos(t) \\ y(t) = a \sin(t) \\ z(t) = b \cos(nt) \quad : n > 0 \end{cases}$$

$$R_c = -a \frac{[1 + n^2 \sin^2(nt)]^{\frac{3}{2}}}{\sqrt{1 + n^2 \sin^2(nt) + n^4 \cos^2(nt)}}$$

$$R_t = a \frac{1 + n^2 \sin^2(nt) + n^4 \cos^2(nt)}{n(n^2 - 1) \sin(nt)}$$



$a =$

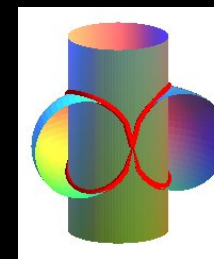
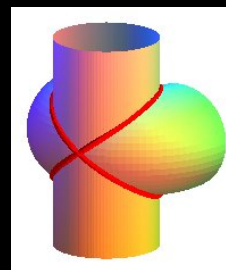
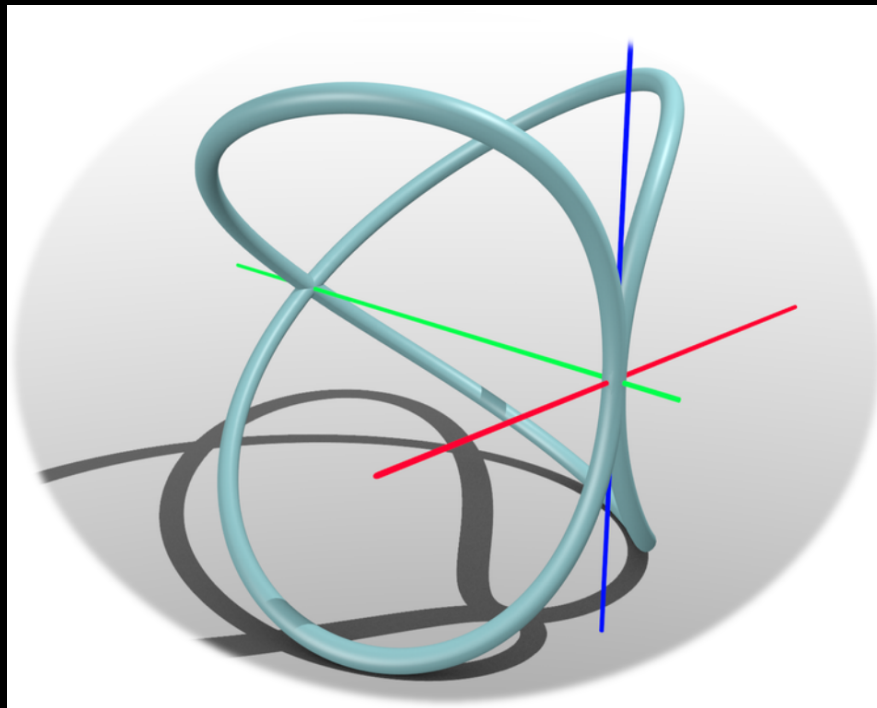
$-\frac{\pi}{2} \leq t =$    $\leq \frac{\pi}{2}$

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$$\vec{r}(t) = (x(t), y(t), z(t)) = \begin{cases} x(t) = a \cos^2(t) \\ y(t) = a \cos(t) \sin(t) \\ z(t) = \pm a \sqrt{[1 - \cos(t)] \cos(t)} \\ -\frac{\pi}{2} \leq t \leq \frac{\pi}{2} \end{cases}$$



$a =$

$b =$

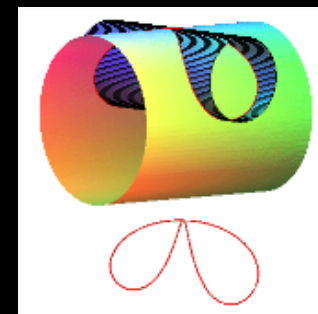
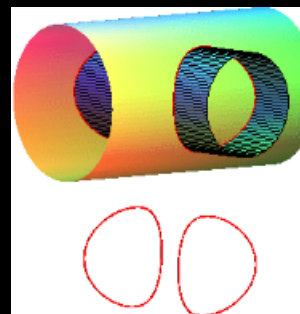
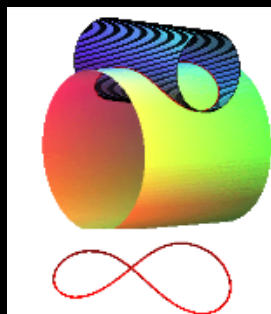
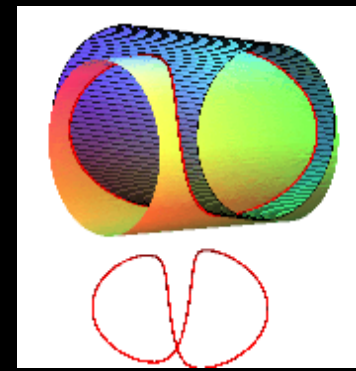
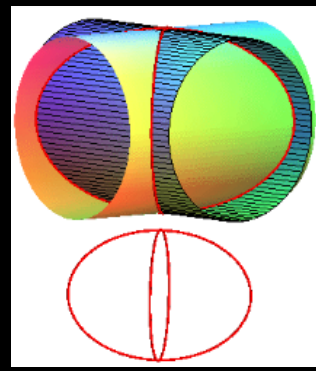
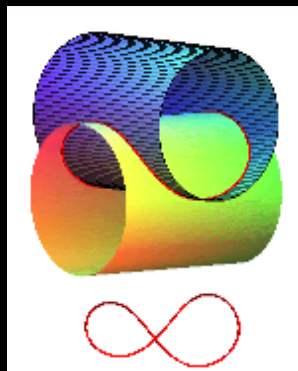
$c =$

GRAFICO

CALCULAR

VOLVER

SALIR



[POSICION](#)



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**SALIR**

$$\vec{r}(t) = (x(t), y(t), z(t)) = \begin{cases} x(t) = a \cos(t) \\ y(t) = \pm \sqrt{b^2 - [2c + a \sin(t)]^2} \\ z(t) = c + a \sin(t) \end{cases}$$

