

PSTAT127 Homework 4

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1)

- (e) Fit a Poisson response model for the number of incidents with the predictors: log of service, type, year and period. Test whether the parameter associated with the service term can be one. Explain why we are interested in such a test

```
library(MASS)
```

```
?ships
```

```
ships
```

##	type	year	period	service	incidents
## 1	A	60	60	127	0
## 2	A	60	75	63	0
## 3	A	65	60	1095	3
## 4	A	65	75	1095	4
## 5	A	70	60	1512	6
## 6	A	70	75	3353	18
## 7	A	75	60	0	0
## 8	A	75	75	2244	11
## 9	B	60	60	44882	39
## 10	B	60	75	17176	29
## 11	B	65	60	28609	58
## 12	B	65	75	20370	53
## 13	B	70	60	7064	12
## 14	B	70	75	13099	44
## 15	B	75	60	0	0
## 16	B	75	75	7117	18
## 17	C	60	60	1179	1
## 18	C	60	75	552	1
## 19	C	65	60	781	0
## 20	C	65	75	676	1
## 21	C	70	60	783	6
## 22	C	70	75	1948	2
## 23	C	75	60	0	0
## 24	C	75	75	274	1
## 25	D	60	60	251	0
## 26	D	60	75	105	0
## 27	D	65	60	288	0
## 28	D	65	75	192	0
## 29	D	70	60	349	2
## 30	D	70	75	1208	11
## 31	D	75	60	0	0
## 32	D	75	75	2051	4
## 33	E	60	60	45	0
## 34	E	60	75	0	0
## 35	E	65	60	789	7
## 36	E	65	75	437	7
## 37	E	70	60	1157	5
## 38	E	70	75	2161	12

```
## 39    E    75    60      0      0
## 40    E    75    75    542     1

library(tidyverse)

## -- Attaching packages ----- tidyverse 1.2.1 --

## v ggplot2 3.0.0    v purrr  0.2.5
## v tibble  1.4.2    v dplyr  0.7.6
## v tidyr   0.8.1    v stringr 1.3.1
## v readr   1.1.1    v forcats 0.3.0

## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()    masks stats::lag()
## x dplyr::select() masks MASS::select()

cleanships <- ships %>% filter(service != 0)
modelfit1 <- glm(incidents ~ log(service) + type + year + period, data = cleanships, family = poisson)
summary(modelfit1)

##
## Call:
## glm(formula = incidents ~ log(service) + type + year + period,
##      family = poisson, data = cleanships)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.2355  -1.0345  -0.4454   0.6005   2.8353
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -8.616856   1.528004  -5.639 1.71e-08 ***
## log(service)   0.886469   0.099297   8.927 < 2e-16 ***
## typeB         -0.330248   0.261301  -1.264  0.2063
## typeC         -0.736295   0.341342  -2.157  0.0310 *
## typeD         -0.284220   0.291989  -0.973  0.3304
## typeE          0.335936   0.242645   1.384  0.1662
## year           0.035468   0.013802   2.570  0.0102 *
## period        0.022079   0.008114   2.721  0.0065 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
##      Null deviance: 614.539  on 33  degrees of freedom
## Residual deviance:  58.114  on 26  degrees of freedom
## AIC: 171.98
##
## Number of Fisher Scoring iterations: 5
```

When we inspect the data closely, we notice that the log of the service is in a close enough range to 1, it is possible to model our rate in which in this case is incidents. This is because we hold constant the count response by using the Poisson regression while keeping the coefficient with offset. Thus incident damage is correlated to service by the data upon further inspection.

(f) Fit the Poisson rate model with all two-way interactions of the three predictors. Does this model fit the

```

data?
modelfit2 <- glm(incidents ~ (type + year + period)^2, data = cleanships, family = poisson(link = "log"),
modelfit2

##
## Call:  glm(formula = incidents ~ (type + year + period)^2, family = poisson(link = "log"),
##       data = cleanships, offset = log(service))
##
## Coefficients:
## (Intercept)      typeB      typeC      typeD      typeE
## -34.656444    -0.122240    -0.550223     2.233244    15.123276
##      year      period  typeB:year  typeC:year  typeD:year
##   0.407120   0.367583   0.005232   0.090512  -0.058216
## typeE:year typeB:period typeC:period typeD:period typeE:period
##  -0.220308  -0.010416  -0.091131   0.023830   0.006272
## year:period
##   -0.005096
##
## Degrees of Freedom: 33 Total (i.e. Null);  18 Residual
## Null Deviance:      146.3
## Residual Deviance: 32.12    AIC: 162

summary(modelfit2)

##
## Call:
## glm(formula = incidents ~ (type + year + period)^2, family = poisson(link = "log"),
##       data = cleanships, offset = log(service))
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -1.8476  -1.0609  -0.1118   0.3878   2.0800
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept) -34.656444  10.105973  -3.429 0.000605 ***
## typeB        -0.122240   3.451462  -0.035 0.971747
## typeC        -0.550223   6.321104  -0.087 0.930635
## typeD         2.233244   5.577499   0.400 0.688860
## typeE        15.123276   5.234048   2.889 0.003860 **
## year          0.407120   0.147188   2.766 0.005675 **
## period        0.367583   0.133900   2.745 0.006047 **
## typeB:year     0.005232   0.048638   0.108 0.914339
## typeC:year     0.090512   0.093349   0.970 0.332239
## typeD:year    -0.058216   0.076622  -0.760 0.447385
## typeE:year    -0.220308   0.077925  -2.827 0.004696 **
## typeB:period  -0.010416   0.028935  -0.360 0.718873
## typeC:period  -0.091131   0.048570  -1.876 0.060619 .
## typeD:period   0.023830   0.061210   0.389 0.697048
## typeE:period   0.006272   0.036799   0.170 0.864658
## year:period  -0.005096   0.001912  -2.666 0.007679 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)

```

```
##
## Null deviance: 146.328 on 33 degrees of freedom
## Residual deviance: 32.116 on 18 degrees of freedom
## AIC: 161.98
##
## Number of Fisher Scoring iterations: 6
```

Yes it does fit the model, no predictors need to be dropped as none are significant as the p value is very close to 1 or is 1, which means we always reject the null hypothesis

- (h) Now fit the rate model with just the main effects and compare it to the interaction model. Which model is preferred?

```
modelfit3 <- glm(incidents ~ period + year + type, family = poisson(link = "log"),
  data = cleanships, offset = log(service))
summary(modelfit3)
```

```
##
## Call:
## glm(formula = incidents ~ period + year + type, family = poisson(link = "log"),
## data = cleanships, offset = log(service))
##
## Deviance Residuals:
## Min 1Q Median 3Q Max
## -2.5348 -0.9319 -0.3686 0.4654 2.8833
##
## Coefficients:
## Estimate Std. Error z value Pr(>|z|)
## (Intercept) -10.079076 0.876149 -11.504 < 2e-16 ***
## period 0.023705 0.008091 2.930 0.003392 **
## year 0.042247 0.012826 3.294 0.000988 ***
## typeB -0.546090 0.178415 -3.061 0.002208 **
## typeC -0.632631 0.329500 -1.920 0.054862 .
## typeD -0.232257 0.287979 -0.807 0.419951
## typeE 0.405975 0.234933 1.728 0.083981 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
## Null deviance: 146.328 on 33 degrees of freedom
## Residual deviance: 59.375 on 27 degrees of freedom
## AIC: 171.24
##
## Number of Fisher Scoring iterations: 5
```

Here we can use the Akaike Information Criteria and compare the 2nd and 3rd model. Under the second model we have it so that our AIC is 165 whereas this new third model has a AIC score of 146, which is smaller than the second. Thus the third model is superior under the Akaike information criterion.

- (i) Fit quasi Poisson versions of the two previous models and repeat the comparison.

```
#model with no interaction effects
modelfit4 <- glm(incidents ~ period + year + type, family = quasipoisson(link = "log"),
  data = cleanships, offset = log(service))
summary(modelfit4)
```

```
##
## Call:
## glm(formula = incidents ~ period + year + type, family = quasipoisson(link = "log"),
##      data = cleanships, offset = log(service))
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.5348  -0.9319  -0.3686   0.4654   2.8833
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -10.07908    1.36829  -7.366 6.35e-08 ***
## period       0.02370    0.01264   1.876  0.0715 .
## year         0.04225    0.02003   2.109  0.0443 *
## typeB       -0.54609    0.27863  -1.960  0.0604 .
## typeC       -0.63263    0.51458  -1.229  0.2295
## typeD       -0.23226    0.44974  -0.516  0.6098
## typeE        0.40597    0.36690   1.107  0.2783
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for quasipoisson family taken to be 2.438934)
##
## Null deviance: 146.328 on 33 degrees of freedom
## Residual deviance: 59.375 on 27 degrees of freedom
## AIC: NA
##
## Number of Fisher Scoring iterations: 5
```

#model with interaction effects

```
modelfit5 <- glm(incidents ~ (type + year + period)^2, data = cleanships, family = quasipoisson(link =
summary(modelfit5)
```

```
##
## Call:
## glm(formula = incidents ~ (type + year + period)^2, family = quasipoisson(link = "log"),
##      data = cleanships)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -3.5599  -1.7315  -0.2022   0.6934   3.4047
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -8.2059461 20.4138758  -0.402  0.6924
## typeB       15.9400228  6.4500394   2.471  0.0237 *
## typeC        7.8666610 11.7094385   0.672  0.5102
## typeD       -5.0890756 12.3807857  -0.411  0.6859
## typeE        9.9483213  8.5534776   1.163  0.2600
## year         0.1094585  0.3004308   0.364  0.7199
## period       0.0061575  0.2762598   0.022  0.9825
## typeB:year   -0.1781189  0.0880348  -2.023  0.0582 .
## typeC:year   -0.0313661  0.1784830  -0.176  0.8625
## typeD:year    0.0145165  0.1552573   0.093  0.9265
## typeE:year   -0.1486057  0.1319298  -1.126  0.2748
```

```
## typeB:period -0.0289428 0.0678055 -0.427 0.6746
## typeC:period -0.1003367 0.1196822 -0.838 0.4128
## typeD:period 0.0434932 0.1398779 0.311 0.7594
## typeE:period 0.0024020 0.0926317 0.026 0.9796
## year:period 0.0004291 0.0039691 0.108 0.9151
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for quasipoisson family taken to be 5.565217)
##
## Null deviance: 614.54 on 33 degrees of freedom
## Residual deviance: 109.75 on 18 degrees of freedom
## AIC: NA
##
## Number of Fisher Scoring iterations: 7
```

```
#model comparison
```

```
anova(modelfit4, modelfit5, test = "F")
```

```
## Analysis of Deviance Table
```

```
##
## Model 1: incidents ~ period + year + type
## Model 2: incidents ~ (type + year + period)^2
## Resid. Df Resid. Dev Df Deviance F Pr(>F)
## 1 27 59.375
## 2 18 109.748 9 -50.373
```

With observe a p-value of .2454 between our comparisons of our two quasi poisson models, this indicates that at a .05 alpha level, we fail to reject the null hypothesis of the main effects models being better. Thus we conclude main effects “modelfit4” quasi poisson is preferred. We note that there exists

- (j) Interpret the coefficients of the main effects of the quasi-Poisson model. What factors are associated with higher and lower rates of damage incidents?

```
#for coefficients tpe b and e
exp(0.32558 - (-0.54334))
```

```
## [1] 2.384334
```

```
#periods
exp(0.38447)
```

```
## [1] 1.468836
```

Given the information above, we observe that boats that are of type B and have lower incident rates compared to those that are from type E and D. Based on the data, we know that that type E boats are 2.38 (rounded value) or about twice as likely to get into an incident that ships of type B.

we observe that the rate of incident increases by 1.467, meaning that ships built after 1964 and before 1974 have higher chance of incident, where ships built before have lower incident rates. This is perhaps because older ships were perhaps easier to navigate/maintain since the technology was well known, whereas newer ships with newer tech are harder to maintain since not many people have expertise with recent tech by nature.

2)

```
# not the same as the S-PLUS dataset
```

```
select <- MASS::select #needed to define select here since tidyverse and Mass interfere with each other
longley
```

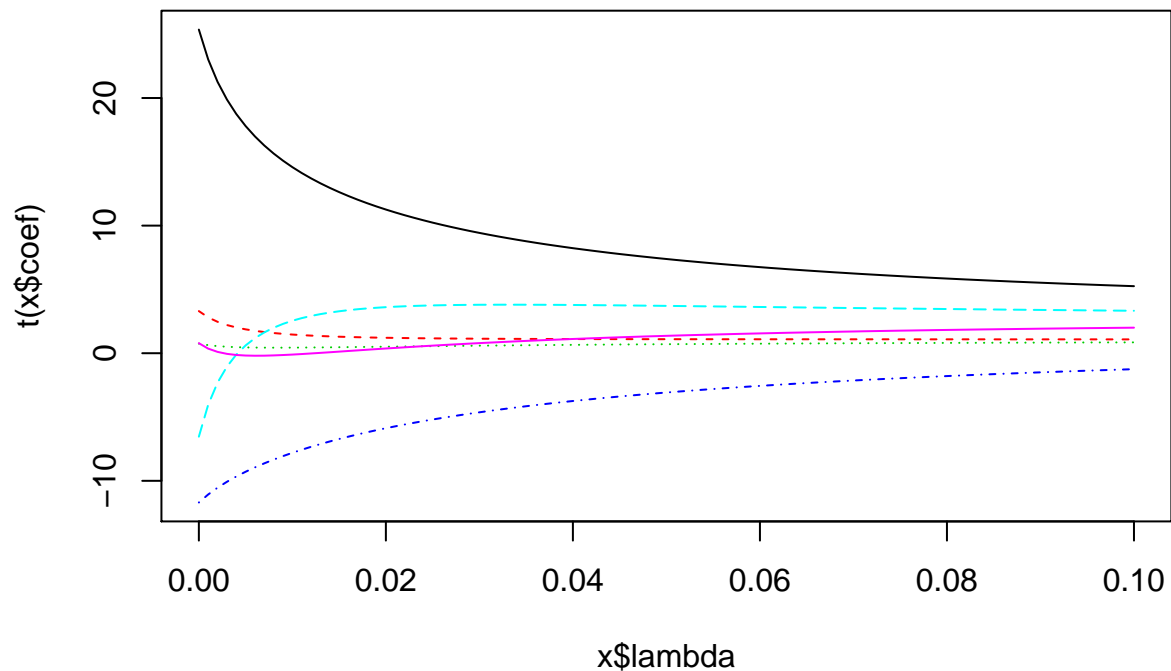
```
## GNP.deflator GNP Unemployed Armed.Forces Population Year Employed
```

```
## 1947      83.0 234.289      235.6      159.0      107.608 1947      60.323
## 1948      88.5 259.426      232.5      145.6      108.632 1948      61.122
## 1949      88.2 258.054      368.2      161.6      109.773 1949      60.171
## 1950      89.5 284.599      335.1      165.0      110.929 1950      61.187
## 1951      96.2 328.975      209.9      309.9      112.075 1951      63.221
## 1952      98.1 346.999      193.2      359.4      113.270 1952      63.639
## 1953      99.0 365.385      187.0      354.7      115.094 1953      64.989
## 1954     100.0 363.112      357.8      335.0      116.219 1954      63.761
## 1955     101.2 397.469      290.4      304.8      117.388 1955      66.019
## 1956     104.6 419.180      282.2      285.7      118.734 1956      67.857
## 1957     108.4 442.769      293.6      279.8      120.445 1957      68.169
## 1958     110.8 444.546      468.1      263.7      121.950 1958      66.513
## 1959     112.6 482.704      381.3      255.2      123.366 1959      68.655
## 1960     114.2 502.601      393.1      251.4      125.368 1960      69.564
## 1961     115.7 518.173      480.6      257.2      127.852 1961      69.331
## 1962     116.9 554.894      400.7      282.7      130.081 1962      70.551
```

```
names(longley)[1] <- "y"
lm.ridge(y ~ ., longley)
```

```
##              GNP      Unemployed  Armed.Forces      Population
## 2946.85636017  0.26352725  0.03648291   0.01116105   -1.73702984
##           Year      Employed
##  -1.41879853  0.23128785
```

```
plot(lm.ridge(y ~ ., longley,
             lambda = seq(0,0.1,0.001)))
```



```
select(lm.ridge(y ~ ., longley,
               lambda = seq(0,0.1,0.0001)))
```

```
## modified HKB estimator is 0.006836982
## modified L-W estimator is 0.05267247
## smallest value of GCV at 0.0057
```

(a) Write the model that is being fitted (with assumptions).

$$Y_i$$

= the i th observation for GNP implicit price deflator (1954=100) where

$$i = 1, \dots, 16$$

, for i th obs/row

The Gross National Product, (GNP), is denoted by

$$x_{i2}$$

The number of unemployed (unemployed) is denoted by

$$x_{i3}$$

Number of people in armed forces (Armed.Forces) is denoted by

$$x_{i4}$$

noninstitutionalized' population greater or equal to 14 years of age. (population) denoted by

$$x_{i5}$$

the year (time) as (Year) denoted by

$$x_{i6}$$

The number of people employed (Employed) denoted by

$$x_{i7}$$

Our regression model tries to predict/model the number of people employed (Employed), thus the model takes the form

$$Y_i = \beta_0 + \sum_{j=1}^7 \beta_j x_{ij} + \epsilon_i$$

where $\epsilon \sim N(0, \sigma^2)$ are iid which follows a normal distribution

(b) Write a brief explanation of the patterns you observe in this plot, as

$$\lambda$$

changes, relative to the OLS estimators.

We notice that the estimated coefficient converges to 0 as

$$\lambda$$

approaches

$$\infty$$

. Why?

When we observe

$$\hat{\beta}$$

(red dashed line and black line) that it gets closer and closer to zero as the value of

$$\lambda$$

increases. This is because the estimates of Beta ridge gets smaller than OLS estimates. Inversely, we notice that

$$\hat{\beta}_{ridge}$$

in pink and blue get bigger than OLS estimates. We also notice that for the green line that as the value of

$$\lambda$$

increases, that $\hat{\beta}_{ridge}$ is approximately equal to OLS estimates.