

ENGN1930B HW3

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Problem 1.7.

$$f = 100 \text{ mm}, \quad z_{\text{img}} = 300 \text{ mm}, \quad \Delta x_{\text{img}} = 10 \mu\text{m}$$

For fulfilling Nyquist Sampling Rate,

$$\Delta x_{\text{samp}} = \frac{\Delta x_{\text{img}}}{2} = \frac{10 \mu\text{m}}{2} = 5 \mu\text{m}$$

$$\Delta x_{\text{samp}} = \frac{z_{\text{samp}}}{z_{\text{img}}} \times \Delta x_{\text{img}} = \frac{z_{\text{samp}}}{300 \text{ mm}} \times 10 \mu\text{m} = 5 \mu\text{m}$$

$$z_{\text{samp}} = \frac{1}{2} \times 300 = \boxed{150 \text{ mm}}$$

Same as the position of focal plane.

Problem 2.1.: Redo

For monochromatic plane wave,

$$E(x, y, z, t) = E_0 \cdot \cos(ckr - \omega t + \phi) \hat{x}$$

amplitude: E_0 , angular freq. = ω ,

$$\phi = 0$$

$$E(x, y, z, t) = E_0 \cdot \cos(ckr - \omega t) \hat{x}$$

$$= \boxed{E_0 \cdot e^{i(ckr - \omega t)} \hat{x}}$$

Problem 2.2.

$$\epsilon_0 = 1.0 \text{ V/m}, \quad n = 1.7, \quad \epsilon_0 = 8.854 \times 10^{-12} \text{ F/m}, \\ c = 3 \times 10^8 \text{ m/s}$$

$$I(\vec{k}) = \frac{1}{2} \times n \times c \times \epsilon_0 \times \vec{E}(\vec{k}) \cdot \vec{E}^*(\vec{k})$$

$$= \frac{1}{2} \times 1.7 \times 3 \times 10^8 \text{ m/s} \times 8.854 \times 10^{-12} \text{ F/m}$$

$$1.0 \text{ V/m} \cdot e^{i(kx + \delta)} \cdot 1.0 \text{ V/m} \cdot e^{-i(kx + \delta)}$$

$$\approx 2.258 \times 10^9 \cdot e^0 = \boxed{2.258 \times 10^9 \text{ W/m}^2}$$