

MATH 151 Lab 5

Put team members' names and section number here.

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Section number 576

```
In [1]: from sympy import *
        from sympy.plotting import (plot, plot_parametric)
```

Question 1

1a

```
In [2]: #8 derivatives
x, n = symbols("x, n")

expr0 = E ** x * (1 + x ** 2)

i = 1
while i <= 8:
    print("f", end = "")
    for j in range(i):
        print("'", end = "")
    print(f"(x) = {diff(expr0, x, i)}")
    i += 1

f'(x) = 2*x*exp(x) + (x**2 + 1)*exp(x)
f''(x) = (x**2 + 4*x + 3)*exp(x)
f'''(x) = (x**2 + 6*x + 7)*exp(x)
f''''(x) = (x**2 + 8*x + 13)*exp(x)
f'''''(x) = (x**2 + 10*x + 21)*exp(x)
f''''''(x) = (x**2 + 12*x + 31)*exp(x)
f'''''''(x) = (x**2 + 14*x + 43)*exp(x)
f''''''''(x) = (x**2 + 16*x + 57)*exp(x)
```

1b

```
In [3]: #formula for derivative
nthderiv = E ** x * (x ** 2 + 2 * n * x + (n ** 2 - n + 1))
print(f"The formula for the nth derivative of f is {nthderiv}")
```

The formula for the nth derivative of f is $(x^2 + 2nx - n + x^2 + 1) \exp(x)$

1c

```
In [4]: #50th
print(f"{diff(expr0, x, 50)}")
print(f"{nthderiv.subs(n, 50)}")

(x**2 + 100*x + 2451)*exp(x)
(x**2 + 100*x + 2451)*exp(x)
```

Question 2

2a

```
In [5]: k, t = symbols("k, t")
y = cos(k * t)
print(f"k = {solve(4 * diff(y, t, 2) + 25 * y, k)}")

k = [-5/2, 5/2, pi/(2*t), 3*pi/(2*t)]
```

2b

```
In [6]: A, B = symbols("A, B")
eq = A * sin(k * t) + B * cos(k * t)
for i in solve(4 * diff(y, t, 2) + 25 * y, k):
    if (4 * diff(eq, t, 2) + 25 * eq).subs(k, i) == 0:
        print(f"Every member of the family of functions y = A sin(kt) + B cos(kt) is a")
    else:
        print(f"Not every member of the family of functions y = A sin(kt) + B cos(kt)
```

Every member of the family of functions $y = A \sin(kt) + B \cos(kt)$ is also a solution for $k = -5/2$.

Every member of the family of functions $y = A \sin(kt) + B \cos(kt)$ is also a solution for $k = 5/2$.

Not every member of the family of functions $y = A \sin(kt) + B \cos(kt)$ is also a solution for $k = \pi/(2t)$.

Not every member of the family of functions $y = A \sin(kt) + B \cos(kt)$ is also a solution for $k = 3\pi/(2t)$.

Question 3

3a

```
In [7]: #derivative
g = ((t - 2) / (2 * t + 1)) ** 9
print(diff(g, t, 1))

-18*(t - 2)**9/(2*t + 1)**10 + 9*(t - 2)**8/(2*t + 1)**9
```

3b

```
In [8]: #simplify
print(simplify(diff(g, t, 1)))

45*(t - 2)**8/(2*t + 1)**10
```

3c

```
In [9]: #horizontal tangent lines
print(f"Function g would have a horizontal tangent line at x = {solve(diff(g, t, 1), t)}")

Function g would have a horizontal tangent line at x = [2]
```

3d

```
In [10]: #derivative
f = (2 * t + 1) ** 5 * (t ** 2 - t + 2) ** 4
print(diff(f, t, 1))

(2*t + 1)**5*(8*t - 4)*(t**2 - t + 2)**3 + 10*(2*t + 1)**4*(t**2 - t + 2)**4

3e
```

```
In [11]: #simplify
print(simplify(diff(f, t, 1)))

(2*t + 1)**4*(t**2 - t + 2)**3*(10*t**2 - 10*t + 4*(2*t - 1)*(2*t + 1) + 20)

3f
```

```
In [12]: #factor
print(factor(diff(f, t, 1)))

2*(2*t + 1)**4*(t**2 - t + 2)**3*(13*t**2 - 5*t + 8)

3g
```

```
In [13]: print("The factored version would be more useful for locating the horizontal tangent l
```

The factored version would be more useful for locating the horizontal tangent lines of $f(t)$ since in its factored form, it is easier to see where t could equal zero, which is really just where the derivative is equal to zero or a horizontal tangent.

Question 4

4a

```
In [14]: #ROC
mu, W, theta = symbols("mu, W, theta")
F = mu * W / (mu * sin(theta) + cos(theta))

print(f"F'(theta) = {diff(F, theta, 1)}")

F'(theta) = W*mu*(-mu*cos(theta) + sin(theta))/(mu*sin(theta) + cos(theta))**2
```

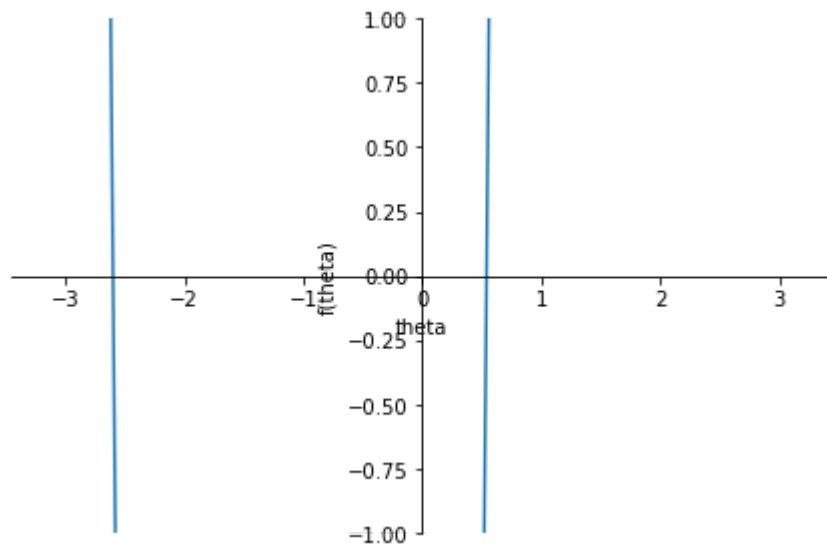
4b

```
In [15]: #ROC = 0
print(f"theta = {solve(diff(F, theta, 1), theta)}")

theta = [2*atan((sqrt(mu**2 + 1) - 1)/mu), -2*atan((sqrt(mu**2 + 1) + 1)/mu)]
```

4c

```
In [16]: #graph
plot(diff(F.subs([(W, 100), (mu, 0.6)]), theta, 1), (theta, -1 * pi, pi), ylim = (-1, 1))
print("According to the graph, the values of theta where dF/dTheta = 0 is about -2.5 and 2.5")
```



According to the graph, the values of θ where $dF/d\theta = 0$ is about -2.5 and 0.5

4d

```
In [17]: #verify (c)
print(f"Given the conditions of part c, dF/dTheta equals zero in the domain of [-pi, pi] when theta equals 0.540419500270584 and -2.60117315331921.")
```

Given the conditions of part c, $dF/d\theta$ equals zero in the domain of $[-\pi, \pi]$ when θ equals 0.540419500270584 and -2.60117315331921.