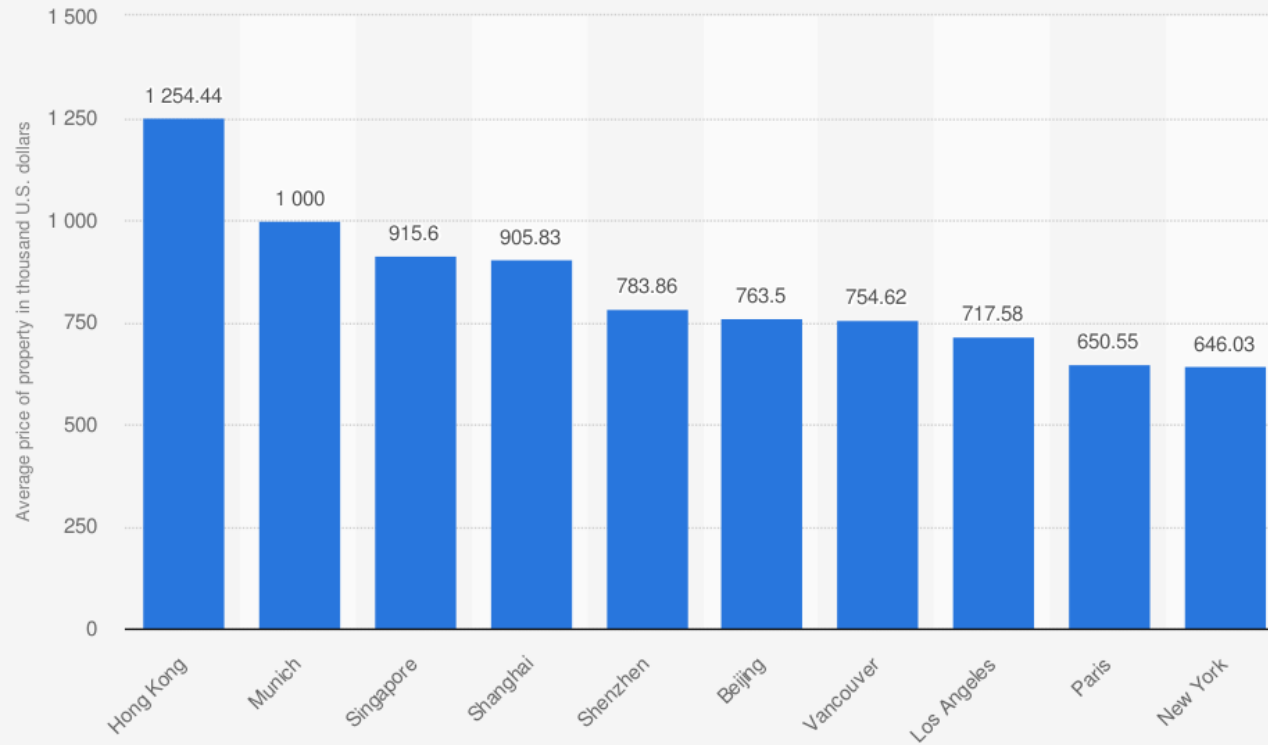


Chapter 20: Mortgages and Mortgage-Backed Securities



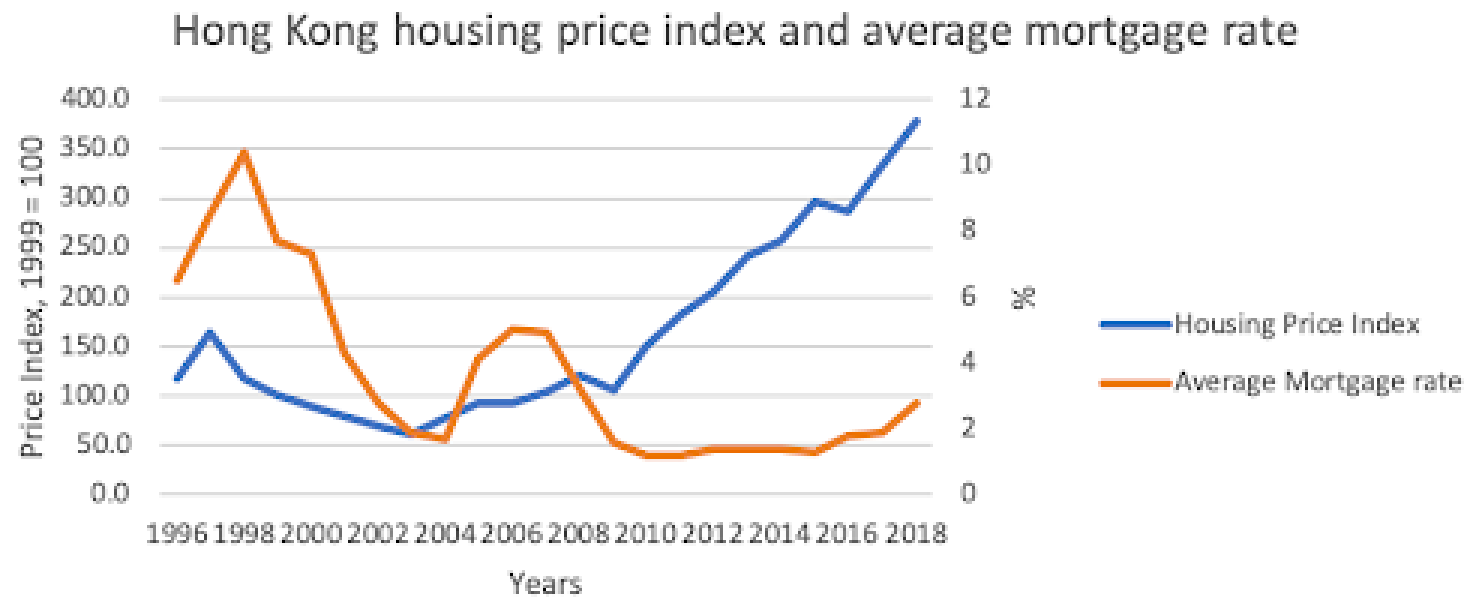


Most expensive residential property markets worldwide in 2020 (in 1,000 U.S. dollars)

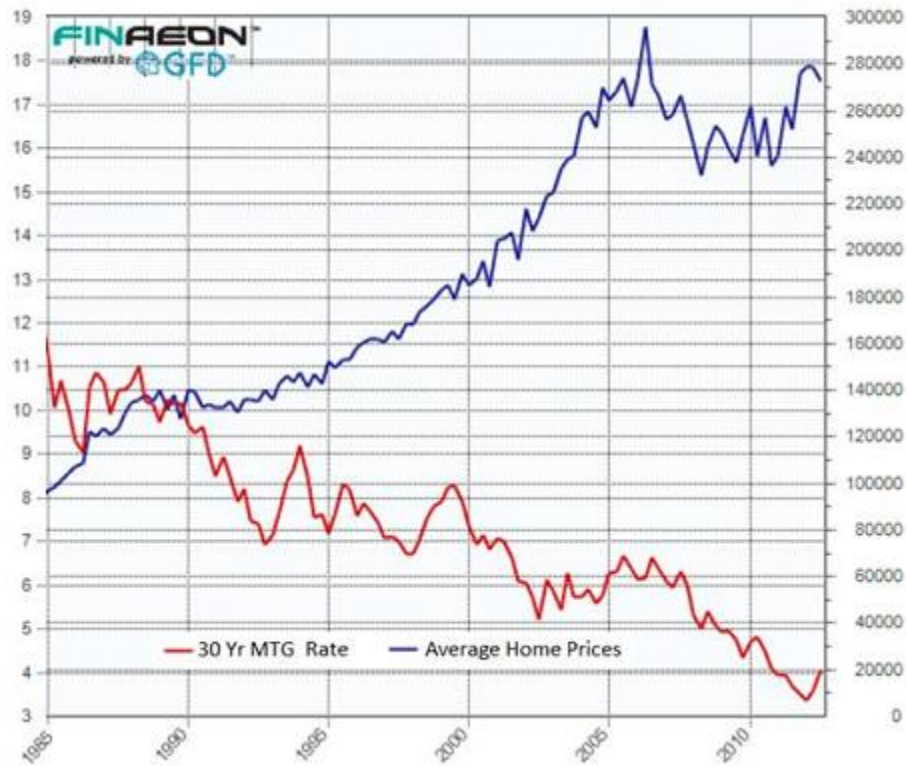


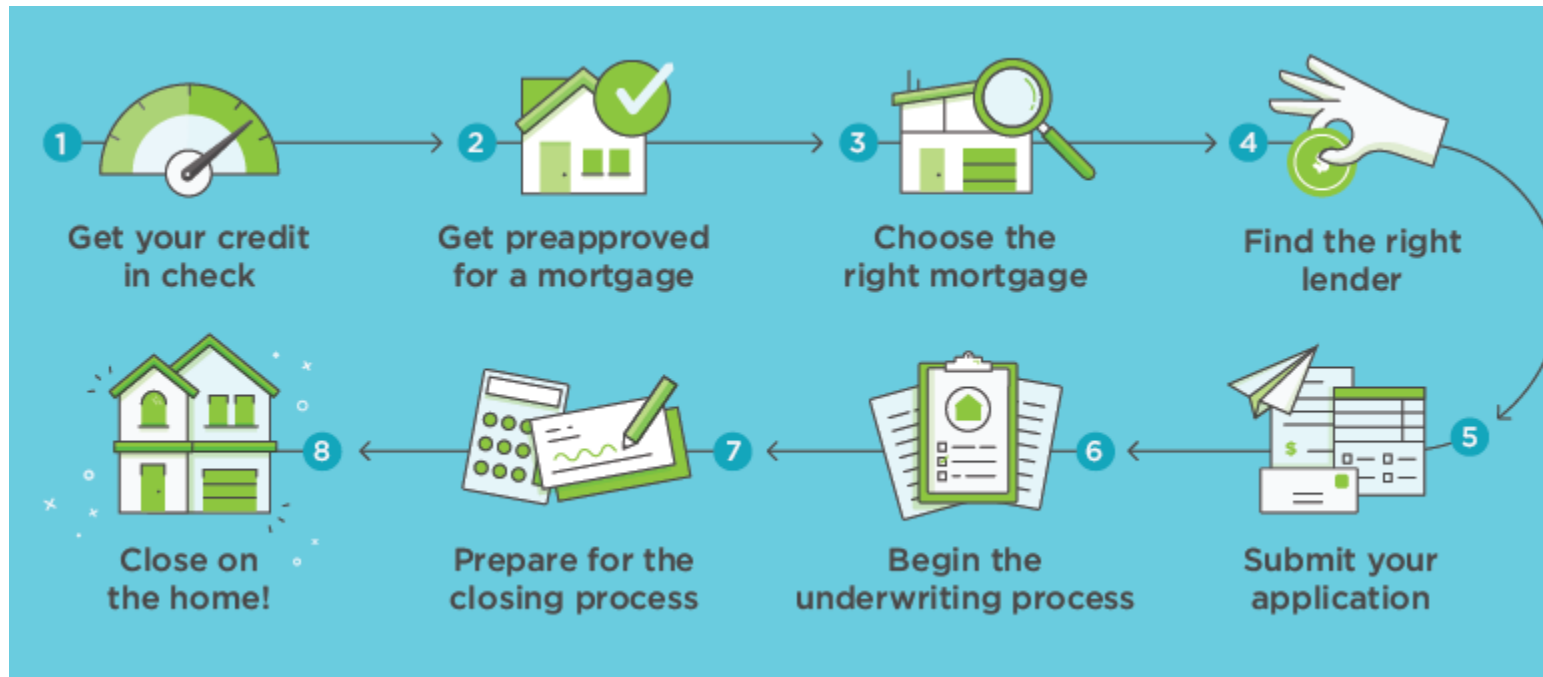
Sources
CBRE Group; Tatler Asia
© Statista 2020

Additional Information:
Worldwide; CBRE Group; 2020



30 Year Conventional Mortgage Rate (Courtesy Winans International) (WIMRT30Y) vs.
Winans US Real Estate Index (tm) - Price Only (WIREI)





MORTGAGE LOANS

- Mortgage loans come in many different varieties.
 - Fixed rate or variable rates
 - Residential or commercial purposes.
- Residential mortgages typically mature in 15 or 30 years and constitute 80% of the total principal of securitized mortgages in the U.S.
- Residential mortgages typically mature in 20 or 30 years and constitute almost 100% of the total principal of securitized mortgages in HK.

Fixed Rate Mortgage Payments

- The most typical mortgage loan in the US is a fixed rate, *level payment* mortgage.
- A homeowner might borrow \$100,000 from a bank at 4% and agree to make payments of $X = \$477.42$ every month for 30 years, where X satisfies

$$X \sum_{n=1}^{360} \frac{1}{\left(1 + \frac{.04}{12}\right)^n} = \$100,000$$

- In general, for a monthly payment X on a T -year mortgage with a mortgage rate y and an original principal amount or loan balance of $B(0)$,

$$X \sum_{n=1}^{12T} \frac{1}{\left(1 + \frac{y}{12}\right)^n} = B(0)$$

$$X \frac{12}{y} \left[1 - \frac{1}{\left(1 + \frac{y}{12}\right)^{12T}} \right] = B(0)$$

- Given X , solve for y or vice versa ([sp. sheet](#))

- Formula for monthly payment

$$X = \frac{B_0 \times \frac{y}{12}}{1 - (1 + \frac{y}{12})^{-12T}}$$

- The fixed monthly payment is often divided into its interest and principal components, a division interesting in its own right as well as for tax purposes;
- Mortgage interest payments are deductible from income for tax purpose while principal payments are not.

- Letting $B(n)$ be the principal amount outstanding after the mortgage payment due on date n , the interest component on the payment on date $n+1$ is

$$B(n) \times \frac{y}{12}$$

and the principal component is

$$X - B(n) \times \frac{y}{12}$$

Remaining principal value

$$B_n = X \frac{12}{y} \left(1 - \frac{1}{(1 + \frac{y}{12})^{12T-n}} \right)$$

Table 20.1: First Rows of an Amortization Table, in Dollars, of a 100,000 Dollar 4% 30-Year Mortgage

Payment Month	Interest Payment	Principal Payment	Ending Balance
			100,000.00
1	333.33	144.08	99,855.92
2	332.85	144.56	99,711.36
3	332.37	145.04	99,566.31
4	331.89	145.53	99,420.78
5	331.4	146.01	99,274.77

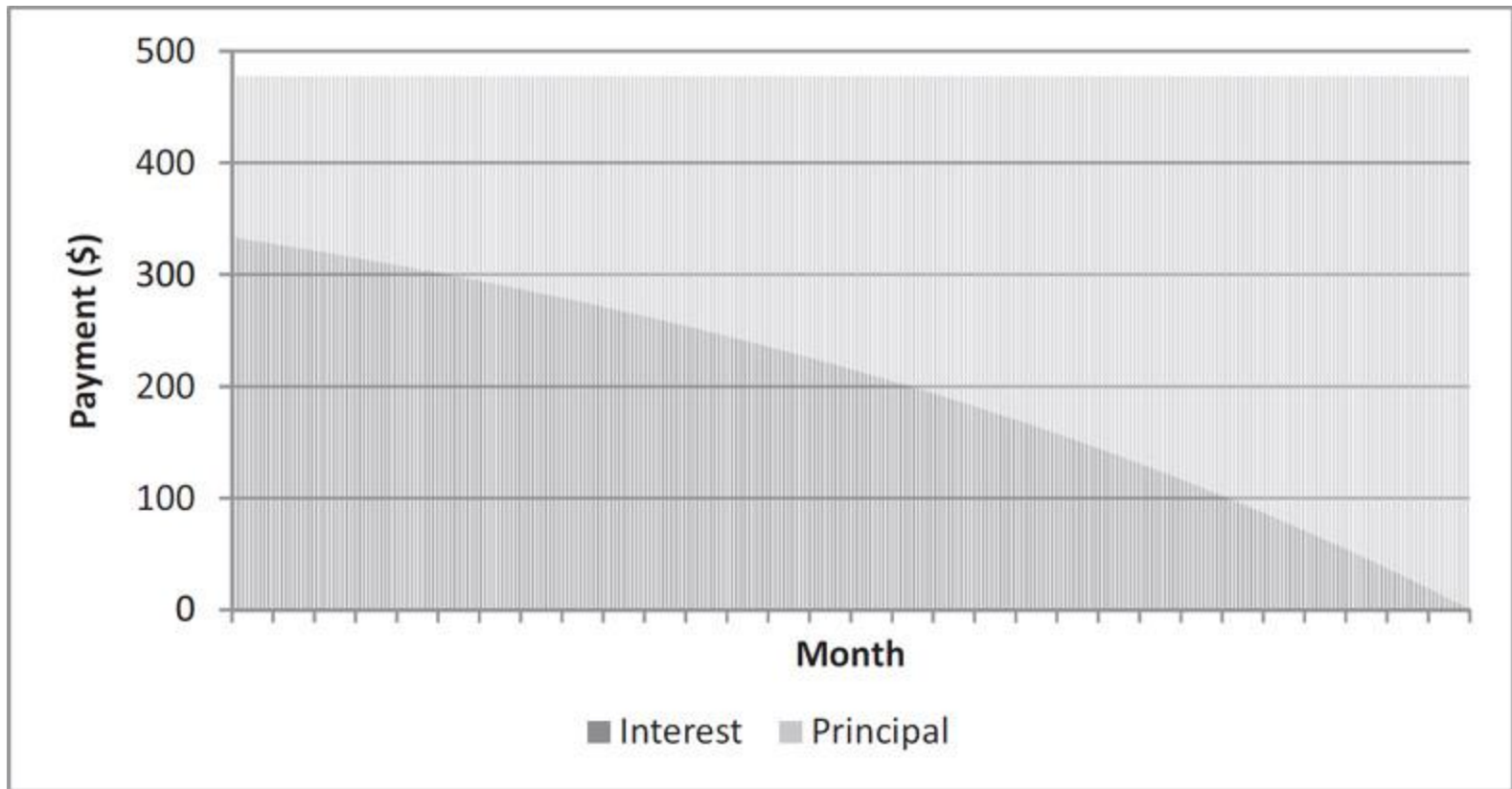


Figure 20.1: Amortization of a \$100,000 4% 30-Year Mortgage

- The outstanding balance of a mortgage on any date can be computed through discounting.
- For example, after 5 years or 60 monthly payments there remain 300 payments. The PV of these payments at 4% is

$$\begin{aligned} \$477.42 \sum_{n=1}^{300} \frac{1}{\left(1 + \frac{.04}{12}\right)^n} &= \$477.42 \frac{12}{.04} \left[1 - \frac{1}{\left(1 + \frac{.04}{12}\right)^{300}} \right] \\ &= \$90,448 \end{aligned}$$

Floating-Rate Mortgage

- In Hong Kong, most mortgages are indexed to either Prime Rate of HIBOR (1m or 3m).
- The calculation of monthly payment is identical to that of fixed-rate mortgages.
- Ex: Consider a 30-yr mortgage of \$1m principal and with rate HIBOR +0.8% initiated today.

Floating-Rate Mortgage

- The MP is

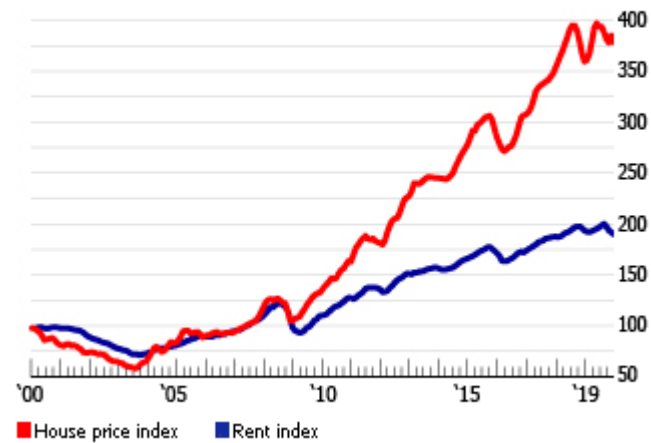
$$X = \frac{\$1m \times (0.19643\% + 0.8\%) / 12}{1 - \frac{1}{\left(1 + (0.19643\% + 0.8\%) / 12\right)^{360}}}$$
$$= \$3,214.76$$

with

interest payment = $\$1m \times (0.19643\% + 0.8\%) / 12 = \830

Principal payment = $\$3214.76 - 830 = \2384.76

Residential Prices vs. Rents



Source: Ratings and Valuation Department, Global Property Guide