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## Best Subset Selection Methods

### Cp statistic

#### Remarks

1. If a model is underfitted,  $\hat{\sigma}^2$ ,  $\hat{\beta}$  and  $\hat{y}$  at a new observation of  $\mathcal{X}_0$  are not unbiased estimators.
2. If a model is overfitted,  $\hat{\sigma}^2$ ,  $\hat{\beta}$  and  $\hat{y}$  at a new observation of  $\mathcal{X}_0$  are still unbiased estimators but with larger variance.
3. Normally, we choose a larger value for  $\alpha_{IN}$  than  $\alpha_{OUT}$  to avoid underfitting a model.
4. The Lack of Fit test in Chapter 1 is a test for testing whether the model is underfitted if there are repeated measurements of  $y$  for the same  $\mathcal{X}$ .

Consider the mean square error of  $\hat{y}(\mathcal{X}_i)$

$$\sum_{i=1}^n \frac{\text{MSE}(\hat{y}(\mathcal{X}_i))}{\sigma^2} = p' + \frac{\text{E}(\hat{\sigma}_{p'}^2) - \sigma^2}{\sigma^2} (n - p')$$

Then, Cp is defined as its estimate, i.e.,

$$Cp = 2p' - n + \frac{\text{ResS.S.}_{p'}}{\hat{\sigma}_{\text{full model}}^2}$$

#### Remarks

1. For each  $p'$ , calculate  $C_p$  for the model with smallest  $\text{ResS.S.}_{p'}$ .
2. Find the model with the smallest  $C_p$ .
3. Find a model with the smallest mean square error on predicted values of  $y$ .