

MATH3423 - Statistical Inference
Assignment 6

1. Q7 in Exercise 4
2. Q13 in Exercise 4
3. Q15 in Exercise 4
4. X has the distribution $P_0(\theta)$. We test the simple hypothesis $H_0 : \theta = 1/2$ against the alternative hypothesis $H_1 : \theta < 1/2$ by taking a random sample of size 12 and rejecting $H_0 : \theta = 1/2$ if and only if the observed values $X_1 X_2 \dots X_{12}$ are such that $\sum_{i=1}^{12} X_i \leq 2$. Find the power of the test $Q(1/2), Q(1/3), Q(1/4), Q(1/12)$.
5. Q4(b) in final exam of 2015

Let (X_1, \dots, X_n) be a random sample from $U(0, \theta)$ with $\theta > 0$.

- (a) **(4 marks)** Find UMP test at the level of significance α for testing $H_0 : \theta \leq \theta_0$ versus $H_1 : \theta > \theta_0$.
- (b) **(2 marks)** Based on the test derived in part (i), calculate the minimum sample size n such that the test for testing $H_0 : \theta \leq \frac{1}{2}$ versus $H_1 : \theta > \frac{1}{2}$ has a power of at least 0.98 at $\theta_1 = \frac{3}{4}$, where $\theta_1 \in \Theta_1$, when $\alpha = 0.05$.
- (c) **(2 marks)** Based on the test derived in part (i), calculate the power at $\theta_1 = \frac{2}{3}$, where $\theta_1 \in \Theta_1$, for testing $H_0 : \theta \leq \frac{1}{2}$ versus $H_1 : \theta > \frac{1}{2}$ when $\alpha = 0.05$ and $n = 10$.