

1. Examine if there is evidence of spatial dependence in a rare and a common species in the BCI tree dataset

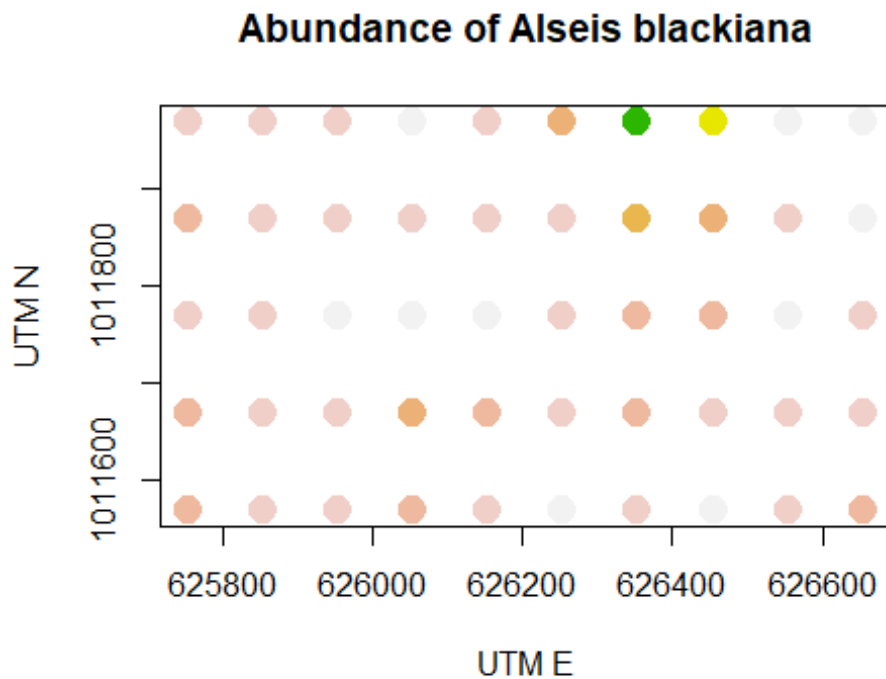
#identify a rare and common tree species in BCI dataset (I chose 'Solanum hayesii' as the rare species with 12 occurrences, and 'Alseis blackiana' as the common species with 983 occurrences)

```
sort(colSums(BCI))
```

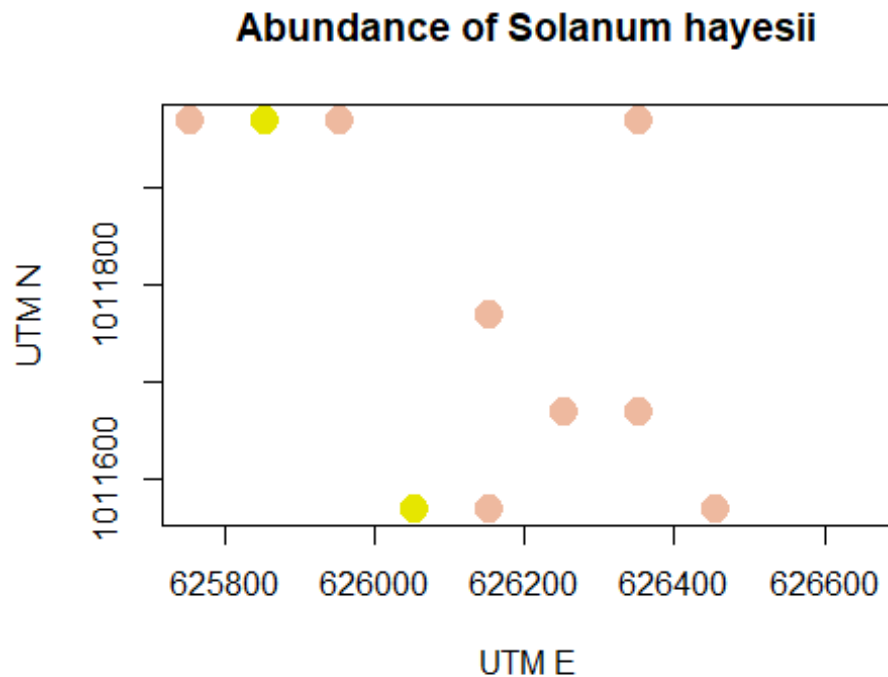
```
BCI_rare <- BCI$Solanum.hayesii  
BCI_common <- BCI$Alseis.blackiana
```

#plot these species with spatial coordinates

```
col_brks = hist(BCI_common, plot=F)$breaks  
col_indices = as.numeric(cut(BCI_common, col_brks))  
cols = rev(terrain.colors(length(col_brks)))  
plot(BCI_xy, cex=2, pch=19, col=cols[col_indices], ylab="UTM N", xlab="UTM E",  
main="Abundance of Alseis blackiana")
```



```
col_brks = hist(BCI_rare, plot=F)$breaks
col_indices = as.numeric(cut(BCI_rare, col_brks))
cols = rev(terrain.colors(length(col_brks)))
plot(BCI_xy, cex=2, pch=19, col=cols[col_indices], ylab="UTM N", xlab="UTM E",
main="Abundance of Solanum hayesii")
```



#use dist() function to calculate distances among occurrences in common and rare species

```
BCI_common_dist <- dist(BCI_common)
```

```
BCI_rare_dist <- dist(BCI_rare)
```

```
BCI_xy_dist <- dist(BCI_xy)
```

```
max_dist <- max(BCI_xy_dist)/2
```

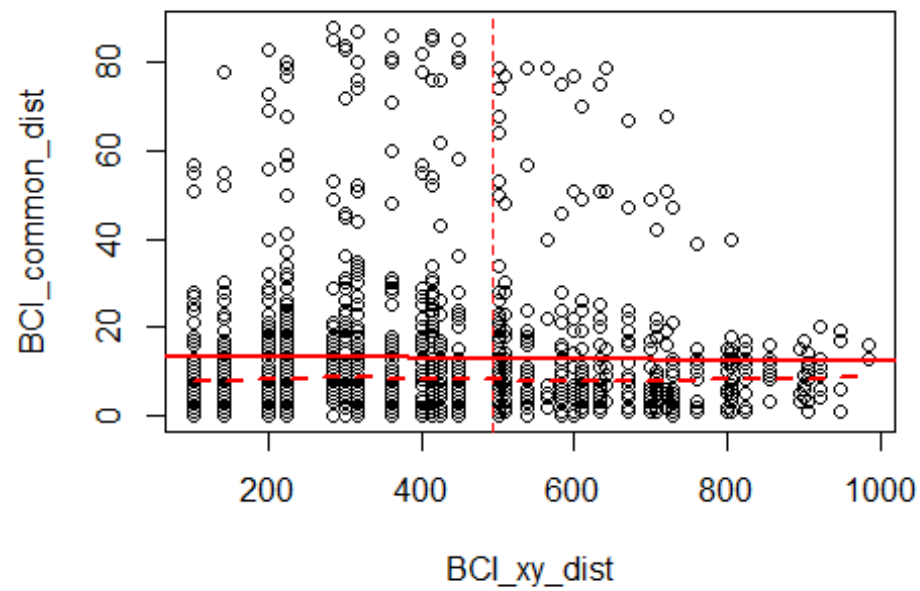
#plot results

```
plot(BCI_xy_dist, BCI_common_dist)
```

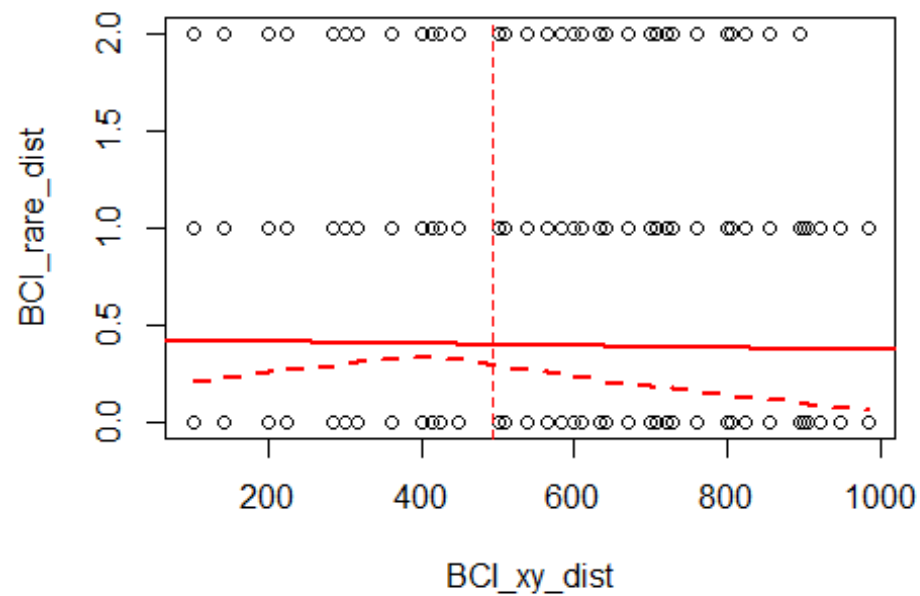
```
abline(lm(BCI_common_dist ~ BCI_xy_dist), lwd=2, col='red')
```

```
lines(lowess(BCI_xy_dist, BCI_common_dist), lwd=2, lty=2, col='red')
```

```
abline(v = max_dist, col='red', lwd=1, lty=2)
```



```
plot(BCI_xy_dist, BCI_rare_dist)
abline(lm(BCI_rare_dist ~ BCI_xy_dist), lwd=2, col='red')
lines(lowess(BCI_xy_dist, BCI_rare_dist), lwd=2, lty=2, col='red')
abline(v = max_dist, col='red', lwd=1, lty=2)
```



```

#use mantel() function to test for correlation
mantel(BCI_xy_dist, BCI_common_dist)
##
## Mantel statistic based on Pearson's product-moment correlation
##
## Call:
## mantel(xdis = BCI_xy_dist, ydis = BCI_common_dist)
##
## Mantel statistic r: -0.02348
##   Significance: 0.59
##
## Upper quantiles of permutations (null model):
##  90%  95% 97.5% 99%
## 0.0895 0.1162 0.1363 0.1573
## Permutation: free
## Number of permutations: 999

mantel(BCI_xy_dist, BCI_rare_dist)
##
## Mantel statistic based on Pearson's product-moment correlation
##
## Call:
## mantel(xdis = BCI_xy_dist, ydis = BCI_rare_dist)
##
## Mantel statistic r: -0.01893
##   Significance: 0.596
##
## Upper quantiles of permutations (null model):
##  90%  95% 97.5% 99%
## 0.0768 0.0987 0.1162 0.1485
## Permutation: free
## Number of permutations: 999

```

I employed a variety of techniques to test for spatial dependence in rare and common tree species from the BCI dataset. First, I plotted each species and their abundance within the spatial grid (BCI_xy) to see if any patterns immediately stood out. The common species, *Alseis blackiana*, appears to be evenly distributed throughout the study plots with a potential 'hotspot' near the northeastern corner. However, I did not observe any particular pattern with the abundance of the rare species, *Solanum hayesii*. My next step was to plot the relationship among species' occurrences and the spatial grid (with distance between species on the y-axis and distance between coordinates on the x-axis). The regression line produced on both rare and common plots were virtually flat suggesting no spatial relationship. I then employed the 'Mantel Test' to test for spatial correlation within rare and common species. The resulting p-values and r statistics (0.61 and -0.023 for common; 0.63 and -0.183 for rare) support my earlier observation of no spatial correlation within rare and common tree species.

2. Build two generalized linear models to predict the abundance of the species 'Drypetes standleyi' using the abundance of other tree species in the study site. Specifically examine the following species as predictor variables:

```
sp_ids <- c("Cordia.lasiocalyx", "Hirtella.triandra", "Picramnia.latifolia", "Quassia.amara",  
"Tabernaemontana.arborea", "Trattinnickia.aspera", "Xylopia.macrantha")
```

```
#create separate vectors for x and y coordinates
```

```
BCI_x <- BCI_xy$x  
BCI_y <- BCI_xy$y
```

```
#create vectors for each species of interest
```

```
drysta <- BCI$Drypetes.standleyi  
corlas <- BCI$Cordia.lasiocalyx  
hirtri <- BCI$Hirtella.triandra  
piclat <- BCI$Picramnia.latifolia  
quaama <- BCI$Quassia.amara  
tabarb <- BCI$Tabernaemontana.arborea  
traasp <- BCI$Trattinnickia.aspera  
xylmac <- BCI$Xylopia.macrantha
```

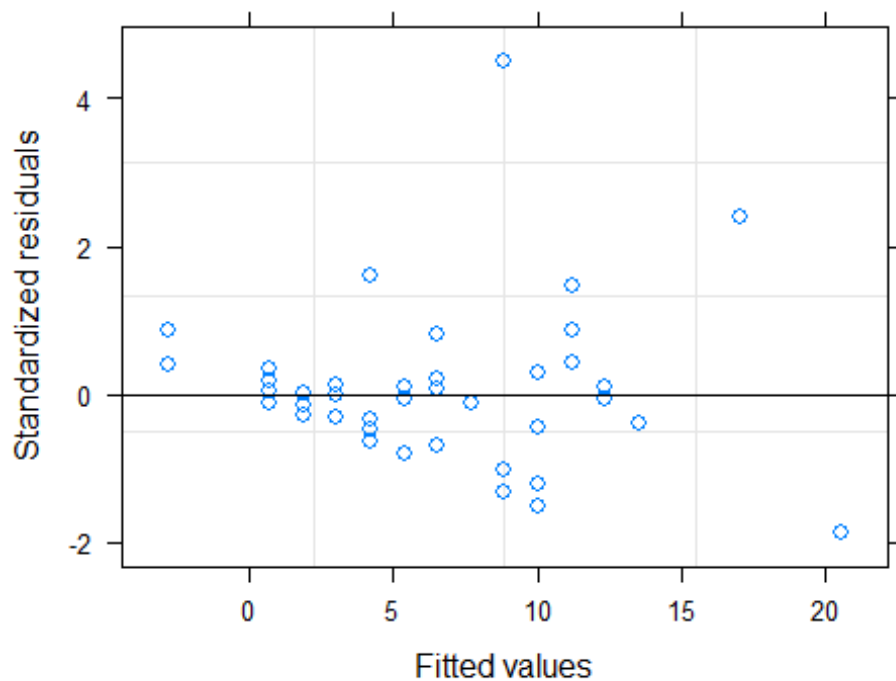
```
#Model 1: only include a single species as a predictor variable
```

```
BCI_gls_1 <- gls(drysta ~ corlas)
```

```
summary(BCI_gls_1)
```

```
## Generalized least squares fit by REML  
## Model: drysta ~ corlas  
## Data: NULL  
## AIC BIC logLik  
## 335.1246 340.7382 -164.5623  
##  
## Coefficients:  
## Value Std.Error t-value p-value  
## (Intercept) -2.782803 1.9173184 -1.451404 0.1532  
## corlas 1.165220 0.2292289 5.083217 0.0000  
##  
## Correlation:  
## (Intr)  
## corlas -0.87  
##  
## Standardized residuals:  
## Min Q1 Med Q3 Max  
## -1.8757378 -0.4356989 -0.1061361 0.1804392 4.5135685  
##  
## Residual standard error: 6.675561  
## Degrees of freedom: 50 total; 48 residual
```

```
plot(BCI_gls_1)
```



#Model 2: include all of the species as predictor variables

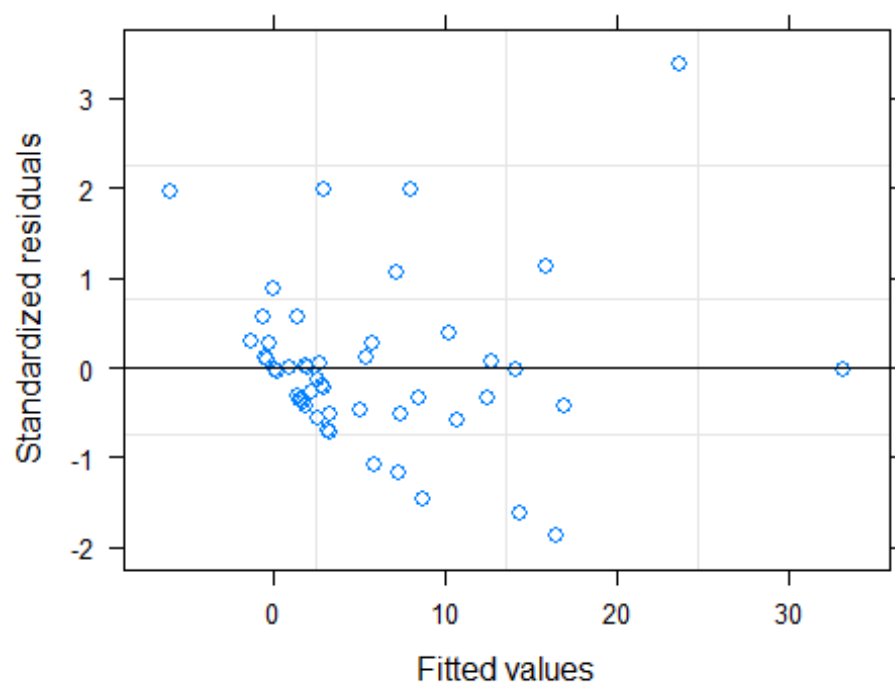
```
BCI_gls_2 <- gls(drysta ~ corlas + hirtri + piclat + quaama + tabarb + traasp + xylmac)
```

```
summary(BCI_gls_2)
```

```
## Generalized least squares fit by REML
## Model: drysta ~ corlas + hirtri + piclat + quaama + tabarb + traasp + xylmac
## Data: NULL
##      AIC      BIC    logLik
## 307.1163 322.7554 -144.5582
##
## Coefficients:
##              Value Std.Error   t-value p-value
## (Intercept) -1.051752  2.1175346 -0.496687  0.6220
## corlas      0.428920  0.2039316  2.103255  0.0415
## hirtri      0.122279  0.0802638  1.523462  0.1351
## piclat      0.662259  0.6358905  1.041468  0.3036
## quaama      4.085661  2.2842770  1.788602  0.0809
## tabarb     -0.249725  0.1491192 -1.674667  0.1014
## traasp      1.349323  0.7147412  1.887848  0.0660
## xylmac      0.548832  0.1468772  3.736672  0.0006
##
```

```
## Correlation:
##      (Intr) corlas hirtri piclat quaama tabarb traasp
## corlas -0.618
## hirtri -0.212 -0.354
## piclat  0.025 -0.019 -0.381
## quaama  0.163 -0.378  0.307 -0.302
## tabarb -0.708  0.245  0.163 -0.113  0.148
## traasp -0.139  0.187 -0.311  0.308 -0.708 -0.144
## xylmac -0.140 -0.125  0.156 -0.463  0.314  0.279 -0.294
##
## Standardized residuals:
##      Min      Q1      Med      Q3      Max
## -1.87708765 -0.42701500 -0.04032793  0.23615609  3.38768871
##
## Residual standard error: 4.539713
## Degrees of freedom: 50 total; 42 residual
```

```
plot(BCI_gls_2)
```

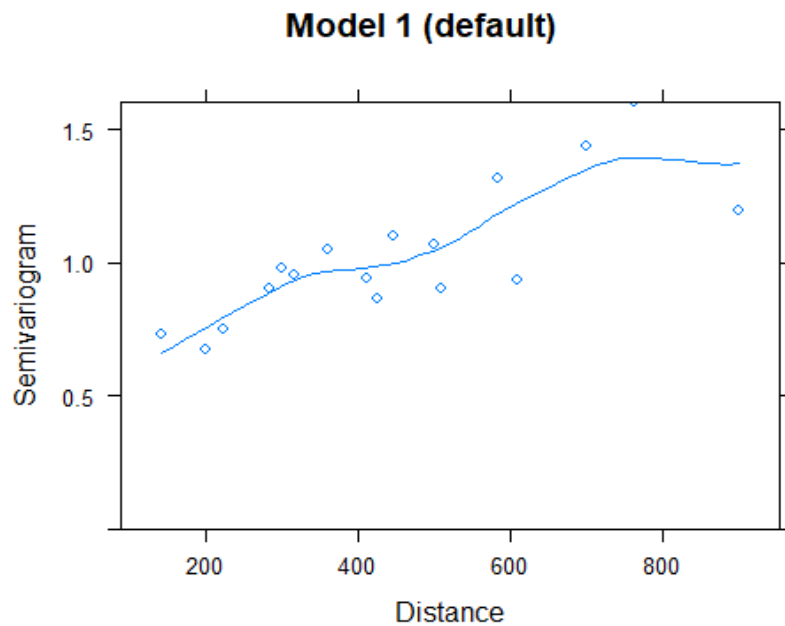


#update both models with exponentially distributed error terms

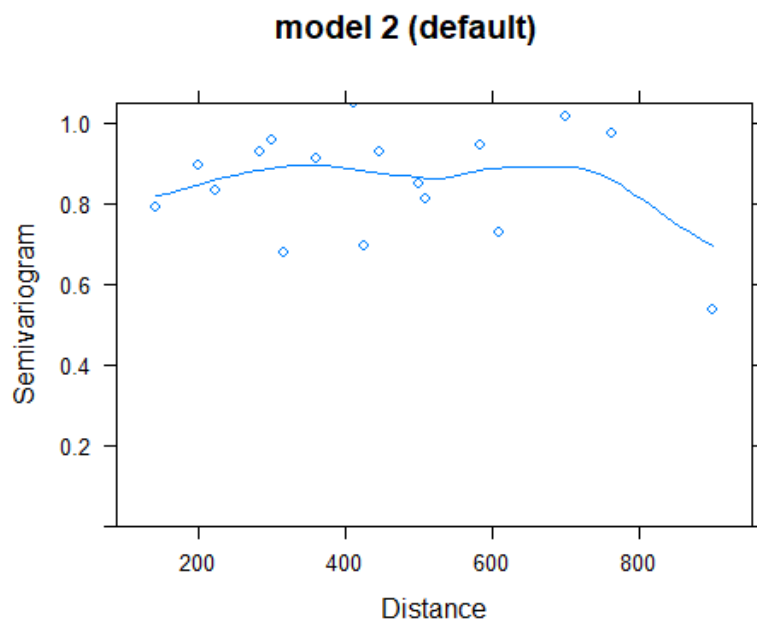
```
BCI_gls_1_exp <- update(BCI_gls_1, corr=corExp(form = ~ BCI_x + BCI_y))  
BCI_gls_2_exp <- update(BCI_gls_2, corr=corExp(form = ~ BCI_x + BCI_y))
```

#plot variograms of models

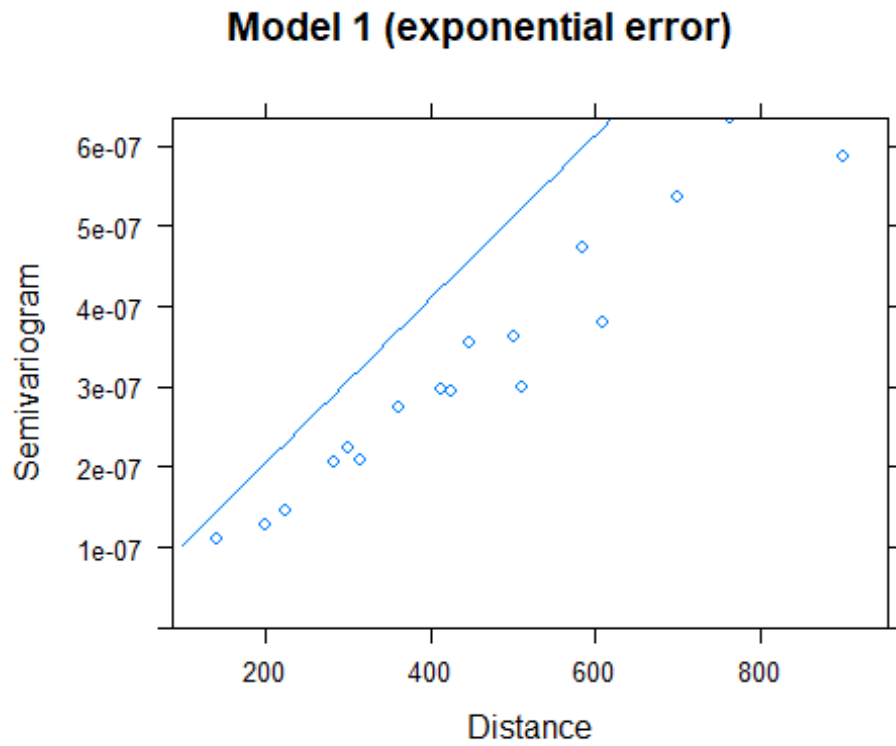
```
plot(Variogram(BCI_gls_1, form= ~ BCI_x + BCI_y), main = "Model 1 (default)")
```



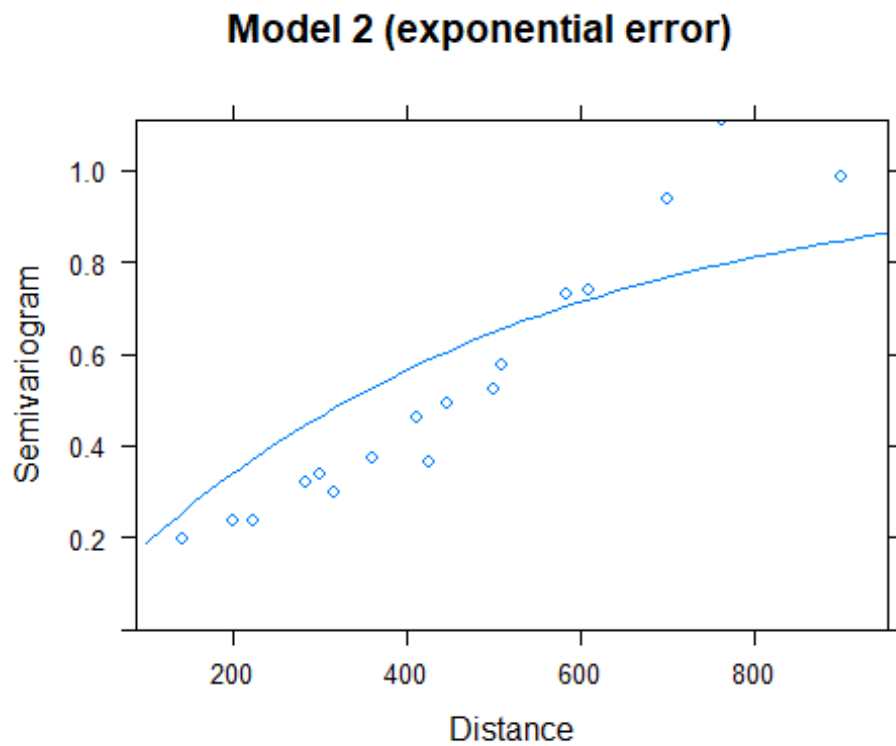
```
plot(Variogram(BCI_gls_2, form= ~ BCI_x + BCI_y), main = "model 2 (default)")
```




```
plot(Variogram(BCI_gls_1_exp, form= ~ BCI_x + BCI_y), main = "Model 1 (exponential error)")
```



```
plot(Variogram(BCI_gls_2_exp, form= ~ BCI_x + BCI_y), main = "Model 2 (exponential error)")
```



#compare fits of models with anova()

```
anova(BCI_gls_1, BCI_gls_1_exp)
```

##	Model	df	AIC	BIC	logLik	Test	L.Ratio	p-value
## BCI_gls_1	1	3	335.12	340.74	-164.56			
## BCI_gls_1_exp	2	4	310.64	318.13	-151.32	1 vs 2	26.48081	<.0001

```
anova(BCI_gls_2, BCI_gls_2_exp)
```

##	Model	df	AIC	BIC	logLik	Test	L.Ratio	p-value
## BCI_gls_2	1	9	307.12	322.76	-144.56			
## BCI_gls_2_exp	2	10	301.61	318.98	-140.80	1 vs 2	7.510175	0.0061

2.1. Did including the spatial error term have a large impact on the coefficients of the model?

Yes, when error terms were included in the model the coefficients appeared to behave better (offer more predictability). In the resulting variograms, data points are arranged in a more linear fashion with a pronounced slope when error terms are included in the model.

2.2. Did including the spatial error terms significantly improve model fit (use function anova to carry out model comparison)?

Yes, including the spatial error terms significantly improved the fit of these models. For the first model, AIC lowered from 340 to 310 with the inclusion of exponential error terms. This effect was less pronounced in the second model (although still significant), where AIC dropped from 307 to 301 following the inclusion of exponential error terms.

2.3. Explain why you did or did not observe a difference in the influence of adding the spatial error term between the two models.

Including the error terms resulted in a better model because these data are not truly independent. Spatial statistics are tricky in modeling plant distributions because of autocorrelation. For example, the plant species of interest may grow in clusters, or there may be another underlying environmental variable such as elevation. Including the error terms in these models accounted for some of this variability.