

Table of Contents

- 1. Statistical Computing Week 2
- 2. Table of Contents
- 3. Front Matter
- 4. Vector and Matrix Arithmetic in R
- 5. Logicals
- 6. Functional and Object-Oriented Programming
- 7. Wrapping Up

Front Matter

Announcements

- Office hours update
 - Tons of people came, felt very productive
 - Some people just used that as time to work on their problem sets without specific questions, which is a good idea!
- PS0 is due 9/12 @ 11.59p
 - I'm generally pleased with the questions that I received and the work I saw people do!
 - This is mostly what my assignments look like
 - 1. Do some stuff
 - 2. Plot the stuff
 - 3. Tell me what you think about the stuff
- PS1 is out!
 - It is still due on 9/18 before class
 - I think it's more straightforward than PSO
 - It's all about writing functions to do things

Check-In

PollEv.com/klintkanopka

Vector and Matrix Arithmetic in R

```
c(1, 2, 3) + c(4, 5, 6)
c(1, 2, 3) + c(4, 5, 6, 7)
c(1, 2, 3) + c(4, 5, 6, 7, 8, 9)
```

```
c(1, 2, 3) + c(4, 5, 6)

# [1] 5 7 9

c(1, 2, 3) + c(4, 5, 6, 7)

c(1, 2, 3) + c(4, 5, 6, 7, 8, 9)
```

```
c(1, 2, 3) + c(4, 5, 6)
# [1] 5 7 9
c(1, 2, 3) + c(4, 5, 6, 7)
# Warning message:
# In c(1, 2, 3) + c(4, 5, 6, 7) :
# longer object length is not a multiple of shorter object length
# [1] 5 7 9 8
c(1, 2, 3) + c(4, 5, 6, 7, 8, 9)
```

```
c(1, 2, 3) + c(4, 5, 6)
# [1] 5 7 9
c(1, 2, 3) + c(4, 5, 6, 7)
# Warning message:
# In c(1, 2, 3) + c(4, 5, 6, 7) :
# longer object length is not a multiple of shorter object length
# [1] 5 7 9 8
c(1, 2, 3) + c(4, 5, 6, 7, 8, 9)
# [1] 5 7 9 8 10 12
```

Vector Arithmetic

- Generally happens *elementwise*
- The first elements from each input are combined
- Then the second elements
- And so on...
- When vectors are the same size, this produces a vector the same length as the inputs
- What if they're not the same length?

Recycling

- R 's general behavior when things aren't the same length is to *recycle* the shorter object
- Behavior is the same regardless of order
- Length of the output is the *maximum* of the lengths of the inputs
- How does this work?
 - R will paste the shorter object to itself end-to-end until it matches the length of the longer object
 - If the longer object is an integer multiple of the length of the longer object, it does this silently
 - If the longer object is not, it throws a warning, but still produces output according to the same rules!

```
v1 <- c(1,2,3)
v2 <- c(1,2,3,4)
v3 <- c(1,2)
mat <- matrix(1:9, nrow=3)

mat

v1 * mat
v2 * mat
v3 * mat</pre>
```

```
v1 \leftarrow c(1,2,3)
v2 \leftarrow c(1,2,3,4)
v3 < -c(1,2)
mat <- matrix(1:9, nrow=3)</pre>
mat
# [,1] [,2] [,3]
# [1,] 1 4 7
# [2,] 2 5 8
# [3,] 3 6 9
v1 * mat
v2 * mat
v3 * mat
```

```
v1 \leftarrow c(1,2,3)
v2 \leftarrow c(1,2,3,4)
v3 < -c(1,2)
mat <- matrix(1:9, nrow=3)</pre>
mat
# [,1] [,2] [,3]
# [1,] 1 4 7
# [2,] 2 5 8
# [3,] 3 6 9
v1 * mat
# [,1] [,2] [,3]
# [1,] 1 4 7
# [2,] 4 10 16
# [3,] 9 18 27
v2 * mat
v3 * mat
```

```
v1 \leftarrow c(1,2,3)
v2 \leftarrow c(1,2,3,4)
v3 < -c(1,2)
mat <- matrix(1:9, nrow=3)</pre>
mat
# [,1] [,2] [,3]
# [1,] 1 4 7
# [2,] 2 5 8
# [3,] 3 6 9
v1 * mat
v2 * mat
# Warning message:
# In v2 * mat :
# longer object length is not a multiple of shorter object length
# [,1] [,2] [,3]
# [1,] 1 16 21
# [2,] 4 5 32
# [3,] 9 12 9
v3 * mat
```

```
v1 \leftarrow c(1,2,3)
v2 \leftarrow c(1,2,3,4)
v3 < -c(1,2)
mat <- matrix(1:9, nrow=3)</pre>
mat
# [,1] [,2] [,3]
# [1,] 1 4 7
# [2,] 2 5 8
# [3,] 3 6 9
v1 * mat
v2 * mat
v3 * mat
# In v3 * mat:
# longer object length is not a multiple of shorter object length
# [,1] [,2] [,3]
# [1,] 1 8 7
# [2,] 4 5 16
# [3,] 3 12 9
```

- Here, recycling happens along the columns
 - For matrices in R, things are usually applied along columns first
- Under the hood:
 - 1. The matrix is unrolled into a vector of the form c(col1, col2, ...)
 - 2. Recycling happens as if two vectors were multiplied
 - 3. The output is reshaped back into the original dimensions of the matrix

```
mat1 <- matrix(1:9, ncol=3)
mat2 <- matrix(1:4, ncol=2)

mat1 + mat1
mat2 * mat2
mat1 + mat2</pre>
```

```
mat1 <- matrix(1:9, ncol=3)</pre>
mat2 <- matrix(1:4, ncol=2)</pre>
mat1 + mat1
# [,1] [,2] [,3]
# [1,] 2 8 14
# [2,] 4 10 16
# [3,] 6 12 18
mat2 * mat2
# [,1] [,2]
# [1,] 1 9
# [2,] 4 16
mat1 + mat2
```

```
mat1 <- matrix(1:9, ncol=3)</pre>
mat2 <- matrix(1:4, ncol=2)</pre>
mat1 + mat1
# [,1] [,2] [,3]
# [1,] 2 8 14
# [2,] 4 10 16
# [3,] 6 12 18
mat2 * mat2
# [,1] [,2]
# [1,] 1 9
# [2,] 4 16
mat1 + mat2
# Error in `mat1 + mat2`:
# ! non-conformable arrays
```

- For two matrix inputs, recycling does **not** happen!
- For standard arithmetic operators, everything is done elementwise
- If two matrices are not the same shape, R throws an error
 - non-conformable arguments or non-conformable arrays
 - No output is produced
 - Execution is halted

- There is a specific matrix multiplication operator, %*%
- Conducts matrix multiplication
 - lacktriangle Requires an A imes B matrix and a B imes C matrix
 - Produces $A \times C$ shaped output
- Works with vectors!
 - lacksquare A vector of length N is treated as either an N imes 1 or 1 imes N matrix, depending on what is needed
 - The output is **always** as a matrix

```
matrix(1:9, ncol=3) %*% matrix(1:9, ncol=3)
matrix(1:9, ncol=3) %*% c(1, 2, 3)
c(1, 2, 3) %*% matrix(1:9, ncol=3)
```

```
matrix(1:9, ncol=3) %*% matrix(1:9, ncol=3)

#     [,1] [,2] [,3]
# [1,]     30     66     102
# [2,]     36     81     126
# [3,]     42     96     150

matrix(1:9, ncol=3) %*% c(1, 2, 3)
c(1, 2, 3) %*% matrix(1:9, ncol=3)
```

```
matrix(1:9, ncol=3) %*% matrix(1:9, ncol=3)
# [,1] [,2] [,3]
# [1,] 30 66 102
# [2,] 36 81 126
# [3,] 42 96 150
matrix(1:9, ncol=3) %*% c(1, 2, 3)
# [,1]
# [1,] 30
# [2,] 36
# [3,] 42
c(1, 2, 3) %*% matrix(1:9, ncol=3)
```

```
matrix(1:9, ncol=3) %*% matrix(1:9, ncol=3)
# [,1] [,2] [,3]
# [1,] 30 66 102
# [2,] 36 81 126
# [3,] 42 96 150
matrix(1:9, ncol=3) %*% c(1, 2, 3)
# [,1]
# [1,] 30
# [2,] 36
# [3,] 42
c(1, 2, 3) %*% matrix(1:9, ncol=3)
# [,1] [,2] [,3]
# [1,] 14 32 50
```

- We want to multiply two matrices, AB = C
 - Here, a_{ij} is the element of matrix A in the ith row and jth column
 - And matrix A is an N imes K matrix and matrix B is a K imes M matrix
- To construct the resultant $N \times M$ matrix, C:

$$c_{ij} = \sum_{k=1}^K a_{ik} b_{kj}$$

- Alternatively C can be constructed through dot products:
 - Where \vec{a}_i is the *i*th *row* vector of A
 - And \vec{b}_j is the *j*th *column* vector of B

$$c_{ij} = ec{a}_i \cdot ec{b}_j$$

If this looks awful, a course in linear algebra could be useful (depending on your subplan and career goals)

Logicals

- Sometimes we want to compare conditions and know if they're TRUE or FALSE
 - Called Boolean after the work of George Boole
 - Only two possible values (dichotomous), and clear rules for evaluation

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- A != B : returns TRUE if the value of A and B are **not** equal, FALSE otherwise

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- A == B : returns TRUE if the value of A and B are equal, FALSE otherwise
- A != B : returns TRUE if the value of A and B are **not** equal, FALSE otherwise
- \blacksquare A > B : returns TRUE if the value of A is strictly greater than B , FALSE otherwise

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- A != B : returns TRUE if the value of A and B are **not** equal, FALSE otherwise
- A > B : returns TRUE if the value of A is strictly greater than B , FALSE otherwise
- A >= B : returns TRUE if the value of A is greater than or equal to B, FALSE otherwise

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- A < B : returns TRUE if the value of A is strictly less than B , FALSE otherwise

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- A >= B : returns TRUE if the value of A is greater than or equal to B, FALSE otherwise
- A < B : returns TRUE if the value of A is strictly less than B , FALSE otherwise
- A <= B : returns TRUE if the value of A is less than or equal to B, FALSE otherwise

- Often we store TRUE or FALSE status in a variable and need to check multiple conditions, or need rules on how to combine them
- Arithmetic with Boolean variables is easy TRUE = 1 and FALSE = 0
 - This can be leveraged to do some really clever stuff!

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A confusing thing is that there are two other logical operators:

• && is a logical AND that ONLY works on single values (not vectors)

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- && is a logical AND that ONLY works on single values (not vectors)
- || is a logical OR that ONLY works on single values (not vectors)
- Both & and | are vectorized, and will do elementwise operations with normal recycling rules

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- && is a logical AND that ONLY works on single values (not vectors)
- || is a logical OR that ONLY works on single values (not vectors)
- Both & and | are vectorized, and will do elementwise operations with normal recycling rules
- Use && and || for control flow!

Functional and Object-Oriented Programming

Functions

- Functions are objects in R that package code
- Functions take named arguments
- Executing a function creates a new environment with the arguments assigned to their names
 - Then they execute their code
 - When a function is done running, its environment is destroyed/lost
- In general, we do not write functions that modify the global variables (this is super dangerous)!
- If you need information that's computed within a function, you need to return it
- This lets you maintain whatever object is returned for future use outside of the function's environment

Let's write a function called RollDice() that rolls an arbitrarily sized die an arbitrary number of times and returns the individual results.

RollDice <- function(){}</pre>

```
RollDice <- function(){
  results <- sample()
}</pre>
```

```
RollDice <- function(){
  results <- sample(x, size, replace = FALSE, prob = NULL)
}</pre>
```

```
RollDice <- function(){
  result <- sample(x = 1:N_sides, size, replace = FALSE, prob = NULL)
}</pre>
```

```
RollDice <- function(N_sides){
  result <- sample(x = 1:N_sides, size, replace = FALSE, prob = NULL)
}</pre>
```

```
RollDice <- function(N_sides){
  result <- sample(x = 1:N_sides, size = N_dice, replace = FALSE, prob = NULL)
}</pre>
```

```
RollDice <- function(N_sides, N_dice){
  result <- sample(x = 1:N_sides, size = N_dice, replace = FALSE, prob = NULL)
}</pre>
```

```
RollDice <- function(N_sides, N_dice){
  result <- sample(x = 1:N_sides, size = N_dice, replace = TRUE, prob = NULL)
}</pre>
```

```
RollDice <- function(N_sides, N_dice){
  result <- sample(x = 1:N_sides, size = N_dice, replace = TRUE, prob = NULL)
  return(result)
}</pre>
```

```
RollDice <- function(N_sides = 6, N_dice = 1){
  result <- sample(x = 1:N_sides, size = N_dice, replace = TRUE, prob = NULL)
  return(result)
}</pre>
```

```
RollDice <- function(N_sides = 6, N_dice = 1){
  result <- sample(x = 1:N_sides, size = N_dice, replace = TRUE, prob = NULL)
  return(result)
}</pre>
```

```
RollDice <- function(N_sides = 6, N_dice = 1){
  result <- sample(x = 1:N_sides, size = N_dice, replace = TRUE, prob = NULL)
  return(result)
}</pre>
```

```
RollDice <- function(N_sides = 6, N_dice = 1){
  result <- sample(x = 1:N_sides, size = N_dice, replace = TRUE, prob = NULL)
  return(result)
}</pre>
```

```
RollDice <- function(N_sides = 6, N_dice = 1){
  result <- sample(x = 1:N_sides, size = N_dice, replace = TRUE, prob = NULL)
  return(result)
}</pre>
```

- We've already seen this, but let's be explicit!
- Some functions are vectorized, meaning they can operate independently on all elements of a vector
- Vectorized functions take in vectors, arrays, or matrices and return objects of the same size with consistent behavior across all elements

```
x <- 0:3
exp(x)
x^2
x == 2
```

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```
x <- 0:3
exp(x)

# [1] 1.0000000 2.718282 7.389056 20.085537

x^2
x == 2</pre>
```

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```
x <- 0:3
exp(x)

# [1] 1.000000 2.718282 7.389056 20.085537

x^2

# [1] 0 1 4 9

x == 2</pre>
```

- We've already seen this, but let's be explicit!
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```
x <- 0:3
exp(x)

# [1] 1.000000 2.718282 7.389056 20.085537

x^2

# [1] 0 1 4 9

x == 2

# [1] FALSE FALSE TRUE FALSE</pre>
```

Object Oriented Programming

- There are lots of different types of objects in R
- These different types of objects are identified internally with "classes"
 - You can use the class() function on an object to see what class it is
 - Things without classes are often called "base objects"
- We want objects that keep our data, code and results neatly organized
- We want functions that do predictable things to these objects
- Object Oriented Programming (OOP) is centered around objects
 - Objects contain data
 - Objects contain code (called *methods*)
 - Methods are specifically designed to operate on the data in the object
- R has a few ways to implement this (S3 and S4 being most common)

Generic Functions (aka Generics)

- Functions that are designed to operate on many different types of objects with a common call
 - print(), summary(), coef(), plot(), etc
- Generics look at the type of object they are called on and then use the *method* associated with that type of object
- print() just prints an object out
 - What that means depends on what the object is!
- summary()
 - Prints out summary statistics for data frames and vectors
 - Prints out whole tables and descriptions for different types of model objects!
- In Part 3 of PS1, you'll start to construct your first model object!

Unit Testing

- Unit testing is an idea we'll introduce now, but it's a practice we should always engage in when writing code!
- The basic idea is that we want to write our code in chunks (often in the form of functions)
 - If we write our code in chunks, we can also test our code in chunks
 - This makes it *much* easier to pinpoint where things may be going wrong
 - This will become much more important very soon once we start to include control flow and loops!
- How do you do this?
 - First, make sure your code gives the correct output under a variety of conditions!
 - Second, see what your code does in unexpected situations
 - How does it handle inputs of the wrong type?
 - How does it handle inputs of the wrong size?
 - How does it handle missing (or NA) inputs?
 - Third, once you validate each individual piece works, make sure they work together

Wrapping Up

Wrapping up

- When you're combining R objects arithmetically, be aware of how things are handled and what conditions do (and do not) trigger warnings and errors!
- Logical statements will help you count objects that satisfy certain conditions and control program behavior in the future
- Writing functions allow you to stop copy-pasting big chunks of code when carrying out repetitive tasks!
- S3 and S4 objects contain both sub objects and code that controls how generic functions act on them!
- Make sure to thoroughly test the different components of your code so that you can pinpoint where problems are coming from

Wrapping up

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