

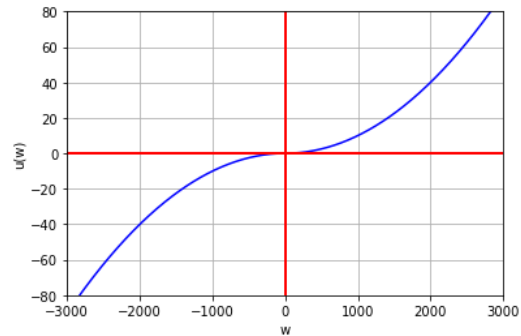
## TIE4203 Decision Analysis in Industrial Operations and Management Solutions to Assignment #2

(a) Anna's wealth utility function:

$$u(w) = \begin{cases} \frac{w^2}{100,000} & w \geq 0 \\ -\frac{w^2}{100,000} & w < 0 \end{cases}$$

$$u'(w) = \begin{cases} \frac{2w}{100,000} & w \geq 0 \\ -\frac{2w}{100,000} & w < 0 \end{cases}$$

$$u''(w) = \begin{cases} \frac{2}{100,000} & w \geq 0 \\ -\frac{2}{100,000} & w < 0 \end{cases}$$

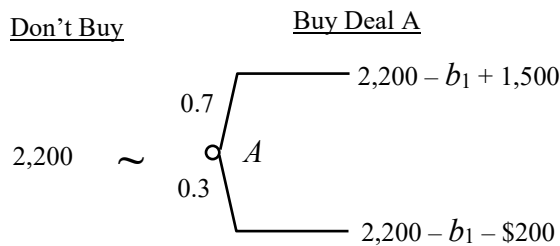


$$\text{Risk tolerance } \rho(w) = \frac{-u'(w)}{u''(w)} = -w \quad \text{for all } w$$

At current wealth of \$2,200, Anna's risk tolerance = - **\$2,200**.

(b) Anna is currently **Risk-Seeking** in attitude as her risk tolerance is negative.

(c) Let Anna's PIBP for Deal  $A$  =  $b_1$ .



Equating the utility of not buying  $A$  with the expected utility of buying  $A$

$$\begin{aligned} u(2,200) &= 0.7 u(2,200 - b_1 + 1,500) + 0.3 u(2,200 - b_1 - 200) \\ u(2,200) &= 0.7 u(3,700 - b_1) + 0.3 u(2,000 - b_1) \end{aligned}$$

Assuming  $b_1 \leq 2,000$

$$2,200^2 = 0.7 (3,700 - b_1)^2 + 0.3 (2,000 - b_1)^2$$

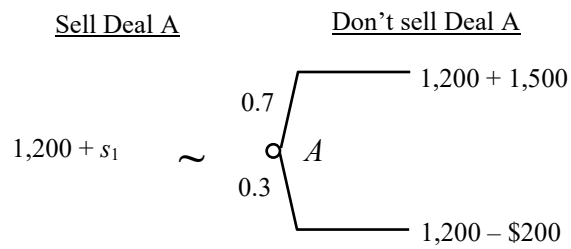
Using an equation solver:  $b_1 = \$1,132.55$

Hence Anna's PIBP for Deal  $A$  = **\$ 1,132.55**

(d) Anna paid \$1,000 for Deal A.

Her new wealth = \$2,200 – \$1,000 = \$1,200 plus Deal A.

Let Anna's PISP for Deal A =  $s_1$



Equating the utility of selling  $A$  to the expected utility of not selling  $A$ :

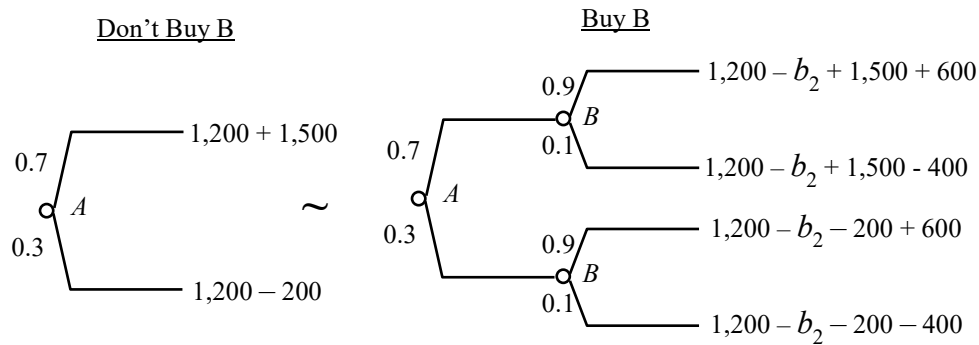
$$\begin{aligned} u(1,200 + s_1) &= 0.7 u(2,700) + 0.3 u(1,000) \\ &= 0.7 (72.900) + 0.3 (10.000) \\ &= 54.030 \end{aligned}$$

Assume  $s_1 \geq -1,200$ :  $(1,200 + s_1)^2 = 54.030 \times 100,000$

$$s_1 = \$1,124.44$$

Anna's PISP for Deal A = **\$ 1,124.44**

(e) Let Anna's PIBP for Deal  $B = b_2$



Equating the expected utility of not buying Deal  $B$  with the expected utility of buying Deal  $B$ :

$$\begin{aligned}
 0.7 u(1,200 + 1,500) &= 0.3 u(1,200 - 200) = \\
 &0.7 (0.9 u(1,200 - b_2 + 1,500 + 600) + 0.1 u(1,200 - b_2 + 1,500 - 400)) + \\
 &0.3 (0.9 u(1,200 - b_2 - 200 + 600) + 0.1 u(1,200 - b_2 - 200 - 400)) \\
 0.7 u(2,700) + 0.3 u(1,000) &= \\
 &0.7 (0.9 u(3,300 - b_2) + 0.1 u(2,300 - b_2)) + 0.3 (0.9 u(1,600 - b_2) + 0.1 u(600 - b_2))
 \end{aligned}$$

Assume  $b_2 \leq 600$ :

$$\begin{aligned}
 0.7 (2,700)^2 + 0.3 (1,000)^2 &= \\
 0.7 (0.9 (3,300 - b_2)^2 + 0.1 (2,300 - b_2)^2) &+ 0.3 (0.9 (1,600 - b_2)^2 + 0.1 (600 - b_2)^2)
 \end{aligned}$$

Using an equation solver:  $b_2 = \$ 520.65$

Anna's PIBP for Deal  $B = \$ \underline{\underline{520.65}}$

(f)

Charlie is risk-neutral.

Charlie's PISP for Deal  $B = EV(B) = 0.9 (600) + 0.1 (-400) = \$ \underline{\underline{500.00}}$