

## IE2111 ISE Principles and Practice II Solutions to Assignment #2

(a)

MARR = 10%.

Total Initial Cost = \$65 million

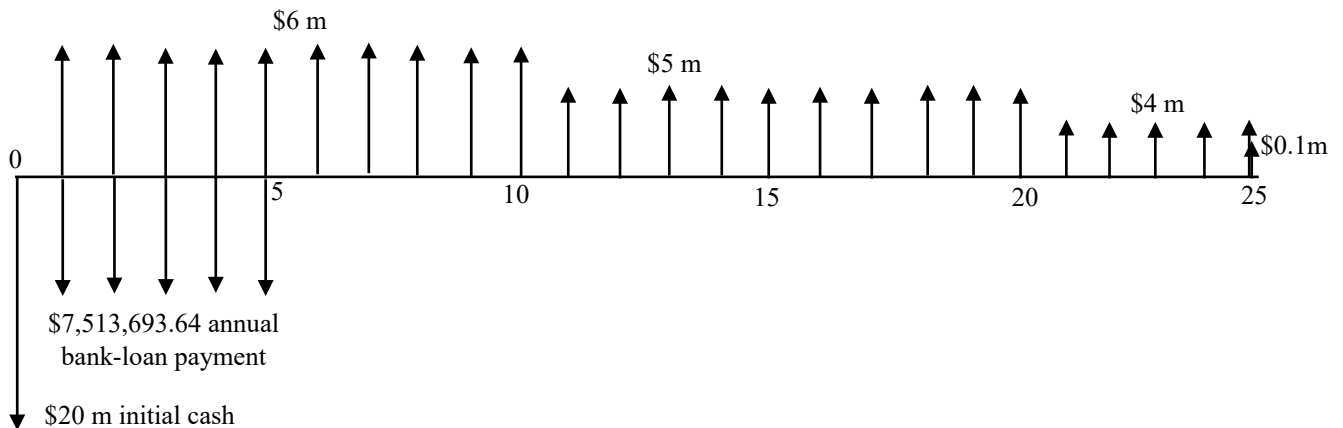
Bank load = \$30 million

Loan interest rate = 8%

Initial Cash Payment = \$20 million.

$$\begin{aligned}\text{Annual repayment amount} &= 30,000,000 [A/P, 8\%, 5] \\ &= 30,000,000 (0.250456455) \\ &= \mathbf{\$ 7,513,693.64}\end{aligned}$$

(b) Cash flow diagram:



(c)

$$\begin{aligned}PW(10\%) &= -20,000,000 && // \text{Initial cash} \\ &\quad -7,513,693.64 [P/A, 10\%, 5] && // \text{Loan repayments years 1 to 5} \\ &\quad +6,000,000 [P/A, 10\%, 10] && // \text{Profits for years 1 to 10} \\ &\quad +5,000,000 [P/A, 10\%, 10] [P/F, 10\%, 10] && // \text{Profit for years 11 to 20} \\ &\quad +4,000,000 [P/A, 10\%, 5] [P/F, 10\%, 20] && // \text{Profit for years 21 to 25} \\ &\quad +100,000 [P/F, 10\%, 25] && // \text{SV at EoY 25} \\ &= -20,000,000 \\ &\quad -7,513,693.64 (3.790786769) \\ &\quad +6,000,000 (6.144567106) \\ &\quad +5,000,000 (6.144567106)(0.385543289) \\ &\quad +4,000,000 (3.790786769)(0.148643628) \\ &\quad +500,000 (0.092295998) \\ &= \mathbf{\$ 2,492,710.07 > 0}\end{aligned}$$

**Hence the project is financially feasible.**

(d) The IRR is  $i$  such that

$$\begin{aligned}PW(i) = & -20,000,000 - \$7,513,693.64 [P/A, i\%, 5] + 6,000,000 [P/A, i\%, 10] \\ & + 5,000,000 [P/A, i\%, 10] [P/F, i\%, 10] + 4,000,000 [P/A, i\%, 5] [P/F, i\%, 20] \\ & + 100,000 [P/F, i\%, 25]\end{aligned}$$

Using an equation solver:  $i = 0.1091$

Hence IRR = **10.91%**

(e) To find the MIRR at financing rate 8% and reinvestment rate 10%:

$$\begin{aligned}|PW(-ve CF at 8\%)| &= 20,000,000 + (7,513,693.64 - 6,000,000) [P/A, 8\%, 5] \\ &= 20,000,000 + 1,513,693.64 (3.992710037) \\ &= \$ 26,043,739.78\end{aligned}$$

$$\begin{aligned}FW(+ve CF at 10\%) &= 6,000,000 [F/A, 10\%, 5] [F/P, 10\%, 15] \\ &+ 5,000,000 [F/A, 10\%, 10] [F/P, 10\%, 5] \\ &+ 4,000,000 [F/A, 10\%, 5] \\ &+ 100,000 \\ &= 6,000,000 (6.1051)(4.1772482) \\ &+ 5,000,000 (15.9374246)(1.61051) \\ &+ 4,000,000 (6.1051) \\ &+ 100,000 \\ &= \$ 305,872,415\end{aligned}$$

$$\begin{aligned}MIRR &= \sqrt[25]{\frac{305,872,415}{26,043,739.78}} - 1 = 0.10355 \\ &= \mathbf{\underline{10.355\%}}\end{aligned}$$

(f) To find the discounted payback period, we compute

for  $k = 1$  to 25:

$$PW_k(10\%) = F_0 + \sum_{j=1}^k \frac{F_j}{(1+0.1)^j}$$

$k$	$F_k$	$PW_k(10\%)$	Sign
0	-20,000,000.00	-20,000,000.00	< 0
1	-1,513,693.64	-21,376,085.12	< 0
2	-1,513,693.64	-22,627,071.60	< 0
3	-1,513,693.64	-23,764,332.03	< 0
4	-1,513,693.64	-24,798,205.16	< 0
5	-1,513,693.64	-25,738,089.81	< 0
6	6,000,000.00	-22,351,246.23	< 0
7	6,000,000.00	-19,272,297.52	< 0
8	6,000,000.00	-16,473,253.24	< 0
9	6,000,000.00	-13,928,667.53	< 0
10	6,000,000.00	-11,615,407.79	< 0
11	5,000,000.00	-9,862,938.30	< 0
12	5,000,000.00	-8,269,784.21	< 0
13	5,000,000.00	-6,821,462.31	< 0
14	5,000,000.00	-5,504,806.04	< 0
15	5,000,000.00	-4,307,845.79	< 0
16	5,000,000.00	-3,219,700.11	< 0
17	5,000,000.00	-2,230,476.77	< 0
18	5,000,000.00	-1,331,182.82	< 0
19	5,000,000.00	-513,642.86	< 0
20	5,000,000.00	229,575.28	> 0
21	4,000,000.00	770,097.56	> 0
22	4,000,000.00	1,261,481.45	> 0
23	4,000,000.00	1,708,194.09	> 0
24	4,000,000.00	2,114,296.48	> 0
25	4,100,000.00	2,492,710.07	> 0

$$PW_{19}(10\%) = - \$ 513,642.86 < 0$$

$$PW_{20}(10\%) = \$ 229,575.28 > 0$$

Discounted Payback period = 20 years.