### ICES-TCADSA

Specifying model parameters

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### Model parameters are what we want to estimate

- We setup a list of model parameters from within R
- The initial value is specified from R
- All the cpp code does is to evaluate the function (and derivatives)
- Optimization is done from R, so values need to be passed from and to many times.
- Simplest example:

```
library(TMB)
compile("scalar.cpp")
dyn.load(dynlib("scalar"))

data <- list()

param <- list()
param$mu <- 0

obj <- MakeADFun(data, param, DLL="scalar")
opt <- nlminb(obj$par, obj$fn, obj$gr)
opt$par</pre>
```

```
#include <TMB.hpp>
template<class Type>
Type objective_function<Type>::operator()()
{
   PARAMETER(mu);
   Type nll = pow(Type(42)-mu,2);
   return nll;
}
```

















# Simple bounds on a parameter (from R)

• Consider the model:

$$X \sim \text{Bin}(100, p)$$

- Let's say we have observed X = 2
- Want to estimate our model parameter p

```
#include <TMB.hpp>
template<class Type>
Type objective_function<Type>::operator()()
{
    DATA_SCALAR(X);
    PARAMETER(p);
    Type nll = -dbinom(X,Type(100),p,true);
    return nll;
}
```

• We get:

```
Estimate Std. Error p 0.02 0.01398284
```

• Now we want to make a 95% confidence interval — see the problem?















# Simple bounds on a parameter (from cpp)

• Consider same model and observation, but now parametrized as:

```
X \sim \text{Bin}(100, p), \text{ where logit}(p) = \alpha
```

• Now we write as:

```
library(TMB)
 compile("p2.cpp")
 dyn.load(dynlib("p2"))
 data <- list()</pre>
 data$X <- 2
 param <- list()</pre>
 param$alpha <- 0
 obj <- MakeADFun(data, param, DLL="p2",
                    silent=TRUE)
 opt <- nlminb(obj$par, obj$fn, obj$gr)</pre>
 summary(sdreport(obj))
      Estimate Std. Error
alpha -3.89182 0.7142857
```

```
#include <TMB.hpp>
template < class Type >
Type trans(Type x){
  return \exp(x)/(Type(1)+\exp(x));
template < class Type >
Type objective_function<Type>::operator()()
  DATA_SCALAR(X);
  PARAMETER(alpha);
  Type p=trans(alpha);
  Type nll = -dbinom(X, Type(100), p, true);
  return nll:
```

• Now we can make a 95% confidence interval:

```
> x < -3.89182 + 0.7142857\% o\% c(-2,2)
> \exp(x)/(1+\exp(x))
             [.1]
                       [,2]
[1,] 0.004867035 0.07847509
```

















#### Exercise

**Exercise 1:** Suggest how to use transformation to parametrize a parameter that is

- a) only positive
- b) only negative
- c) between 2 and 5
- d) an increasing vector

















#### Often we have more than one

• The following parameter types are available:

Template Syntax	C++ type	R type
PARAMETER(name)	Туре	numeric(1)
PARAMETER_VECTOR(name)	vector <type></type>	vector
PARAMETER_MATRIX(name)	matrix <type></type>	matrix
PARAMETER_ARRAY(name)	array <type></type>	array

- Just like with data we can specify a list of possibly many parameter objects
- Naturally we need to match each parameter object on the cpp side

















### Exercise: Probability vector

• For a single probability parameter we can use the inverse logit transformation

$$p = \exp(\alpha)/(1 + \exp(\alpha)), \text{ where } \alpha \in \mathcal{R}$$

• For a probability vector  $p = (p_1, \dots, p_n) \in ]0, 1[^n \text{ with } \sum p = 1 \text{ we can use the following transformation:}$ 

$$p = \begin{pmatrix} \exp(\alpha_1)/(1 + \sum_{i=1}^{n-1} \exp(\alpha_i)) \\ \exp(\alpha_2)/(1 + \sum_{i=1}^{n-1} \exp(\alpha_i)) \\ \vdots \\ \exp(\alpha_{n-1})/(1 + \sum_{i=1}^{n-1} \exp(\alpha_i)) \\ 1 - \sum_{i=1}^{n-1} \exp(\alpha_i)/(1 + \sum_{i=1}^{n-1} \exp(\alpha_i)) \end{pmatrix}$$
 where  $p = \begin{pmatrix} \exp(\alpha_{n-1})/(1 + \sum_{i=1}^{n-1} \exp(\alpha_i)) \\ 1 - \sum_{i=1}^{n-1} \exp(\alpha_i)/(1 + \sum_{i=1}^{n-1} \exp(\alpha_i)) \end{pmatrix}$ 

where  $\alpha \in \mathbb{R}^{n-1}$ 

- Assume we observed the vector (128,158,92,122) from a four dimensional multinomial.
- write the code to estimate the p-vector

















## Collapsing parameters, or fixing them

- The map argument of the MakeADFun can be used to couple elements in a parameter object
- If we have a parameter vector alpha of length 4, then the statement:

  obj <- MakeADFun(data, param, map=list(alpha=factor(c(1,2,3,3))))
- will collapse the last two parameters.
- They will be initialized to the mean of the last two initializations
- The optimizer will estimate a common value for both parameters
- This structure is perfect for testing many model hypotheses
- In addition if NA is set, as in:

```
obj <- MakeADFun(data, param, map=list(alpha=factor(c(1,2,NA,4))))
```

• then the optimizer treat that parameter (here the third) as fixed.