Object-Oriented Python!

classes, subclasses, self and super

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PyLadies-ATX Tech Talk July 18, 2016

Reference version: with bonus notes slides!

OOP!



• This version of the presentation is meant to be used as a reference, rather than presented.

Pages with this appearance contain notes about what I plan to say about the previous slide (the one in the tiny preview at the top of the page).

I hope that you find this useful as a reference.

In this presentation...

All code samples are written with Python 3 in mind.

We will be editing code in a text editor, and running it in the interactive console. When we make changes to our text file, we will need to do the following:

```
if using the built-in console:
    quit()
    python3
    from example import *
if using ipython:

run example.py
```

You will need to do this after each change to the code in a text file. Alternatively, you could use an IDE, such as PyCharm, and that might make the process easier as well.

To make life easier, code examples have been put online at: pydancing.wordpress.com/oop

Before we begin...some nifty python tricks

Save this in a text file called stars.py:

```
def func0(myvar):
    print('myvar = {}'.format(myvar))
    print('type(myvar) = {}'.format(type(myvar)))
def func1(*args):
    print('args = {}'.format(args))
    print('type(args) = {}'.format(type(args)))
def func2(myvar, *args):
    print('myvar = {}'.format(myvar))
    print('args = {}'.format(args))
def func3(myvar, *args, **kwargs):
    print('myvar = {}'.format(myvar))
    print('args = {}'.format(args))
    print('kwargs = {}'.format(kwargs))
    print('type(kwargs) = {}'.format(type(kwargs)))
```

stars.py (for reference)

```
def func0(myvar):
    print('mvvar = {}'.format(mvvar))
    print('type(myvar) = {}'.format(type(myvar)))
def func1(*args):
    print('args = {}'.format(args))
    print('type(args) = {}'.format(type(args)))
def func2(myvar, *args):
    print('myvar = {}'.format(myvar))
    print('args = {}'.format(args))
def func3(myvar, *args, **kwargs):
    print('mvvar = {}'.format(mvvar))
    print('args = {}'.format(args))
    print('kwargs = {}'.format(kwargs))
   print('type(kwargs) = {}'.format(type(kwargs)))
```

Predict the outcome of each of these, and test them in the console:

```
func0(5)
func0()
func0(1,2,3)
```

```
func1(5)
func1()
func1(1,2,3)
```

stars.py (for reference)

```
def func0(myvar):
    print('myvar = {}'.format(myvar))
    print('type(myvar) = {}'.format(type(myvar)))
def func1(*args):
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    print('type(args) = {}'.format(type(args)))
def func2(myvar, *args):
    print('myvar = {}'.format(myvar))
    print('args = {}'.format(args))
def func3(myvar, *args, **kwargs):
    print('mvvar = {}'.format(mvvar))
    print('args = {}'.format(args))
    print('kwargs = {}'.format(kwargs))
    print('type(kwargs) = {}'.format(type(kwargs)))
```

And these:

```
func2(1,2,3,4,5)
func2()
func2(1)
func2(colors)
```

```
func2(*colors)
func2(*triples)
func2(*range(8))
```

stars.py (for reference)

```
def func0(myvar):
    print('myvar = {}'.format(myvar))
    print('type(myvar) = {}'.format(type(myvar)))
def func1(*args):
    print('args = {}'.format(args))
    print('type(args) = {}'.format(type(args)))
def func2(myvar, *args):
    print('myvar = {}'.format(myvar))
    print('args = {}'.format(args))
def func3(myvar, *args, **kwargs):
    print('mvvar = {}'.format(mvvar))
    print('args = {}'.format(args))
    print('kwargs = {}'.format(kwargs))
    print('type(kwargs) = {}'.format(type(kwargs)))
```

And these:

```
func3(1,2,3,4,5)
func3(1,2,3,a=88,b=99)
func3(a=55,b=66,myvar=0)
func3(mathyfolks)
func3(0, mathyfolks)
```

```
func3(0,**mathyfolks)
func3(*colors,**mathyfolks)
func3(**mathyfolks)
func3(**junk)
```

Star Operators

- ► Within the parameters of a function definition:
 - * packs all the extra positional arguments into a tuple
 - ** packs all the extra keyword arguments into a dictionary
- ▶ Within the arguments of a function call:
 - * unpacks a tuple, list, or other sequence type into positional arguments
 - ** unpacks a dictionary into keyword arguments



A quick note...

For this presentation, we won't always begin with the "right" way to do things.

I will frequently start with a not-great approach, just so we can examine the problems. We will refactor the code and make it better.

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A quark note...

For this presentation, we won't always begin with the "right" way to do things.

I will frequently start with a not great approach, just so we can examine the problems. We will refactor the code and make it better.

• I will also ask from time to time what you expect to happen in a situation. "Wrong" answers will be embraced enthusiastically. Some of the ideas that I will introduce are a little bit counter-intuitive. To really understand, we will need to examine our intuition, see how it is different from reality, and take a look at the reason for those differences.

Programming Paradigms

In Procedural Programming, the focus is on step-by-step instructions for the computer. These procedures will operate on data, but the procedures and the data structures are sort of separate concepts.

In Object-Oriented Programming, the code is conceptualized around objects that bundle together relevant values (attributes) and functions (methods).

Programming Paradigms

In Procedural Programming, the focus is on step-by-step instructions for the computer. These procedures will operate on data, but the procedures and the data structures are sort of senarate concents

In Object-Oriented Programming, the code is conceptualized around objects that bundle together relevant values (attributes) and functions (methods).

• There are other paradigms, but these are the two that Python is most commonly used for.

What kinds of objects can you make?

- ► Bank Account
 - attributes: balance, minimum balance, interest rate
 - methods: deposit, withdraw, check balance
- GUI Widget
 - attributes: location, size, color
 - methods: click, drag, mouseover
- Game Character
 - attributes: strength, experience points, inventory
 - methods: move, interact, attack
- User
 - attributes: name, password, other profile information
 - ► methods: log in, edit profile,

Our first homemade object

Let's create our first class:

```
class Thing:
   pass
```

That's all it takes!

Now that we have a new class, we can create an instance of that class:

```
thing = Thing()
```

And we can assign attributes to this object:

```
thing.a = 5
thing.b = 'hi there'
```

Of course, it doesn't actually do anything...

Our first interesting object

Most interesting objects need to be initialized.

In python, we define an __init__ method on our class to handle the initialization.

```
class Rectangle:
    def __init__(self, width, length):
        self.width = width
        self.length = length
```

(Note that there are double underscores at the start and end of the word init.)

OOP!

```
Our first interesting object

Most interesting objects need to be initialized.
In pythos, we define an __likel__ method on our class to handle the

second of __likel__ (wil, wildth, length);

of __likel__ (wil, _likel__ tength);

of __likel__ likel__ likel__ tength

of __likel__ likel__ likel__ tength

(block that there are double underscores at the start and and of the word (wil.)
```

- The <u>__init__</u> method that we are defining here is sometimes called a magic method. You can call it directly, but you don't usually. Instead, python uses this method automatically whenever a new instance of the class is created.
- The first argument passed to init is the newly created instance of the class.
 Call this self.
 - (This is not specific to init: the first argument passed to any method is the instance, and it should always be called self. Python wont enforce this, but your fellow coders and future self will thank you.)
- Notice that <u>__init__</u> does not return anything! It sets the values of attributes on the newly created object. It should never contain a return statement.

Our first interesting object

To make this example more useful, lets add another method.

```
class Rectangle:
    def __init__(self, width, length):
        self.width = width
        self.length = length

    def area(self):
        return self.width * self.length
```

Let's make a rectangle! In the console:

```
from shapes import *
r = Rectangle(3,5)
r.width
r.length
r.area
r.area()
dir(r)
isinstance(r,Rectangle)
r
```

We will want a better representation of our rectangle than <__main__.Rectangle at 0x101e45ba8>

Better represenation

There are two special methods that we can use to return a string representation of our objects: __str__ and __repr__.

- __str__ should be used for a string representation that is useful to the end-user.
- ► __repr__ should be used for a string representation that is useful to the programmer. This is what the console shows.

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Better representation

There are two special methods that we can use to return a string representation of or or dejects. __str___ and __stpg.__

- _str___ elocable be used for a string representation that is useful to the __str___ elocable be useful for a string representation that is useful to the programmer. This is what the consider shows.

 It is considered a good practice to make the output of __repr__ something that can recreate the object, if possible. If this is not possible, a useful description for debugging purposes should be enclosed in

Better representation

Let's add a __repr__ method to our class:

```
class Rectangle:
    def __init__(self, width, length):
        self.width = width
        self.length = length
    def __repr__(self):
        return 'Rectangle(%s,%s)' % (self.width, self.length)
   def area(self):
        return self.width * self.length
```

Load the new code in the interactive interpreter, make a new rectangle object, and see how it is displayed.

One more method...maybe an attribute?

Suppose we need the length of the diagonal of our rectangle.

Since the diagonal of a rectangle with sides l and w is $\sqrt{l^2 + w^2}$, we can write a method:

```
from math import sqrt

class Rectangle:
     :
     @property
     def diagonal(self):
        return round(sqrt(self.length**2 + self.width**2), 2)
```

The **@property** decorator makes a method seem like an attribute.

One more method...maybe an attribute?



You may not be familiar with decorator. (This is the first context I ever saw them). A
decorator is a way of changing a function into something else (usually another
function). The best explaination of decorators I have found is at:
pythonconquerstheuniverse.wordpress.com/2012/04/29/python-decorators/

Subclassing

We can create a subclass of any existing class—whether that class is a built-in class or something that we've made ourselves.

In shapes.py, add:

```
class Square(Rectangle):
    def __init__(self, side):
        self.side = side
```

In the console:

```
s = Square(5)
dir(s)
```

Where does the area method come from? What happens when you run s.area()?

Subclassing

When subclassing, you must make sure that all necessary attributes for the superclass are initialized on your subclass.

We could do that manually, or we could use the super function*.

The **super** function returns the superclass of the class you're currently writing.

Subclassing

We can fix our **Square** class like this:

```
class Square(Rectangle):
    def __init__(self, side):
        self.side = side
        super().__init__(side, side)
```



Now, try this in the terminal:

```
s = Square(8)
s.side
s.width
s.height
s.area()
```

```
isinstance(s, Square)
isinstance(s, Rectangle)
s
```

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└─Subclassing

```
Subclassing
We can't car Square (dear the this
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```

- Since Square is a subclass of Rectangle, we say Rectangle is a superclass of Square.
- super is a built-in python function that, when used inside a class method, gets the superclass of the class (it's a little more complicated once we get to multiple inheritence, but we'll talk about that later.
- In Python 2, you need to provide arguments for super. The arguments should be the name of the class that you are currently writing (not the superclass!) and self. So in our example, it would be: super(Square, self). __init__(side, side)
- Notice that our object s identifies itself as a rectangle still. That is less than ideal, and we'll fix it in the next slide.

Refactoring time

When you find yourself having to make lots and lots of little changes every time you make a new subclass, it's time to take a step back, think over your entire project, and refactor your code.

Let's create a new base class, Shape, which we won't instantiate directly, but will hold the some code that will be common to all our shapes.

Refactoring time

```
class Shape:
    def __init__(self, *args, **kwargs):
        self.args = args
        self.kwarqs = kwarqs
    def __repr__(self):
        shape = self.__class__._name__
        all\_args = []
        for arg in self.args:
            all_args.append(repr(arg))
        for kw. arg in self.kwargs.items():
            all_args.append('{0}={1}'.format(kw, repr(arg)))
        comma_sep_args = ', '.join(all_args)
        return '{0}({1})'.format(shape. comma_sep_args)
```

Changes to the Base Class

Let's assume that we want every subclass of shape to be able to calculate its area.

```
class Shape:
     :
     def area(self):
        raise NotImplementedError
```

This doesn't force subclasses to implement an area method, it's just a convention for working with other programmers.

OOP!



If you need to absolutely force certain methods to be implemented, look into the
 abc module of the standard library. That will allow you to create an Abstract Base
 Class to which you can add abstract methods which must be implemented on any
 subclass before the subclass can be instantiated. You can read more about the
 abc
 module at: https://docs.python.org/3/library/abc.html

Changes to the Base Class

Finally, let's make shape a property of our base class:

Now let's get subclassin'

There are two main ways that we could handle the parameters for initializing the Rectangle class:

```
class Rectangle(Shape):
    def __init__(self, width, length):
        self.width = width
        self.length = length
        super().__init__(width, length)
```

```
class Rectangle(Shape):
    def __init__(self, *args):
        self.width, self.length = sorted(args)
        super().__init__(*args)
```

Putting conditions on init

```
class Triangle(Shape):
    def __init__(self, *args):
        a, b, c = sorted(args)
        if a + b \le c:
            raise ValueError('Cannot construct triangle with sides given.
        self.sides = (a.b.c)
        super().__init__(*args)
    def area(self):
        semi = sum(self.sides)/2
        a.b.c = self.sides
        return math.sqrt(semi*(semi-a)*(semi-b)*(semi-c))
```

Errors are objects too

You can subclass errors, to get your own, special ones:

```
class GeometryError(ValueError):
    pass
```

Let's change the previous error line to use our new error:

```
raise GeometryError('Cannot construct triangle with sides given.')
```

Your turn...

Make a Circle class.

This is one possible solution:

```
class Circle(Shape):

   def __init__(self, radius):
       self.radius = radius
       super().__init__(radius)

   def area(self):
       return 3.14 * self.radius**2
```

Equality!

Load shapes.py into the console, and try this:

What happens? Any ideas why?

If python doesn't have any instructions on how to determine equality, it goes by an object's location in memory.

Since these are two different instances, python says they're not equal, even though they're identical.

If we want different behavior, we have to tell it how to determine equality.

Equality!

To tell python how to determine equality, we add another special method, called

```
__eq__:
class Shape:
    def __eq__(self. other):
        if self.__class__ != other.__class__:
             return False
         if (self.args == other.args):
             return True
        return False
```

Now try Circle(3) == Circle(3) again.

Operator Overloading / More Special Methods

Open **fractions.py** in a text editor.

```
class Fraction:
    def __init__(self, numerator, denominator=1):
        if not all([isinstance(i,int) for i in (numerator,denominator)]):
            raise ValueError('Arguments of Fraction must be integers')
        g = gcd(numerator,denominator)
        self.n = int(numerator/g)
        self.d = int(denominator/q)
    def neg (self):
        return Fraction(-self.n.self.d)
    def abs (self):
        return Fraction(abs(self.n).abs(self.d))
    def __add__(self. other):
        if not isinstance(other, Fraction):
            other = Fraction(other)
        n = self.n * other.d + self.d * other.n
        d = self_*d * other_*d
        return Fraction(n. d)
    def __sub__(self, other):
        return self + (-other)
    def __mul__(self, other):
        if not isinstance(other. Fraction):
            other = Fraction(other)
        n1. d1 = self.n. self.d
```

Operator Overloading / More Special Methods

Here are some common operators and the methods to implement on your classes.

	.1 1
operation	method
obj + other	add
obj - other	sub
obj * other	mul
obj // other	floordiv
obj / other *	div
obj / other *	*truediv
obj % other	mod
obj ** other	pow

operation	method
other + obj	radd
other - obj	rsub
other * obj	rmul
other // obj	rfloordiv
other / obj *	rdiv
other / obj **	rtruediv
other % obj	rmod
other ** obj	rpow

^{*} only in Python 2

^{**} in Python 3, or in Python 2, with from __future__ import division

OOP!

ere are some com asses.	mon operators and	the methods to impleme	nt on your
operation	method	operation	method
obj + other	add	other + obj	radd
obj - other	sub	other - obj	rsub
obj * other	mul	other * obj	rmul
obj // other	floordiv	other // obj	_rfloordiv_
obj / other "	div	other / obj *	rdiv
obj / other "	truediv	other / obj ""	rtruediv
obj % other	mod	other % obj	rmod
obj ** other	pow	other ** obj	rpow

• obj is the instance of the object that you are writing a class for, other is the object that will be added/subtracted/multiplied/etc. to it

Operator Overloading / More Special Methods

We implemented __eq__ on our shapes class, but there are more comparison operators than just that.

operation	method
<pre>obj == other</pre>	eq
obj != other	ne
obj < other	lt
obj > other	gt
obj <= other	le
obj >= other	ge

-Operator Overloading / More Special Methods



• For our fractions class, we could either implement all six comparisons, or we could implement __eq__ plus just one of __lt__ , __gt__ , __le__ , or __ge__ and use the class decorator @total_ordering.

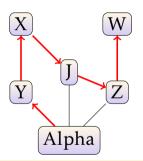
Multiple Inheritance

Python allows a class to inherit from multiple classes.

Multiple Inheritance: Method Resolution Order

In uncomplicated cases, when Python is looking for a method or attribute, it checks the parent classes from left to right, depth first.

```
class X:
    pass
class Y(X):
    pass
class W:
    pass
class Z(W):
    pass
class 1:
    pass
class Alpha(Y.J.Z):
    pass
```



```
>>> Alpha.mro()
[<class 'multi.Alpha'>, <class 'multi.Y'>,
<class 'multi.X'>, <class 'multi.J'>,
<class 'multi.Z'>, <class 'multi.W'>, <class 'object'>]
```

Multiple Inheritance: Method Resolution Order

MROs get more complicated if the diagram of classes contains cycles.

class A:

#stuff

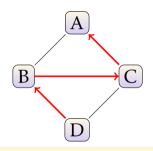
class B(A):

#stuff

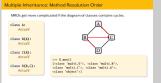
class C(A):

#stuff

class D(B,C):
 #stuff



Order



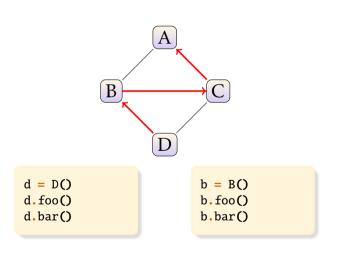
• Emphasize that it's important that if This is a parent class of That, then This must come after That in the MRO.

Multiple Inheritance: Method Resolution Order

Now let's look at what happens when we actually call some methods from a class that uses multiple inheritance.

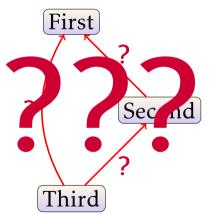
Multiple Inheritance: Method Resolution Order

```
class A:
    def foo(self):
        print('foo from A')
class B(A):
    def foo(self):
        print('foo from B')
        super().foo()
    def bar(self):
        print('bar from B')
class C(A):
    def foo(self):
        print('foo from C')
        super().foo()
    def bar(self):
        print('bar from C')
class D(B.C):
    def foo(self):
        print('foo from D')
        super().foo()
```



Multiple Inheritance: My Weirdest Example

```
class First:
    pass
class Second(First):
    pass
class Third(First, Second):
    pass
```



Let's try running this code, and see what happens.

Multiple Inheritance: Important Points

Python's multiple inheritance allows you to create a class that inherits from more than one class. It's not as hard as some claim, but you do need to be aware of a few things:

- Python determines where to look for methods and attributes by the Method Resolution Order. This also determines what method gets called by super()
- ► The approach to the Method Resolution Order, is left-to-right, depth-first, guarantees that each class only appears once, and that parent classes appear after all classes that inherit from them.
- A common pattern is to have a base class that you want to modify with small modifier classes Because the overall approach to the Method Resolution Order is left-to-right, you should **not** use class MvClass(BaseClass, Modifier1, Modifier2).

Instead, use class MyClass(Modifier2, Modifier1, BaseClass):

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Multiple Inheritance: Important Points

Multiple Inheritance: Important Points

Pythor's multiple inheritance allows you to create a class that inherits from more than
one class. Not not the and a source class, 100, 200 more fall to assure at 4 feet theyer.

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mortifier classes finesses the court approach to the Method Methodson Onle is
class Piclass (Standardon, Methodson Once in
class Piclass (Standardon), Methodson Once in
clas

• When working in Python 2, you must create your classes by subclassing the built-in object class MyClass(object): instead of class MyClass: . Otherwise, you will have broken and unpredictable multiple inheritance behavior.

Back to the shapes

We're going to work with the shapes.py code again, so please copy the slightly updated version from pydancing.wordpress.com/oop

OOP!

Back to the shapes

Wire going to exist with the shapes by code again, so please capy the slightly updated version from pydancing eroriginess.com/eep

• One problem with the code we've written for our various shapes is that even though the base class handles kwargs, the subclasses don't, and don't pass any along to super, so the base class won't actually get any kwargs. This update fixes that.

Mixin Classes

A mixin class is a class meant to be inherited together with a "true" base class.

Usually mixins provide a feature that you might want to add to several classes.

Mixin: Colors With Our Shapes

Let's create a mixin class that allows us to create colored versions of the shapes we have in shapes.py.

```
class ColorMixin:
    is colored = True
    def __init__(self, *args, **kwargs):
        color = kwarqs.get('color', None)
        if color is None:
            color = random.choice(COLORS)
            kwarqs['color'] = color
        self.color = color
        super().__init__(*args, **kwargs)
```

Now, what should we do to create a **ColoredCircle** class?

Mixin: Inheriting Color

For each shape that we want a colored version of, we need to create a class that inherits from our ColorMixin and the original shape.

```
class ColoredCircle(ColorMixin, Circle):
    pass
```

Since all the work is done in the parent classes, we don't need much code here. In real-world code, it is best to include a docstring and perhaps some doctests.

Then to instantiate our new class:

```
y = ColoredCircle(5, color='Yellow')
r = ColoredCircle(11)
```

Pythonic Protocols

Python doesn't have interfaces the way Java and many other staticly-typed languages do.

Because traditionally Python relies heavily on duck typing, for your object to be treated like one of a category of objects, all you have to is implement the right methods. This is sometimes loosely called a Protocol.

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Pythonic Protocols

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Python describ have interfaces the way Java and many other staticly-typed languages do.

Because staticisally Python reflects beauty on plant styring, for your object to be traveled the own of actingery of depicts, also have to in implement the right methods. This is sometimes loosely called a Protocol.

• You *can* create interfaces in Python (see Zope) but it's not necessary the way it is in other languages, because Python generally relies on Duck-Typing and supports multiple inheritance

Protocols

To create a container object, implement:

- ▶ __len__
- __getitem__
- __setitem__ (if you want a mutable container)
- __delitem__ (if you want a mutable container)
- ► __iter__ (if you want your container to be iterable)

To create an iterator, either write a generator (a function that uses the yield
statement to return a sequence of values) or write a new class that implements:

- __iter__
- __next__



Protocols

To create a context manager object that works in a with statement:

- __enter__
- __exit__

```
with Thing(foo) as bar:
   bar.blah()
   # do stuff with bar in the indented block
   # and when the block ends, perform whatever
   # clean-up actions are necessary.
```

To create an object that can be called like a function, implement:

Subclassing Built-In Types

Although duck typing is the "Pythonic" way, if your object needs to interact with code that will do isinstance checks, you should subclass the type that you need it to be. You can then change the methods however you want.

—Subclassing Built-In Types

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Subclassing Built-In Types

• Remember, when you write a method on a subclass, the method with the same name on the superclass is replaced.

Frequently Asked Question

by people who have done OOP in other languages

How do I make attributes of an object private or protected?

This is somewhat discouraged in Python. In general, the Pythonic mindset is to document your code well, follow conventions, and trust that other programmers won't do stupid things unless they have a really good reason.

A convention is that names that begin with one underscore shouldn't be accessed directly. If you do this, you should provide another way to access the attribute.

Protection for Attributes

Let's change our **Circle** class to follow this convention:

```
class Circle(Shape):
    def __init__(self, radius, **kwargs):
        self. radius = radius
        super().__init__(radius. **kwarqs)
    @property
    def radius(self):
        return self. radius
    def area(self, dp=2):
        return round(math.pi * self._radius**2. dp)
```

That does not prevent someone else from using or changing the attribute.

mycircle. radius = 0 will work.

Stronger Protection for Attributes

There is a stronger form of protection you can use:

```
class Circle(Shape):
    def __init__(self, radius, **kwargs):
        self. radius = radius
        super().__init__(radius. **kwargs)
    @property
    def radius(self):
        return self. radius
    @radius.setter # circle.radius = <something> will call this
    def radius(self. name):
        raise AttributeError("Don't do that!")
    def area(self, dp=2):
        return round(math.pi * self.__radius**2, dp)
```

Stronger Protection for Attributes

Behind the scenes, what Python does in this case is called **name-mangling**.

```
It stores self.__radius as self.__Circle__radius.
```

The good news is mycircle._radius = 0 will result in an error message. The bad news is, if someone is determined to break things, they can do mycircle._Circle__radius = 0.

The End. (I'm serious this time.) Questions