

**Lemma 1.** *Show that there exists no smallest positive rational number.*

*Proof.* Suppose for contradiction that  $i$  is the smallest positive rational number.  $i/2$  is also rational, and  $0 < i/2 < i$ . This is a contradiction, thus there is no smallest positive rational number. ■