

## Exercise 3.3.7

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Claim: all nodes reachable from  $u$  will be marked as visited.

*Proof.* By induction, on distance from  $u$ . (for every node  $v$ , which is reachable from  $u$ , there is some path from  $u$  to  $v$ ).

Let  $k_v$  be the distance from  $u$  to  $v$ .

Base case:  $k_v=0$ . (can get to  $v$  in zero steps, so  $v$  must equal  $u$ ). So  $v=u$ . Thus  $u$  is marked as visited.

IH: suppose all nodes distance  $d$  from  $u$  will be marked. Show nodes  $d+1$  distance from  $u$  get marked. These nodes get explored when their neighbors, which are distance  $d$  from  $u$  get explored. So the nodes at distance  $d+1$  from  $u$  get visited. ■