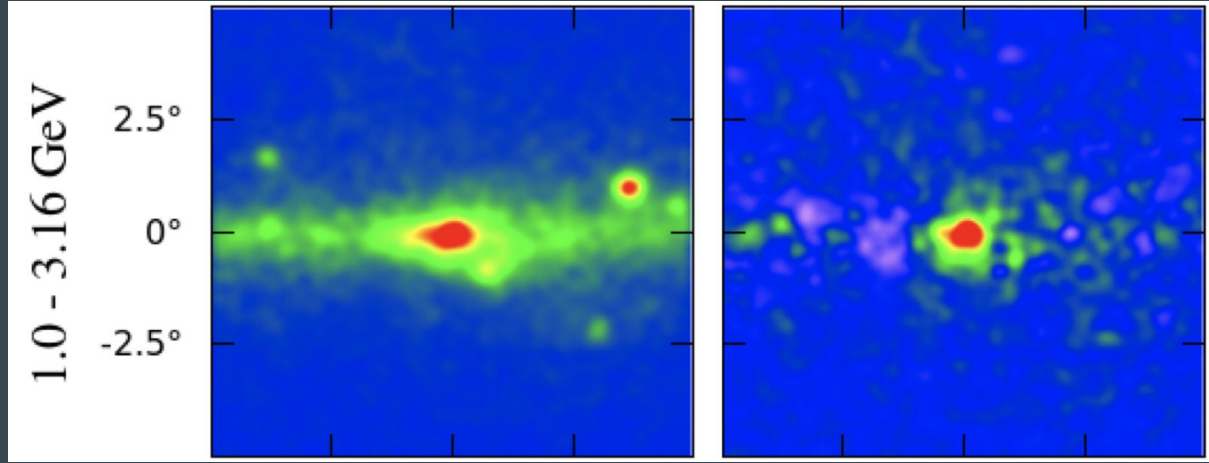


Gravitational Waves and the Galactic Center Excess: Using Millisecond Pulsars to Probe Physics Beyond the Standard Model

...

Kayla Bartel

The Galactic Center Excess (GCE)

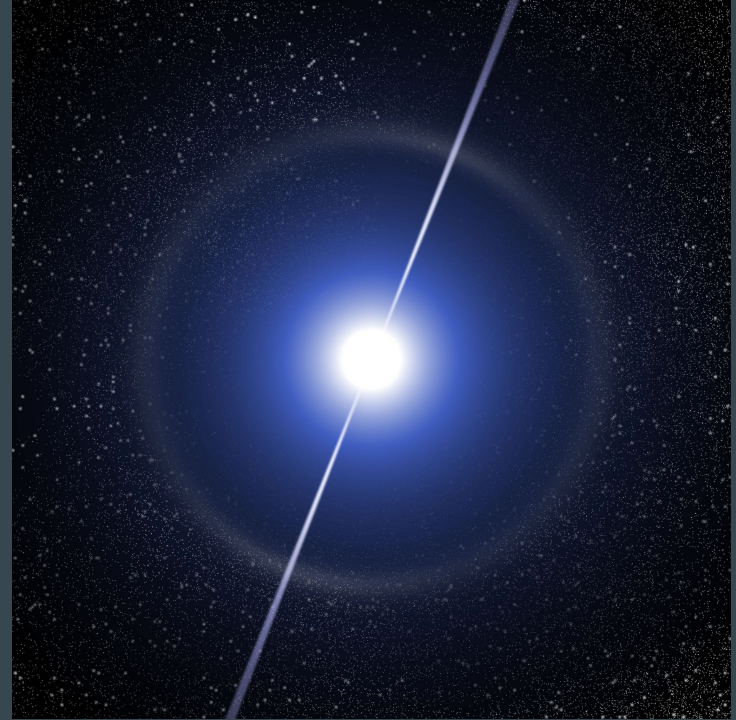
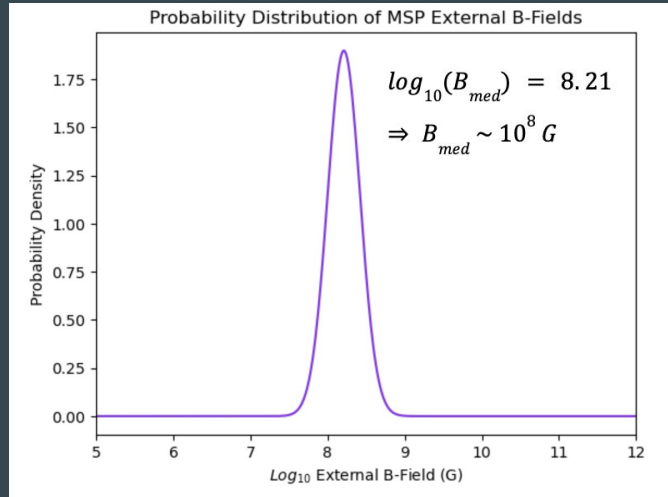


Daylan, et al. (2014)

- Source of high energy gamma rays (1-3 GeV) (Holst, 2024)
- Two potential causes: annihilating DM or unresolved population of MSPs (Slatyer, 2022)

Millisecond Pulsars (MSPs)

- Rapidly rotating (periods of milliseconds) neutron stars
- Emit gamma rays
- Have strong magnetic fields (Ploeg, 2021):



https://commons.wikimedia.org/wiki/File:Pulsar_2.jpg

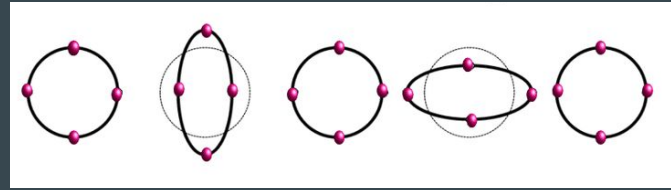
Gravitational Waves (GWs)

- Caused by rotating objects with axial asymmetry (Agarwal, 2022)
- Characterized by ellipticity, which can be found from an MSP's internal magnetic field (Miller, 2023):

$$\epsilon \approx 10^{-8} \frac{B_{int}}{10^{12}}$$

- Amplitude of (Miller, 2023):

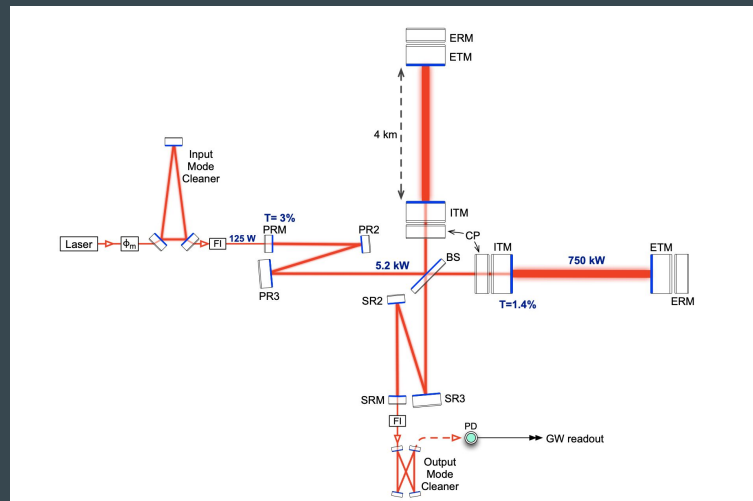
$$h_0 = \frac{16\pi^2 G}{c^4} \frac{I_{zz} \epsilon f_{rot}^2}{d}$$



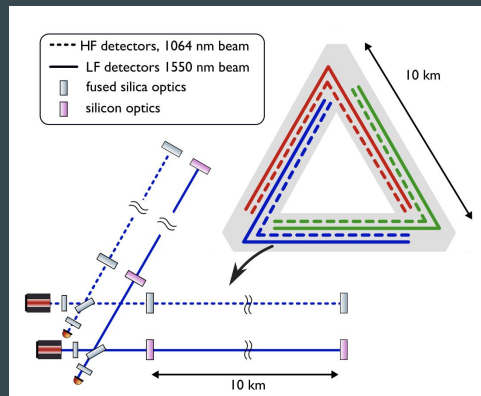
Belahcene, 2019

Gravitational Wave Detectors

- Use laser interferometry to detect gravitational waves (Abbott, 2009)
- Current detectors: aLIGO (Abbott, 2009), aVIRGO (Acernese, 2014), KAGRA (Aso, 2013)
- Future detector: Einstein Telescope (Rowlinson, 2021)



Advanced LIGO, 2015



Rowlinson, 2021

How do we generate a population of MSPs and the corresponding the GW signal?

Sample the MSP density distribution to get population

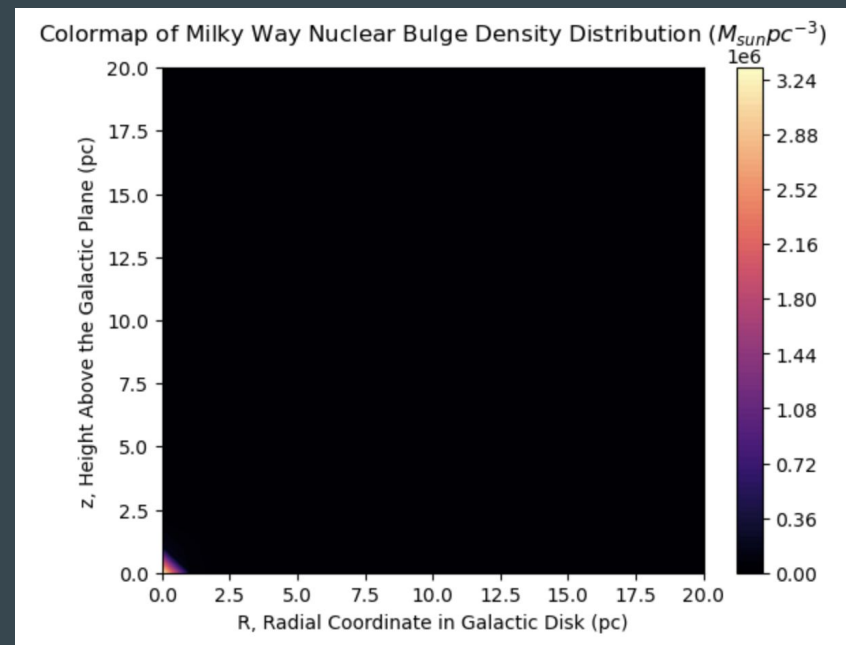
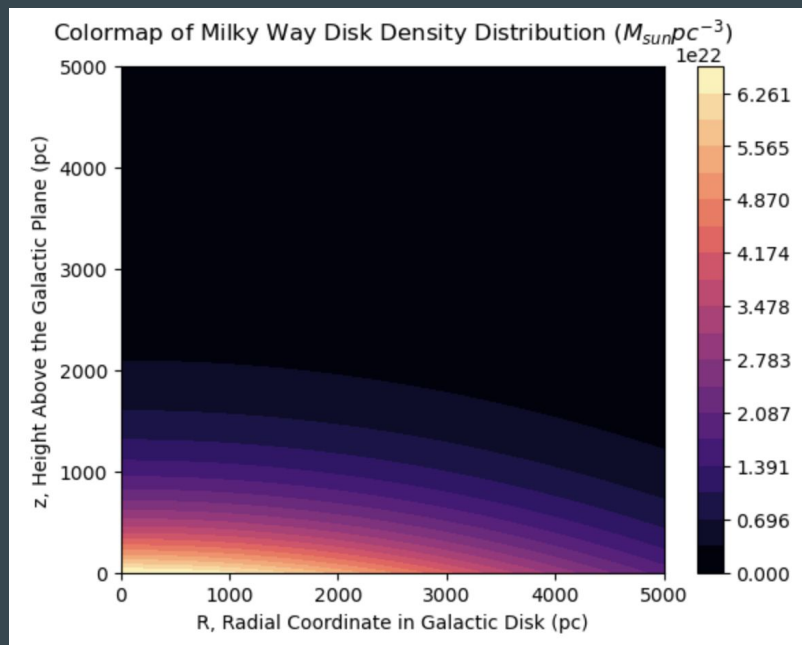
Find the ellipticity distribution from the internal B-fields

Calculate the GW signal using
$$h_0 = \frac{16\pi^2 G}{c^4} \frac{I_{zz} \epsilon f_{rot}^2}{d}$$
 and the GW frequency using
$$f_{GW} = 2f_{rot}$$

Constrain the signal using GW detector sensitivities

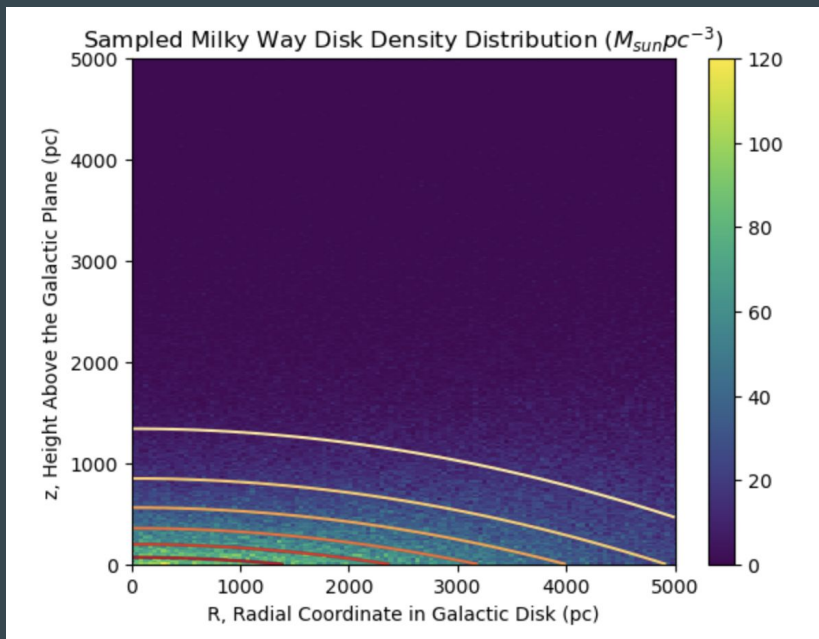
Millisecond Pulsar Densities in the Milky Way

- 2 populations: the Milky Way Disk and the Milky Way Nuclear Bulge

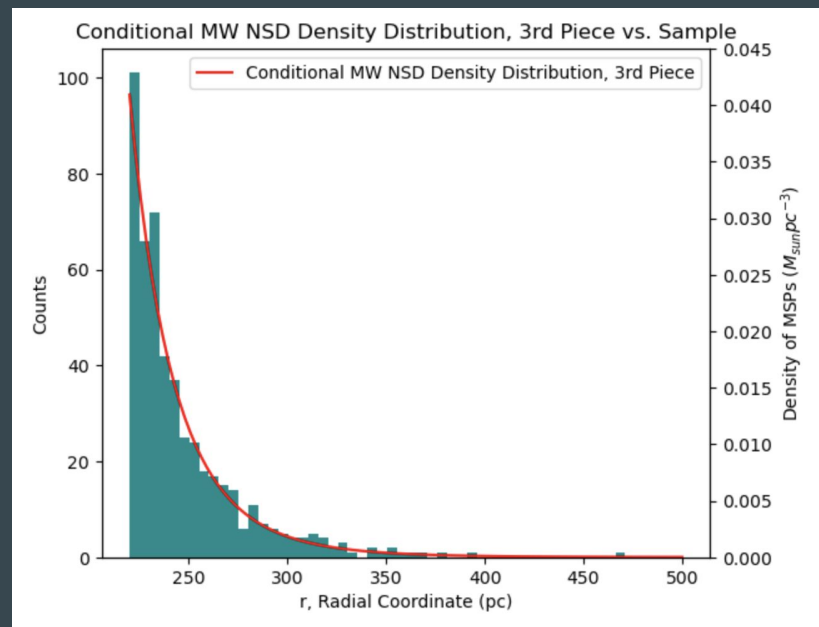


Sampling the MSP Population

MCMC Method

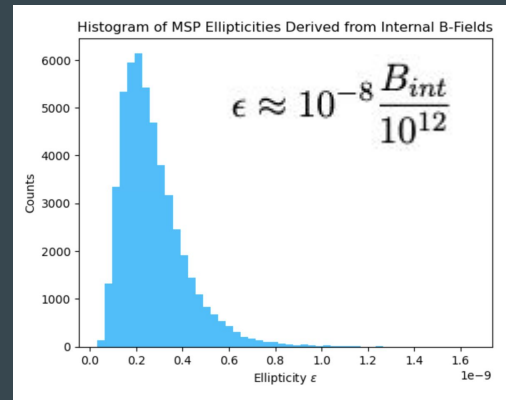
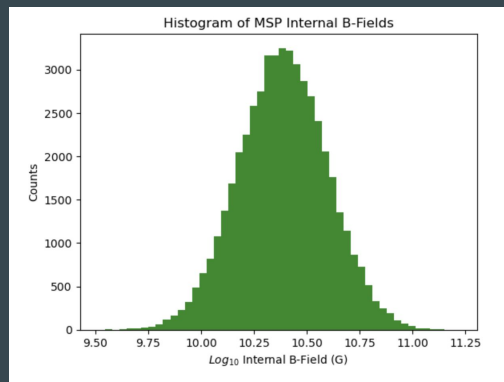
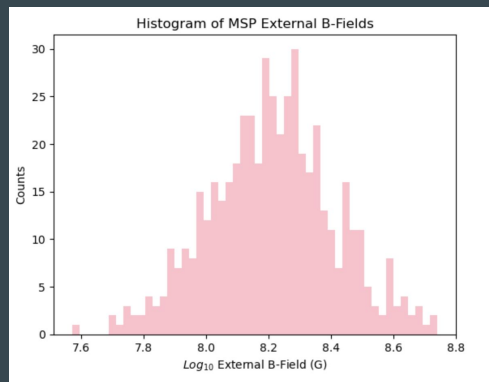


Inverse Transform Method



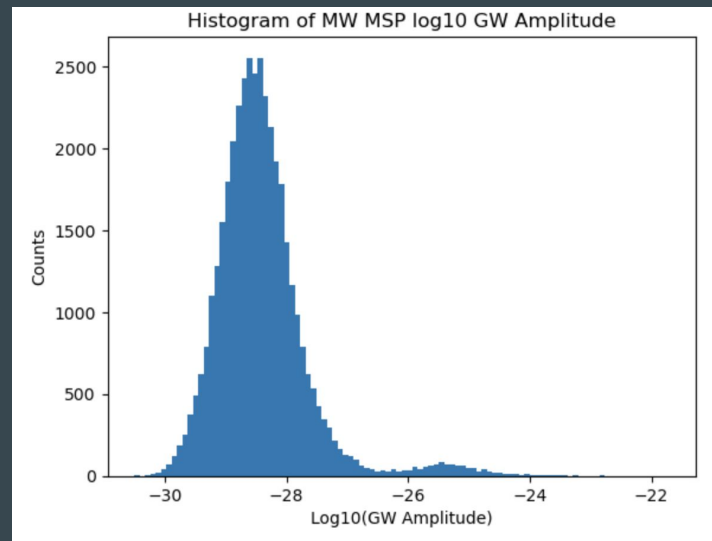
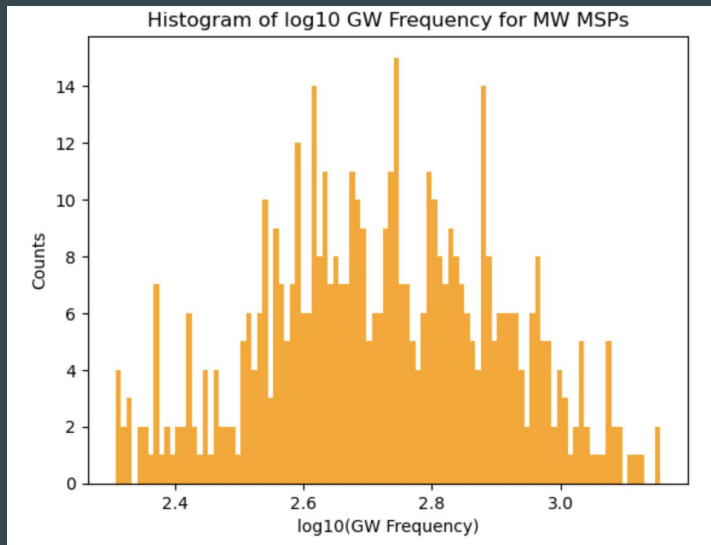
Ellipticity Distribution of MSPs

- External B-field \rightarrow internal B-field \rightarrow ellipticity (Miller, 2023)



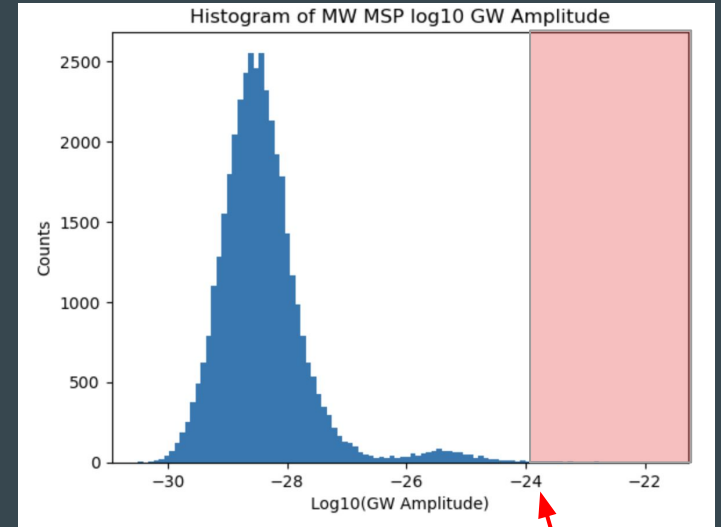
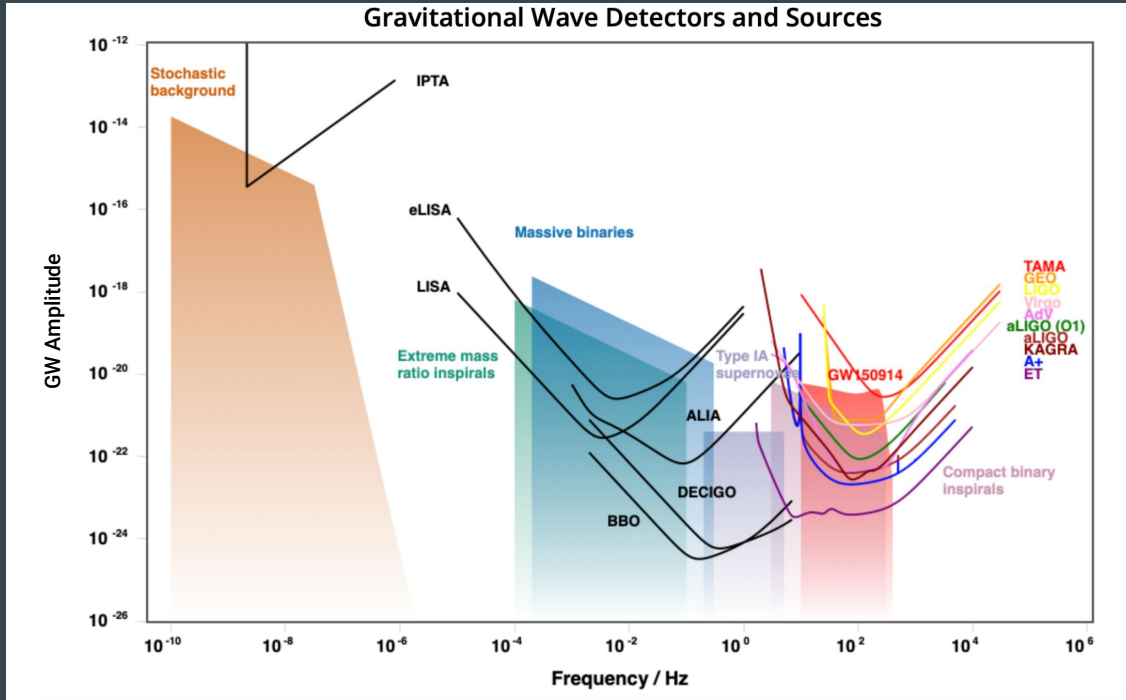
- Ellipticity minimums are $\sim 10^{-9}$ (Woan, 2018)

Generating the GW Signal



Analysis and Possibility of Detection Pt. I

- GW amplitudes on the order of $10^{-24} - 10^{-20}$

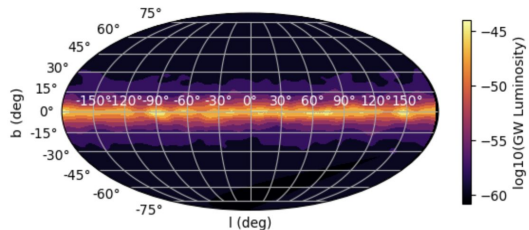


Max.
Sensitivity

Analysis and Possibility of Detection Pt. II

No Detector Constraints

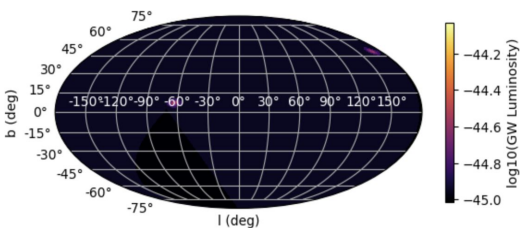
Sampled MW Disk and Bulge Population of MSPs with log10 Smoothed (1.7 deg) GW Luminosity in Galactic Coordinates



Conservative Constraints

$> \sim 10^{-23}$ (aVIRGO, aLIGO, Kagra)

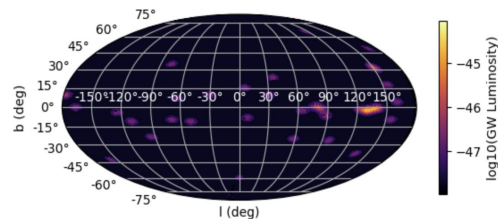
Sampled MW Disk and Bulge Population of MSPs with log10 Smoothed (1.7 deg) GW Luminosity in Galactic Coordinates (conservative)



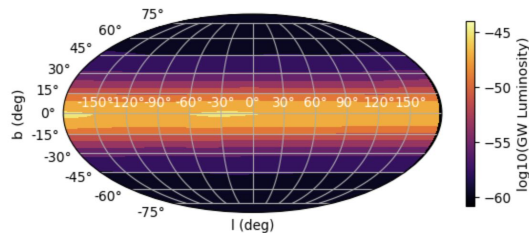
Optimal Constraints

$> \sim 10^{-24}$ (ET)

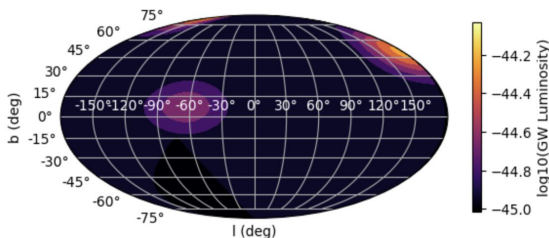
Sampled MW Disk and Bulge Population of MSPs with log10 Smoothed (1.7 deg) GW Luminosity in Galactic Coordinates (best)



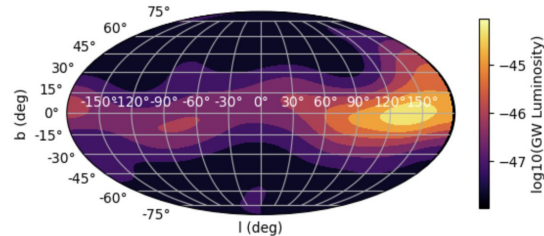
Sampled MW Disk and Bulge Population of MSPs with log10 Smoothed (10 deg) GW Luminosity in Galactic Coordinates



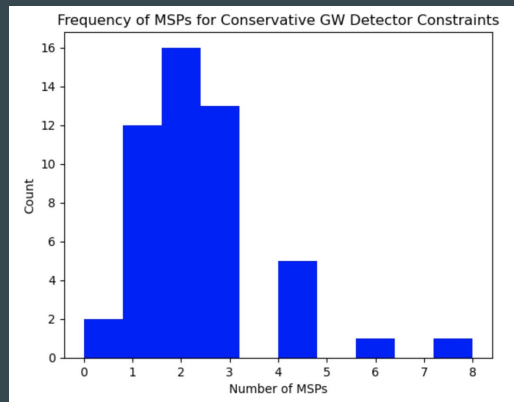
Sampled MW Disk and Bulge Population of MSPs with log10 Smoothed (10 deg) GW Luminosity in Galactic Coordinates (conservative)



Sampled MW Disk and Bulge Population of MSPs with log10 Smoothed (10 deg) GW Luminosity in Galactic Coordinates (best)

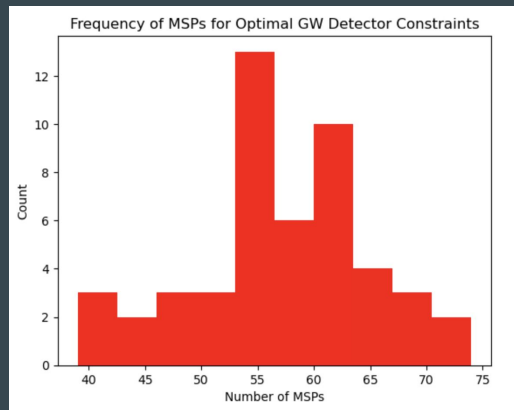


Analysis and Possibility of Detection Pt. III

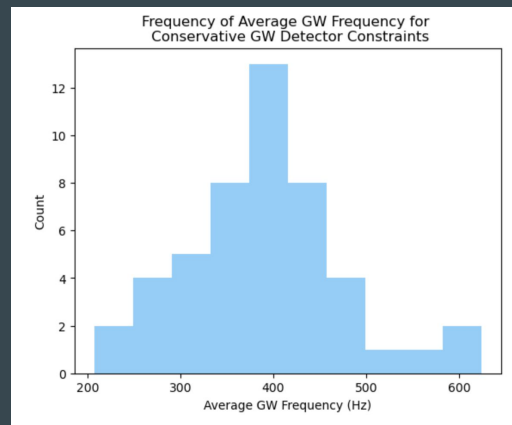


Ave. Number
of MSPs
detectable:

Conservative:
2

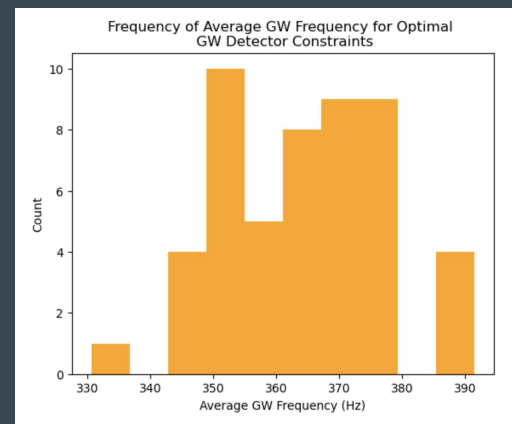


Optimal:
57



Ave. GW
Frequency
detectable:

Conservative:
390 Hz



Optimal:
360 Hz

Conclusion

- Only Advanced LIGO/Virgo (with sensitivities above $\sim 3 \cdot 10^{-23}$), Kagra (with sensitivities above $\sim 10^{-23}$), and ET (with sensitivities above $\sim 10^{-24}$) would be capable of detecting the GW signal
- if MSPs are responsible for the GCE, then between ~ 2 – 57 pulsars should be detectable on average with a corresponding GW frequency range of 360–390 Hz
- GW detectors sensitive to frequencies in the hundreds of hertz, sensitive to gravitational waves from MSPs, must see at least a few MSPs, otherwise there are strong constraints placed on MSP's contribution to the GCE
- Future work: get a more robust statistical picture of our population of MSPs and the corresponding detectability

References

Sources:

- Ian Holst and Dan Hooper. A New Determination of the Millisecond Pulsar Gamma-Ray Luminosity Function and Implications for the Galactic Center Gamma-Ray Excess. 2024. arXiv:2403.00978[astro-ph.HE].
- Tracy Slatyer. “Les Houches Lectures on Indirect Detection of Dark Matter”. In: SciPost Physics Lecture Notes (May 2022). issn: 2590-1990. doi:10.21468/scipostphyslectnotes.53. url: <http://dx.doi.org/10.21468/SciPostPhysLectNotes.53>
- Harrison Ploeg. The Galactic Millisecond Pulsar Population: Implications for the Galactic Center Excess. 2021. arXiv:2109.08439 [astro-ph.HE]
- Deepali Agarwal et al. “Targeted search for the stochastic gravitational wave background from the galactic millisecond pulsar population”. In: Physical Review D 106.4 (Aug. 2022). issn: 2470-0029. doi:10.1103/physrevd.106.043019. url: <http://dx.doi.org/10.1103/PhysRevD.106.043019>.
- Andrew L. Miller and Yue Zhao. “Probing the Pulsar Explanation of the Galactic-Center GeV Excess Using Continuous Gravitational Wave Searches”. In: Physical Review Letters 131.8 (Aug. 2023). issn: 1079-7114. doi:10.1103/physrevlett.131.081401. url: <http://dx.doi.org/10.1103/PhysRevLett.131.081401>
- B P Abbott et al. “LIGO: the Laser Interferometer Gravitational-Wave Observatory”. In: Reports on Progress in Physics 72.7 (June 2009), p. 076901. issn: 1361-6633. doi:10.1088/0034-4885/72/7/076901. url: <http://dx.doi.org/10.1088/0034-4885/72/7/076901>.

References

Sources:

F Acernese et al. “Advanced Virgo: a second-generation interferometric gravitational wave detector”. In: Classical and Quantum Gravity 32.2 (Dec. 2014), p. 024001. issn: 1361-6382. doi:10.1088/0264-9381/32/2/024001. url:<http://dx.doi.org/10.1088/0264-9381/32/2/024001>

Yoichi Aso et al. “Interferometer design of the KAGRA gravitational wave detector”. In: Physical Review D 88.4 (Aug. 2013). issn: 1550-2368. doi:10.1103/physrevd.88.043007. url:<http://dx.doi.org/10.1103/PhysRevD.88.043007>.

Samuel Rowlinson et al. “Feasibility study of beam-expanding telescopes in the interferometer arms for the Einstein Telescope”. In: Physical Review D 103.2 (Jan. 2021). issn: 2470-0029. doi:10.1103/physrevd.103.023004. url:<http://dx.doi.org/10.1103/PhysRevD.103.023004>

Images (slides 1–5):

<https://arxiv.org/abs/1402.6703>

https://commons.wikimedia.org/wiki/File:Pulsar_2.jpg

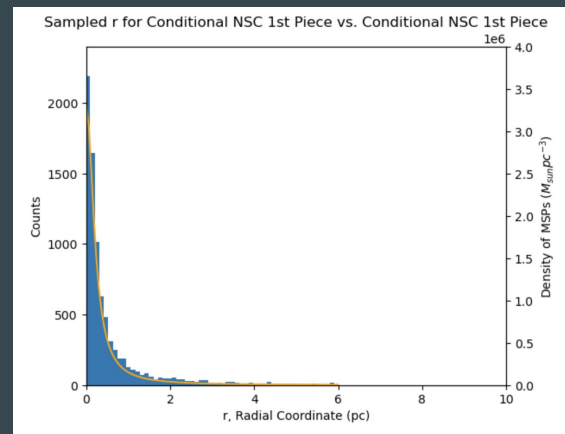
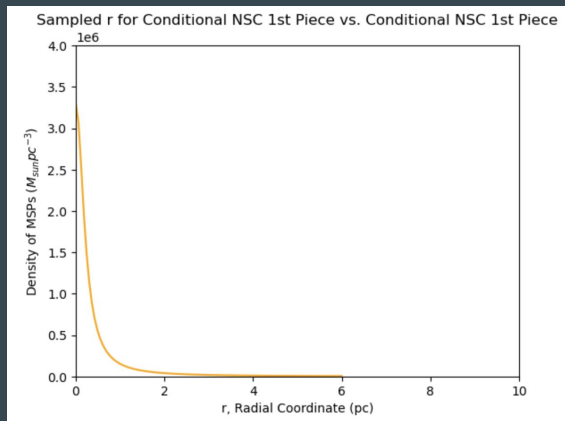
Searching for gravitational waves produced by cosmic strings in LIGO-Virgo data - Scientific Figure on ResearchGate. Available from: https://www.researchgate.net/figure/Effect-of-a-passing-gravitational-wave-propagating-in-the-z0-plan-with-plus_fig4_342436340 [accessed 14 May, 2024]

<https://upload.wikimedia.org/wikipedia/commons/f/f5/LISA-waves.jpg>

Methods of Sampling

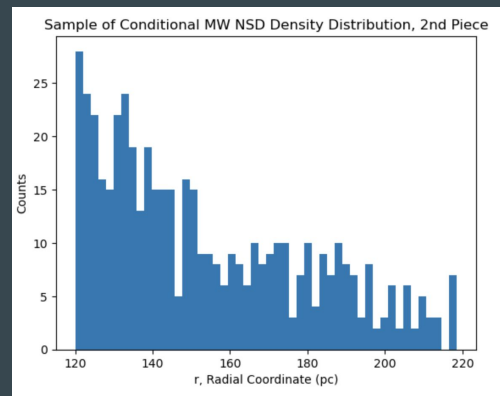
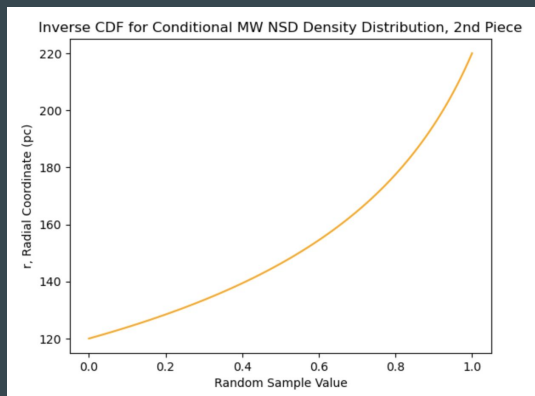
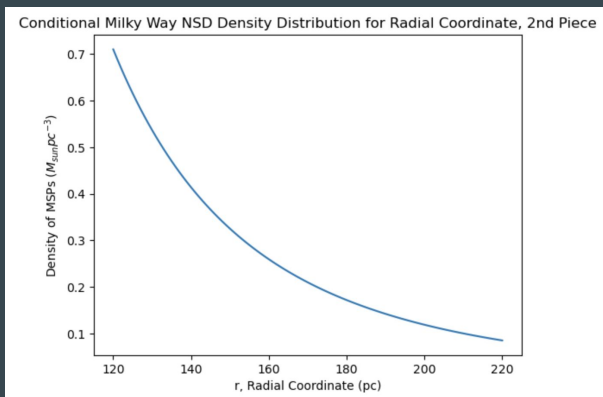
Monte Carlo Markov Chain (MCMC) Sampling

- Method for generating a sample from a given distribution using a number of random walkers



Inverse Transform Sampling

- Method for generating a sample from a given distribution using the inverse CDF of a function



Sampling a 2D Distribution

- 2-variable functions are hard to sample \rightarrow we need a way to hold one variable constant while sampling the other
- Split the function to be sampled into 2 conditional functions $f(x|y)$ and $f(y|x)$

