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AMATH 301 Section A  
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### Problem 1

a)

```
x1=0;  
for i=1:25000000  
    x1=x1+0.1;  
end  
x1
```

```
x2=0;  
for i=1:12500000  
    x2=x2+0.2;  
end  
x2
```

```
x3=0;  
for i=1:10000000  
    x3=x3+0.25;  
end  
x3
```

```
x4=0;  
for i=1:5000000  
    x4=x4+0.5;  
end  
x4
```

b)

```
y1=abs(2500000-x1)  
y2=abs(2500000-x2)  
y3=abs(2500000-x3)  
y4=abs(2500000-x4)
```

c)  $y_1$  is larger than  $y_2$  where  $y_1 - y_2 = 0.001148897223175$ . This is because the values for  $x_1$  and  $x_2$  are not the same, which can be seen in the workspace. When performing loops with many iterations such as the loops used to calculate  $x_1$  and  $x_2$ , the return value of the loop will contain some degree of error due to the fact that matlab cannot store binary floating point numbers.

d)  $y_3$  and  $y_4$  are exactly zero, but  $y_1$  and  $y_2$  are not.

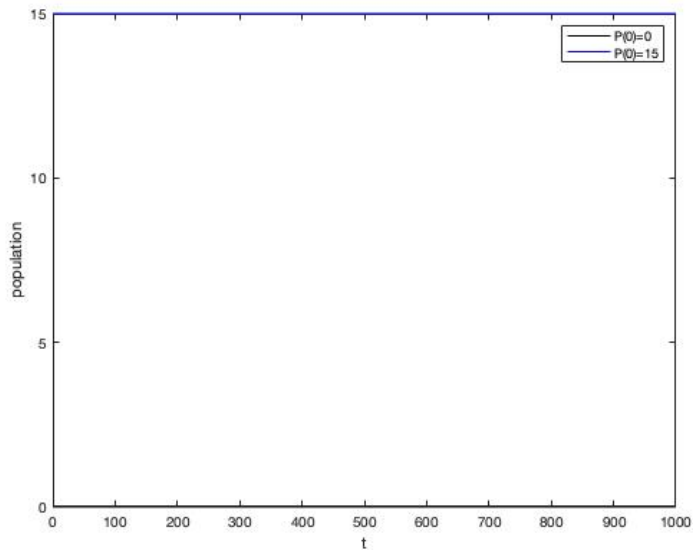
e) The  $y$  values that are exactly zero are exactly zero because their corresponding  $x_3$  and  $x_4$  values are exactly 2500000. Matlab stores binary numbers and 0.5 and 0.25 can be stored as binary numbers 0.1 and 0.01, whereas 0.2 and 0.1 cannot be stored as binary numbers, so they contain some degree of error when used in calculations.

## Problem 2

a)

```
a=P(0,1000,2,30);
b=P(15,1000,2,30);
t=0:1000;
plot(t,a,'k',t,b,'b')
xlabel('t')
ylabel('population')
legend('P(0)=0','P(0)=15')

function pop=P(P0,T,r,K)
    pop=zeros(1,T+1);
    pop(1)=P0;
    for t=2:T+1
        pop(t)=r*pop(t-1)*(1-pop(t-1)/K);
    end
end
```



Given the definition of equilibrium, these graphs make sense. Each solution for  $P$  has initial conditions of  $P(0)=\text{steady state}$  and so  $P(t)$  will remain at this steady state (since once  $P(t)=\text{steady state}$ , it will remain at that value for all future times), hence the solutions graphs being horizontal lines.

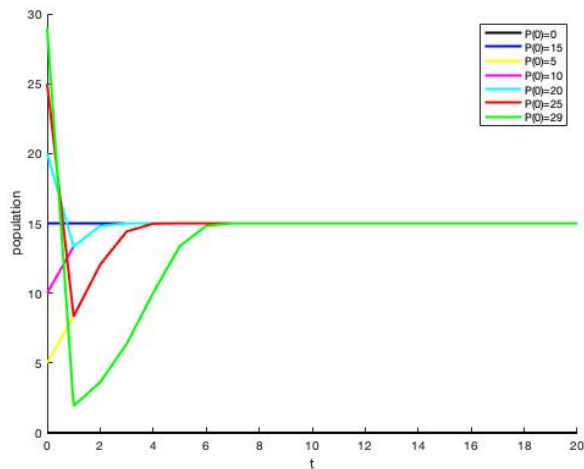
b)

```
clear all; close all;clc
a=P(0,20,2,30);
b=P(15,20,2,30);
c=P(5,20,2,30);
d=P(10,20,2,30);
e=P(20,20,2,30);
f=P(25,20,2,30);
g=P(29,20,2,30);

t=0:20;
hold on
plot(t,a,'k','LineWidth',2)
plot(t,b,'b','LineWidth',2)
plot(t,c,'y','LineWidth',2)
plot(t,d,'m','LineWidth',2)
plot(t,e,'c','LineWidth',2)
plot(t,f,'r','LineWidth',2)
plot(t,g,'g','LineWidth',2)
hold off

xlabel('t')
ylabel('population')
legend('P(0)=0','P(0)=15','P(0)=5','P(0)=10','P(0)=20','P(0)=25','P(0)=29')

function pop=P(P0,T,r,K)
    pop=zeros(1,T+1);
    pop(1)=P0;
    for t=2:T+1
        pop(t)=r*pop(t-1)*(1-pop(t-1)/K);
    end
end
```



The equilibrium  $P_2^*=15$  is stable, as all of the solutions to  $P$  with different starting values (shown in the legend) tend towards the solution for  $P$  where  $P(0)=P_2^*=15$ ; all solutions tend towards  $P(t)=15$ . The equilibrium  $P_1^*=0$  is unstable because all of the solution curves tend away from that particular solution of  $P(t)$  with initial condition  $P(0)=P_1^*=0$ .

c)

```
r1=1.1;
A=P(15,1000,1.1,30);
Eq1=A(1,end);

r2=1.5;
B=P(15,1000,1.5,30);
Eq2=B(1,end);

r3=2;
C=P(15,1000,2,30);
Eq3=C(1,end);

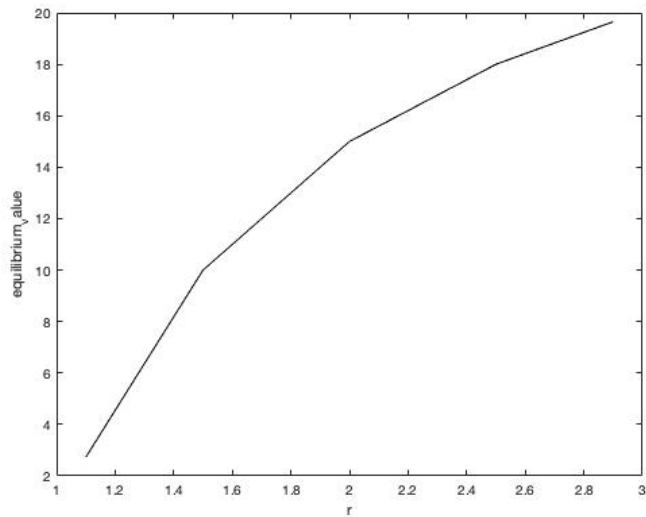
r4=2.5;
D=P(15,1000,2.5,30);
Eq4=D(1,end);

r5=2.9;
E=P(15,1000,2.9,30);
Eq5=E(1,end);

r=[1.1,1.5,2,2.5,2.9];
Equilibria=[Eq1,Eq2,Eq3,Eq4,Eq5];

plot(r,Equilibria,'k')
xlabel('r')
ylabel('equilibrium_value')

function pop=P(P0,T,r,K)
    pop=zeros(1,T+1);
    pop(1)=P0;
    for t=2:T+1
        pop(t)=r*pop(t-1)*(1-pop(t-1)/K);
    end
end
```



d)

```
clear all; close all; clc
r1=3.1;
A=P(15,1000,3.1,30)
P1000r1=A(1,end)
P999r1=A(1,end-1)

r2=3.2;
B=P(15,1000,3.2,30);
P1000r2=B(1,end);
P999r2=B(1,end-1);

r3=3.3;
C=P(15,1000,3.3,30);
P1000r3=C(1,end);
P999r3=C(1,end-1);

r4=3.4;
D=P(15,1000,3.4,30);
P1000r4=D(1,end);
P999r4=D(1,end-1);

r5=3.44;
E=P(15,1000,3.44,30);
P1000r5=E(1,end);
P999r5=E(1,end-1);

r=[3.1,3.2,3.3,3.4,3.44];
P1000=[P1000r1,P1000r2,P1000r3,P1000r4,P1000r5];
P999=[P999r1,P999r2,P999r3,P999r4,P999r5];

hold on
plot(r,P1000,'r')
plot(r,P999,'k')
xlabel('r')
ylabel('equilibrium_value')
```

