The Hash Array-Mapped Trie (HAMT)

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Logistics

- I'm (probably) gone next Tuesday
- This Thursday: course / exam review
- Next Thursday (probably): present projects / competition
- None of the HAMT particulars will be on the exam

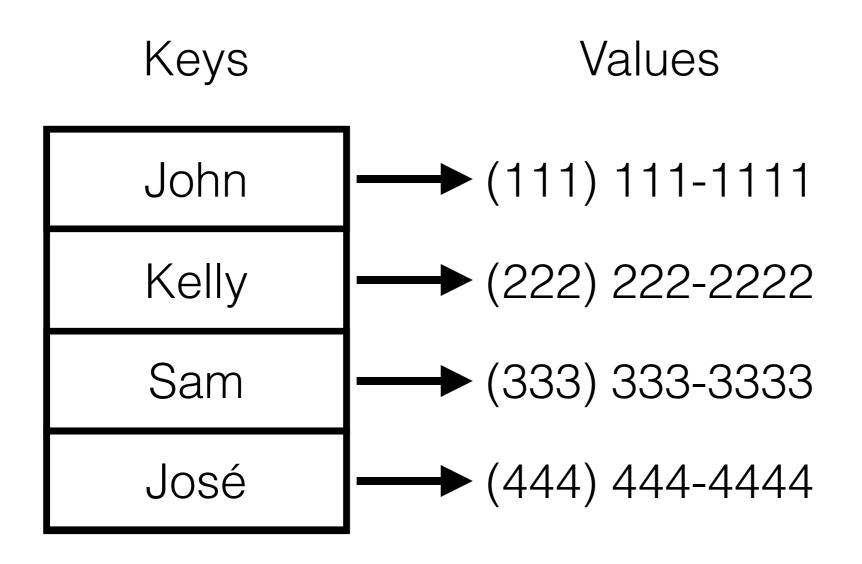
HAMT — High-Level Benefit

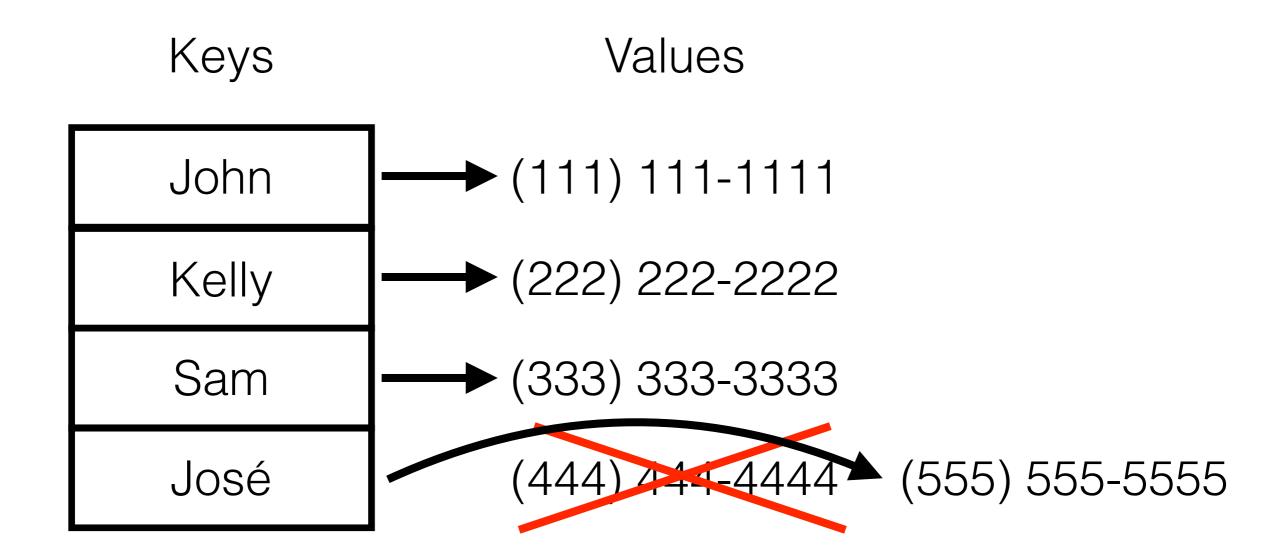
- Persistent hash map / set with:
 - Constant time insertion
 - Constant time lookup
 - Robust cache performance

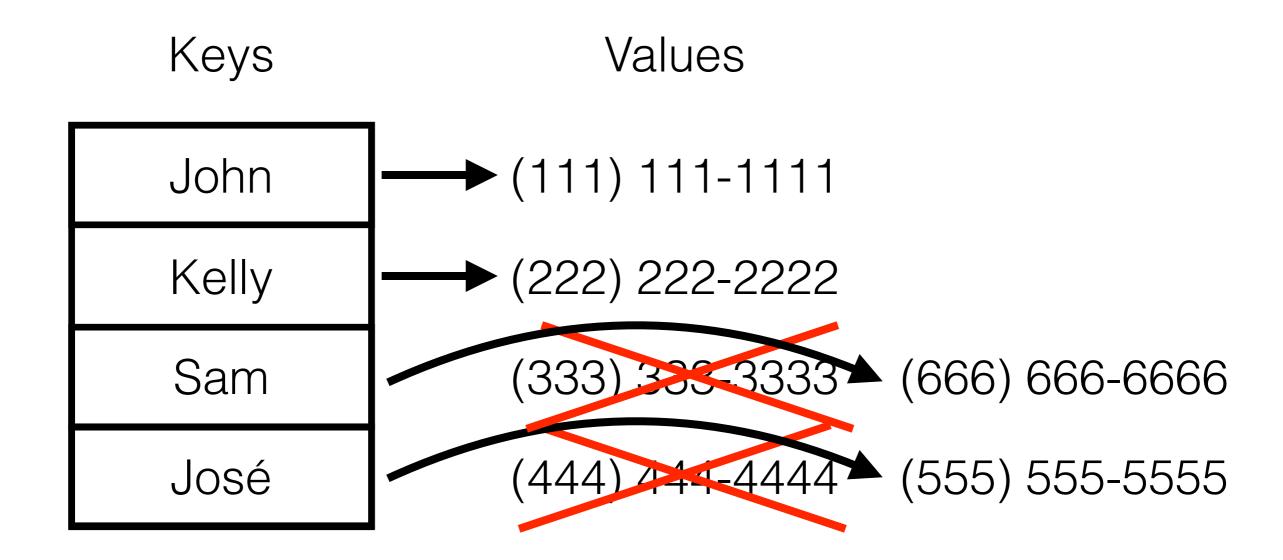
Problems with other DS

- Lookup / insertion for balancing binary trees:
 - log(n) with imperative version
 - Not persistent data structure
- Same thing with hash tables...
- Coming up with persistent hash map is hard!

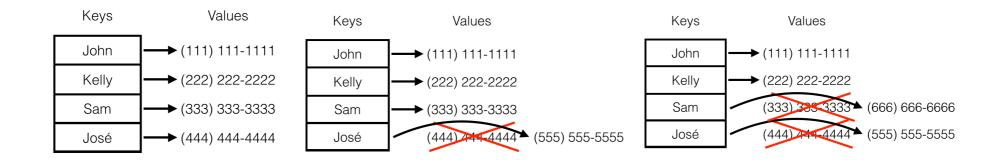
Motivation: phone books over time...

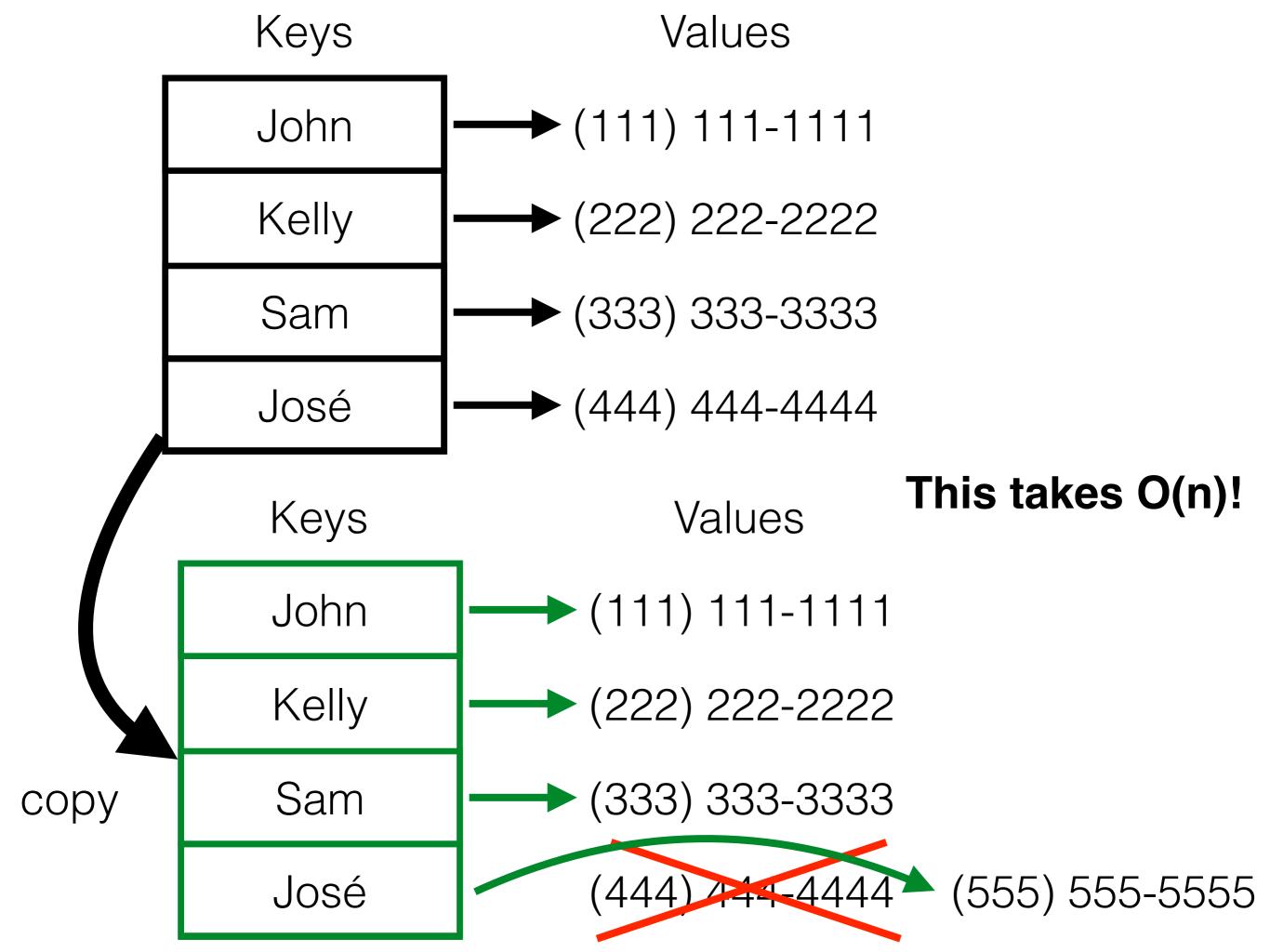




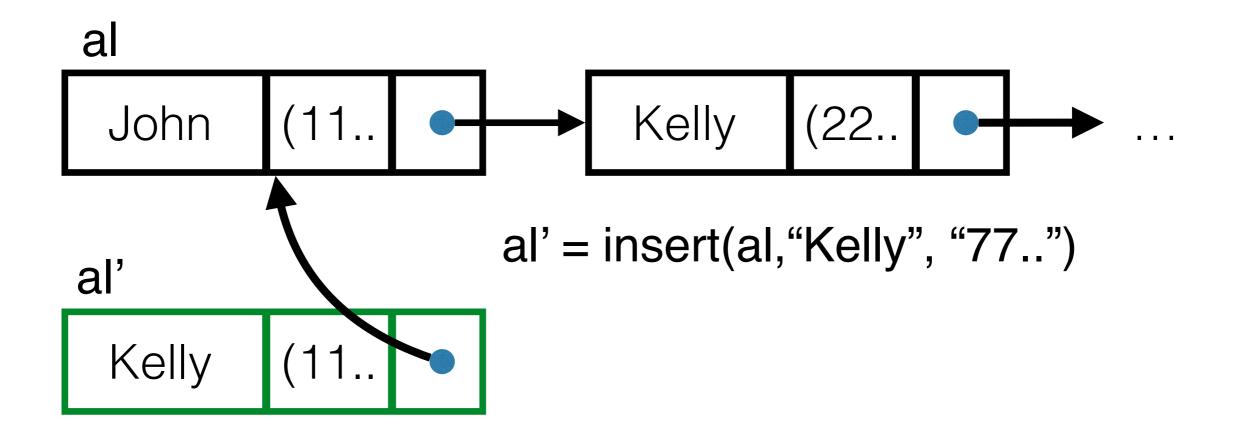


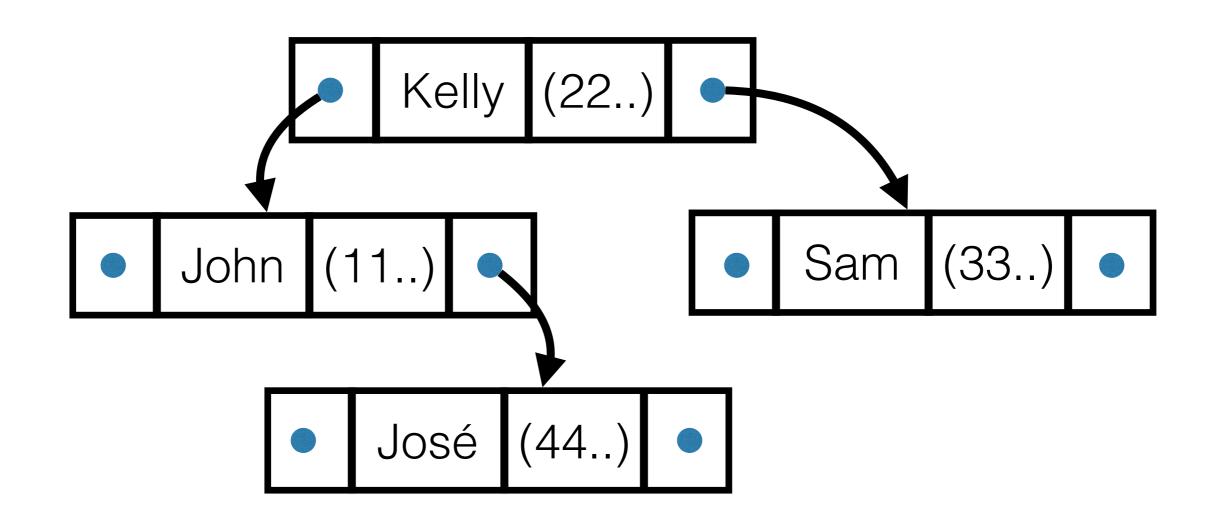
... Aug 10 Aug 11 Aug 12 ...





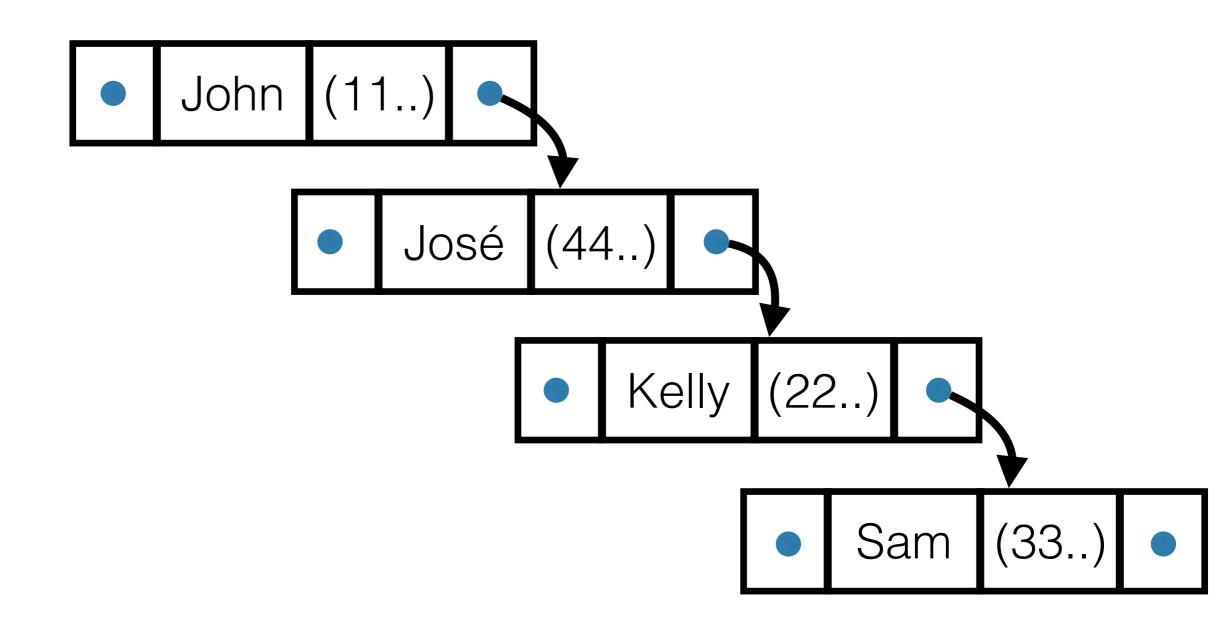
Inserting into association list: either O(1) or O(n) Depends if you want time or space...





Balanced binary trees are good....

But unbalanced binary trees are not...!



(Naive insertion **potentially** leads to O(n)!)

What's one way to **approximate** balanced binary trees?

(I.e., if I want to insert n names and end up with an "almost" balanced tree?)

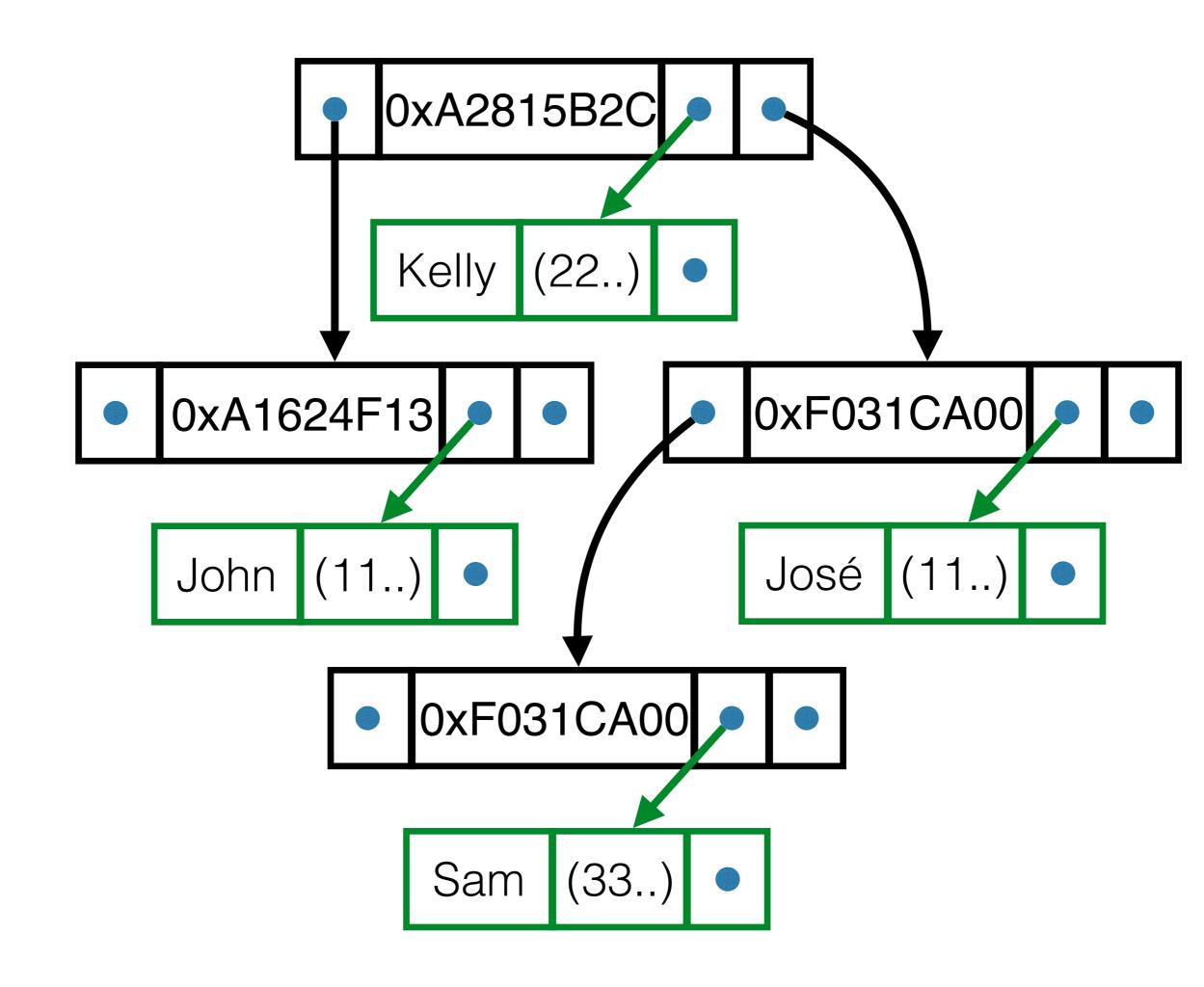
Insight: randomize insertion order

I can do this by storing a **hash**!

Now: each node of our binary tree stores a **hash** and an **association list**

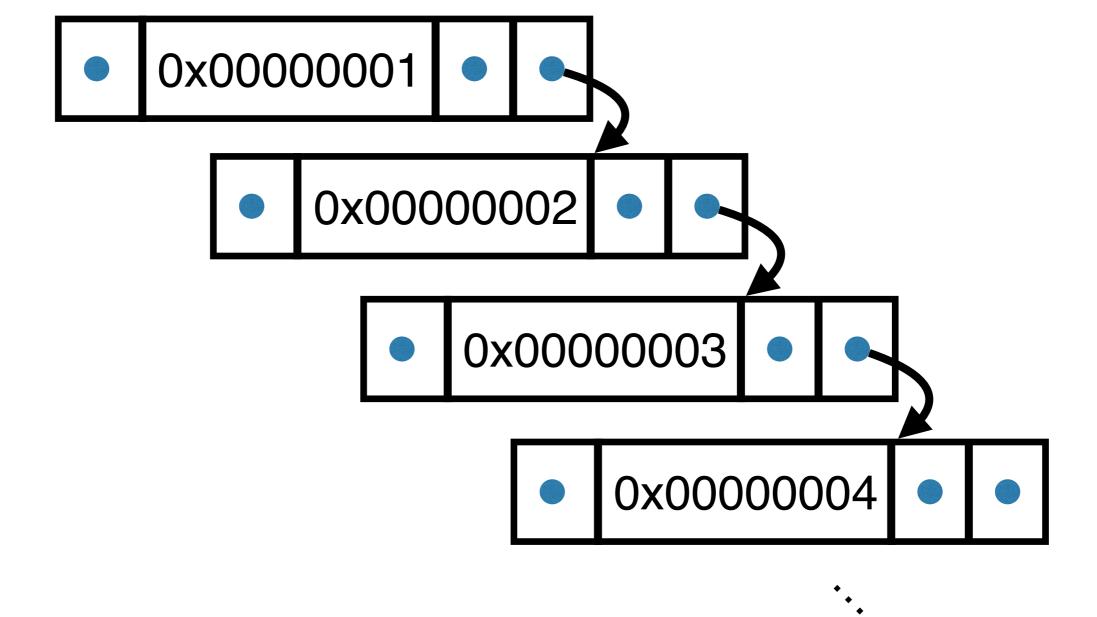
(Why do you need this?)

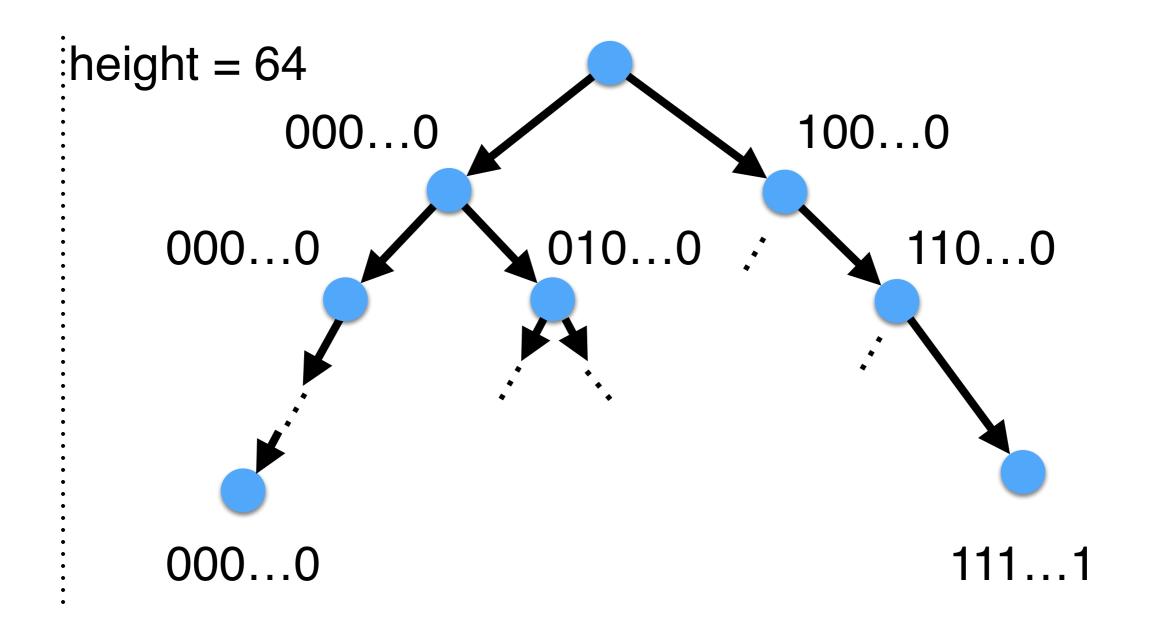
Store hashes as keys into a tree, back it with association list



Instead of tree, why not use a trie?

0x10000001
0x10000002
0x10000003
0x10000004
0x10000005





Now each successive bit in the trie indexes a successive bit in the hash

(Of course, each leaf still needs to be backed by assn. list!)

Now lookup takes **at most** 64! (Because that's how long our hash is!)

Ergo: Insertion takes ~O(1) time!

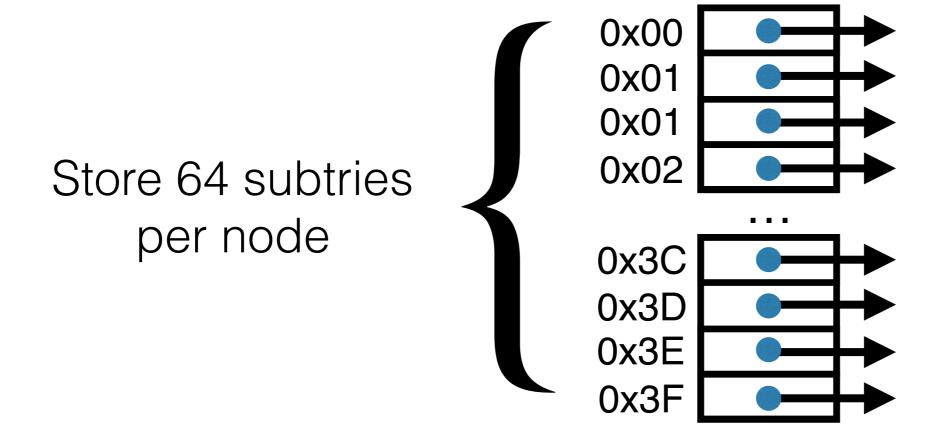
64 is still pretty crummy constant factors!

And it always takes 64 if we use a trie!

How can we do better..?

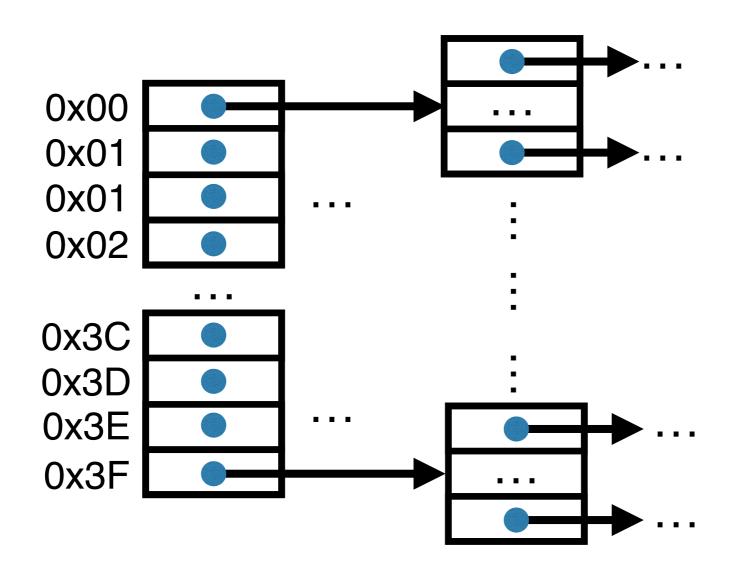
How can we do better..?

Idea: store more than 1 bit per node!



(Can vary this up / down)

Now our trie looks like this!



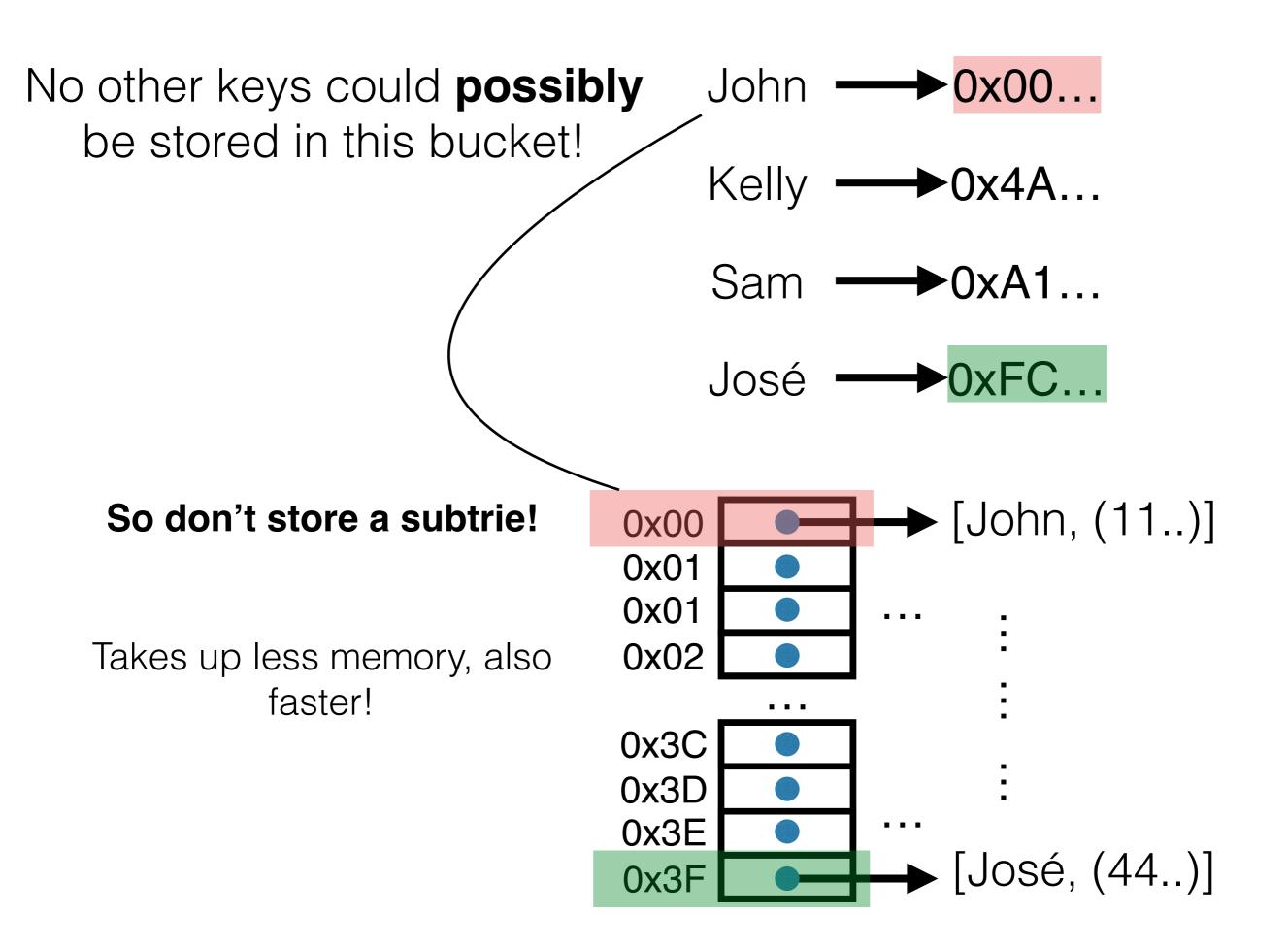
To insert, walk over **chunks** of the hash!

(Walk through on board...)

Get better constant factors by storing more subtries per node

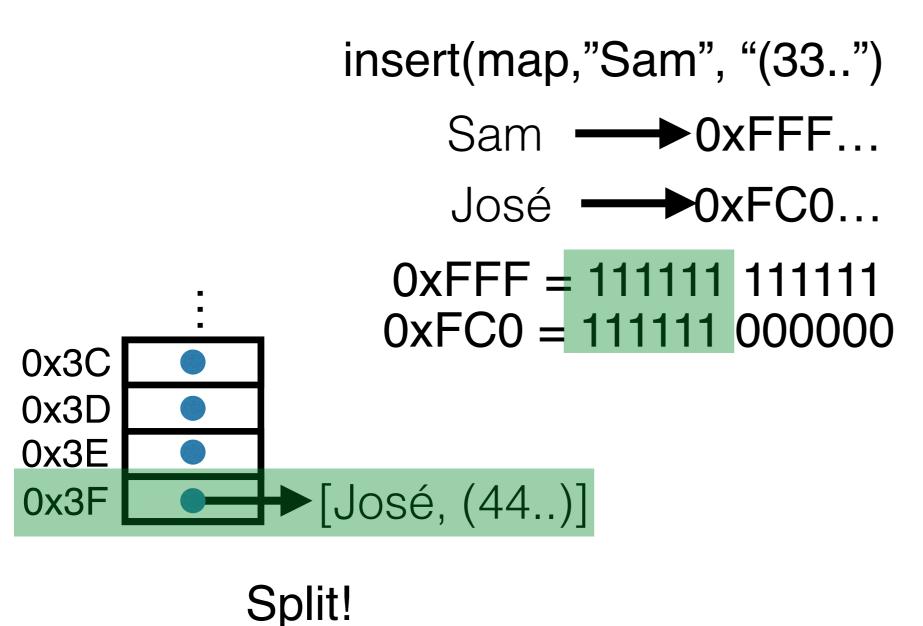
(Downside: each node takes more memory)

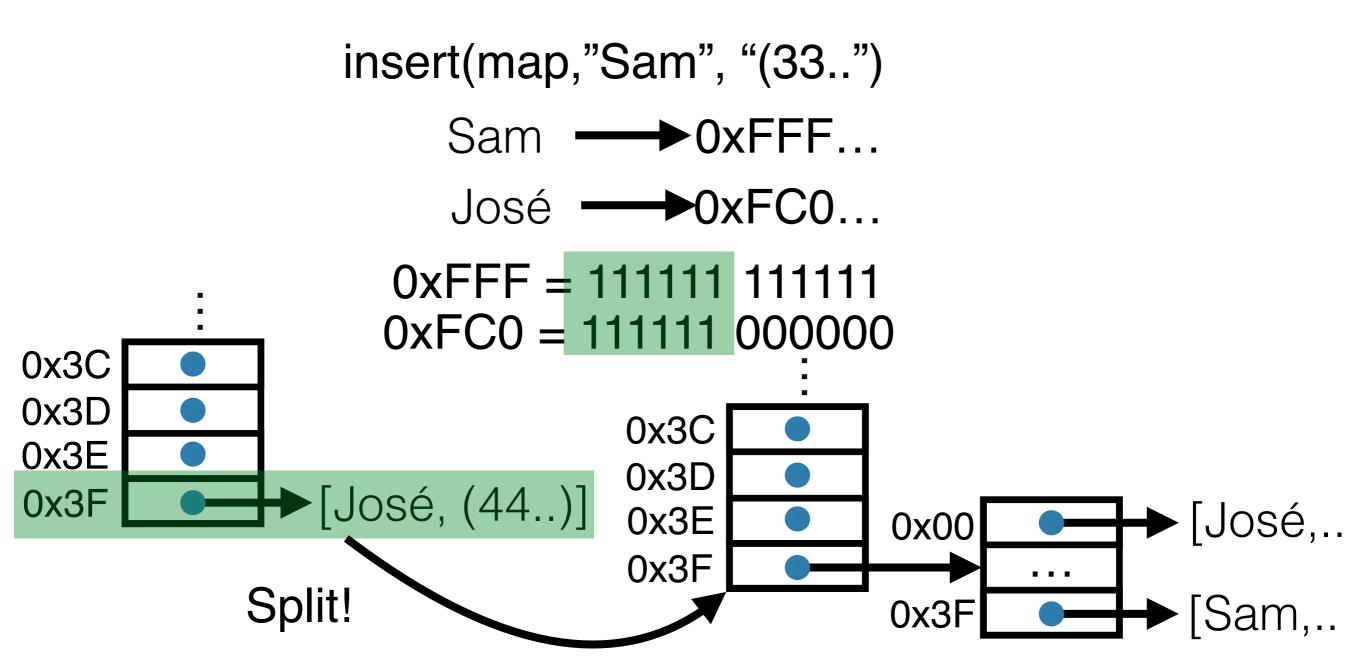
Don't store the **whole** trie until we really **need** to



Question now: how do we implement insert?

Observation: form **new** subtries in case of collision at some node





Don't store the **whole** trie until we really **need** to

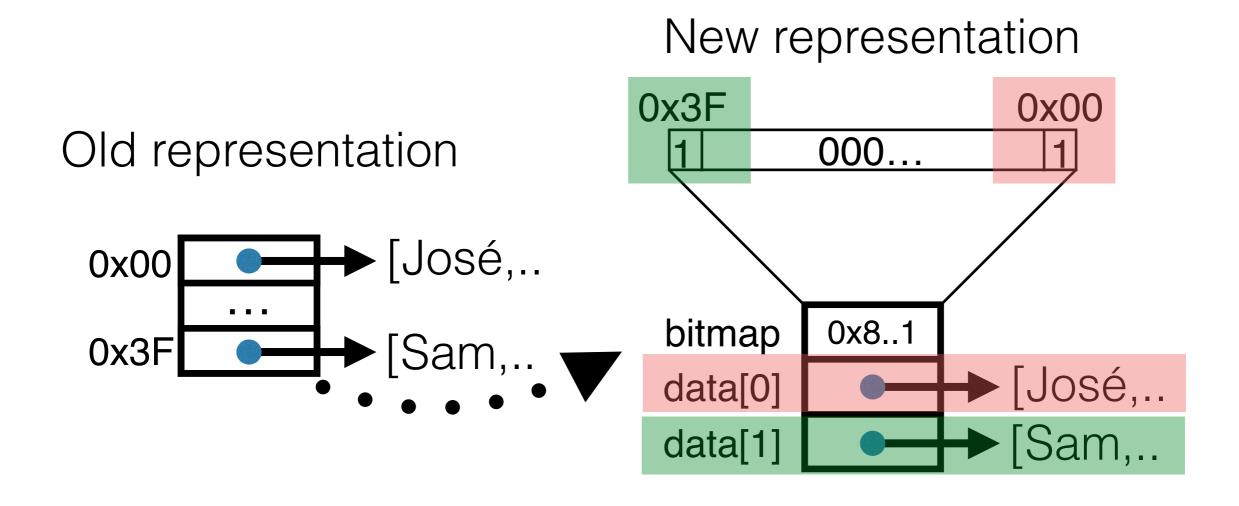
(Reduces space the trie takes up! Storing fewer keys = fewer places taken up!)

Storing 64 subtries is **still** very expensive!

Solution: store array of subtries, length of array is n where n is number of occupied buckets!

(Kris illustrates on board...)

Idea: use bitmap!



Putting it all together

Store hashes as keys into a tree, back it with association list

Instead of tree, use trie

Lower constant factors: store n (= 64 in our ex) subtries (Con: more space for each subtrie!)

Two clever hacks:

- Don't store subtries until you absolutely need to
- Use bitmap to reduce the need for n subtries until needed

Result

- Fast persistent hash map!
- Great constant factors
- Low overhead when it's not storing much stufff
- Higher overhead as it fills up, but never far past constant factor!
- Useful in implementing interpreters, any other place when you need efficient hash map
- Most of the time a regular HT is probably fine, but think of HAMT!