

Logica: Declarative Data Science for Mere Mortals

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ABSTRACT

Logica (= Logic + aggregation) is a freely available, open-source, feature-enhanced version of Datalog that automatically compiles logic rules to several SQL platforms, i.e., a lightweight, serverless SQLite engine, a multi-user client-server PostgreSQL system, and a highly scalable, parallel BigQuery instance. Logica combines the beginner-friendly declarative features of Datalog (intuitive, pattern-based queries in the style of QBE), with advanced analytical features needed by data science practitioners when processing large, real-world datasets. The system has been used for data science applications and training in industry, and in graduate-level courses in academia. Logica allows beginners to seamlessly progress from traditional (toy) examples to intermediate and advanced use cases.

1 INTRODUCTION

Datalog has a long and venerable history in databases [16, 17], e.g., as a family of languages for theoreticians studying the expressive power of queries [2], as a logical foundation for non-monotonic reasoning [25, 26], and as a language for teaching the foundations of databases [1]. After much excitement and research activity in the late 1980s and early 1990s, interest temporarily waned¹, before it saw a resurgence in academia and industry in the 2000s [7, 12] which continues to this day [3]. Datalog now has many applications, bridging the gap between specification and implementation, e.g., in program analysis [14, 18, 20], declarative networking [13, 15], knowledge graphs [5], and ML/AI [4, 9, 27]. For these and other use cases, a number of specialized Datalog systems and prototypes have been implemented (e.g., see [5, 11, 14] among many others).

Somewhat surprisingly, however, despite these many successful application areas, there has been a lack of freely available, scalable implementations of Datalog that support real-world data science applications. In contrast, Python’s success in data science can be explained by the fact that it is widely available and that it is both, an excellent language for beginners and a production-level language for data science, ML, and AI applications, i.e., there is a continuous path—from beginner to expert—within a single framework. If the user-friendly, declarative features of Datalog could be combined with the robust, well-engineered features of SQL databases in a widely available implementation, a similar path would allow beginners to advance from simple, declarative queries to more complex data-intensive analysis use cases.

In this demonstration, we present our answer to this challenge: Logica is a freely available, open-source Datalog variant, designed to combine the declarative features of a logic-based rule language with features needed in real-world data science applications. The

¹“No practical applications of recursive query theory . . . have been found to date” by Michael Stonebraker in *Readings in Database Systems, 3rd Edition* is symptomatic.

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compact syntax inspired by logic programming is well-suited for both simple OLAP-style aggregations and more complex tasks encountered in data science. Logica is a descendant of Yedalog [6] (and thus Dyna [9]) and inherits several features through this lineage, e.g., a programmer-friendly syntax for aggregators, functional predicates, user-defined functions, and complex data types. Logica source code, tutorials, and demonstration notebooks are available online [22, 23].

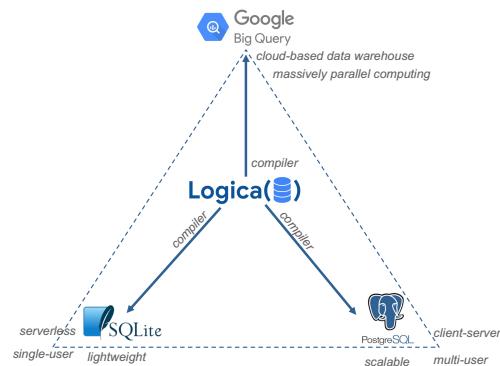


Figure 1: Logica programs can be executed on a single-user SQLite engine; a multi-user, client-server PostgreSQL system; and the massively parallel BigQuery data warehouse in the cloud.

Logica rules feature both, (i) the traditional *positional* Datalog syntax, making pattern-based, QBE-style queries intuitive and convenient, especially for low-arity relations (e.g., knowledge graphs represented as triples), and (ii) the *name-based* syntax known from SQL. This latter feature makes SQL queries, and thus Logica, more robust to schema changes² and is a practical necessity when dealing with schemas involving more than a handful of columns.

In Section 2 we introduce a few of the key features of Logica by example, starting from simple Datalog queries, to intermediate ones, and ending with more advanced, analytical examples. The use of Logica in practice (e.g., in notebook environments) is discussed in Section 3. In Section 4 we describe the plans for our interactive Logica demonstration: it will feature not only the examples discussed in the next section, but several additional examples that users can execute live, from their own laptops, during the conference. Finally, in Section 5, we summarize the unique features of Logica and our future plans for using Logica in education.

2 LOGICA BY EXAMPLE

2.1 Some Datalog Basics

Datalog rules are implications of the form *head* :- *body*, i.e., whenever the conjunction of *literals* (atoms or their negation) in the *body* is true, the logic atom in the *head* is true as well.

²For example, adding new columns to a schema will regularly “break” queries in positional syntax, while queries with name-based syntax often remain unaffected.

Transitive Closure. The following rules derive a new, transitive relation `Ancestor(x,y)` from a given relation `Parent(x,y)`. The first rule states that parents are ancestors. The second, *recursive* rule specifies that a fact `Parent(x,z)` and a derived fact `Ancestor(z,y)` can be *joined* to derive a new fact `Ancestor(x,y)`:

```

1 Ancestor(x,y) :- Parent(x,y);
2 Ancestor(x,y) :- Parent(x,z), Ancestor(z,y);

```

Note that *predicates* (relation names) begin with an uppercase letter in Logica, while logical *variables* are denoted in lowercase. Rules are terminated by a semicolon, as in SQL. Similar to *Query-by-Example* (QBE) [1, 29], Datalog is a pattern-based language, i.e., multiple occurrences of the same variable in a rule body (e.g., `z` in the second rule above) correspond to an implicit join.

Graph Queries. The ease of computing transitive closures indicates that Datalog is a powerful *graph query language*, sharing features with specialized languages, such as SPARQL and Cypher. *Regular path queries* (RPQs) [28], can be expressed easily via rules, making Datalog an excellent choice for querying knowledge- and provenance graphs [8]. Assume you want to compute `LCA(x,y,a)`, the *lowest common ancestor* `a` of two nodes `x` and `y` in a given family tree or provenance graph. An elegant, declarative solution is:

```

1 CA(x,y,a) :- Ancestor(x,a), Ancestor(y,a), x != y;
2 NonLCA(x,y,a) :- CA(x,y,a), CA(x,y,b), Ancestor(b,a);
3 LCA(x,y,a) :- CA(x,y,a), ~NonLCA(x,y,a);

```

The first rule defines a common ancestor `a` of two distinct nodes `x` and `y` (via an implicit join on `a`). The second rule finds common ancestors `a` for which a “better” (i.e., lower) ancestor `b` exists. These non-LCA ancestors are then discarded by the third rule, which uses negation³ to derive all remaining true LCAs.

2.2 Logica Variables & Named Arguments

The Logica examples above employ the classic *positional* Datalog syntax, i.e., in which an n -ary predicate occurrence $P(x_1, \dots, x_n)$ must include *terms* (logic variables or data values) in all n argument positions. This facilitates pattern-based (i.e., QBE-style) queries with implicit joins, and is intuitive and convenient for relations with few attributes (columns) as shown in the graph queries above. However, traditional (non-graph) relations often have many more columns, and the positional syntax becomes inconvenient, error-prone, and unnecessarily brittle (queries regularly break, e.g., when new columns are added to base relations). To this end, Logica also supports *named arguments* so that queries can only refer to those attributes that are needed to specify the desired query.

Confronting the Real World. In a more realistic setting, the binary `Parent(x,y)` relation above will be populated from a `Person()` table that has many more columns. For simplicity, we use a 4-ary relation with attributes `name:`, `dob:` (date-of-birth), `mother:`, and `father:` here. Symbols ending in a colon (color-coded green) are *attribute names* and are often (but not always) followed by data values (e.g., strings) or logic variables.

A base table for `Person()` may include facts of the form:

```

1 Person(name: "Joe Doe", dob:"1990-08-15"),
   mother:"Jane Doe", father:"John Doe";
2 Person(name: "John Doe", dob:"1966-05-20"),
   mother:"Alice Wang", father:"Robert Doe");
3
4

```

³In Logica a negated literal “ $\neg A$ ” is written as “ $\sim A$ ”.

From such a base table with named arguments, we can populate the binary parent relation (with positional syntax) as follows:

```

1 Parent(x,y) :- Person(name:x, mother:mother, father:father),
2   y in [mother,father];

```

The person atom in the body of the rule uses only three attributes (i.e., does *not* mention `dob:`) and introduces *logic variables* `x`, `mother`, and `father`, respectively, representing domain values. The second conjunct in the rule body, i.e., the construct “`y in [mother,father]`” effectively specifies a *disjunction* (the parent `y` can be either the mother or the father of `x`) and would require two, nearly identical, rules in standard Datalog syntax.

The *attribute:variable* pattern (e.g., “`mother:mother`” above) is quite common, so Logica defines a convenient abbreviation: By omitting a logic variable, an *implicit* variable with the same name as the attribute becomes available. In this way, we can write the previous rule even more concisely as follows:

```

1 Parent(x,y) :- Person(name:x, mother:, father:),
2   y in [mother,father];

```

Translating Recursive Rules. Several variants and fragments of Datalog exist and they can differ significantly in their handling of recursion and negation, and consequently in their expressive power and computational complexity [1]. Many SQL systems now support a limited form of (linear) recursion through common table expressions (CTEs). When compiling Datalog to SQL there are two natural approaches: (1) employ the `WITH RECURSIVE` construct and CTEs, or (2) unroll recursive rules to a fixed depth k . Both approaches have advantages and disadvantages, e.g., (1) cannot handle non-linear recursion, while (2) may result in incomplete answers when the recursion depth required exceeds the fixed “unroll-depth” k set for a given program. Experience with Logica’s approach (2) has rarely presented a real limitation: A double-recursive variant of the `Ancestor` program above, e.g., can handle chains of length $O(2^k)$ given an unroll-depth of k .

2.3 A Data Science Use Case

Consider a data engineer working for the Seattle Public Library (SPL), who is tasked with analyzing loan data for decision support and new library services. She accesses the external `LibraryLoans()` table via the library’s PostgreSQL database, and begins to explore the data in her Jupyter notebook. First, she wants to visualize the types of materials (books, e-books, DVDs, etc.) that are popular, i.e., having more than 30K checkouts per type. For materials which have no checkouts in a given month, missing values should be padded with zeros, to keep the plotting code simple.

```

1 LoansByMonth(material:PopularMat(), month:AnyMonth()) += 0;
2 LoansByMonth(material:, month:)=+ loans :-
3   LibraryLoans(material:, month:, loans:),
4   material = PopularMat();
5
6 PopularMat() = material :- MatCount(material) > 30000;
7 MatCount(material) += 1 :- LibraryLoans(material:);
8 AnyMonth() = i + 1 :- i in Range(12);

```

She defines a new result relation `LoansByMonth()` that aggregates loans by material-type and month, for popular materials. The function `PopularMat()`, defined in L6 and used in L1 and L4 includes only materials with more than 30K checkouts total. `MatCount()` sums up checkouts for each material-type. The external `LibraryLoans()` contains counts of loans, grouped by material

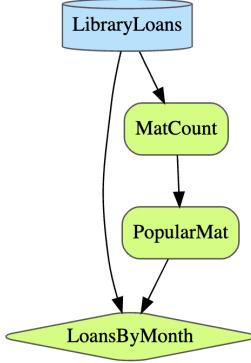


Figure 2: Logica dataflow graph for the Seattle Library example

and month. The multi-valued function `AnyMonth()` returns integers $1, \dots, 12$ matching the representation used in `LibraryLoans()` for the months of the year.

Figure 2 depicts the dataflow for the result relation (with diamond shape) `LoansByMonth()` of the SPL example above. This graph is automatically generated by Logica, when the program is run in a Jupyter notebook. The output depends on the external database table `LibraryLoans()` in PostgreSQL and intermediate *grounded* functional predicates (rounded boxes) `MatCount()` and `PopularMat()`.

Migrating from PostgreSQL to BigQuery. In our demonstration scenario [23], the engineer is happy with the result, but notices that query evaluation took more than 15 seconds. While this is fine for an initial exploration, a deeper analysis on an even larger volume has been requested, so the engineer changes the Logica directive `@Engine("psql")` in the notebook to `@Engine("bigquery")`. After pushing the data to Google’s scalable, distributed BigQuery data warehouse, she is pleased to see that once the data is loaded to BigQuery the very same Logica rules now take less than 2 seconds to execute.⁴

3 LOGICA & DATALOG FOR THE REST OF US

Figure 1 depicts the high-level architecture of Logica: A Python-based source-to-source compiler translates Logica rules to one of the supported SQL dialects (SQLite, PostgreSQL, or BigQuery), each with its unique performance characteristics and use cases.

The Triangle of Power. For light-weight, embedded, and single-user applications, the SQLite engine is an excellent choice. It has the additional benefit that SQLite (like Python) is often readily available on most users’ machines. On the other hand, when business data resides in a multi-user, client-server database, the Logica-to-PostgreSQL compiler option will be convenient for declarative data science applications. Since PostgreSQL (unlike BigQuery) requires composite types to be explicitly defined, the Logica compiler had to be extended with type inference [21]. For applications that need scalable compute resources to handle large volumes of data and to perform complex analysis tasks, the Logica-to-BigQuery compiler will be the platform of choice.

First Things First. Logica installation via Python is easy, and

```
python3 -m pip install logica
```

will do the trick. Logica can be directly run in a terminal and requires no extra packages when compiling to SQLite, since

⁴The SPL dataset is about 3 GB in size and has 14 million rows [23].

Python 3 comes with SQLite built in. This provides a convenient on-ramp for data analysis: A user can start running their first Logica programs with SQLite and as their needs grow, move to PostgreSQL or BigQuery.

Using Notebooks. Logica has been integrated with Jupyter. To use Logica in a notebook, simply install Logica, and then run

```
from logica import colab_logica
```

After that, the `%%logica` Jupyter magic will be available in the notebook. Users can then write their Logica programs in a notebook cell, and on the magic line specify a comma-separated list of predicates that they would like to be executed [23]. Results of the execution will then be shown in the notebook UI and stored in pandas dataframes, whose names coincide with the Logica predicate symbols. This provides a simple and seamless integration of data analysis, visualization, and ML workflows through notebooks.

Database Access. Logica can read and write tables that exist in a user’s database. For example, to populate a database table with the derived facts of the Logica predicate `MatCount()` above, the user simply adds the line:

```
@Ground("MatCount");
```

While a Logica program is executing in a notebook, the user can monitor progress via a dynamically updating dataflow graph (cf. Figure 2) where node colors indicate whether a relation is still being computed (grey) or has been finalized (green).

4 DEMONSTRATION PLAN

Core Demo. After a brief introduction and motivation, our Logica demonstration will include the following steps:

- (1) A gentle introduction to declarative (Datalog) querying with Logica, using classic examples such as `Ancestor(x,y)` (for computing transitive closures), intermediate graph queries such as `LCA(x,y)`, and their application for querying provenance [8] and knowledge graphs via RPQs [28].
- (2) Intermediate examples that highlight the commonalities and differences between standard Datalog rules and systems and Logica: programmer-friendly syntax enhancements (for mixing positional and named arguments), data science extensions for user-defined functions and aggregation (e.g., the SPL example above), composite data types, and notebook integration.
- (3) An advanced data science use case (expanding on the SPL example) that involves multiple SQL engines simultaneously to illustrate data import/export and performance differences.

Go Logica and Logica-to-Go. In addition to giving a live demo of the Logica system using interactive notebooks (“*Go Logica!*”), we plan to invite conference attendees to participate in the demonstration session by running Logica notebooks in the cloud through Google colab [23]. In this way, participants will get a first-hand experience of the power of declarative rules for data science.

During the conference we will also provide a “*Logica-to-Go*” clinic for interested participants, i.e., a 5–10 minute installation walk-through whose goal is to empower participants to run their own instance of Logica with Python and SQLite. We believe that many attendees will have Python 3—and thus also SQLite—pre-installed on their laptop computers, making installation of a minimal, SQLite-based Logica system straightforward. By leaving

the demo-session with a self-contained Logica installation and beginner’s tutorial, participants will be independent of online and cloud resources, and will be able to experiment on their own laptops with declarative querying and data analysis examples, whether on their way home from the conference with unreliable internet access, or cast away on an island like Robinson Crusoe.

5 CONCLUSIONS

Datalog has had a long and venerable (some might say turbulent) history in the database community [16, 17]. Database *theory* [1] cannot be imagined without it, but it is the many new (or rediscovered) *applications* that have led to a resurgence of Datalog in industry and academia in the last 10–20 years. Despite the more abundant and novel use cases, and the continued interest in declarative, Datalog-like languages in academia and industry, it is somewhat surprising that there is a shortage of freely available, scalable Datalog systems, i.e., which can handle practical database and data science applications, in addition to the usual toy examples encountered in a database theory course.

Powerful Datalog engines have been developed in industry and research labs (e.g., see [5, 6, 11] among many others [16]), but these are often not freely available, can be hard to install and use, or may even have been abandoned. Instructors who are eager to teach foundations of databases, declarative programming, or new applications [12, 13] may also find it difficult to identify suitable systems. While there are some excellent open-source systems (e.g., for teaching relational languages [24]), and specialized systems (e.g., for answer set programming [10]), these are generally not suitable for data-intensive or data science applications.

The first author has developed Logica, a powerful open-source tool that combines the elegance and declarative expressiveness of logic rules, with down-to-earth practical language features, e.g., for user-defined functions, aggregation, and complex data types that are necessary for real-world data science applications [22]. The core of the system is a source-to-source compiler that generates SQL code for different systems, currently SQLite, PostgreSQL, and BigQuery. With our demonstration, and using various examples, we will illustrate that there is a common path, from beginner to expert analyst, that data science students and practitioners can follow, all while staying in the framework of declarative, rule-based data science.

The last author has extensive experience teaching database and information science courses at the undergraduate and graduate level, and has recently begun, assisted by the second author, to use Logica for teaching, e.g., as a declarative modeling and query language, and for checking and enforcing integrity constraints (in the context of data cleaning and repair).

Plans for the Future. We believe that Logica fills an important practical need by combining the powerful features of a declarative rule language with the robust features of well-engineered SQL database systems, resulting in a novel hybrid language that supports a wide range of users and uses. Logica’s ability to handle large, real-world datasets provides a promising avenue for teaching, and we plan to develop new course materials using Logica in the future. We are also planning Logica extensions (or a preprocessor) to automatically translate RPDs to Datalog—e.g., similar to [8]—to better support use cases involving provenance and knowledge graphs. For OLAP-style workloads we are also considering to add DuckDB [19] as a new target platform.

REFERENCES

- [1] Serge Abiteboul, Richard Hull, and Victor Vianu. 1995. *Foundations of Databases*. Addison-Wesley.
- [2] S. Abiteboul and V. Vianu. 1991. Datalog extensions for database queries and updates. *J. Comput. System Sci.* 43, 1 (1991), 62–124.
- [3] Mario Alviano and Andreas Pieris (Eds.). 2022. *4th Intl. Workshop on the Resurgence of Datalog in Academia and Industry*. CEUR Workshop Proceedings, Vol. 3203.
- [4] Luigi Bellomarini, Ruslan R. Fayzrakhmanov, Georg Gottlob, Andrey Kravchenko, Eleonora Laurenza, Yavor Nenov, Stéphane Reissfelder, Emanuel Sallinger, Evgeny Sherkhonov, Sahar Vahdati, and Lianlong Wu. 2022. Data science with Vadalog: Knowledge Graphs with machine learning and reasoning in practice. *Future Generation Computer Systems* 129 (2022), 407–422.
- [5] Luigi Bellomarini, Emanuel Sallinger, and Georg Gottlob. 2018. The Vadalog System: Datalog-based Reasoning for Knowledge Graphs. *VLDB* 11, 9 (2018), 975–987.
- [6] Brian Chin, Daniel von Dincklage, Vuk Ercegovac, Peter Hawkins, Mark S. Miller, Franz Och, Christopher Olston, and Fernando Pereira. 2015. Yedalog: Exploring Knowledge at Scale. In *DROPS-IDN/v2/document/10.4230/LIPIcs.SNAPL.2015.63*. Schloss-Dagstuhl: Leibniz Zentrum für Informatik.
- [7] Oege de Moor, Georg Gottlob, Tim Furche, and Andrew Jon Sellers (Eds.). 2011. *Datalog Reloaded: 1st Intl. Workshop*. LNCS, Vol. 6702. Springer.
- [8] Saumen C. Dey, Sven Köhler, Shawn Bowers, and Bertram Ludäscher. 2012. Datalog as a Lingua Franca for Provenance Querying and Reasoning. In *4th Workshop on the Theory and Practice of Provenance (TaPP)*, Umut A. Acar and Todd J. Green (Eds.). USENIX Association.
- [9] Jason Eisner and Nathaniel W. Filardo. 2011. Dyna: Extending Datalog for Modern AI. See [7], 181–220.
- [10] Martin Gebser, Roland Kaminski, Benjamin Kaufmann, and Torsten Schaub. 2019. Multi-shot ASP solving with clingo. *Theory and Practice of Logic Programming* 19, 1 (Jan. 2019), 27–82.
- [11] Todd J. Green. 2015. LogiQL: A Declarative Language for Enterprise Applications. In *Symposium on Principles of Database Systems (PODS)*. ACM, 59–64.
- [12] Joseph M. Hellerstein. 2010. The declarative imperative: experiences and conjectures in distributed logic. *SIGMOD Record* 39, 1 (Sept. 2010), 5–19.
- [13] Joseph M. Hellerstein and Peter Alvaro. 2020. Keeping CALM: when distributed consistency is easy. *CACM* 63, 9 (Aug. 2020), 72–81.
- [14] Herbert Jordan, Bernhard Scholz, and Pavle Subotić. 2016. Soufflé: On Synthesis of Program Analyzers. In *Computer Aided Verification (LNCS)*. Springer, 422–430.
- [15] Boon Thau Loo, Tyson Condie, Minos Garofalakis, David E. Gay, Joseph M. Hellerstein, Petros Maniatis, Raghu Ramakrishnan, Timothy Roscoe, and Ion Stoica. 2006. Declarative networking: language, execution and optimization. In *Intl. Conf. on Management of Data (SIGMOD)*. ACM, 97–108.
- [16] David Maier, K. Tuncay Tekle, Michael Kifer, and David S. Warren. 2018. Datalog: concepts, history, and outlook. In *Declarative Logic Programming: Theory, Systems, and Applications*. Vol. 20. ACM and Morgan & Claypool, 3–100.
- [17] Jack Minker, Dietmar Seipel, and Carlo Zaniolo. 2014. Logic and Databases: A History of Deductive Databases. In *Handbook of the History of Logic*, Jörg H. Siekmann (Ed.). Computational Logic, Vol. 9. North-Holland, 571–627.
- [18] Aaditya Naik, Jonathan Mendelson, Nathaniel Sands, Yuepeng Wang, Mayur Naik, and Mukund Raghothaman. 2021. Spqr: An Interactive Environment for Exploring Code using Query-by-Example. In *34th ACM Symposium on User Interface Software and Technology*. ACM, 84–99.
- [19] Mark Raasveldt and Hannes Mühliesen. 2019. Duckdb: an embeddable analytical database. In *International Conference on Management of Data (SIGMOD)*. ACM, 1981–1984.
- [20] Bernhard Scholz, Herbert Jordan, Pavle Subotić, and Till Westmann. 2016. On fast large-scale program analysis in Datalog. In *25th Intl. Conf. on Compiler Construction*. ACM, New York, NY, USA, 196–206.
- [21] Evgeny Skvortsov. 2023. Full support of PostgreSQL engine comes to Logica. <https://opensource.googleblog.com/2023/09/full-support-of-postgresql-engine-comes-to-logica.html>
- [22] Evgeny Skvortsov. 2023. Logica Project. <https://logica.dev/> links to source code, tutorials, and an online playground.
- [23] Evgeny Skvortsov, Yilin Xia, and Bertram Ludäscher. 2023. Logica: Demonstration Notebook. <http://tinyurl.com/LogicaDeclarativeDataScience>
- [24] Fernando Sáenz-Pérez. 2018. Relational calculi in a deductive system. *Expert Systems with Applications* 97 (May 2018), 106–116.
- [25] Allen Van Gelder, Kenneth A. Ross, and John S. Schlipf. 1991. The Well-founded Semantics for General Logic Programs. *J. ACM* 38, 3 (July 1991), 619–649.
- [26] Victor Vianu. 2021. Datalog Unchained. In *Symposium on Principles of Database Systems (PODS)*. ACM, 57–69.
- [27] Jin Wang, Jiacheng Wu, Mingda Li, Jiaqi Gu, Ariyam Das, and Carlo Zaniolo. 2021. Formal semantics and high performance in declarative machine learning using Datalog. *The VLDB Journal* 30, 5 (Sept. 2021), 859–881.
- [28] Peter T. Wood. 2012. Query Languages for Graph Databases. *ACM SIGMOD Record* 41, 1 (April 2012), 50–60.
- [29] M. M. Zloof. 1977. Query-by-Example: A data base language. *IBM Systems Journal* 16, 4 (1977), 324–343.