



Watershed

Time limit: 1000 ms
Memory limit: 256 MB

We have been asked to evaluate the drainage of a rectangular region in a nearby town. To do so, we will model the region using a rectangular grid of 1 meter square cells. We have recorded the elevation of each cell, and our model assumes the following:

- Each cell initially contains 1 liter of water.
- Water will flow from cells with higher elevations to adjacent cells with lower elevation. Two cells are adjacent if they share a border, and therefore a cell can have at most 4 adjacent cells.
- When a cell has more than one adjacent cell with lower elevation, the water is equally split between these adjacent cells.
- No water will flow into or out of the rectangular region.
- If water cannot flow out of a cell, we will put a drain in the cell.

What is the maximum amount of water that will be collected by a drain.

Standard Input

The first line contains two space-separated integers n and m , giving the number of rows and columns in the rectangular region.

The next n lines give the elevations in each of the cells of the grid. Each line will contain m integers.

Standard Output

Output the maximum number of liters of water that can flow through a drain. Your output should be within 10^{-4} of the exact answer.

Constraints and notes

- $1 \leq n$
- $1 \leq m$
- $1 \leq n \times m \leq 10^5$

Each elevation value will be a non-negative integer less than or equal to 10^9 .

Input	Output	Explanation																																																																																			
<div><div>3 3 3 2 3 2 1 2 3 2 3</div></div>	<div>9.000000</div>	All of the cells drain towards the center square, so the total volume of water collected by the drain is 9 liters.																																																																																			
<div><div>3 3 3 3 3 3 3 3 3 3 3</div></div>	<div>1.000000</div>	Since all cells are at the same elevation, no cell drains into another one. Therefore, the maximum water collected by any drain is 1 liter.																																																																																			
<div><div>4 5 1 2 3 4 3 2 3 4 5 4 3 4 5 4 3 4 4 3 2 1</div></div>	<div>10.375000</div>	<p>The table below shows the direction that water flows from each cell.</p> <div><table><tr><td>1</td><td>←</td><td>2</td><td>←</td><td>3</td><td>←</td><td>4</td><td>→</td><td>3</td></tr><tr><td>↑</td><td></td><td>↑</td><td></td><td>↑</td><td></td><td>↑</td><td></td><td>↑</td></tr><tr><td>2</td><td>←</td><td>3</td><td>←</td><td>4</td><td>←</td><td>5</td><td>→</td><td>4</td></tr><tr><td>↑</td><td></td><td>↑</td><td></td><td>↑</td><td></td><td>↓</td><td></td><td>↓</td></tr><tr><td>3</td><td>←</td><td>4</td><td>←</td><td>5</td><td>↓</td><td>4</td><td>→</td><td>3</td></tr><tr><td>↑</td><td></td><td></td><td></td><td>↓</td><td></td><td>↓</td><td></td><td>↓</td></tr><tr><td>4</td><td></td><td>4</td><td>→</td><td>3</td><td>→</td><td>2</td><td>→</td><td>1</td></tr></table></div> <p>Based on this flow, the table below shows the contribution of each cell to the drianage in the top left corner.</p> <table><tr><td>1</td><td>1</td><td>1</td><td>1/2</td><td>0</td></tr><tr><td>1</td><td>1</td><td>1</td><td>3/8</td><td>0</td></tr><tr><td>1</td><td>1</td><td>1/2</td><td>0</td><td>0</td></tr><tr><td>1</td><td>0</td><td>0</td><td>0</td><td>0</td></tr></table>	1	←	2	←	3	←	4	→	3	↑		↑		↑		↑		↑	2	←	3	←	4	←	5	→	4	↑		↑		↑		↓		↓	3	←	4	←	5	↓	4	→	3	↑				↓		↓		↓	4		4	→	3	→	2	→	1	1	1	1	1/2	0	1	1	1	3/8	0	1	1	1/2	0	0	1	0	0	0	0
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Note that some cells have their flow split in multiple directions. For example, the lowest cell with an elevation of 5 has its flow split 4 ways, 2 of which flow towards the upper left corner. Thus, it contributes 1/2 liter to the top left corner. The other cell with

Input	Output	Explanation
		<p>elevation 5 also has its flow split 4 ways. $\frac{1}{4}$ of the flow goes to the left and eventually to the top left corner. Another $\frac{1}{4}$ of the flow goes up, and then splits again, with $\frac{1}{2}$ of the $\frac{1}{4}$ going to the left and making its way to the top left corner. Thus, this cell contributes $\frac{3}{8}$ liter to the top left cell.</p>