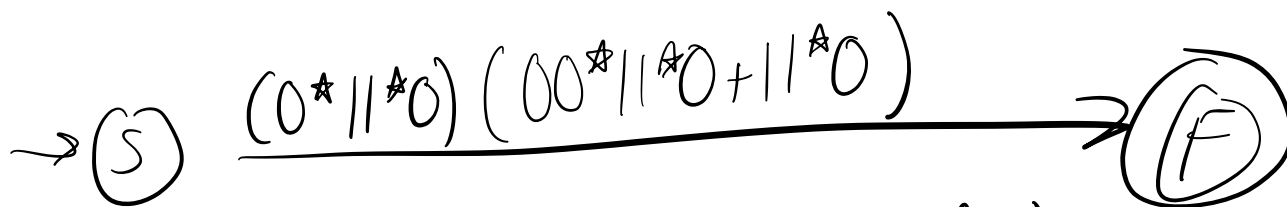
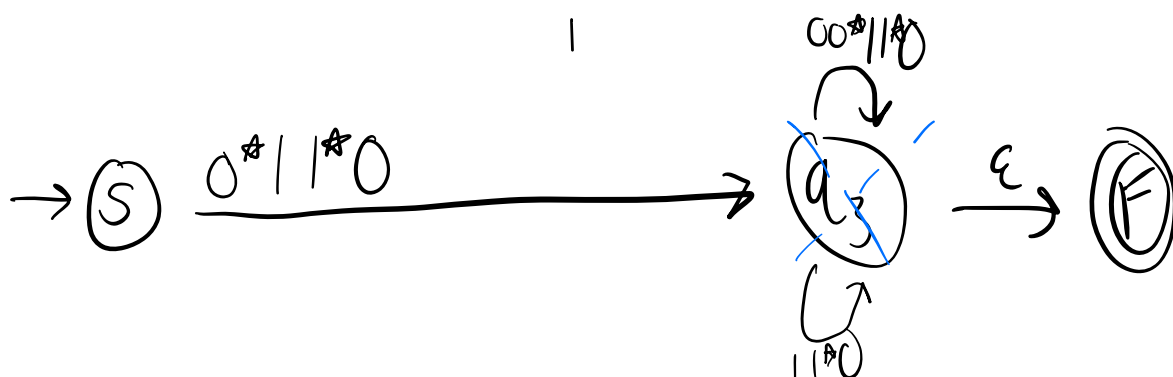
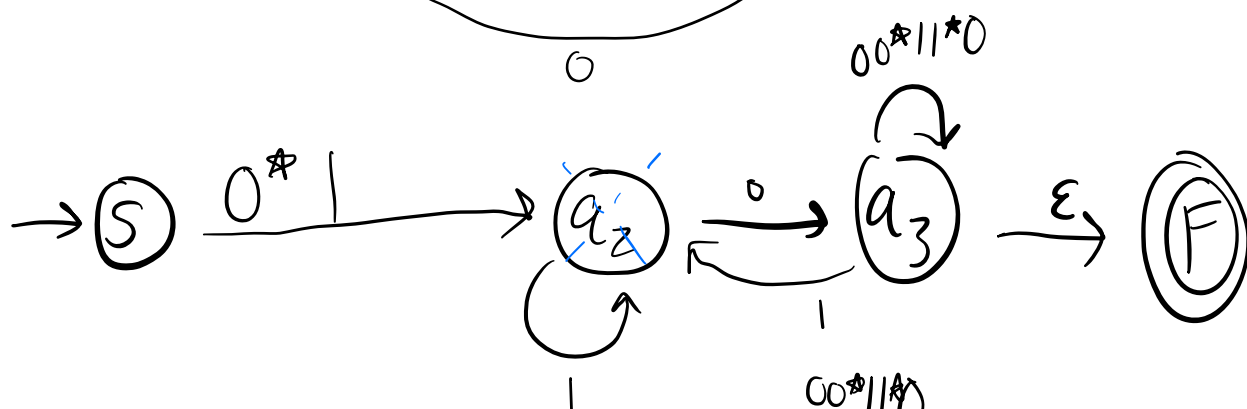
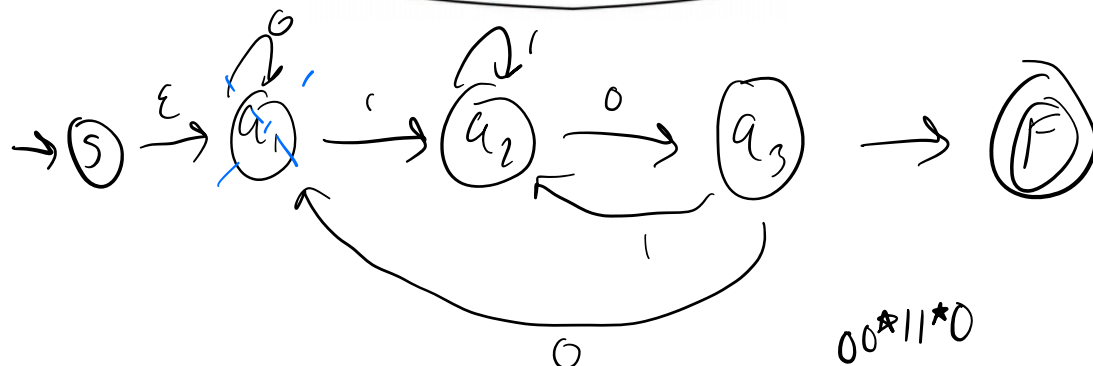
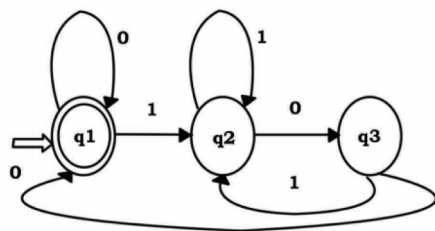
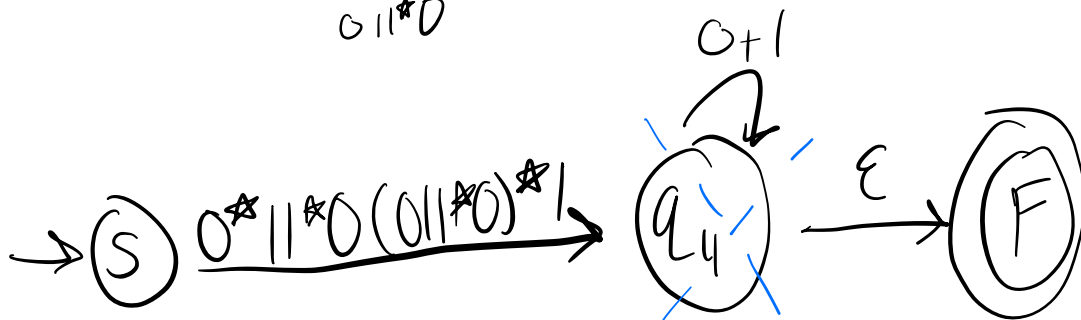
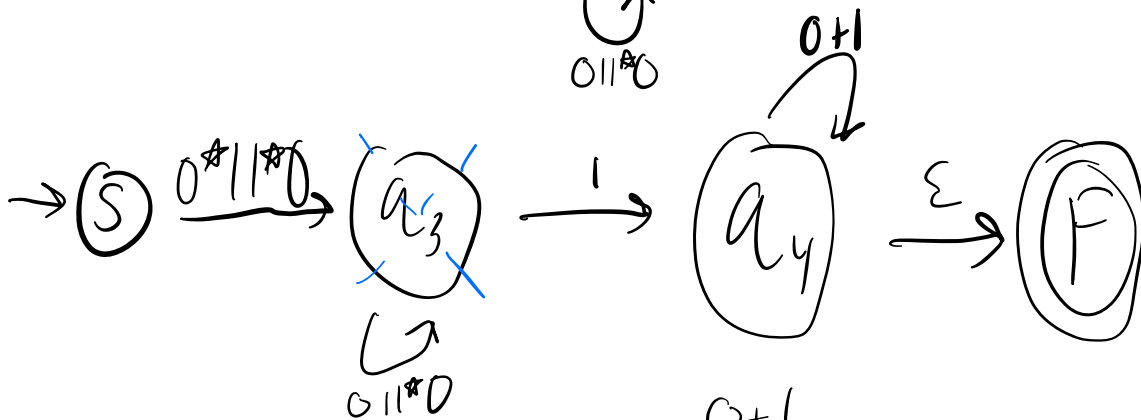
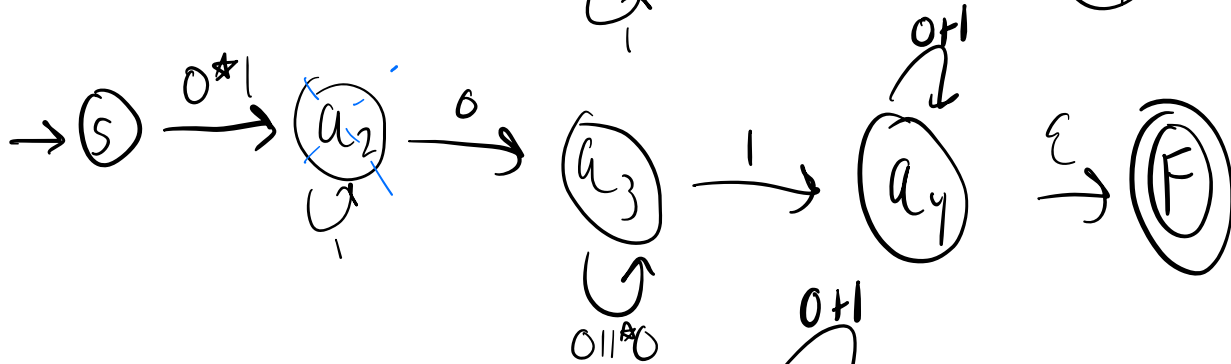
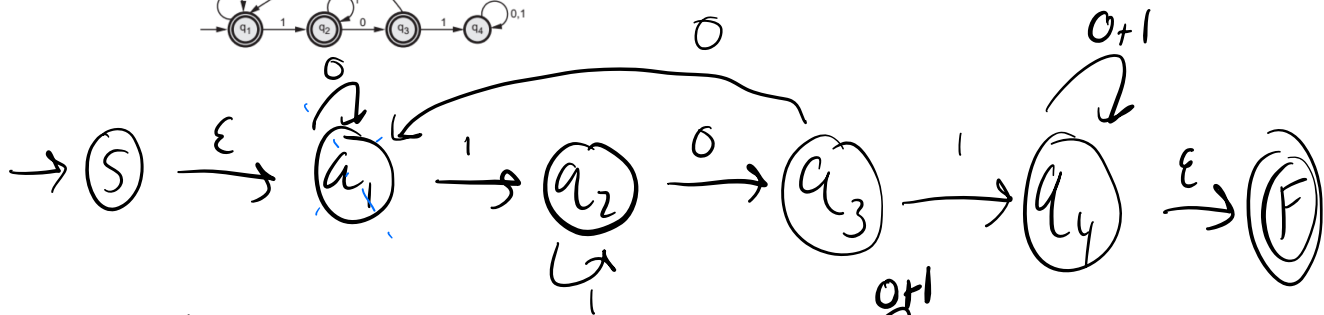
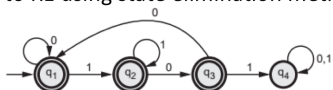


1. Convert the given FA to RE using state elimination method.



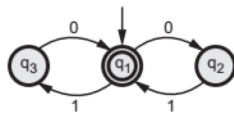
RE = $(0^*|1^*0)(00^*|1^*0+11^*0)$

2. Convert the given FA to RE using state elimination method.



RE = $[0^*11^*0(011^*0)^*1](0+1)$

3. Convert the given FA to RE using Arden's theorem.



$$\begin{aligned}
 * q_1 &: \epsilon + 0q_3 + 1q_2 \\
 q_2 &: 0q_1 \\
 q_3 &: 1q_1
 \end{aligned}$$

$$\begin{aligned}
 R &= RP + Q \\
 R &= QP^*
 \end{aligned}$$

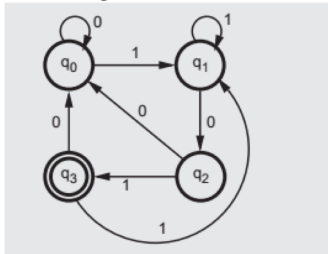
$$q_1 = \epsilon + 0(1q_1) + 1(0q_1)$$

$$q_1 = \epsilon + 01q_1 + 10q_1$$

$$\begin{array}{ccccccc}
 q_1 & = & q_1 & (01 + 10) & + & \epsilon \\
 \underbrace{}_R & & \underbrace{}_R & \underbrace{}_P & & \underbrace{}_Q
 \end{array}$$

$$q_1 = \epsilon (01 + 10)^*$$

4. Convert the given FA to RE using Arden's theorem.



$$\begin{aligned}
 q_0 &= \epsilon + 0q_0 + 0q_2 + 0q_3 & R &= RP + Q \\
 q_1 &= 1q_0 + 1q_1 + 1q_3 & R &= QP^* \\
 q_2 &= 0q_1 \\
 * q_3 &= 1q_2
 \end{aligned}$$

$$q_3 = 1(0q_1) = 10q_1$$

$$q_1 = 1q_0 + 1q_1 + 1(10q_1)$$

$$\underset{\substack{\vee \\ R}}{q_1} = \underset{\substack{\vee \\ R}}{q_1} (\underset{\substack{\vee \\ P}}{1+110}) + \underset{\substack{\vee \\ Q}}{1q_0}$$

$$q_1 = 1q_0 (1+110)^*$$

$$q_0 = \epsilon + 0q_0 + 0q_2 + 0q_3$$

$$q_0 = \epsilon + 0q_0 + 00q_1 + 010q_1$$

$$q_0 = \epsilon + q_1(00 + 010) + 0q_0$$

$$q_0 = \epsilon + 1q_0(1+110)^*(00+010) + 0q_0$$

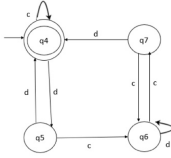
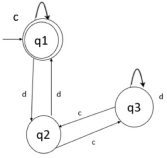
$$\underset{\substack{\vee \\ R}}{q_0} = \underset{\substack{\vee \\ R}}{q_0} \left[\underset{\substack{\vee \\ P}}{1(1+110)^*} + \underset{\substack{\vee \\ Q}}{(00+010)+0} \right] + \epsilon$$

$$q_0 = [1(1+110)^* + (00+010)+0]^*$$

$$q_3 = 01q_1 = 1q_0(1+110)^* 01$$

$$q_3 = 1[1(1+110)^* + (00+010)+0]^* (1+110)^* 01$$

5. Find whether the given FA are equivalent to each other.



$I_{h_1} = I_{h_2}$
 $F_{h_1} = F_{h_2}$

	c	d
(a_1, a_4)	(a_1, a_4)	(a_2, a_5) ✓
(a_2, a_5)	(a_3, a_6)	(a_1, a_4) ✓
(a_3, a_6)	(a_2, a_5)	(a_3, a_6) ✓
(a_4, a_7)	(a_3, a_6)	(a_1, a_4) ✓

The 2 FAs are equivalent to each other.