

1. State that pumping lemma for regular sets and show that the regular set  $L = \{0^{n^2} \mid n \geq 1\}$   
(or)  $L = \{0^k \mid k = i^2, i \geq 1\}$  is not regular.

$L$  is regular

$P$  = pumping language.

$$S = 0^{P^2}$$

$$S = xyz$$

$y$  = is a string of 0's

The language is regular because no matter what the language is going to contain a string of 0's.

2. State that pumping lemma for regular sets and show that the regular set  $L = \{W/W^8/W\}$  is a set of input string  $\{0,1\}$  or  $\{a,b\}$

$L$  is regular  
 $p =$  pumping length

$$s = 1^p 0^p 0^p 1^p$$

$$s = xyz$$

$y =$  string of 1's at the end

$$x(y^i)z \in L \text{ for all } i$$

ex.  $i=2$

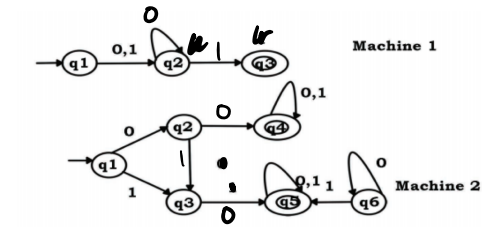
$$x(y^2)z = 10011$$

The string is not in the language.

Doesn't meet Pumping Lemma

The language is not regular via contradiction.

3. Verify the two finite automaton M1 ,M2 given are equivalent over the input symbol{0,1}



Here is the table,

States	0	1
q1	q2	q2
q2	q2	q3
q3	null	null

states	0	1
q1	q2	q3
q2	q4	q3
q3	q5	null
q4	q4	q4
q5	q5	q5
q6	q6	q5

States	0	1
$(a_1, a_1)$	$(a_2, a_2)$	$(a_2, a_3)$
$(a_2, a_2)$	$(a_2, a_4)$	

↑  
Intermediate / Final

The 2 machines are not equal.

4.  $L = \{0^n / n \geq 1\}$ . Find CFG.

Any number of 0's  $\geq 1$ . Ex: 0, 00, 000, ...

$S \rightarrow 0A$

$A \rightarrow 0A \mid \epsilon$

5. Find  $L(G)$  where  $S \rightarrow SS/bS/Sb/a$

$$L(G) = a^* \Sigma^* + b \Sigma^+$$

6. Consider the grammar  $G = (\{A, S\}, \{a, b\}, p, s)$  where  $p$  consist of  $S \rightarrow aAS/a$   $A \rightarrow SbA/SS/ba$   
Draw the derivation tree for string "aabbba"

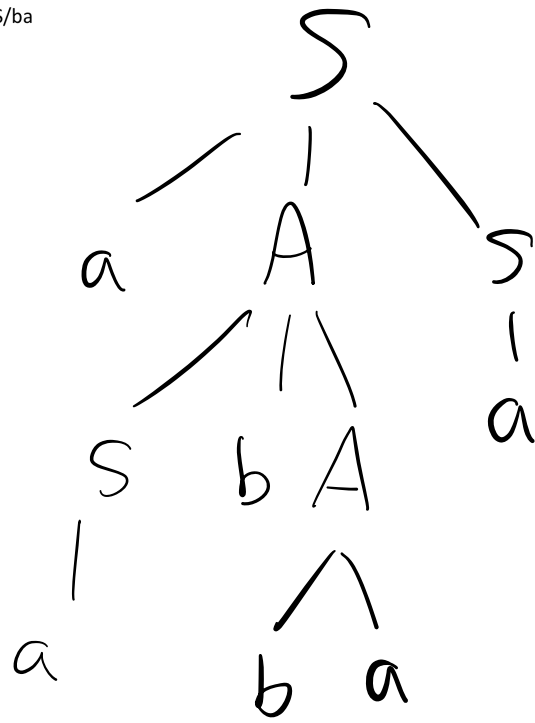
$$S \rightarrow aAS$$

$$S \rightarrow aSbAS$$

$$S \rightarrow aabAS$$

$$S \rightarrow aabbaS$$

$$S \rightarrow aabbbaa$$



7. Derive the string "aabbabba" for LMD, RMD and parse tree using CFG given by G where production is  $S \rightarrow aB/ba$ ,  $A \rightarrow a/aS/bAA$   $B \rightarrow b/bS/aBB$

LMD

$$S \rightarrow aB$$

$$S \rightarrow aaBB$$

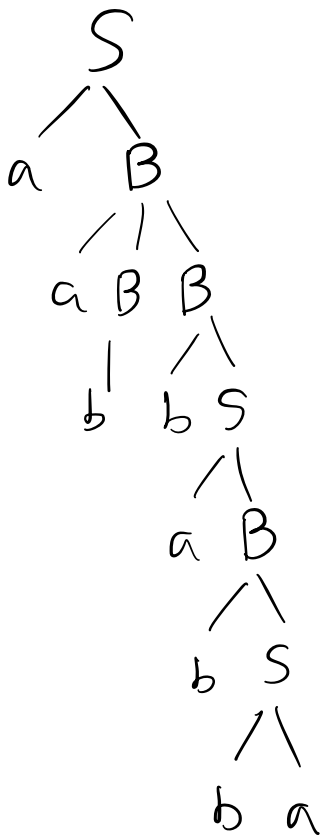
$$S \rightarrow aabB$$

$$S \rightarrow aabbs$$

$$S \rightarrow aabbab$$

$$S \rightarrow aabbabS$$

$$S \rightarrow aabbabba$$



RMD

$$S \rightarrow aB$$

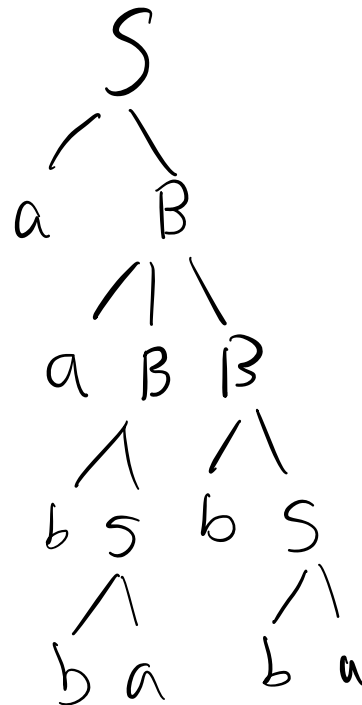
$$S \rightarrow aaBB$$

$$S \rightarrow aaBbS$$

$$S \rightarrow aaBbbba$$

$$S \rightarrow aabSbbba$$

$$S \rightarrow aabbabba$$



8. Prove that given CFG is ambiguous  $S \rightarrow 0B/1A$   $A \rightarrow 0/0S/1AA$   $B \rightarrow 1/1S/0BB$

$S \rightarrow 0B/1A$   
 $A \rightarrow 0/0S/1AA$   
 $B \rightarrow 1/1S/0BB$

<u>0011</u>	
$S \rightarrow 0B$	$S \rightarrow 0B$
$B \rightarrow 0BB$	$S \rightarrow 0B$
$B \rightarrow 1$	$B \rightarrow 0BB$
$B \rightarrow 1$	$B \rightarrow 1S$
✓	$S \rightarrow$
	X

<u>101001</u>	
$S \rightarrow 1A$	$S \rightarrow 1A$
$A \rightarrow 0S$	$A \rightarrow 0S$
$S \rightarrow 1A$	$S \rightarrow 1A$
$A \rightarrow 0S$	$A \rightarrow 0$
$S \rightarrow 0B$	X
$B \rightarrow 1$	
✓	

The CFG is not ambiguous



9. Consider the CFG  $G$  given below. Find a CFG  $G'$  with no  $\epsilon$ -productions and no unit productions.  $S \rightarrow ABA$   $A \rightarrow aA | \epsilon$   $B \rightarrow bB | \epsilon$

$$S \rightarrow ABA$$
$$A \rightarrow aA | \epsilon$$

$$B \rightarrow bB | \epsilon$$

removing  $\epsilon$ -productions

$$S \rightarrow ABA | BA | AB | B$$

$$A \rightarrow aA | a$$

$$B \rightarrow bB | b$$

$$S \rightarrow ABA | BA | AB | B | AA | A$$

$$A \rightarrow aA | a$$

$$B \rightarrow bB | b$$

removing unit productions

$$S \rightarrow ABA | BA | AB | bB | b | AA | aA | a$$

$$A \rightarrow aA | a$$

$$B \rightarrow bB | b$$

10. Find a reduced grammar equivalent to the grammar:  $S \rightarrow aAa$ ,  $A \rightarrow bBB$ ,  $B \rightarrow ab$ ,  $C \rightarrow aB$   
 $aB$

$S \rightarrow aAa$ ,  $A \rightarrow bBB$ ,  $B \rightarrow ab$ ,  $C \rightarrow aB$

$C$  is unreachable so it can be removed

$S \rightarrow aAa$ ,  $A \rightarrow bBB$ ,  $B \rightarrow ab$