

Q1 K-sorted array. Sort the array
each element is atmost k distance
from sorted position

	0	1	2	3	4	5	6	
Eg	6	5	3	2	8	10	9	3-sorted
sorted	2	3	5	6	8	9	10	
dist	3	1	1	3	0	1	1	

Solⁿ → Simply sort the array.

TC: $N \log N$

Idea Do you agree that min elem
has to be between idex 0 to k
yes

Because correct pos is 0 & it can
be at max distance k.

Similarly 2nd min 1 - k+1
3rd min 2 - k+2

Solⁿ

Use heap

1) Build min heap $O-k$

```
2) for (i = k+1 ; i < n ; i++) {  
    extract min ()  
    insert (arr[i])  
}
```

At the end of loop, keep extracting min till empty heap.

TC: $k + (n-k) \log k$

0	1	2	3	4	5	6
6	5	3	2	8	10	9
2	3	5	6	8	9	10

3-sorted



Q2 Median of running stream of integers. Find median after every integer comes in.

Eg-

10 30 20 40 50 60 70

median

$\Rightarrow 30$

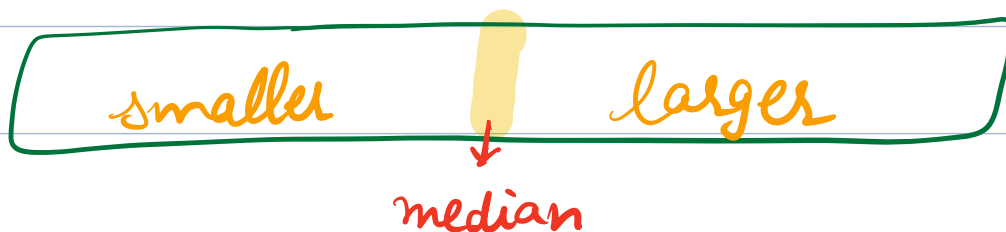
1 2 3 4

$\frac{2+1}{2} = 2.5$

Median is the middle elem of the sorted version of the array

Brute force: Sort after each number comes in

$$\text{size}(\text{small}) - \text{size}(\text{large}) \leq 1$$

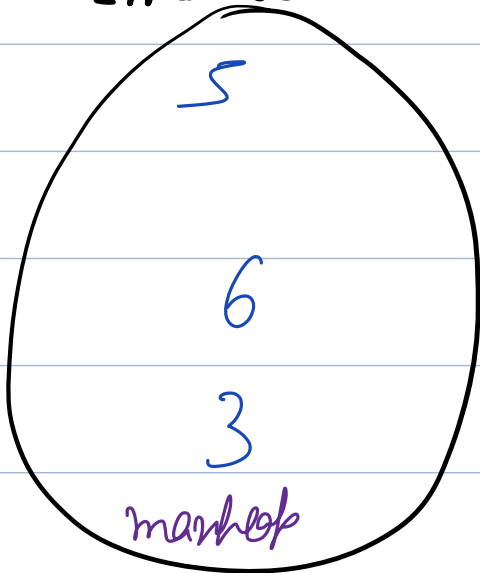


median divides in almost half.

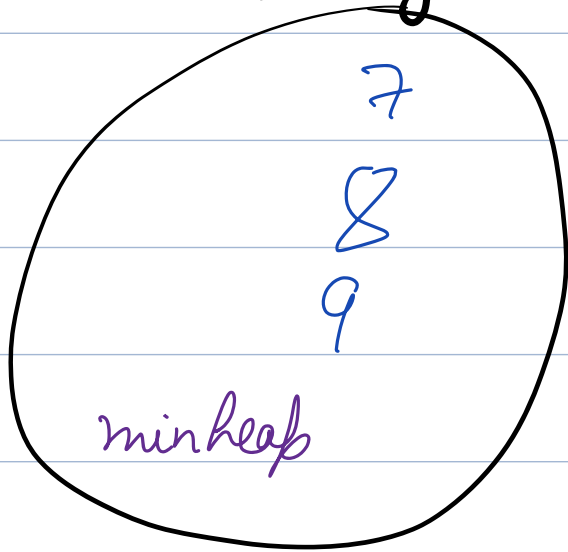
9 8 7 3 6 5

med 9 8.5 8 7.5 7 6.5

smaller



larger



when $n = \text{even}$

$$\text{median} = \frac{\max(A) + \min(B)}{2}$$

$n = \text{odd}$

$$\text{median} = \begin{cases} \max(A) & \text{if } A \text{ larger} \\ \min(B) & \text{if } B \text{ larger} \end{cases}$$

Code

```
for(i=0; i<n; i++) {
```

```
    // elem = x comes
```

```
    if (x < max of A) {
```

```
        insert x in A
```

```
        if (size(A) - size(B) > 1) {
```

```
            extract Max from A
```

```
            insert in B
```

```
        }
```

```
    }
```

```
else {
```

```
    insert x in B
```

```
    if (size(B) - size(A) > 1) {
```

```
        extract min from B
```

```
        insert in A
```

```
    }
```

{done}

TC : $O(n \log n)$

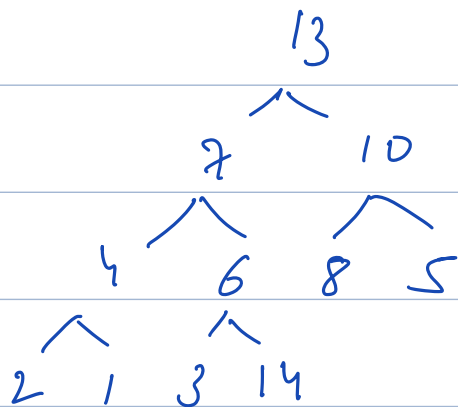
SC : $O(N)$

Q1 Sort the given array using heaps
Heapsort

array $\xrightarrow{TC: O(N)}$ heap $\xrightarrow{TC: O(n \log n)}$ extract
min n times
& put in new array

TC: $O(n \log n)$ SC: $O(N)$

0	1	2	3	4	5	6	7	8	9	10
14	13	10	7	6	8	5	2	1	3	4
4										14



1) Build max heap in array

$i = n - 1$

while ($i > 0$) {

swap ($a[0], a[i]$)

$i--$

heapify ($0, arr, i$)

}

SC: $O(1)$

Q2 Find k^{th} largest element in array.

Eg - 8 5 1 2 3 6 9 7

$k=3$

ans = 7

- Solutions -
- 1) sort & return arr[n-k]
 - 2) sort & Binary search
 - 3) Max heap & extract-max k times

How to do with heaps

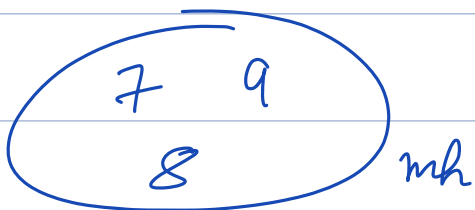
- 1) Build max heap.
- 2) Extract max k times

TC: $O(N) + k \log N$

SC: $O(1)$

Minheap \Rightarrow 8 5 1 2 3 6 9 7

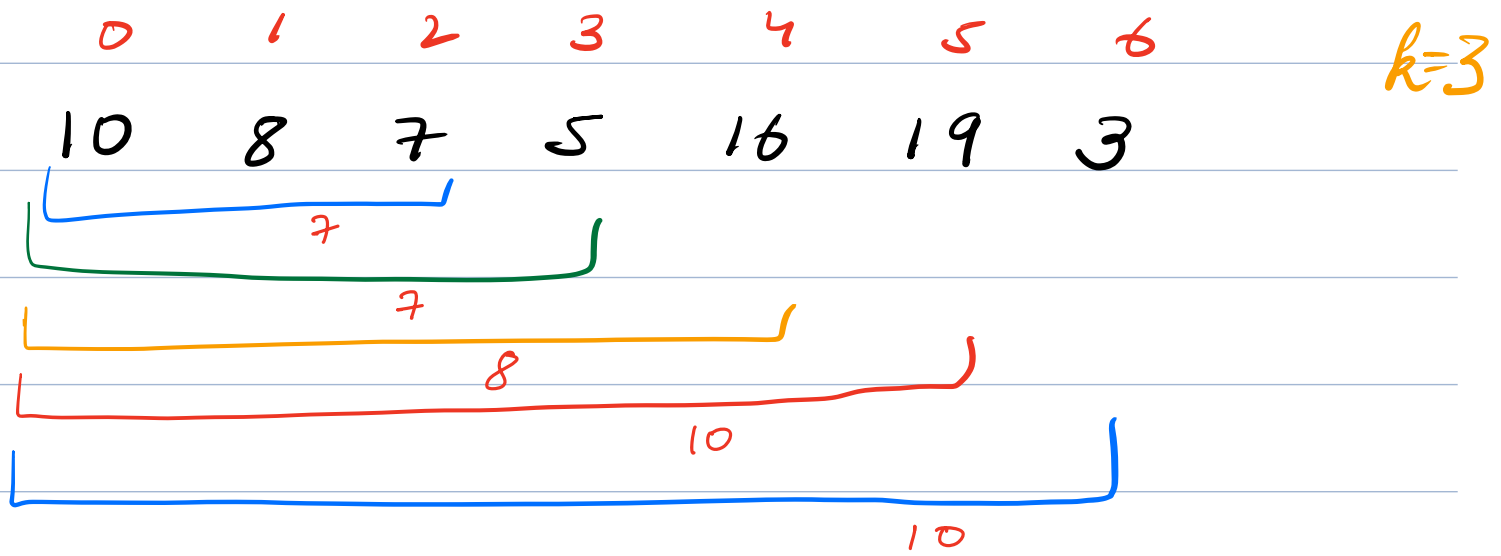
$k=3$



ans = mh.min()

SC: $O(k)$

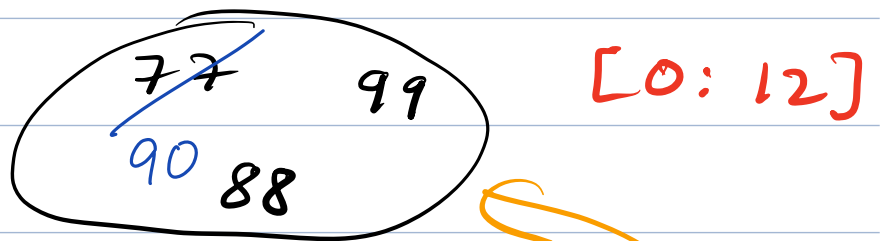
Q3 Find K^{th} largest for every prefix $[0-i]$



Brute force: For each window, iterate on the whole window. $O(n^2)$

Idea Maintain the k largest no.s of the present window

Eg- $k=3$



$a[13] = 90$

Will you put 90 in the set
Need to compare with min of the set

⇒ minheap

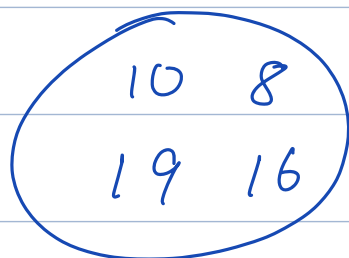
remove min (77)
insert 90.

What is the k^{th} largest?
min of heap

Dry run

0	1	2	3	4	5	6
10	8	7	5	16	19	3

$k=4$



⇒ 5

⇒ 7

⇒ 8

⇒ 8

Code

```
list<int> ans  
min heap mh  
for (i=0; i<k; i++)  
    mh.insert(a[i])  
ans.insert(mh.getmin())
```

```
for (i=k; i<n; i++) {  
    elem = a[i]  
    if (elem > mh.getmin()) {  
        mh.deletemin()  
        mh.insert(elem)  
        ans.add(mh.getmin())  
    }  
}
```

$$TC : k \log k + (n-k) \log k \\ \Rightarrow n \log k$$

$$SC : O(k) + n - k + 1 \\ \Rightarrow O(N)$$