

Queue \rightarrow First in First out

Operations:

(insert) enqueue(x)

(remove) deque (n)

front ()

isEmpty()

rear () back

5 7 3 | counter

0	1	2	3	4	5
10	20	30	40	50	60
	↑				↑
	front				rear

Queue using array

```
class Queue {  
    int size  
    int arr[size]  
    int front =  
    int rear = -1
```



starting id_x of queue
ending id_x of queue

```
enqueue(int x) {  
    if (rear == size - 1) cout << "Queue Full"<br>    else<br>        rear++        arr[rear] = x
```

```
}  
  
dequeue() {  
    if (rear - front + 1 == 0) // size of the queue<br>        cout << "Empty Queue"<br>    else<br>        front++
```

```
}
```


Q1 Given k . Series is made up of 1, 2. Return k^{th} num.

Series \Rightarrow

	1	2	3	4	5	6	7	8
	1	2	11	12	21	22	111	112

$k=7$ ans = 111

$k=4$ ans = 12

Brute Iterate from 1. check if num has only 1, 2. If yes, count++. when count = k , end.

Idea

First 2 no.s are 1, 2

From 1, what all num we can get directly \Rightarrow

From 2, \Rightarrow

21 22 111 112 121 122

From $x \Rightarrow$ 1) $10^*x + 1$
Code 2) $10^*x + 2$

queue <int> q

q.enqueue(1)

+ x 3 4

q.enqueue(2)

21 22 111 112 121 122

cnt = 1

while (cnt != k) {

int x = q.front()

q.dequeue()

cnt++

q.enqueue ($10x + 1$)

q.enqueue ($10x + 2$)

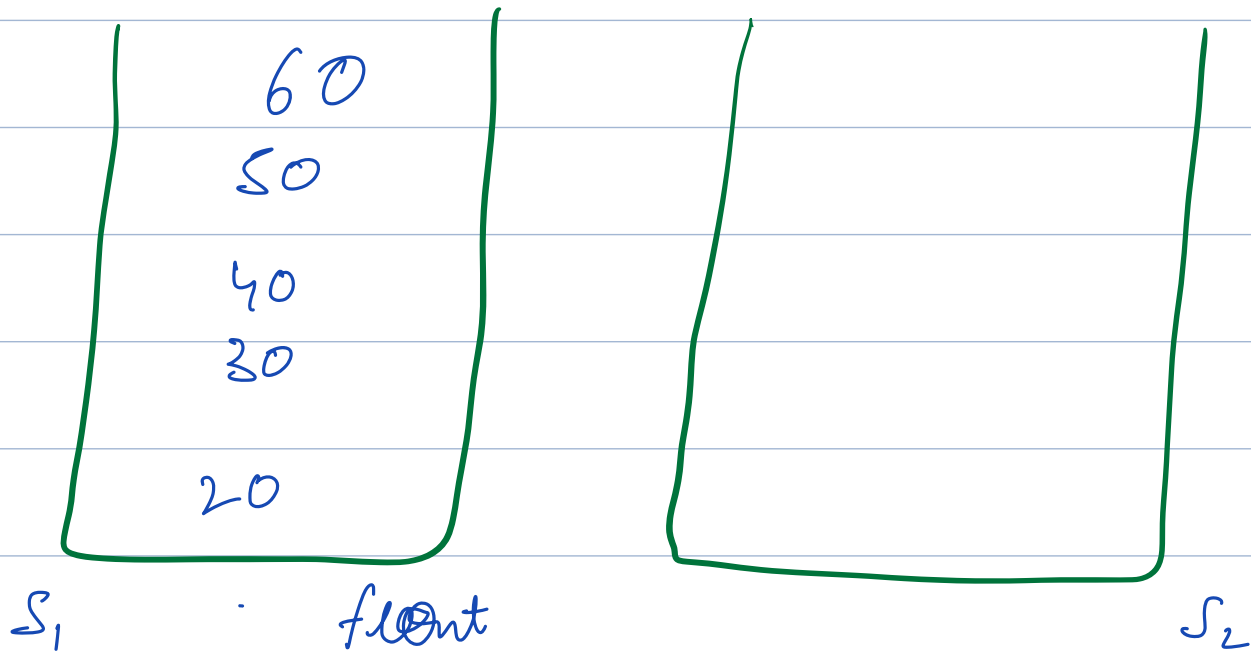
}

return q.front()

TC: } $O(k)$
SC: }

Q3 Implement Queues using stacks (only)

Idea: Use 2 stacks

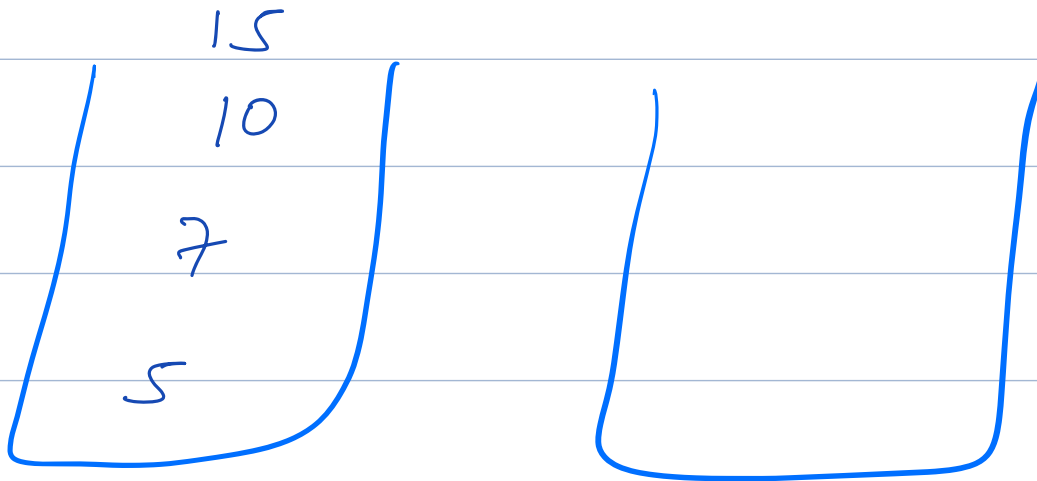


enqueue \rightarrow Just put on top of S_1

deque \rightarrow Need to remove bottom elem.

- 1) Remove all elem & put in S_2
- 2) $S_2.\text{pop}()$
- 3) Put all contents of S_2 back in S_1

dry run.



Code

```
void enqueue (x) {
```

```
    s1.push(x)
```

```
}
```

```
void dequeue () {
```

```
    if (s1.empty())
```

```
        print ("Error")
```

```
    while (!s1.empty())
```

```
        s2.push(s1.top())
```

```
        s1.pop()
```

```
}
```

$s_2.$ pop()

while (! $s_2.$ empty())

$s_1.$ push ($s_2.$ top())

$s_2.$ pop()

}

}

TC

enqueue $\rightarrow O(1)$

dequeue $\rightarrow O(n)$

Doubly ended queue

Deque



front

back

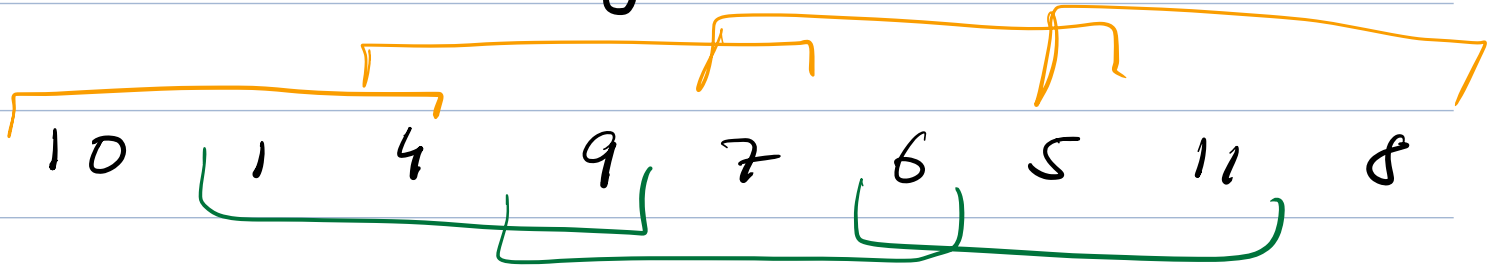
Sliding window maximum

Deque ^{CRUD}

VVV Imp

Adobe GS Amazon Microsoft

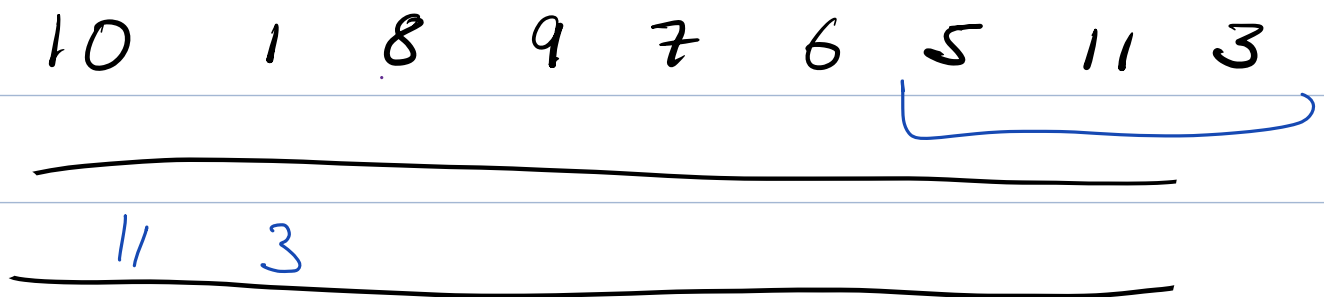
Array of size N . Find max elem of every subarray of size K .



$k=3$ ans $\Rightarrow \{10, 9, 9, 9, 7, 11, 11\}$

Brute: Check all subarrays of size K & find max. TC: $O(n^2)$

Idea $k=3$



front



#	access	last	elem	stack
#	access	first	elem	queue

Deque (Doubly ended queue)

$k=4$

3 15 6 15 12 4 2 10 9 18

15 15 15 15 12 10 18

18

First prepare the deque for first window

new_elem

rear < new_elem

remove rear

rear ≥ new_elem

insert at rear

repeat

remove elem

check with front



if equal

if not

remove from
front

do nothing

Max \Rightarrow front element

Code

```
Deque <int> dq;
for (i = 0; i < k; i++) {
    while (!dq.empty() &&
           dq.rear() < arr[i])
        dq.pop_rear();
    dq.push_rear(arr[i]);
}
```

```
ans.insert(dq.front());
```

```
int s = 1          e = k
```

```
while (e < n) {
```

```
    while (!dq.empty() &&
           dq.rear() < arr[e])
        dq.pop_rear();
    dq.push_rear(arr[e]);
```

TC: $O(n)$
SC: $O(n)$

```
    if (dq.front() == arr[s-1])
```

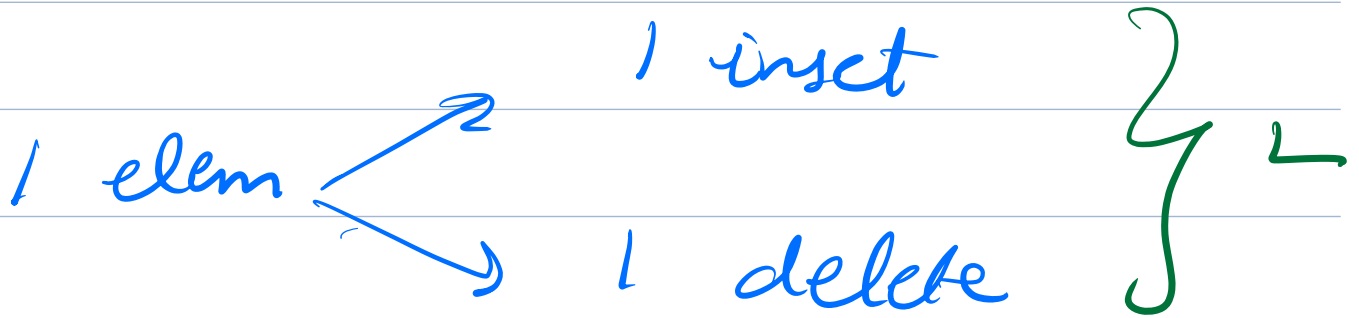
```
        dq.pop_front();
```

```
    ans.insert(dq.front());
```

Stt

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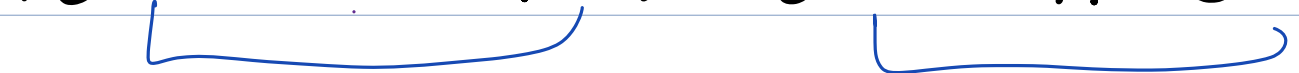
1 \rightarrow 2 op
N \rightarrow 2N op

<done>

Idea

k=3

10 1 8 9 7 6 5 11 3



8



front

