

Check if given elem exists

$A = \{ 2, 4, 11, 15, 6, 8, 14, 9 \}$

$Q = \{ 4, 10, 17, 14 \}$

Solⁿ \Rightarrow Iterate for each query element
TC: $O(NQ)$

Solⁿ 2 \Rightarrow Direct Access Table (DAT)

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
		1		1		1		1	1		1			1	1

Advantage \rightarrow Insert, Search $\Rightarrow O(1)$

Disadvantage \rightarrow 1) Space wastage
2) Cannot create big arrays

How to solve this issue

$A = \{ 21 \quad 42 \quad 37 \quad 45 \quad 99 \quad 30 \}$
 $\downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow$
 $1 \quad 2 \quad 7 \quad 5 \quad 9 \quad 0$

Let's say I can only create array of size = 10

0	1	2	3	4	5	6	7	8	9
\emptyset	\emptyset	\emptyset	0	0	\emptyset	0	\emptyset	0	\emptyset
1	1	1			1		1		1

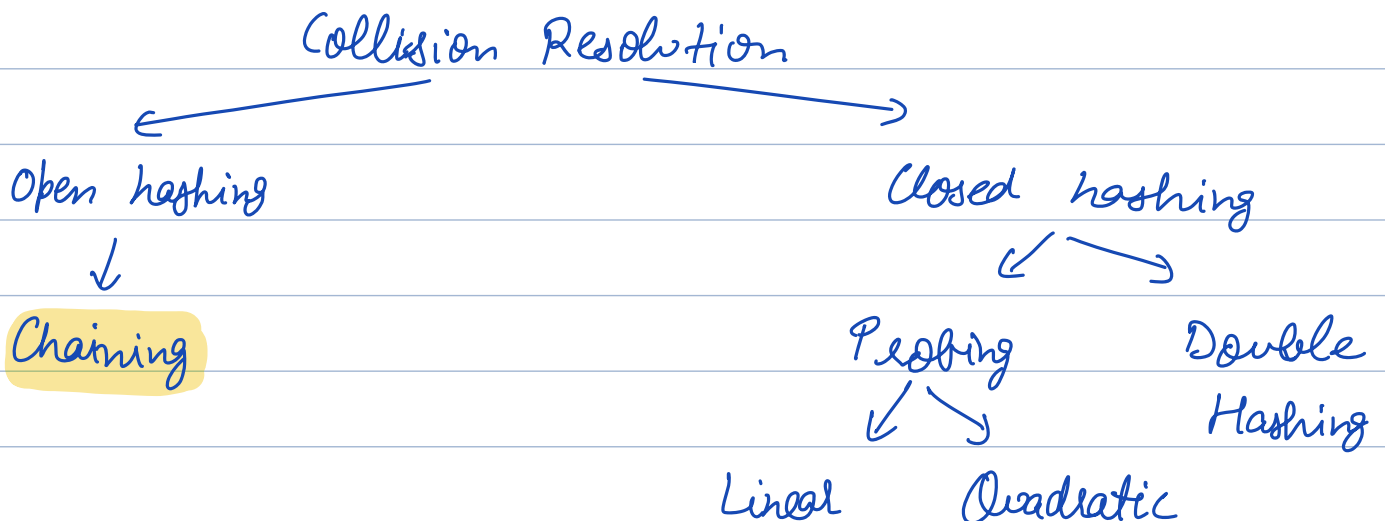
Can I take a list of 10? yes

Issue \Rightarrow Collision

21	2	41
\downarrow		\downarrow
1		1

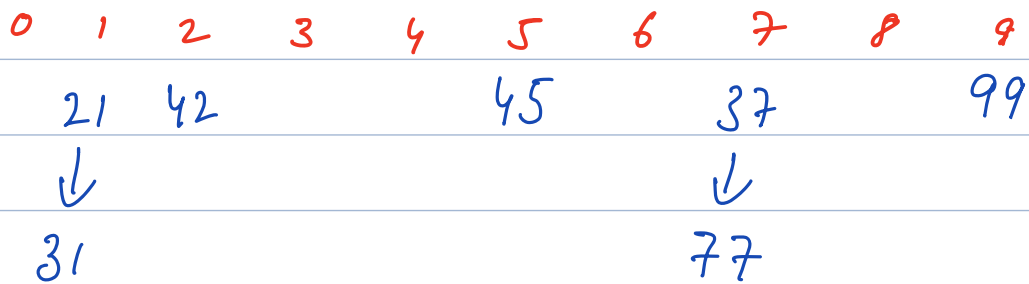
value A \rightarrow hash func \rightarrow same value
value B \rightarrow hash func \rightarrow

Collision Resolution



Chaining

$A = \{ 21, 42, 37, 45, 77, 99, 31 \}$



Each hash value is a linked list

TC of insert

if at tail $\Rightarrow O(n)$

if at head $\Rightarrow O(1)$

TC of search/delete

Average \Rightarrow less than 1 (Lambda)

worst case $\Rightarrow O(n)$

What is λ (Lambda / Load factor)

Ratio of num of elements / size of DAT

0 16

1

2

3 11 \rightarrow 27 \rightarrow 19

4

5

6 22 \rightarrow 6

7

num of elems = 6

DAT size = 8

$$\lambda = 6/8 = 0.75$$

lets say predefined threshold = 0.7

We need to do rehashing using diff hash function

Create DAT with double size of original DAT

$$\text{Now } \lambda = \frac{6}{16} = 0.375 < \text{threshold}$$

(within threshold)

0 6

1 11

2 27

3 19

...

...

...

...

...

15 22

Code

```
class HashMapNode {  
    int key  
    int value  
}  
ArrayList<HashMapNode> buckets [ 4 ]
```

0
1 30 → 200 → 20
2
3

// 4 is size of DAT

```
void insert ( key, value ) {  
    idx = hash ( key )  
    if value in buckets [ idx ]  
        // already present  
    else {  
        buckets [ idx ]. add ( new HashMapNode ( key, value ) )  
        size ++ // total number of elements  
        lamda = size / buckets . length  
        if ( lamda > threshold )  
            rehash ()  
    }  
}
```

```
int hash ( int key ) {  
    int ans = key % buckets . size ()  
    return ans  
}
```

```
void rehash() {
```

```
    int original_size = buckets.size()
```

```
    ArrayList<HashMapNode> old_buckets = buckets
```

```
    int new_size = 2 * original_size
```

```
    buckets.resize(new_size)
```

```
    for (i=0; i< old_buckets.size(); i++) {
```

```
        for (HashMapNode hmnode: old_buckets[i]) {
```

```
            insert(node.key, node.val)
```

```
        }
```

```
    }
```

```
}
```

```
bool search(int key) {
```

```
    int idx = hash(key)
```

```
    bool ans = false
```

```
    for (HashMapNode hmNode: buckets[idx]) {
```

```
        if (hmNode.key == key)
```

```
            ans = true
```

```
    }
```

```
    return ans
```

```
}
```

```
void delete (int key) {  
    int idx = hash (key)  
  
    for (HashMapNode hmNode : buckets [idx]) {  
        if (hmNode.key == key) {  
            // remove this entry from  
            // ArrayList  
        }  
    }  
    size --  
}
```

{done}