

Q1 Given N array elem, rearrange such that
→ all elems \leq $arr[0]$ are to the left of $arr[0]$
→ all elems $>$ $arr[0]$ are to the right of $arr[0]$

Eg- 0 1 2 3 4 5 6 7 8 9 10
10 3 8 15 6 12 2 18 7 15 14

⇒ ≤ 10 10 > 10

0 1 2 3 4 5 6 7 8 9 10
10 3 8 15 6 12 2 18 7 15 14

temp 3 8 6 2 7 10 14 15 18 12 15

SC: $O(n)$ } $O(1)$
TC: $O(n)$ }

0	1	2	3	4	5	6	7	8	9	10
2	3	8	15	6	12	2	18	15	15	14
					$\uparrow P_2$	$\uparrow P_1$				

```
void rearrange (int a[], int N) {
```

```
    P1 = 1          P2 = n - 1
```

```
    while (P1 ≤ P2) {
```

```
        if (a[P1] ≤ a[0])
            P1 ++
```

```
        else if (a[P2] > a[0])
            P2 --
```

```
    } else {
```

```
        swap(a[P1], a[P2])
```

```
        P1 ++      P2 --
```

```
    }
```

```
    swap(a[0], a[P2])
```

TC: $O(n)$

SC: $O(1)$

Q2 Given N array elem, rearrange subarray $[s:e]$ st $ar[s]$ is correct position of subarray. Return correct pos

what to change in above code?

```
int rearrange (int ar[], int N) {
```

```
    P1 = s + 1      P2 = e      s ---- e
```

```
    while (P1 ≤ P2) {
```

```
        if (ar[P1] ≤ ar[s])  
            P1 ++
```

```
        else if (ar[P2] > ar[s])  
            P2 --
```

```
    } else {
```

```
        swap(a[P1], a[P2])
```

```
        P1 ++      P2 --
```

```
    }
```

TC: $O(n)$

```
    swap(a[s], a[P2])
```

SC: $O(1)$

```
    return P2
```

}

How to sort subarray [s:e]

```
void Qsort (int ar[], int s, int e) {
```

```
    if (s > e) return
```

```
    p = rearrange (ar, s, e) } O(n) T.C
```

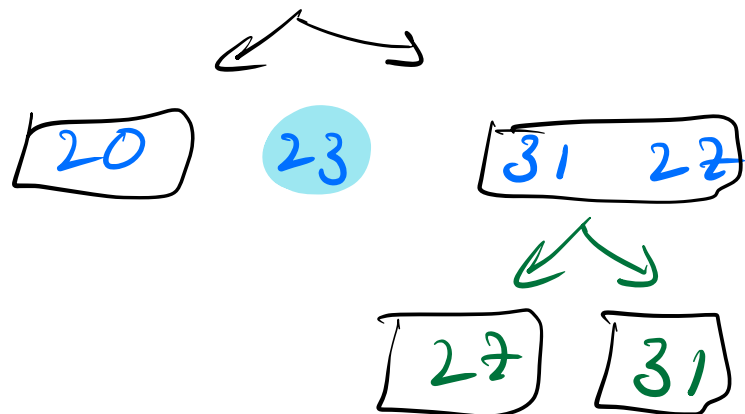
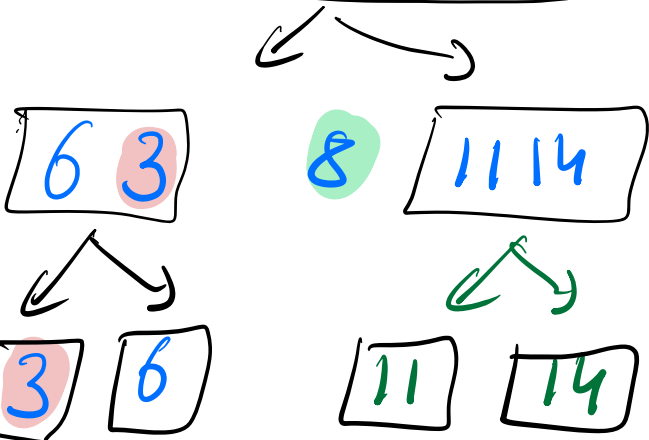
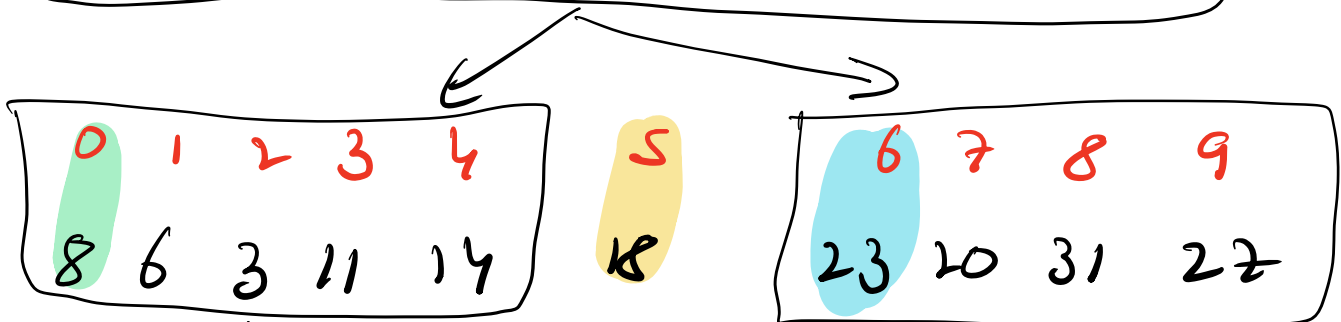
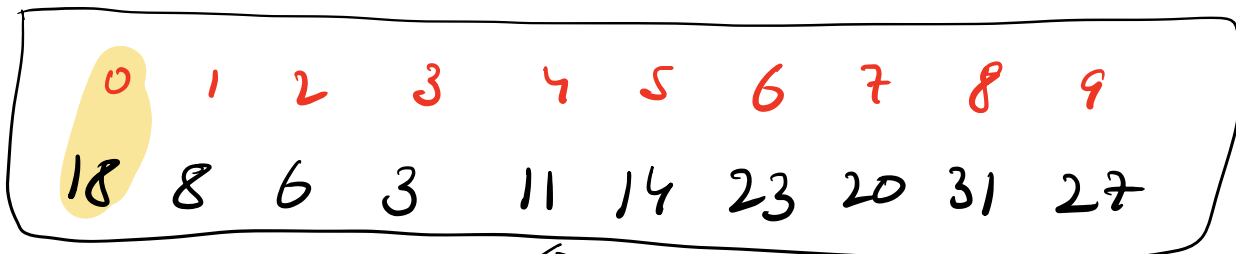
```
    // now recurse
```

s ---- p ---- e

```
    Qsort (arr, s, p-1)
```

```
    Qsort (arr, p+1, e)
```

```
}
```



Time Complexity.

Best Case

$$T(N) = N + T(N/2) + T(N/2)$$

$$T(N) = 2T(N/2) + O(N)$$

We know this is $O(n \log n)$

Worst Case

$$T(N) = N + T(N-1) + T(1)$$

$$T(N) = N + T(N-1)$$

$$T(N) = 2N + T(N-2)$$

⋮

$$T(N) = kN + T(N-k)$$

$$k = ?$$

$$T(N) = O(N^2) \quad \text{worst case}$$

Eg of worst case Any sorted array.

2 3 4 5 6 7 8

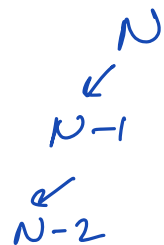
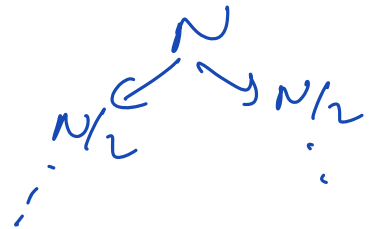
$$\underbrace{N + N-1 + N-2 + \dots + 1}_{= \frac{n(n+1)}{2}}$$

$$\Rightarrow O(n^2)$$

SC best : $\log n$

worst : n

{done}

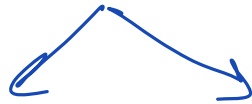


● Main Concept:

Instead of picking the start of subarray as reference, pick random index

0	1	2	3	4	5	6
9	6	8	2	10	11	14
10				9		

6 8 2 9 10 14 11



14 11

This random picking makes average TC:
 $O(n \log n)$

```
int rearrange (int a[], int N) {
```

```
    int s = rand(1, e)
```

```
    swap(a[s], a[r]) → so that ref is now at s.
```

```
    P1 = s + 1    P2 = e
```

```
    while (P1 ≤ P2) {
```

```
        if (a[P1] ≤ a[s])
```

```
            P1 ++
```

```
        else if (a[P2] > a[s])
```

```
            P2 --
```

```
    } else {
```

```
        swap(a[P1], a[P2])
```

```
        P1 ++
```

```
        P2 --
```

```
    }
```

```
    swap(a[s], a[P2])
```

```
    }
```

```
    return P2
```

```
}
```


Comparator

Q Given N array elem, sort in increasing order of no of factors.

If 2 elem has same no of factors, element with less value should come first

Note: Cannot use extra space

Eg	9	3	4	8	16	37	6	13	15
factors	3	2	3	4	5	2	4	2	4

3 13 37 4 9 6 8 15 16

sort(arr, comp)

comparator function.

Comparator allows to sort using our rules.

```
bool comp (int a, int b) {
```

```
// if you want a to appear before b  
// in the sorted order, return true  
// else return false.
```

```
    int f1 = factors(a)  
    int f2 = factors(b)
```

```
    if (f1 < f2)
```

```
        return true
```

```
    else if (f1 > f2)
```

```
        return false
```

```
    else if (f1 == f2) {
```

```
        if (a < b)
```

```
            return true
```

```
else  
    return false
```

```
}
```

```
}
```

```
sort(arr, comp)
```

Q4 K closest points to origin (0,0)

Given list of points \Rightarrow
return K closest points to origin

Eg - $\begin{matrix} 1, 3 \\ \sqrt{10} \\ \sqrt{x^2 + y^2} \end{matrix}$ $\begin{matrix} -2, 2 \\ \sqrt{8} \end{matrix}$ $K=1$ ans = $[-2, 2]$

Eg $\begin{matrix} 1, 3 \\ 10 \end{matrix}$ $\begin{matrix} 1, -1 \\ 2 \end{matrix}$ $\begin{matrix} 2, -1 \\ 5 \end{matrix}$ $K=2$
ans = $[[1, -1], [2, -1]]$

Distance from origin of point x, y

$$\text{sqrt}(x^2 + y^2)$$

We need to sort on basis of distance.

Ques If I compare $x^2 + y^2$ instead of $\text{sqrt}(x^2 + y^2) \Rightarrow$ this works

Idea: Sort using comparator

Code

```
bool cmp (pair<int, int> a, pair<int, int> b) {
```

```
    long d1 = (long) a.first * a.first +  
              (long) a.second * a.second
```

```
    long d2 = (long) b.first * b.first +  
              (long) b.second * b.second
```

```
    if (d1 < d2)
```

```
        return true
```

```
    else
```

```
        return false
```

```
list<pair<int, int>> closest (list<pair<int, int>> A, int K) {
```

```
    list<pair<int, int>> ans .
```

```
    sort (A, cmp)
```

```
    for (i=0 ; i<K ; i++) {
```

```
        ans.insert (A[i])
```

```
    }
```

```
    return ans
```

TC: $O(n \log n)$
SC: $O(n)$

0	1	2	3	4	5	6
10	20	30	40	50	60	70

1 to 10^6 all spf spf(i)

$1 \rightarrow 10^6$

$10^6 + 1 \Rightarrow \text{cnt}[\text{spf}(i)]++$

