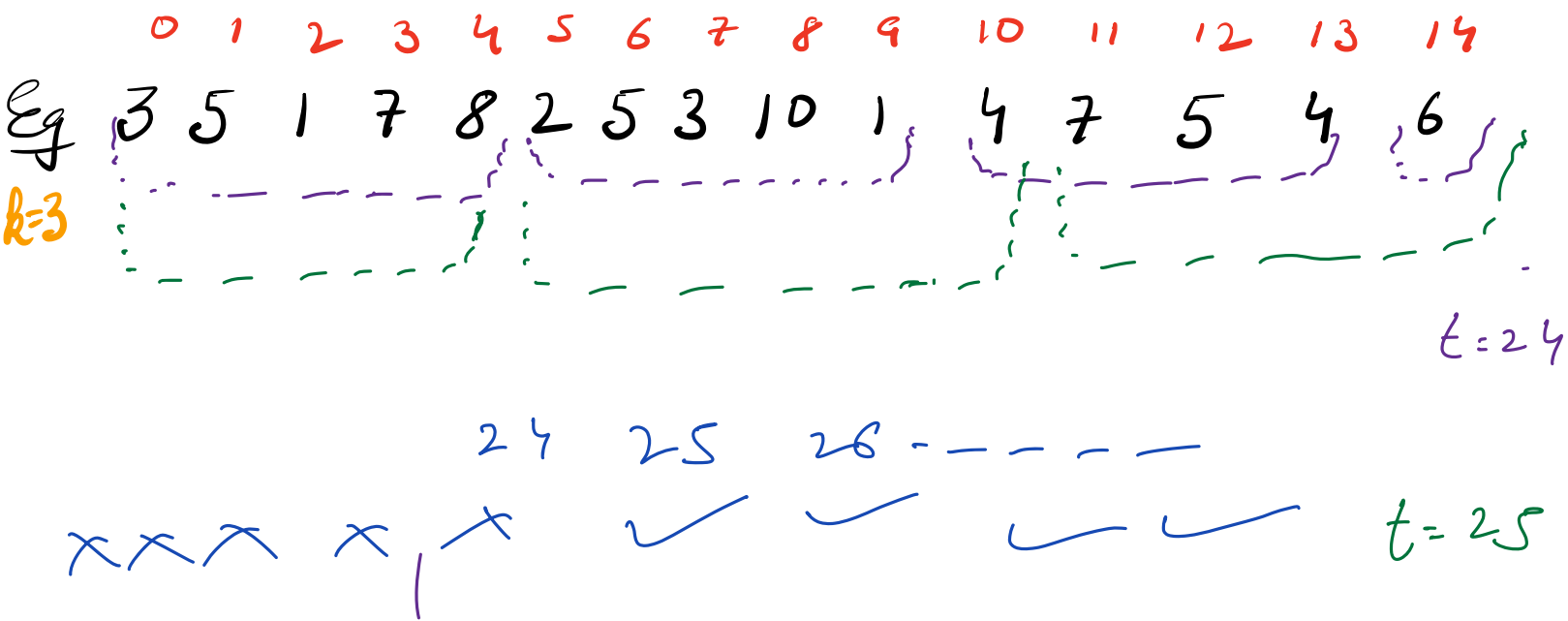


Q1) Given N tasks, K workers & time taken for each task, find min time to complete all tasks.

Note: Single worker can only do continuous set of tasks

Note: All workers start at same time = 0

Note: A task is only assigned to 1 worker



Idea: Binary Search

Can you finish all tasks in 30 min?

Yes

Can you finish all tasks in 10 mins?

NO

8 9 10 - - - - - 30 31 32
 F F F T T T

Search: **Target** : Min time to finish all
 tasks with k workers

$l = \max(arr)$ $h = \text{sum}(arr)$

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14
 3 5 1 7 8 2 5 3 10 1 4 7 5 4 6

$k = 4$

l h m

10 71 40

$ans = 40$

10 39 24

$ans = 24$

10 23 16

17 23 20

21 23 22

$ans = 22$

21 21 21

22 21 STOP!!!

Code

```
int workers (int time [], int N, int K) {
```

```
    l = max(all)    h = sum(all)
```

```
    while (l <= h) {
```

```
        m = (l+h)/2
```

```
        if (check (time, N, K, m)) {
```

```
            ans = m,    h = m-1
```

```
        }
```

```
    } else {
```

```
        l = m + 1
```

```
    }
```

Tc: $O(n \log(\text{sum} - \text{max} + 1))$

Sc: $O(1)$

```
    return ans
```

max

sum

1 mid $\rightarrow O(n)$

$(\text{sum} - \text{max} + 1) \Rightarrow n \times \log(\text{sum} - \text{max} + 1)$

bool check (int m, int time [], int N, int k) {

 s = 0 c = 1

 for (i = 0; i < N; i++) {

 s = s + time[i]

 if (s > m) {

 c++

 s = time[i]

 if (c > k) return false

 }

 }

 return true

}

TC: $O(n)$

SC: $O(1)$



7 4

s = 7 s = 4 m = 10

Q2 Given N cows & M stalls, all stalls are on x -axis at diff location. Place all N cows in such a way such that min distance b/w any 2 cows is maximised

Note 1 One stall has only 1 cow

Note 2 All cows have to be placed

	0	1	2	3	4
Eg	1	2	4	8	9
	C_1		C_2		C_3

cows = 3
ans = dist = 3

	0	1	2	3	4	5	6	7	8
Eg	2	6	11	14	19	25	30	39	43
	C_1			C_2			C_3		C_4

cows = 4

ans = 12

Idea: Binary Search

Can you place cows at atleast 20 distance

NO

Can you place cows at atleast 5 distance

YES

3 4 5 - - ~~14~~ - - - 20 21 22
T T T T T T F F F F F F F

Search

Target: distance b/w 2 cows

l: Min distance b/w 2 stalls

h: $arr[n-1] - arr[0]$

0 1 2 3 4 5 6 7 8

2 6 11 14 19 25 30 39 43

l h m

3 41 22

X

cows = 4

3 21 12

✓

ans = 12

13 21 17

X

13 16 14

X

13 13 13

X

13 12 STOP!!!

Code

```
int moo (int dist [], int N, int cows) {
```

```
    l = min adjacent distance
```

```
    h = dist [n-1] - dist [0]
```

```
    while (l ≤ h) {
```

```
        m = (l+h)/2
```

```
        if (check (m, dist, N, cows)) {
```

```
            ans = m            l = m+1
```

```
        }
```

TC:

```
    else h = m-1
```

```
}
```

SC: $O(1)$

```
return ans
```

```
}
```



$$n \times \log (\text{dist}[n-1] - \text{dist}[0] - \text{min_dist} + 1)$$

```

bool check(int m, int dist[], int N, int cows) {
    last_cow = dist[0]
    count = 1
    for (i=1; i<N; i++) {
        if (dist[i] - last_cow >= m) {
            c++, last_cow = dist[i]
            if (c == cows) return true
        }
    }
    return false
}

```

TC: $O(n)$

SC: $O(1)$

{done}

Monotonicity

