



Trees 1

Song: Get Down | Storm
- Feja
 ↑
 Friend

Topics To Cover:

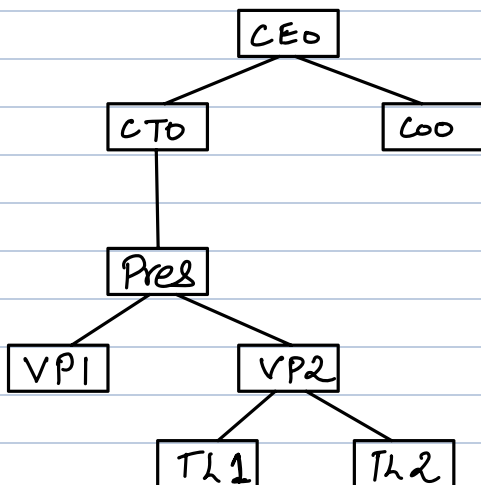
- Trees Intro
- Naming Convention
- Trees Traversal
- ★ - Iterative inorder
- ★ - Construct tree with $pre[]$ & $in[]$

Hi Everyone!!!

Linear Data Structure:

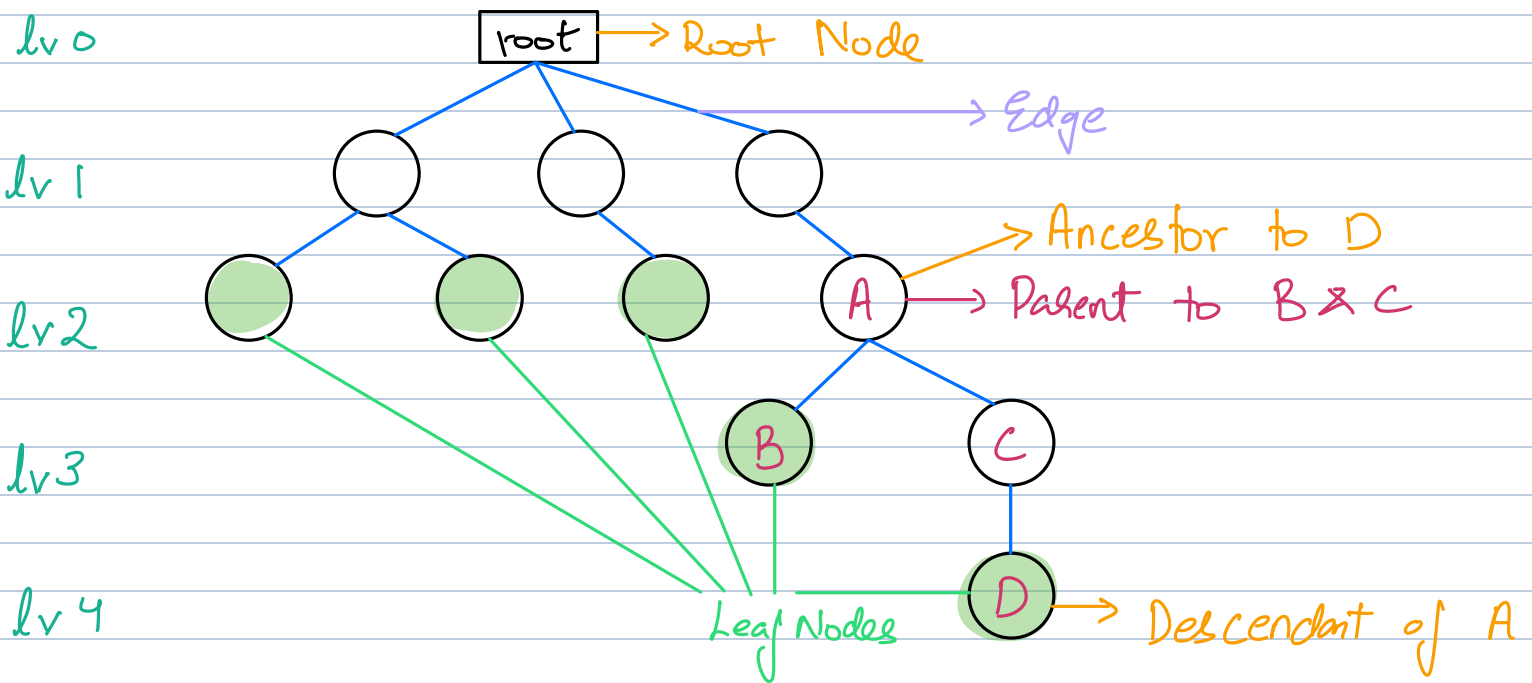
1. Array
2. LL
3. Stacks
4. Queues
5. String

Hierarchical Data Structures:



1. Family Tree
2. Folder Structure
3. Taxonomy
4. Politics / Polity.

Trees

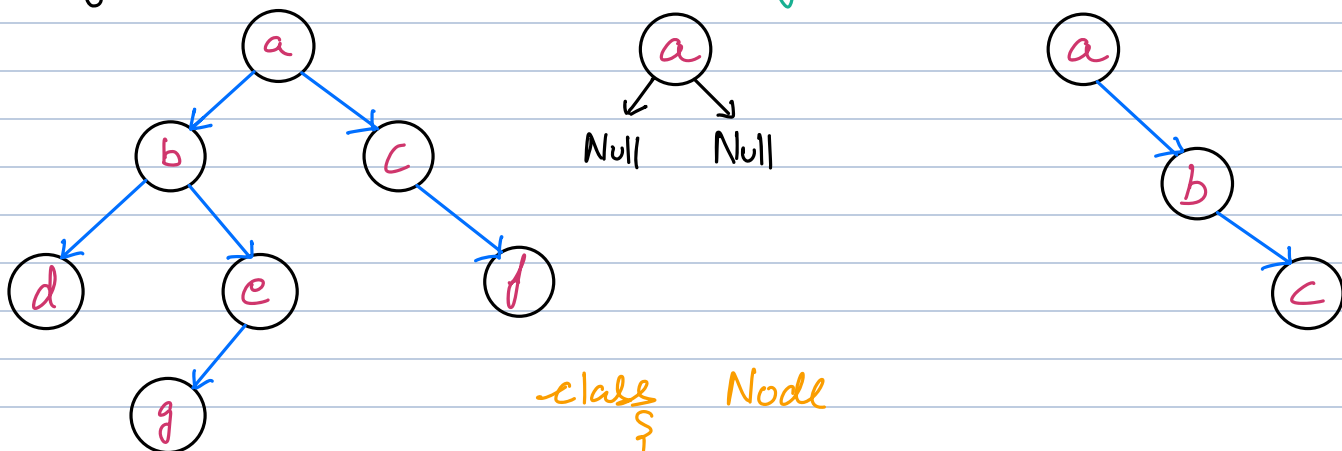


Height: longest path from root to leaf.

* height based on edges: 4

height based on nodes: 5

Binary Tree: It has a maximum of 2 children



class Node

```
{
    int data;
    Node left, right;
```

```
Node (int x)
```

```
{
    |
```

```

data = x;
left = Null;
right = Null;
}
}

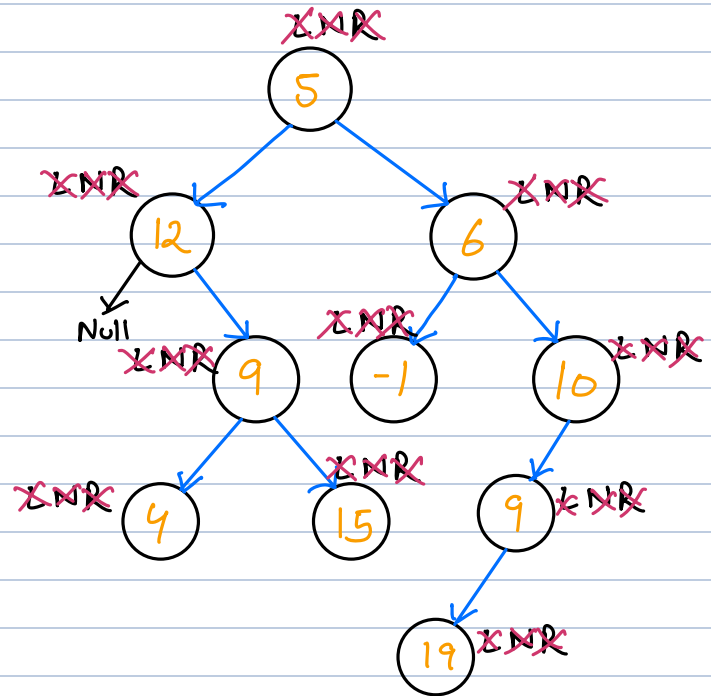
```

Traversal in a Tree.

Inorder Traversal

L N R
Left Node Right

Inorder : 12 4 9 15
output 5 -1 6 19
9 10



```

void inorder (Node node)
{

```

```

    if (node == Null)
        return;

```

```

    inorder (node.left);

```

```

    print (node.data);

```

```

    inorder (node.right);

```

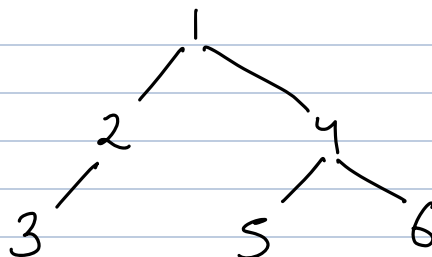
```

}

```

TC: $\Theta(N)$

SC: $\Theta(\text{ht. of Tree})$



print: 3, 2, 1, 5
4, 6

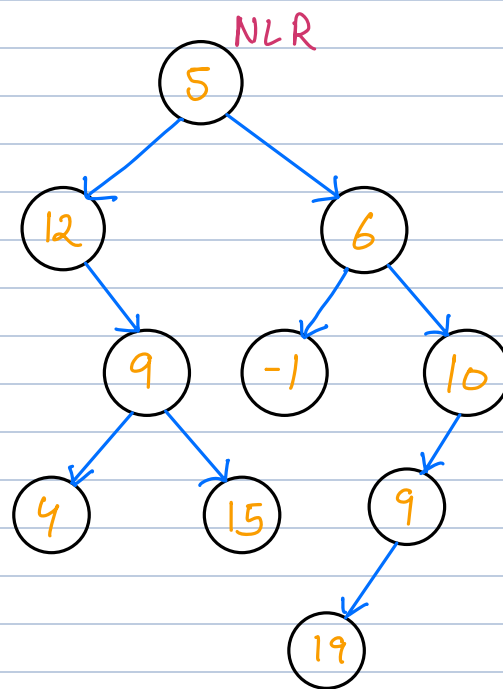
Preorder Traversal

N L R
Node Left Right.

output : 5, 12, 9, 4, 15,
6, -1, 10, 9, 19

```
void preorder (Node node)
{
    if (node == Null)
        return;

    print (node.data);
    preorder (node.left);
    preorder (node.right);
}
```



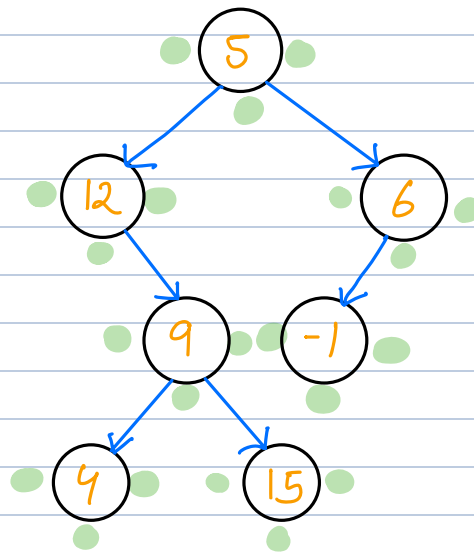
Post order :

L R N
Left Right Node

Preorder : 5, 12, 9, 4, 15, 6, -1

Inorder : 12, 4, 9, 15, 5, -1, 6

Postorder : 4, 15, 9, 12, -1, 6, 5



```
void postorder (Node node)
```

```
{
    if (node == Null)
        return;
```

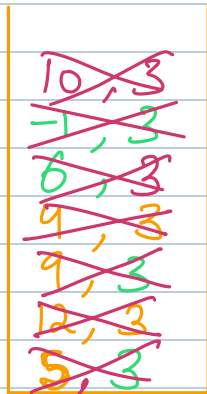
```
    postorder (node.left);
```

```
    postorder (node.right);
```

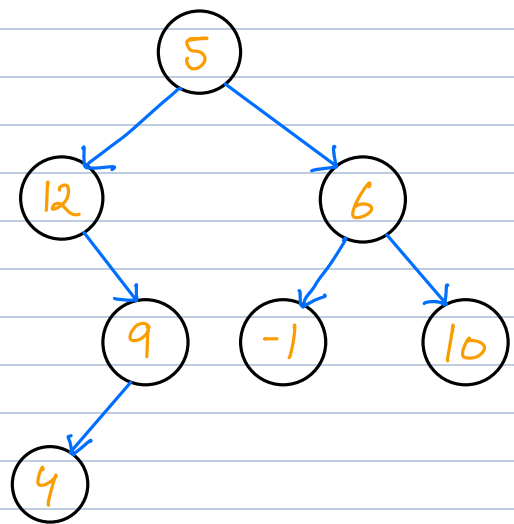
```
    print (node.data);
}
```

Inorder Traversal using iteration.

1. Call left child
2. Print Data
3. Call Right child
4. Go to the parent Node



```
class pair {
    Node node;
    int state;
}
```



Step 1: put root in stack.

Step 2: Perform operations acc to states till stack is empty.

output: 12, 4, 9, 5, -1, 6, 10

States :

0 - Go towards left

1 - Print Node

2 - Go towards right

3 - Pop the Node.

```
fn { iterative_inorder (Node root)
```

```
    stack <pair> st;
```

```
    p = pair (root, 0);
```

```
    st.push (p);
```

```
    while (st.size != 0)
```

```
    {
        top-p = st.peek();
```

```
        if (top-p.state == 0)
```

```
        {
            if (top-p.node.left != Null)
```

```
                Tp = pair (top-p.node.left, 0);
```

```
                st.push (Tp);
```

```
            }
        }
```

```
        else if (top-p.state == 1)
```

```
        {
            print (top-p.node.data);
```

```
        else if (top-p.state == 2)
```

```
        {
            if (top-p.node.right != Null)
```

```
                Tp = pair (top-p.node.right, 0);
```

```
                st.push (Tp);
```

```
            }
        }
```

```
        else # state == 3
```

```
        {
            st.pop();
```

```
            continue;
```

```
        }
```

```
    }
    top-p.state ++;
```

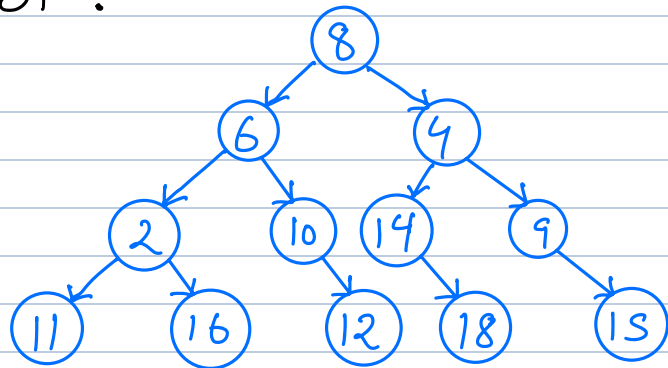
TC: $\Theta(N)$

SC: $\Theta(\text{height of the tree})$

→ This is done for
states 0, 1, 2

Break: 10:44 - 10:54

Q. Given preorder[] & inorder[] of Binary Tree with distinct values
Construct BT.



pre: [8, 6, 2, 11, 16, 10, 12, 4, 14, 18, 9, 15]

Annotations: ps points to 8, LST is underlined from 6 to 12, ps+LST points to 12, RST is above the tree, pe points to 15.

in: [11, 2, 16, 6, 10, 12, 8, 14, 18, 4, 9, 15]

Annotations: is points to 11, LST is underlined from 11 to 12, root idx points to 8, RST is underlined from 14 to 15, ie points to 15.

1. Use pre order to find root node b/w ps & pe
2. Search for root node in inorder b/w is & ie
3. Count elements in LST in inorder
4. Create division based on this Count.

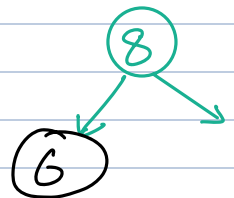
In { create-Tree (pre[], ps, pe, in[], is, ie)

if (ps > pe)
return Null;

int root-data = pre[ps];

Node node = Node (root-data)

root-idx = In.search (root-data)



```
int LST = root-idx - is;
```

```
node.left = create-tree(pre, ps+1, ps+LST, in, is, root-idx-1);
```

```
node.right = create-tree(pre, ps+LST+1, pe, in, root-idx+1, ie);
```

```
return node;
```

priority queue \rightarrow $\langle \text{data}, \text{int} \rightarrow \text{priority} \rangle$