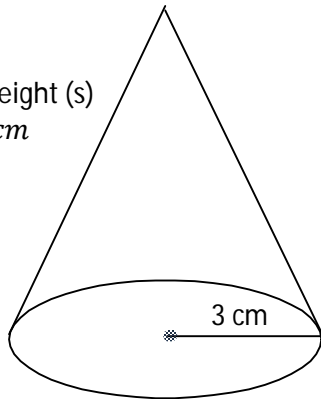


M10 - 2.2 - Cone/Square Pyramid Surface Area Notes

Cone

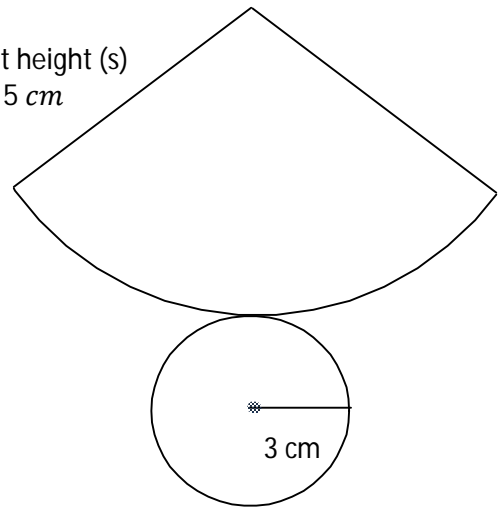
Slant height (s)
 $s = 5 \text{ cm}$



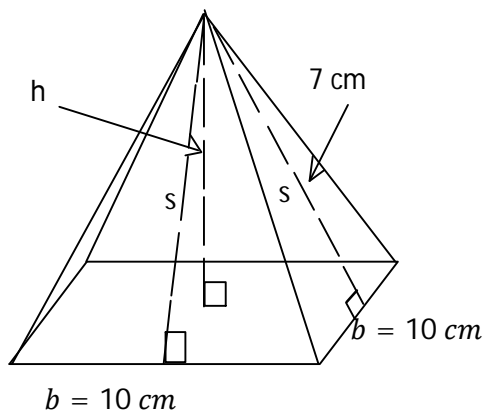
$$\begin{aligned} SA &= \pi r^2 + \pi rs \\ SA &= (3.14)(3)^2 + (3.14)(3)(5) \\ SA &= 28.27 + 47.12 \\ SA &= 75.40 \text{ cm}^2 \end{aligned}$$

Net Area

Slant height (s)
 $s = 5 \text{ cm}$



Square Based Pyramid



Method 1

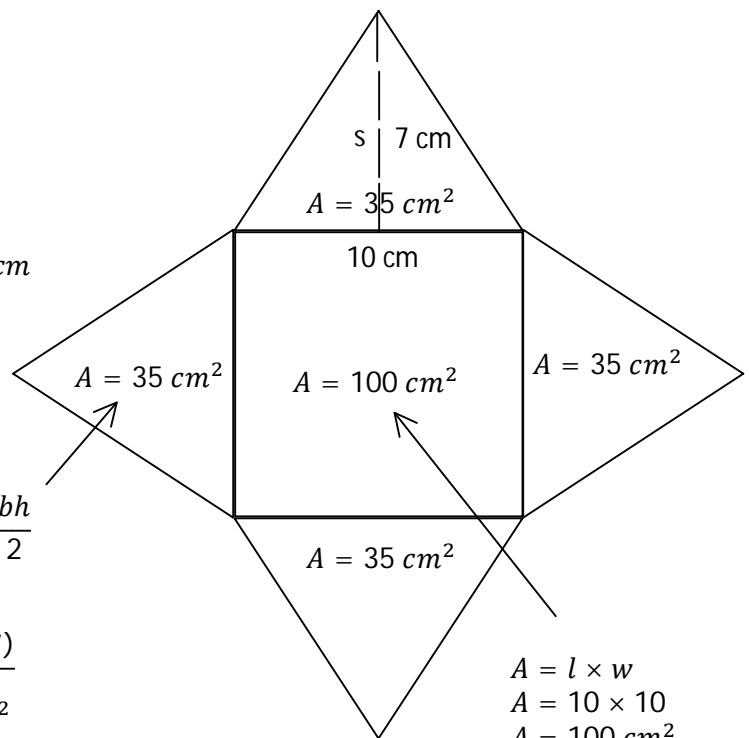
$$\begin{aligned} SA &= 35 + 35 + 35 + 35 + 100 \\ SA &= 240 \text{ cm}^2 \end{aligned}$$

Method 2

$$\begin{aligned} SA &= 2bs + b^2 \\ SA &= 2(10)(7) + (10)^2 \\ SA &= 140 + 100 \\ SA &= 240 \text{ cm}^2 \end{aligned}$$

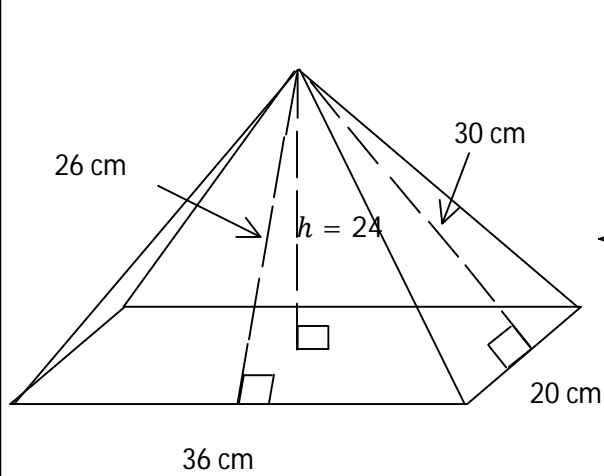
$$A = \frac{bh}{2}$$

$$\begin{aligned} A &= \frac{(10)(7)}{2} \\ A &= 35 \text{ cm}^2 \end{aligned}$$



$$\begin{aligned} A &= l \times w \\ A &= 10 \times 10 \\ A &= 100 \text{ cm}^2 \end{aligned}$$

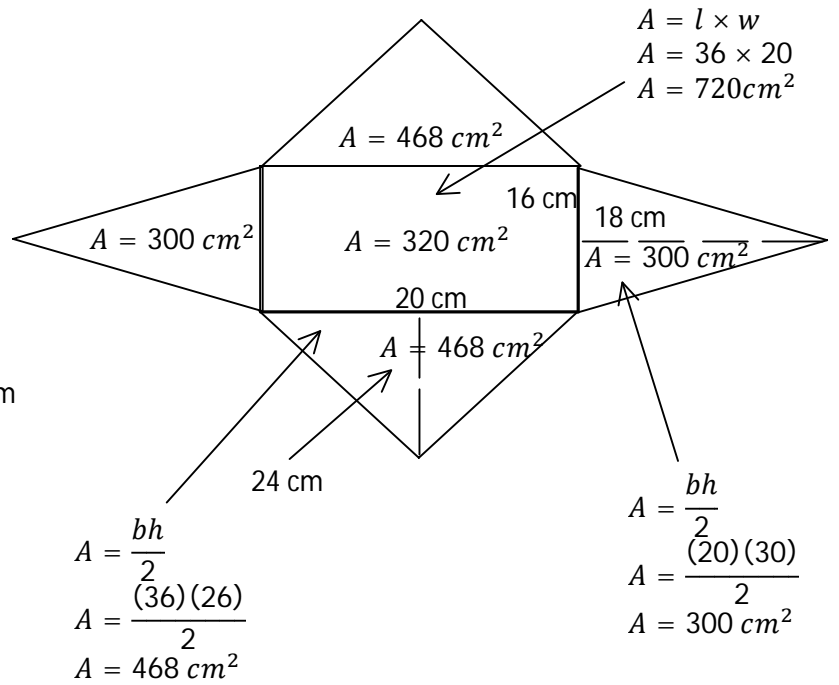
M10 - 2.2 - Rectangular Pyramid/Sphere Surface Area Notes



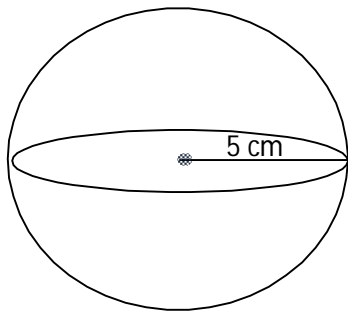
$$SA = 300 + 300 + 468 + 468 + 720$$

$$SA = 600 + 936 + 720$$

$$SA = 2256 \text{ cm}^2$$



Sphere



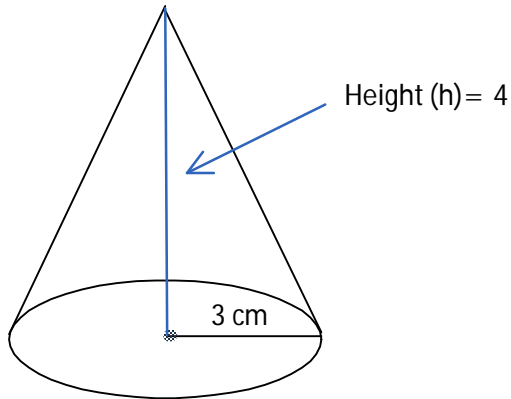
$$SA = 4\pi r^2$$

$$SA = 4(3.14)(5)^2$$

$$SA = 314 \text{ cm}^2$$

M10 - 2.2 - Surface Area of Cone Pythagoras Notes

Cone



$$SA = \pi r^2 + \pi r s$$

$$r = 3$$
$$s = ?$$

$$c^2 = a^2 + b^2$$

$$s^2 = 3^2 + 4^2$$

$$s^2 = 9 + 16$$

$$s^2 = 25$$

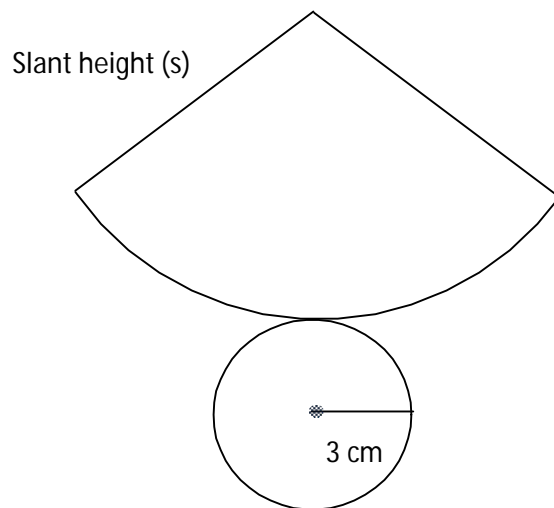
$$s = \sqrt{25}$$

$$s = 5$$

$$r = 3$$

$$s = 5$$

Net Area



Step 2: Determine the Surface Area of the Cone.

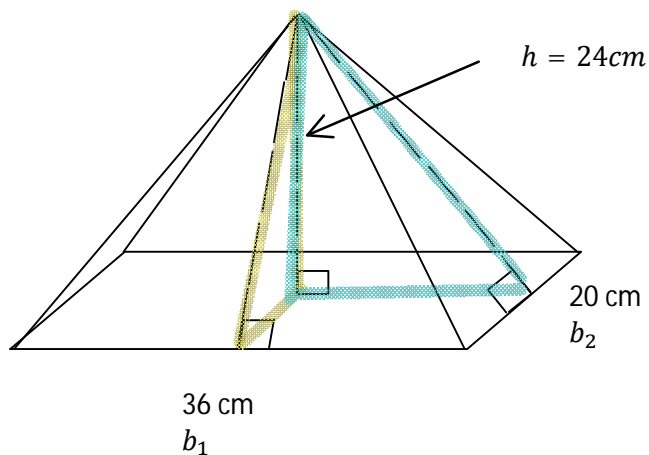
$$SA = \pi r^2 + \pi r s$$

$$SA = \pi(3)^2 + \pi(3)(5)$$

$$SA = 9\pi + 15\pi$$

$$SA = 24\pi \text{ cm}^2$$

M10 - 2.2 - Surface Area of a Rectangular Pyramid Pythagoras Notes



$$SA = \text{Area of Triangles} + \text{Area of Base}$$

$$SA = 2 \times \frac{b_1 s_1}{2} + 2 \times \frac{b_2 s_2}{2} + b_1 b_2$$

$$SA = b_1 s_1 + b_2 s_2 + b_1 b_2$$

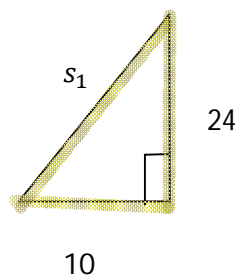
$$b_1 = 36$$

$$s_1 = ?$$

$$b_2 = 20$$

$$s_2 = ?$$

Step 1: Solve for s_1 using the Pythagorean Thm:

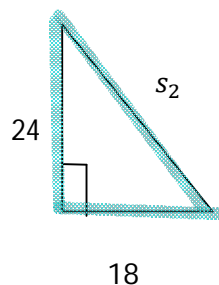


$$(s_1)^2 = 10^2 + 24^2$$

$$(s_1)^2 = 676$$

$$s_1 = 26$$

Step 2: Solve for s_2 using the Pythagorean Thm:



$$(s_2)^2 = 18^2 + 24^2$$

$$(s_2)^2 = 900$$

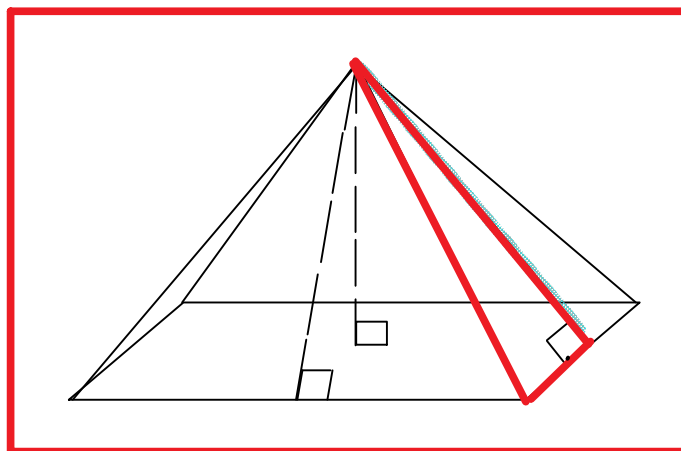
$$s_2 = 30$$

Step 3: Find the Surface Area

$$SA = b_1 s_1 + b_2 s_2 + b_1 b_2$$

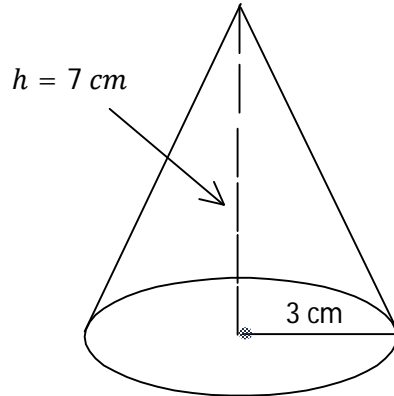
$$SA = (36)(26) + (20)(30) + (36)(20)$$

$$SA = 2256\text{cm}^2$$



M10 - 2.3 - Cone/Sphere Volume Notes

Cone



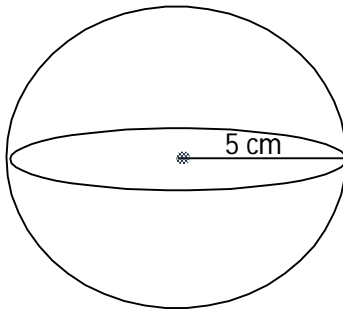
$$V = \frac{1}{3} \times (\text{area of base}) \times h$$

$$V = \frac{1}{3} \times (\pi r^2) \times h$$

$$V = \frac{1}{3} \times ((3.14)(3)^2) \times 7$$

$$V = 66.0\text{ cm}^3$$

Sphere



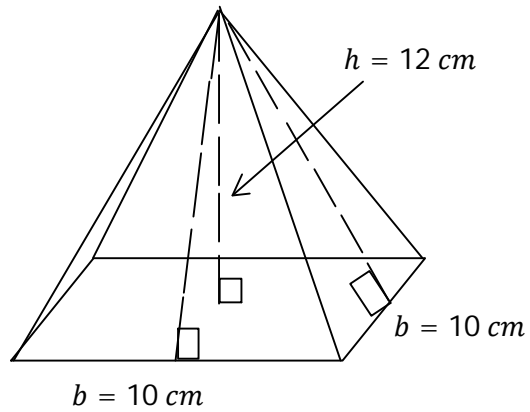
$$V = \frac{4}{3} \pi r^3$$

$$V = \frac{4}{3} (3.14)(5)^3$$

$$V = 523.6\text{ cm}^3$$

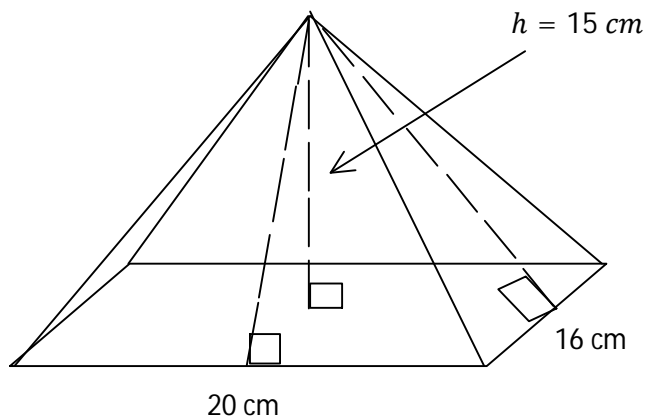
M10 - 2.3 - Pyramid Volume Notes

Square Based Pyramid



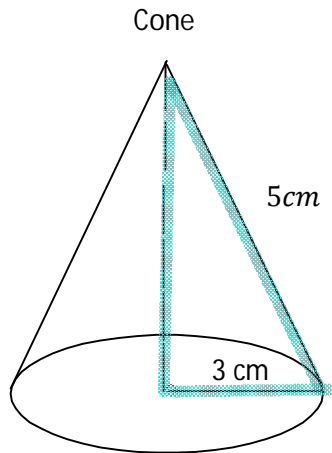
$$\begin{aligned}V &= \frac{1}{3} \times (\text{area of base}) \times h \\V &= \frac{1}{3} \times (l \times w) \times h \\V &= \frac{1}{3} \times (10 \times 10) \times 12 \\V &= 400\text{ cm}^3\end{aligned}$$

Rectangular Based Pyramid



$$\begin{aligned}V &= \frac{1}{3} \times (\text{area of base}) \times h \\V &= \frac{1}{3} \times (l \times w) \times h \\V &= \frac{1}{3} \times (20 \times 16) \times 15 \\V &= 1600\text{ cm}^3\end{aligned}$$

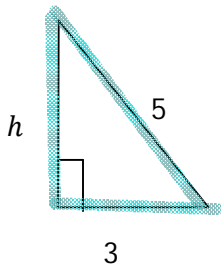
M10 - 2.3 - Cone Volume Pythagoras Notes



$$V = \frac{1}{3} \times (\text{area of base}) \times h$$
$$V = \frac{1}{3} \times (\pi r^2) \times h$$

$$r = 3$$
$$h = ?$$

Step 1: Find h using the Pythagorean Thm.



$$5^2 = 3^2 + h^2$$
$$5^2 - 3^2 = h^2$$
$$h^2 = 5^2 - 3^2$$
$$h^2 = 16$$
$$h = \sqrt{16}$$
$$h = 4$$

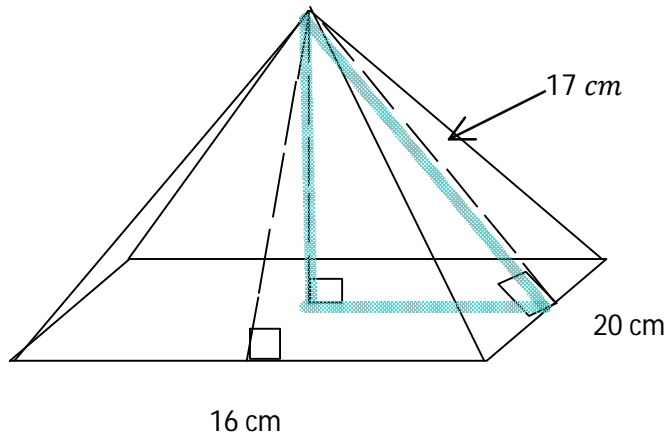
Step 2: Solve the volume.

$$V = \frac{1}{3} \times (\pi(3)^2) \times 4$$

$$\boxed{V = 12\pi \text{ cm}^3}$$

M10 - 2.3 - Pyramid Volume Pythagoras Notes

Rectangular Based Pyramid

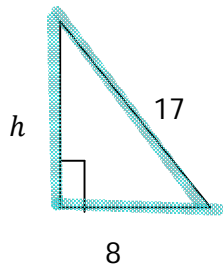


$$V = \frac{1}{3} \times (\text{area of base}) \times h$$

$$V = \frac{1}{3} \times (l \times w) \times h$$

$$\begin{aligned} l &= 20\text{cm} \\ w &= 16\text{cm} \\ h &=? \end{aligned}$$

Step 1: Solve for the height, h , of the pyramid using the Pythagorean Thm.



$$\begin{aligned} 17^2 &= 8^2 + h^2 \\ 17^2 - 8^2 &= h^2 \\ h^2 &= 17^2 - 8^2 \\ h^2 &= 225 \\ h &= \sqrt{225} \\ h &= 15 \end{aligned}$$

Step 2: Find the Volume.

$$V = \frac{1}{3} \times 20 \times 16 \times 15$$

$$\boxed{V = 1600\text{cm}^3}$$