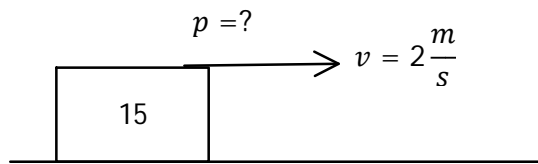


# P11 - 5.1 - Momentum

What is the momentum of a 15kg object moving at  $2 \frac{m}{s}$ .



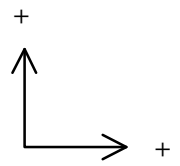
$$p = mv$$

$$p = 15 \times 2$$

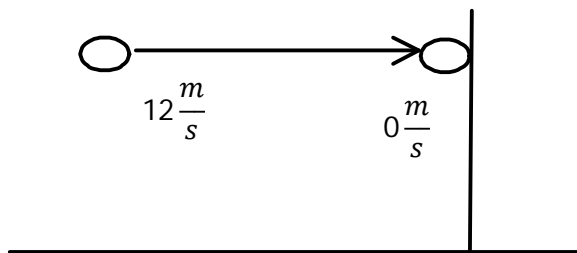
$$p = 30 \frac{kgm}{s}$$

$$p = mv$$

$$\frac{kgm}{s} = Ns$$



A 1kg Snowball with a Velocity of  $12 \frac{m}{s}$  is thrown directly at a wall where it comes to a complete stop. What is the Snowball's Change in Momentum,  $\Delta p$  (Impulse).



$$\Delta p = m\Delta v$$

$$\Delta p = m(v_f - v_i)$$

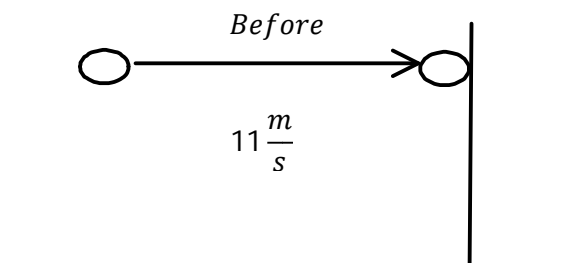
$$\Delta p = 1(0 - 12)$$

$$\Delta p = m\Delta v$$

$$\Delta p = -12 \frac{kgm}{s}$$

Notice the  $\Delta p$  is Negative.

A 2kg Basketball with a Velocity of  $11 \frac{m}{s}$  is thrown directly at a Wall where bounces off the Wall at  $8 \frac{m}{s}$ . What is the Snowball's Change in Momentum,  $\Delta p$  (Impulse).



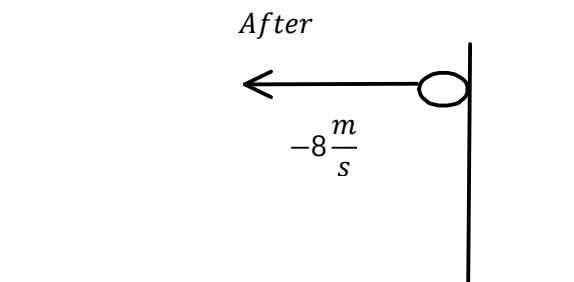
$$\Delta p = m\Delta v$$

$$\Delta p = m(v_f - v_i)$$

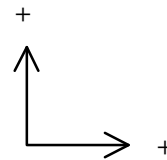
$$\Delta p = 2(-8 - (11))$$

$$\Delta p = m\Delta v$$

$$\Delta p = -38 \frac{kgm}{s}$$



# P11 - 5.2 - Momentum Notes



A 0.1kg piece of Gum is thrown directly at a wall at  $5 \frac{m}{s}$  where it sticks to the wall and smushes in 0.2s. What is the Net Force exerted on the Wall by the Gum.

$$\begin{aligned}\Delta p &= F_{net}t \\ m\Delta v &= F_{net}t \\ F_{net} &= \frac{m\Delta v}{t} \\ F_{net} &= \frac{0.1 \times (0 - 5)}{0.2} \quad \Delta v = v_f - v_i\end{aligned}$$

$$F_{net} = -2.5 \text{ N}$$

$$\begin{aligned}F_{net} &= ma \\ F_{net} &= m \frac{\Delta v}{t} \\ F_{net} \times t &= m\Delta v \\ F_{net}t &= \Delta p\end{aligned}$$

$$a = \frac{\Delta v}{t}$$

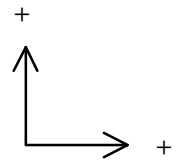
$$\Delta p = F_{net}t$$

A Pitcher throws a 0.15 kg Ball at a Velocity of  $21 \frac{m}{s}$  directly at a Catcher who Stops the Ball exerting a Force of 25 N on the Ball. How long does it take the ball to stop?

$$\begin{aligned}\Delta p &= F_{net}t \\ m\Delta v &= F_{net}t \\ t &= \frac{m\Delta v}{F_{net}} \\ t &= \frac{0.15 \times (0 - 21)}{-25}\end{aligned}$$

$$t = 0.126 \text{ s}$$

# P11 - 5.3 - Conservation of Momentum Notes

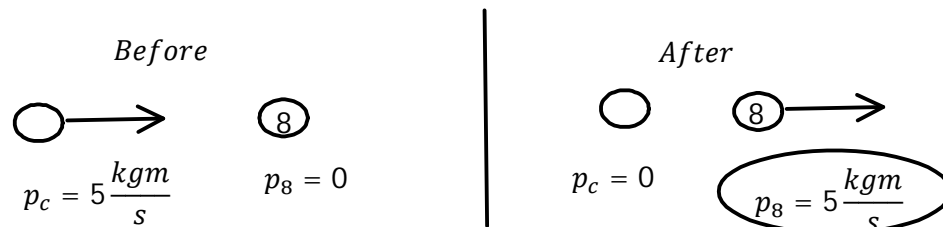


*The Law of the Conservation of Momentum: Momentum must be conserved!*

A Pool Player shoots the Cue Ball with a Momentum of  $5 \frac{\text{kgm}}{\text{s}}$  at the Eight Ball at Rest. The Cue Ball comes to a complete Stop, the Eight ball will continue with a Momentum of  $5 \frac{\text{kgm}}{\text{s}}$ .

What is the Change in Momentum on the Cue Ball?

What is the Change in Momentum of the Eight Ball?



$$\Delta p_c = p_{fc} - p_{ic}$$

$$\Delta p_c = 0 - 5$$

$$\Delta p_c = -5 \frac{\text{kgm}}{\text{s}}$$

$$\Delta p_8 = p_{f8} - p_{i8}$$

$$\Delta p_8 = 5 - 0$$

$$\Delta p_8 = 5 \frac{\text{kgm}}{\text{s}}$$

$$\Delta p_c = \Delta p_8$$

$$p_{fc} - p_{ic} = p_{f8} - p_{i8}$$

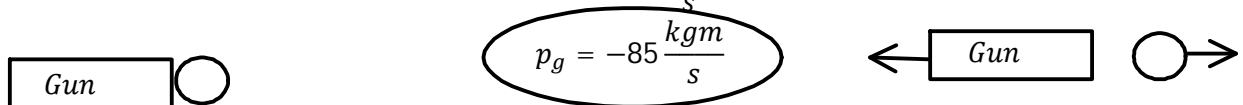
$$0 - 5 = 5 - 0$$

$$5 \frac{\text{kgm}}{\text{s}} = -5 \frac{\text{kgm}}{\text{s}}$$

Equal and Opposite

Momentum Before = Momentum After

A Bullet is fired from a Gun with a momentum of  $85 \frac{\text{kgm}}{\text{s}}$ . What is the recoil Momentum of the Gun.



$$\Delta p_g = \Delta p_b$$

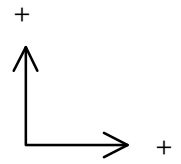
$$p_{fg} - p_{ig} = p_{fb} - p_{ib}$$

$$p_{fg} - 0 = 0 - 85$$

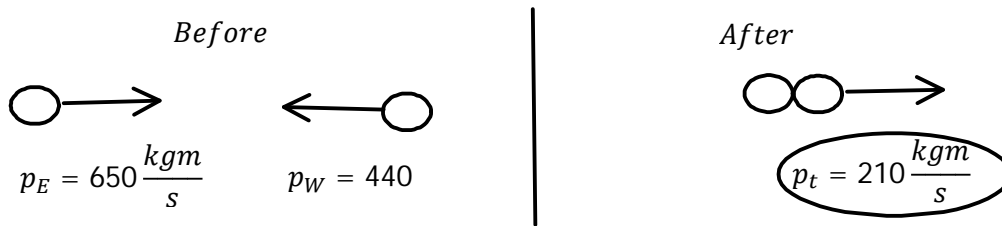
$$p_{fg} = -85 \frac{\text{kgm}}{\text{s}}$$

Momentum Left = Momentum Right

# P11 - 5.3 - Conservation of Momentum Notes



A Hockey Player with a Momentum of  $650 \text{ N East}$ , collides with a Hockey Player with a Momentum of  $440 \text{ N East}$ . If they Stick together, What is their Final Momentum?

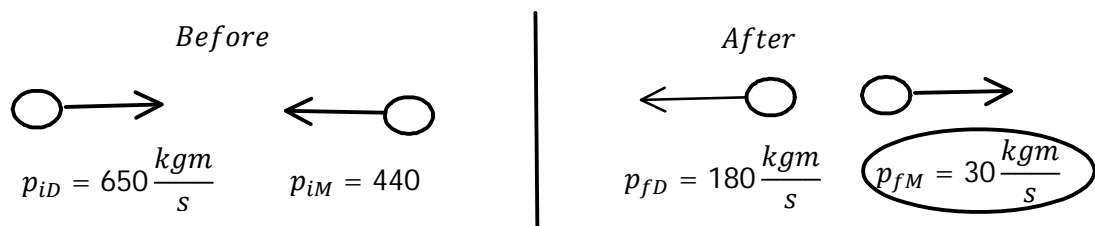


$$\begin{aligned}\Delta p_b &= \Delta p_t \\ p_{fb} - p_{wb} &= p_{ta} \\ 650 - 440 &= p_{ta}\end{aligned}$$

$$p_{ta} = 210 \text{ N East}$$

Momentum Before = Momentum After

A Hockey Player Doug with a Momentum of  $650 \text{ N East}$ , collides with a Hockey Player Mike with a Momentum of  $440 \text{ N East}$ . If they Bounce off each other, and Doug's Final Momentum is  $180 \frac{\text{kgm}}{\text{s}}$ , What is Mike's Final Momentum?



$$\begin{aligned}p_{iD} + p_{iM} &= p_{fD} + p_{fM} \\ 650 - 440 &= -180 + p_{fM} \\ p_{fM} &= 30 \frac{\text{kgm}}{\text{s}}\end{aligned}$$

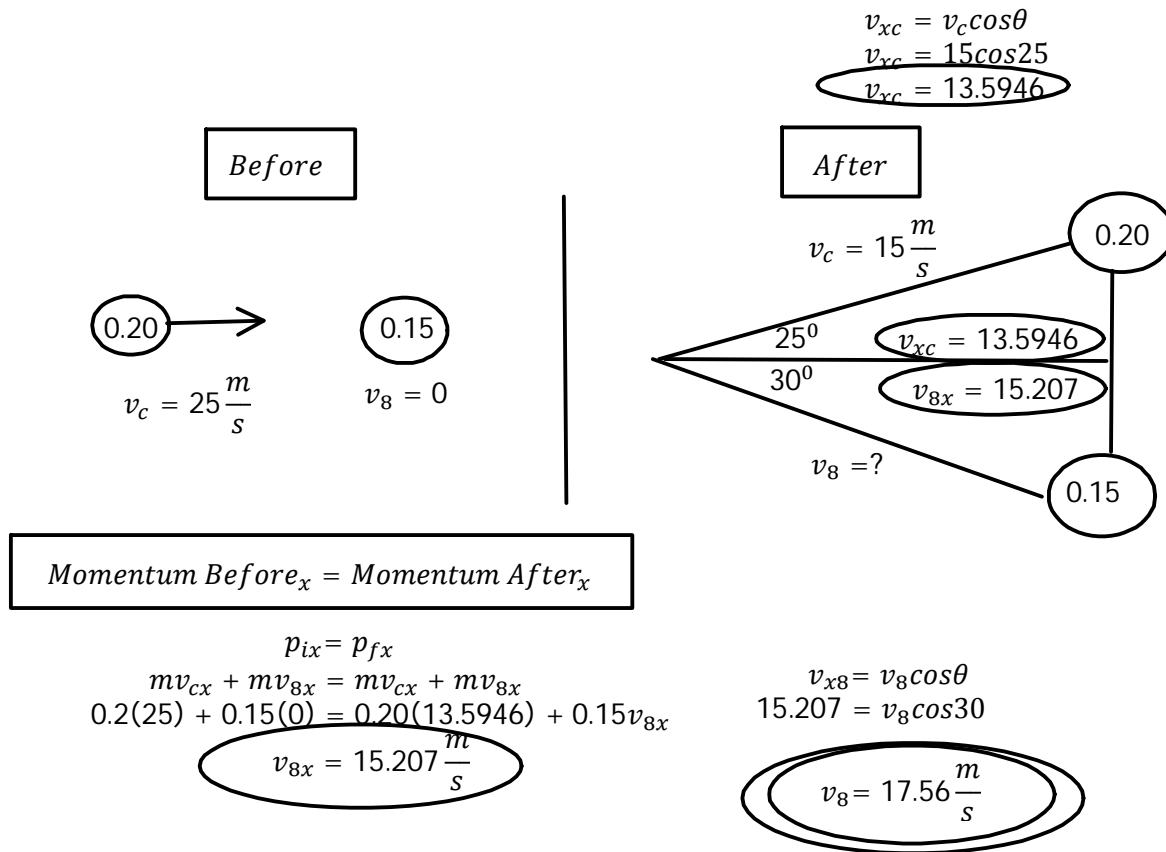
$$p_i = p_f$$

$$p_{1i} + p_{2i} = p_{1f} + p_{2f}$$

$$m_1 v_{1i} + m_2 v_{2i} = m_1 v_{1f} + m_2 v_{2f}$$

# P12 - 5.4 - Momentum Trig Notes

A Pool Player shoots the Cue Ball with a mass of 0.2 kg with a velocity of  $25 \frac{m}{s}$  at the Eight Ball with a mass of 0.15 kg at Rest. The Cue Ball deflects at a velocity of  $15 \frac{m}{s}$  at an angle of  $25^\circ$  above the horizontal and the Eight ball deflects at an angle of  $30^\circ$  below the horizontal. What is the velocity of the Eight ball.



# P12 - 5.4 - Momentum Trig Notes

A Pool Player shoots the Cue Ball with a mass of 0.2 kg with a velocity of  $25 \frac{m}{s}$  at the Eight Ball with a mass of 0.15 kg at Rest. The Cue Ball deflects at a velocity of  $15 \frac{m}{s}$  at an angle of  $25^\circ$  above the horizontal and the Eight ball deflects at an angle below the horizontal. What is the resultant velocity and direction of the Eight ball.

**Before**

$v_c = 25 \frac{m}{s}$   
 $v_8 = 0$

**After**

$v_c = 15 \frac{m}{s}$   
 $25^\circ$   
 $\theta$   
 $v_8 = ?$

$v_{xc} = v_c \cos \theta$   
 $v_{yc} = v_c \sin \theta$   
 $v_{xc} = 15 \cos 25$   
 $v_{xc} = 13.5946$   
 $v_{yc} = 15 \sin 25$   
 $v_{yc} = 6.339$

$p_{ix} = p_{fx}$   
 $mv_{cx} + mv_{8x} = mv_{cx} + mv_{8x}$   
 $0.2(25) + 0.15(0) = 0.20(13.5946) + 0.15v_{8x}$   
 $v_{8x} = 15.207 \frac{m}{s}$

$v_{x8} = v_8 \cos \theta$   
 $15.207 = v_8 \cos \theta$   
 $v_8 = \frac{15.207}{\cos \theta}$

$v_{y8} = v_8 \sin \theta$   
 $v_{y8} = \left( \frac{15.207}{\cos \theta} \right) \sin \theta$   
 $v_{y8} = 15.207 \tan \theta$

**Momentum Up = Momentum Down**  
 $p_{cy} = p_{8y}$   
 $mv = mv$   
 $0.2(6.339) = 0.15(15.207 \tan \theta)$   
 $\tan \theta = 0.5561$   
 $\theta = 28.08^\circ$

$v_8 = \frac{15.207}{\cos \theta}$   
 $v_8 = \frac{15.207}{\cos 28.08^\circ}$   
 $v_8 = 17.24^\circ \frac{m}{s} \text{ } 28.08^\circ \text{ below horizontal. [SoE]}$