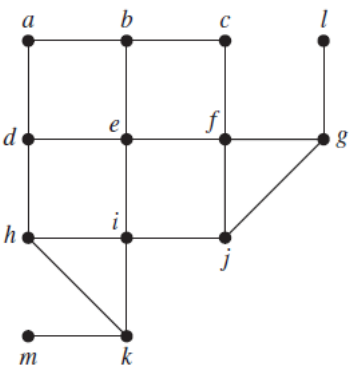


Professionalism

Excellence

Respect

Answer all the questions. The weight of each question is mentioned at the right side. When answering a question, please answer all the subsections of it at once

1.		Prove that every amount of postage of 12 cents or more can be formed using just 4-cent and 5-cent stamps.	6
2.	i)	Suppose that there are 9 faculty members in the mathematics department and 11 in the computer science department. How many ways are there to select a committee to develop a discrete mathematics course at a school if the committee is to consist of three faculty members from the mathematics department and four from the computer science department?	3
	ii)	What is the minimum number of students required to be sure that at least 9 students were born in the same month?	3
3.	i)	What is the composite of the relations R and S , where R is the relation from $\{1, 2, 3\}$ to $\{1, 2, 3, 4\}$ with $R = \{(1, 1), (1, 4), (2, 3), (3, 1), (3, 4)\}$ and S is the relation from $\{1, 2, 3, 4\}$ to $\{0, 1, 2\}$ with $S = \{(1, 0), (2, 0), (3, 1), (3, 2), (4, 1)\}$?	3
	ii)	How many edges are there in a graph with 8 vertices each of degree five?	3
4.	i)	Use Huffman coding to encode these symbols with given frequencies: a : 0.20, b : 0.10, c : 0.15, d : 0.25, e : 0.30. What is the average number of bits required to encode a character?	3
	ii)	<p>ii. Use breadth-first search, starting from node “e”, to find a spanning tree for the graph given below. Show the steps with graphs, no text is required to answer this question.</p> 	3
5.		Devise a recursive algorithm for computing $b^n \bmod m$, where b , n , and m are integers with $m \geq 2$, $n \geq 0$, and $1 \leq b < m$.	6
		Best of Luck!!!	