Homework 4 - Week 4

Akylas Stratigakos 12 Jun 2018

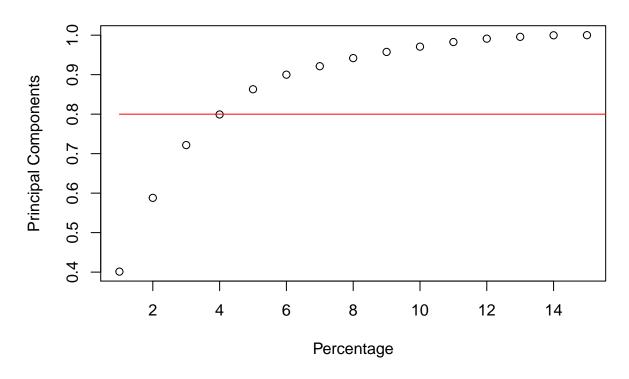
Question 9.1

lines(Threshold, type="l", col="red")

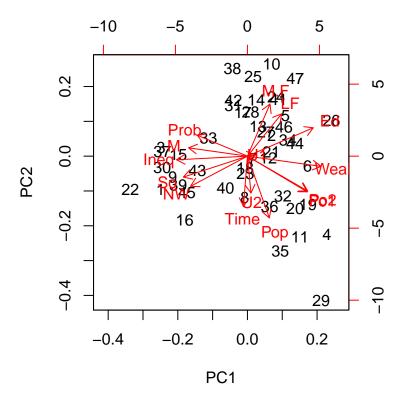
In this task a linear regression model will be applied on the "uscrime" data, after reducing the dimensions of the predictors via Principal Component Analysis. Besides dimensionality reduction, PCA will also ensure no colinearity between the predictors. First, I will apply PCA on the dataset (without the response collumn, i.e. crime). In order to select a reasonable number of PCs, I plot the cumulative variance explained by the PCs (which depends on the eigenvalues of each component), and will select a number that explains around 80% of the total variance in the predictors.

```
datapath=paste("C:/Users/a.stratigakos/Desktop/edx/Introduction to Analytics Modelling"
               ,"/Week 2/UScrime_data.txt",sep="")
uscrime<-(read.table(datapath,header =TRUE))</pre>
#PCA without the response variable
PC=prcomp(uscrime[,-16], center = TRUE, scale. = TRUE)
summary(PC)
Importance of components:
                                        PC3
                                                 PC4
                          PC1
                                 PC2
                                                         PC5
                                                                 PC6
Standard deviation
                       2.4534 1.6739 1.4160 1.07806 0.97893 0.74377
Proportion of Variance 0.4013 0.1868 0.1337 0.07748 0.06389 0.03688
Cumulative Proportion 0.4013 0.5880 0.7217 0.79920 0.86308 0.89996
                           PC7
                                   PC8
                                           PC9
                                                  PC10
                                                           PC11
Standard deviation
                       0.56729 0.55444 0.48493 0.44708 0.41915 0.35804
Proportion of Variance 0.02145 0.02049 0.01568 0.01333 0.01171 0.00855
Cumulative Proportion 0.92142 0.94191 0.95759 0.97091 0.98263 0.99117
                          PC13
                                 PC14
                                         PC15
Standard deviation
                       0.26333 0.2418 0.06793
Proportion of Variance 0.00462 0.0039 0.00031
Cumulative Proportion 0.99579 0.9997 1.00000
Threshold=matrix(0.8,nrow=16)
VarExpl=cumsum((PC$sdev)^2)/sum(PC$sdev^2)
plot(VarExpl,main='Cumulative Proportion of variance explained',
     ylab='Principal Components',
     xlab="Percentage")
```

Cumulative Proportion of variance explained



biplot(PC,choices = 1:2,scale = 1)



PCcoeff=PC\$rotation scores=PC\$x

As can be seen above, the first 4 Components explain around 80% of the variance, so I'll select them as the predictors. Additionally, the biplot of the first 2 PCs is shown, which shows the **coefficients** (eigenvectors or weights) of each variable and it's usefull for qualitatevely analysis. Afterwards, I proceed with applying a linear regression using the Crime collumn as response and the **scores** (i.e. original data points projected on the new dimensions) as the predictors. This methodology will be referred to as "PCA regression".

```
Crime=uscrime[,16];Sc1=scores[,1];Sc2=scores[,2]
Sc3=scores[,3];Sc4=scores[,4]
PCdf=data.frame(Crime,Sc1,Sc2,Sc3,Sc4)
PCmodel=lm(Crime~.,data=PCdf)
summary(PCmodel)
```

Call:

lm(formula = Crime ~ ., data = PCdf)

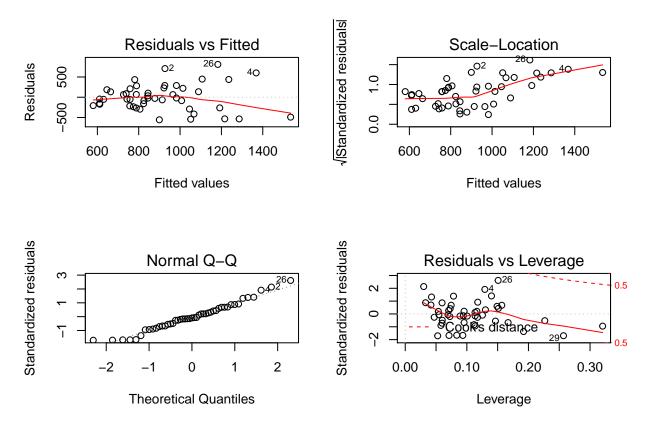
Residuals:

Min 1Q Median 3Q Max -557.76 -210.91 -29.08 197.26 810.35

Coefficients:

Estimate Std. Error t value Pr(>|t|)
(Intercept) 905.09 49.07 18.443 < 2e-16 ***
Sc1 65.22 20.22 3.225 0.00244 **

```
Sc2
              -70.08
                          29.63
                                 -2.365
                                         0.02273 *
Sc3
               25.19
                          35.03
                                  0.719
                                         0.47602
Sc4
               69.45
                          46.01
                                  1.509
                                         0.13872
Signif. codes:
                        0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 336.4 on 42 degrees of freedom
Multiple R-squared: 0.3091,
                                Adjusted R-squared: 0.2433
F-statistic: 4.698 on 4 and 42 DF, p-value: 0.003178
layout(matrix(c(1,2,3,4),2,2)) # optional 4 graphs/page
plot(PCmodel)
```



a=summary(PCmodel)\$coefficients
Rsq=summary(PCmodel)\$r.squared
adRsq=summary(PCmodel)\$adj.r.squared
Fstat=summary(PCmodel)\$fstatistic

Above we can see some diagnostics about the PCA regression such as F-statistic, R squared and adjusted R square. Since PCA is a linear combination of the original dataset, the PCA regression will be also be this transformation multiplied by the regression's coefficients, which in turn results again in a linear combination of the original variables. Note the variables **scaled**. Due to space limitations I will only show the first coefficient and first Principal Component in the equation:

```
Y = 905.0851064 + 65.2159301 * X_{np} * \begin{pmatrix} -0.3037119 \\ -0.3308813 \\ 0.3396215 \\ 0.3086341 \\ 0.3109929 \\ 0.1761776 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3037119 \\ -0.3
```

where:

$$X = (M \ So \ Ed \ Pol \ \dots \ Ineq \ Prob \ Time)$$

I also fitted a simple linear regression model, with the whole dataset as a predictor and plotted the diagnostics. Afterwards I used the two models to make a prediction based on the new datapoint given in Question 8.2. Note that in order to make a prediction with the PCA regression I need to map the new data point into the Principal Components. After **scaling** them, I use matrix multiplication with the corresponding eigenvectors (coefficients), and then use them for prediction.

```
#Simple linear reg
fit <- lm( Crime~., data=uscrime)
summary(fit)</pre>
```

Call:

lm(formula = Crime ~ ., data = uscrime)

Residuals:

Min 1Q Median 3Q Max -395.74 -98.09 -6.69 112.99 512.67

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept) -5.984e+03
                                   -3.675 0.000893 ***
                       1.628e+03
М
             8.783e+01
                        4.171e+01
                                    2.106 0.043443 *
So
            -3.803e+00
                       1.488e+02
                                  -0.026 0.979765
Ed
             1.883e+02 6.209e+01
                                    3.033 0.004861 **
                       1.061e+02
                                    1.817 0.078892 .
Po1
             1.928e+02
            -1.094e+02 1.175e+02
                                   -0.931 0.358830
Po2
            -6.638e+02 1.470e+03
LF
                                  -0.452 0.654654
             1.741e+01 2.035e+01
M.F
                                    0.855 0.398995
            -7.330e-01 1.290e+00
                                   -0.568 0.573845
Pop
NW
             4.204e+00
                        6.481e+00
                                    0.649 0.521279
U1
            -5.827e+03 4.210e+03
                                  -1.384 0.176238
U2
             1.678e+02 8.234e+01
                                    2.038 0.050161 .
```

```
Wealth
            9.617e-02 1.037e-01
                                    0.928 0.360754
Ineq
            7.067e+01 2.272e+01 3.111 0.003983 **
Prob
            -4.855e+03 2.272e+03 -2.137 0.040627 *
            -3.479e+00 7.165e+00 -0.486 0.630708
Time
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Residual standard error: 209.1 on 31 degrees of freedom
Multiple R-squared: 0.8031,
                              Adjusted R-squared: 0.7078
F-statistic: 8.429 on 15 and 31 DF, p-value: 3.539e-07
lmRsq=summary(fit)$r.squared
lmadRsq=summary(fit)$adj.r.squared
lmFstat=summary(fit)$fstatistic;
#Predict
M = 14.0; So = 0; Ed = 10.0; Po1 = 12.0; Po2 = 15.5; LF = 0.640
M.F = 94.0; Pop = 150; NW = 1.1; U1 = 0.120; U2 = 3.6; Wealth = 3200
Ineq = 20.1; Prob = 0.04; Time = 39.0
new.df <- data.frame(1,M,So, Ed, Po1, Po2, LF, M.F, Pop, NW, U1, U2, Wealth, Ineq, Prob, Time)
y=matrix(c(M,So, Ed, Po1, Po2, LF, M.F, Pop, NW, U1, U2, Wealth, Ineq, Prob, Time),nrow=1,ncol=15)
#Map data frame into the first 2 PC
newScores=((y-PC$center)/t(PC$scale))%*%PCcoeff[,1:4]
new.PCdf <- data.frame(1,Sc1=newScores[,1],Sc2=newScores[,2],Sc3=newScores[,3],Sc4=newScores[,4])
PCpred=predict(PCmodel, new.PCdf) #Scaling needs fixing
#LM pred
LMpred=predict(fit, new.df)
PCpred
     PC1
1112.678
LMpred
       1
155.4349
```

Question 10.1

In this Question the focus is to find a good model for the "uscrime" data using (a) a regression tree and (b) a random forest, while also provide some qualitative takeaways from analyzing the results.

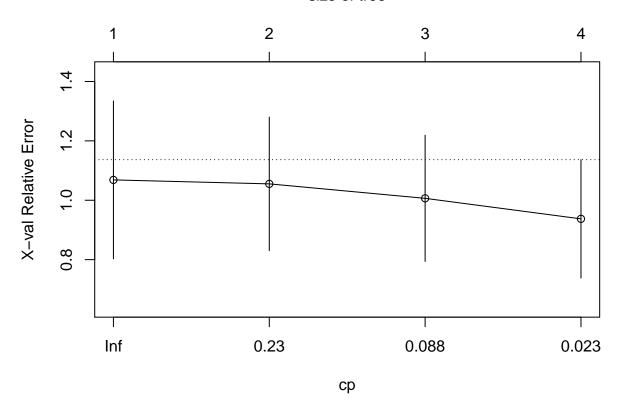
Part a: First, a regression tree model will be fitted in the dataset, by using the standard recursive binary split. For this purpose the **tree** package is utilized.

Root node error: 6880928/47 = 146403

n=47

plotcp(rtree) # visualize cross-validation results

size of tree



summary(rtree) # detailed summary of splits

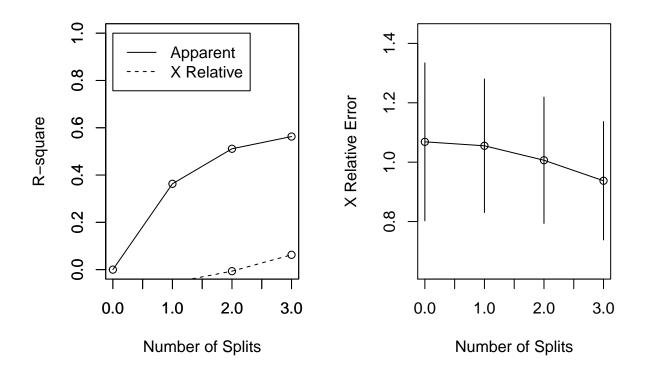
```
Call:
rpart(formula = Crime ~ ., data = uscrime, method = "anova")
 n = 47
          CP nsplit rel error
                                 xerror
1 0.36296293
                  0 1.0000000 1.0685435 0.2659092
                  1 0.6370371 1.0551764 0.2248958
2 0.14814320
                  2 0.4888939 1.0064809 0.2126293
3 0.05173165
4 0.01000000
                  3 0.4371622 0.9373906 0.1992577
Variable importance
   Po1
          Po2 Wealth
                                               NW
                       Ineq
                              Prob
                                         Μ
                                                     Pop
                                                           Time
```

Ed

```
17
           17
                  11
                         11
                                10
                                       10
    I.F
           So
     1
            1
Node number 1: 47 observations,
                                   complexity param=0.3629629
  mean=905.0851, MSE=146402.7
  left son=2 (23 obs) right son=3 (24 obs)
  Primary splits:
      Po1
             < 7.65
                         to the left, improve=0.3629629, (0 missing)
      Po2
             < 7.2
                         to the left, improve=0.3629629, (0 missing)
            < 0.0418485 to the right, improve=0.3217700, (0 missing)
                                       improve=0.2356621, (0 missing)
             < 7.65
                         to the left,
                                       improve=0.2002403, (0 missing)
      Wealth < 6240
                         to the left,
  Surrogate splits:
      Po2
            < 7.2
                         to the left, agree=1.000, adj=1.000, (0 split)
      Wealth < 5330
                         to the left, agree=0.830, adj=0.652, (0 split)
            < 0.043598 to the right, agree=0.809, adj=0.609, (0 split)
      Prob
             < 13.25
                         to the right, agree=0.745, adj=0.478, (0 split)
                         to the right, agree=0.745, adj=0.478, (0 split)
           < 17.15
      Ineq
Node number 2: 23 observations,
                                   complexity param=0.05173165
  mean=669.6087, MSE=33880.15
  left son=4 (12 obs) right son=5 (11 obs)
  Primary splits:
      Pop < 22.5
                                    improve=0.4568043, (0 missing)
                      to the left,
        < 14.5
                      to the left,
                                    improve=0.3931567, (0 missing)
      NW < 5.4
                      to the left,
                                    improve=0.3184074, (0 missing)
      Po1 < 5.75
                                    improve=0.2310098, (0 missing)
                      to the left,
      U1 < 0.093
                      to the right, improve=0.2119062, (0 missing)
  Surrogate splits:
           < 5.4
                       to the left, agree=0.826, adj=0.636, (0 split)
      М
           < 14.5
                       to the left, agree=0.783, adj=0.545, (0 split)
      Time < 22.30055 to the left, agree=0.783, adj=0.545, (0 split)
           < 0.5
                       to the left, agree=0.739, adj=0.455, (0 split)
      So
                      to the right, agree=0.739, adj=0.455, (0 split)
           < 10.85
Node number 3: 24 observations,
                                   complexity param=0.1481432
  mean=1130.75, MSE=150173.4
  left son=6 (10 obs) right son=7 (14 obs)
  Primary splits:
           < 7.65
                       to the left, improve=0.2828293, (0 missing)
      NW
                       to the left, improve=0.2714159, (0 missing)
           < 13.05
                     to the left, improve=0.2060170, (0 missing)
      Time < 21.9001
      M.F < 99.2
                      to the left, improve=0.1703438, (0 missing)
      Po1 < 10.75
                       to the left, improve=0.1659433, (0 missing)
  Surrogate splits:
                       to the right, agree=0.750, adj=0.4, (0 split)
      Ed
         < 11.45
                       to the left, agree=0.750, adj=0.4, (0 split)
      Ineq < 16.25
      Time < 21.9001
                     to the left, agree=0.750, adj=0.4, (0 split)
      Pop < 30
                       to the left, agree=0.708, adj=0.3, (0 split)
      LF
                      to the right, agree=0.667, adj=0.2, (0 split)
           < 0.5885
Node number 4: 12 observations
```

mean=550.5, MSE=20317.58

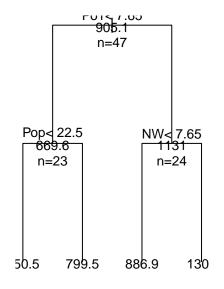
```
Node number 5: 11 observations
 mean=799.5455, MSE=16315.52
Node number 6: 10 observations
 mean=886.9, MSE=55757.49
Node number 7: 14 observations
 mean=1304.929, MSE=144801.8
# create additional plots
par(mfrow=c(1,2)) # two plots on one page
rsq.rpart(rtree) # visualize cross-validation results
Regression tree:
rpart(formula = Crime ~ ., data = uscrime, method = "anova")
Variables actually used in tree construction:
[1] NW Po1 Pop
Root node error: 6880928/47 = 146403
n=47
       CP nsplit rel error xerror
1 0.362963
               0 1.00000 1.06854 0.26591
2 0.148143
                   0.63704 1.05518 0.22490
               1
3 0.051732
              2 0.48889 1.00648 0.21263
4 0.010000
              3 0.43716 0.93739 0.19926
```

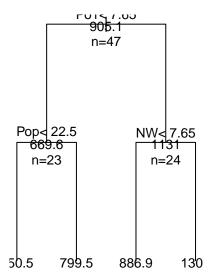


The function automatically selects the regression tree which minimizes the cross-validation error. A variety of diagnostics such as the cross-validation results vs number splits, importance of the variables and the improvement of the model for each split are plotted above. The most important are Police expenditure in 1960, expenditure in 1959, wealth and income inequality. We can plot the regression tree in order to visualize the results better. Additionally, we can prune the tree in order to avoid overfitting the data.

Regression Tree for Crime

Pruned Regression Tree for Crim





The prune method results in the same model as the initial regression. The first split is made for **Police expenditure in 1960**<**7.65**. If this inequality is true, the second split is made for **State Population**<**22.5**, while if its not true we check whether the **Number of non-whites per 1000 people is** <**7.65**. Overall the tree has 3 nodes, and 4 leaves.

Part b: Now we apply a random forest algorithm in the dataset. Generally, random forests improve significantly over the simple regression trees, but they are harder to interpret. The **randomForest** package was used.

IncNodePurity 204293.55 18358.69

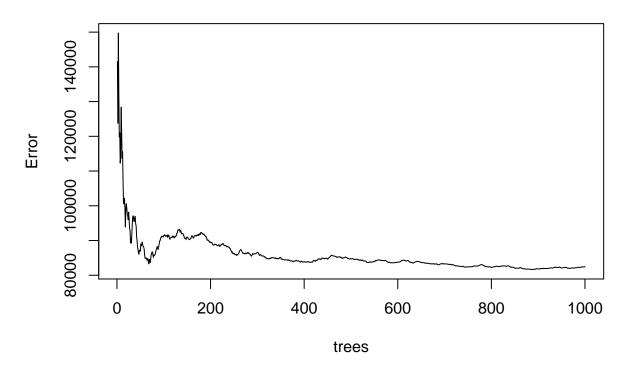
М

So

```
Ed
           258121.29
Po1
           1234820.69
           1072613.32
Po2
LF
           270494.90
M.F
           274824.77
           335363.36
Pop
NW
           536890.06
U1
           138162.18
U2
           175420.12
Wealth
           692032.60
Ineq
           213707.90
Prob
           712482.08
           222096.78
Time
```

plot(rf,main="Random Forest")

Random Forest



In the plot above we can see the relative error vs the number of trees used. For each tree 5 predictors were utilized. The **importance** function shows that the most important variables are Police expenditure in 1960, Police expenditure in 1959, probability of imprisonment and wealth.

Question 10.2

Logistic regression is a go-to method for binary classification problems and for calculating probability of events. For example it could be used to calculate the probability of penalty kick success in soccer. List of predictors could include height of the player, whether he uses right or left foot to shoot the ball, strength of his kick, arm span of the goalkeeper etc.

Question 10.3

Part 1: In this task I'll use a logistic regression in order to find a good predictive model for whether credit applicants are "good" or "bad". I define as positive state in my model the "bad" state. First I'll load the data and do some manipulation in order to produce more presentable results (create binary output by setting "good" as 0 and "bad" as 1). I use a 80/20 split in my dataset, for training and test set. I use the package caret in order to produce the confusion matrix and some helpfull diagnostics, such as accuracy, sensitivity and specificity. I'll also plot some diagnostics of the logistic regression such as z-stat of the coefficients.

```
datapath=paste("C:/Users/a.stratigakos/Desktop/edx/Introduction to Analytics Modelling"
               ,"/Week 4/German credit.txt",sep="")
library(caret)
German credit<-(read.table(datapath,header =TRUE))</pre>
str(German_credit)
'data.frame':
               999 obs. of 21 variables:
$ A11 : Factor w/ 4 levels "A11", "A12", "A13",...: 2 4 1 1 4 4 2 4 2 2 ...
       : int 48 12 42 24 36 24 36 12 30 12 ...
 $ A34 : Factor w/ 5 levels "A30", "A31", "A32", ...: 3 5 3 4 3 3 3 5 3 ...
 $ A43 : Factor w/ 10 levels "A40", "A41", "A410", ...: 5 8 4 1 8 4 2 5 1 1 ...
 $ X1169: int 5951 2096 7882 4870 9055 2835 6948 3059 5234 1295 ...
 $ A65 : Factor w/ 5 levels "A61", "A62", "A63", ...: 1 1 1 1 5 3 1 4 1 1 ...
 $ A75 : Factor w/ 5 levels "A71", "A72", "A73", ...: 3 4 4 3 3 5 3 4 1 2 ...
        : int 2 2 2 3 2 3 2 2 4 3 ...
 $ X4
 $ A93 : Factor w/ 4 levels "A91", "A92", "A93",...: 2 3 3 3 3 3 3 1 4 2 ...
 $ A101 : Factor w/ 3 levels "A101", "A102",...: 1 1 3 1 1 1 1 1 1 1 ...
 $ X4.1: int 2 3 4 4 4 4 2 4 2 1 ...
 $ A121 : Factor w/ 4 levels "A121", "A122",..: 1 1 2 4 4 2 3 1 3 3 ...
 $ X67 : int 22 49 45 53 35 53 35 61 28 25 ...
 $ A143 : Factor w/ 3 levels "A141", "A142", ...: 3 3 3 3 3 3 3 3 3 ...
 $ A152 : Factor w/ 3 levels "A151", "A152",...: 2 2 3 3 3 2 1 2 2 1 ...
 $ X2
       : int 1 1 1 2 1 1 1 1 2 1 ...
 : int 1 2 2 2 2 1 1 1 1 1 ...
 $ A192 : Factor w/ 2 levels "A191", "A192": 1 1 1 1 2 1 2 1 1 1 ...
 $ A201 : Factor w/ 2 levels "A201", "A202": 1 1 1 1 1 1 1 1 1 1 1 ...
 $ X1.1: int 2 1 1 2 1 1 1 1 2 2 ...
Actual<-ifelse(German_credit[,21]==1, "GOOD", "BAD")</pre>
German credit[which(German credit[,21]==1),21]=0
German_credit[which(German_credit[,21]==2),21]=1
                                                 #BAD
spec = c(train = .80, test = .20)
g = sample(cut(seq(nrow(German_credit)), nrow(German_credit)*cumsum(c(0,spec)),labels = names(spec)))
traind=as.data.frame(German credit[g=="train",])
testd=as.data.frame(German_credit[g=="test",])
#transform to X=0 GOOD, X=1 BAD
#Predictive model with logistic regression
logitMod <- glm(X1.1~., data=traind, family=binomial(link="logit"))</pre>
summary(logitMod)
Call:
glm(formula = X1.1 ~ ., family = binomial(link = "logit"), data = traind)
Deviance Residuals:
   Min
             1Q
                  Median
                               3Q
                                       Max
-2.2575 -0.6780 -0.3515
                           0.6963
                                    2.6243
```

Coefficients:

```
Estimate Std. Error z value Pr(>|z|)
(Intercept) 7.630e-01 1.240e+00
                                    0.615 0.538278
A11A12
            -5.980e-01
                        2.492e-01
                                   -2.399 0.016420 *
A11A13
            -1.268e+00 4.339e-01
                                   -2.923 0.003471 **
                        2.667e-01
A11A14
            -1.891e+00
                                   -7.092 1.32e-12 ***
Х6
             2.505e-02 1.053e-02
                                    2.379 0.017337 *
A34A31
             2.680e-01
                        6.256e-01
                                    0.428 0.668424
A34A32
            -5.607e-01
                        5.029e-01
                                   -1.115 0.264931
A34A33
            -4.490e-01
                        5.396e-01
                                   -0.832 0.405387
                                   -2.791 0.005261 **
A34A34
            -1.421e+00
                        5.091e-01
A43A41
            -1.614e+00
                        4.162e-01
                                   -3.878 0.000105 ***
A43A410
            -1.901e+00
                        8.391e-01
                                   -2.265 0.023497 *
                        2.948e-01
                                   -3.289 0.001004 **
A43A42
            -9.697e-01
A43A43
            -1.018e+00
                        2.853e-01
                                   -3.568 0.000359 ***
            -6.799e-01
                        8.065e-01
                                   -0.843 0.399214
A43A44
A43A45
             1.809e-02
                        6.082e-01
                                    0.030 0.976273
                                   -0.604 0.545860
A43A46
            -2.735e-01
                        4.528e-01
A43A48
            -2.080e+00
                        1.306e+00
                                   -1.592 0.111307
A43A49
            -7.535e-01
                        3.797e-01
                                   -1.984 0.047220 *
                        4.969e-05
                                    2.441 0.014627 *
X1169
             1.213e-04
                                   -0.936 0.349359
A65A62
            -2.976e-01
                        3.180e-01
                        4.299e-01
                                   -1.080 0.280094
A65A63
            -4.643e-01
A65A64
            -1.456e+00
                        5.937e-01
                                   -2.453 0.014173 *
A65A65
            -1.097e+00
                        3.108e-01
                                   -3.529 0.000417 ***
                        4.715e-01
                                    0.454 0.650027
A75A72
             2.139e-01
A75A73
             3.307e-01
                        4.481e-01
                                    0.738 0.460518
A75A74
            -5.892e-01
                        4.838e-01
                                   -1.218 0.223213
A75A75
            -8.321e-02
                       4.533e-01
                                   -0.184 0.854350
Х4
             3.515e-01
                        1.016e-01
                                    3.460 0.000540 ***
A93A92
            -7.354e-02
                       4.294e-01
                                   -0.171 0.864030
A93A93
            -4.435e-01
                        4.191e-01
                                   -1.058 0.289925
                        5.258e-01
                                   -0.530 0.596049
A93A94
            -2.787e-01
A101A102
             3.098e-01
                        4.678e-01
                                    0.662 0.507772
A101A103
                        5.004e-01
                                   -2.191 0.028437 *
            -1.097e+00
X4.1
             5.084e-02
                        9.911e-02
                                    0.513 0.607978
A121A122
                        2.928e-01
                                    0.728 0.466371
             2.133e-01
A121A123
             2.344e-01
                        2.702e-01
                                    0.867 0.385786
A121A124
             8.491e-01 4.776e-01
                                     1.778 0.075432 .
X67
            -1.367e-02
                       1.049e-02
                                   -1.303 0.192427
A143A142
            -6.222e-01 4.828e-01
                                   -1.289 0.197547
A143A143
            -8.858e-01
                        2.736e-01
                                   -3.238 0.001204 **
                        2.681e-01
                                   -1.499 0.133877
A152A152
            -4.019e-01
A152A153
            -6.747e-01
                        5.389e-01
                                   -1.252 0.210574
X2
                        2.256e-01
                                    0.697 0.486016
             1.571e-01
A173A172
             3.819e-01
                        7.684e-01
                                    0.497 0.619145
A173A173
             3.090e-01
                        7.359e-01
                                    0.420 0.674548
A173A174
             4.466e-01
                        7.625e-01
                                    0.586 0.558038
            -2.826e-02
                        2.919e-01
                                    -0.097 0.922868
A192A192
            -3.959e-01
                        2.305e-01
                                   -1.717 0.085902 .
A201A202
            -1.224e+00
                        6.569e-01
                                   -1.864 0.062358 .
```

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

```
Null deviance: 980.03 on 798
                                  degrees of freedom
Residual deviance: 700.80 on 750
                                  degrees of freedom
AIC: 798.8
Number of Fisher Scoring iterations: 5
predicted <- predict(logitMod, testd, type="response") # predicted scores</pre>
Prediction=ifelse(predicted>0.5,'BAD',"GOOD")
cM=confusionMatrix(table(Prediction, Actual[g=="test"]))
confusionMatrix(table(Prediction, Actual[g=="test"]))
Confusion Matrix and Statistics
Prediction BAD GOOD
      BAD
            26
      GOOD 32
              120
               Accuracy: 0.73
                 95% CI: (0.6628, 0.7902)
   No Information Rate: 0.71
   P-Value [Acc > NIR] : 0.2954
                  Kappa : 0.3091
Mcnemar's Test P-Value: 0.2207
            Sensitivity: 0.4483
            Specificity: 0.8451
         Pos Pred Value: 0.5417
         Neg Pred Value: 0.7895
             Prevalence: 0.2900
         Detection Rate: 0.1300
   Detection Prevalence: 0.2400
      Balanced Accuracy: 0.6467
       'Positive' Class : BAD
Acc=round(cM$overall[1],digits=2)
Sens=round(cM$byClass[1],digits=2)
Spec=cM$byClass[2]
```

(Dispersion parameter for binomial family taken to be 1)

The coefficients are not all important as evident from the diagnostics, which means the model could be improved via subset selection or some other method. In the above example the **Threshold** for selecting one of the states (i.e. classifying) of the response **0.5**. The accuracy of the model was **0.73** which is pretty good. If we did not know any more specifics about the problem at hand this would effective. In the case that the bad valued differently the various errors, for example a "bad" creditor given a loan is more costly than a "good" one being denied a loan, we would like to check the sensitive and specifity of the model. In this case the model has sensitivity of **0.45**, which is depentant on the True positive and False negative errors ("bad" creditors classified as "good"). Based on this the model does not perform well and we shall see in the following part how to optimize it.

Part 2: Given that the false negative errors ("bad" creditors classified as "good") is 5 times more costly

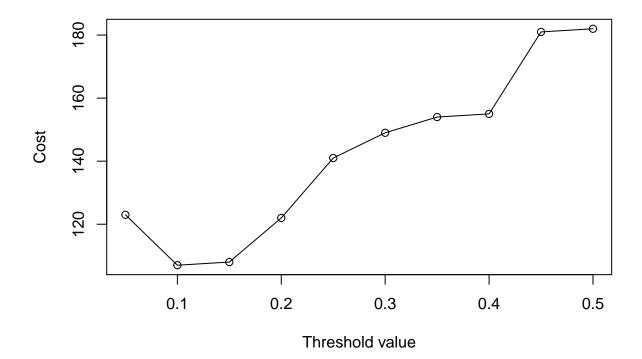
than the false positive errors ("good" creditors identifyied as "bad") we would like to have a our model to minimize the **Total cost function**. In this case the cost function is:

$$Cost = FN * 5 * C + FP * C$$

where C= positive constant. We could have plotted a **ROC** curve and select an appropriate cut-off point, but since we have the specific cost function I have decided to follow a different approach. This is equivalent to saying that we would like a model with higher **sensitivity**. In the following code I tried to create a simple optimization with a "for" loop, rather than use a premade package. For this task, I trained the model with 80% of the data, since the model remains the same for different Thresholds, calculated the cost function based on the perfomance on the test set for various Thresholds and selected the model which **minimizes** the total cost. I do not think there is need for validation set here, since the model remains the same.

```
Cost=matrix(OL,nrow=10,ncol=1)
range=seq(0.05,0.5,0.05)
for (i in 1:10){
   Pred2=ifelse(predicted>range[i],'BAD',"GOOD")
   temp=confusionMatrix(table(Pred2,Actual[g=="test"]))
   Cost[i]=temp$table[2,1]*5+temp$table[1,2]
}
plot(range,Cost,xlab="Threshold value",ylab="Cost",main="Cost vs Threshold",type="o")
```

Cost vs Threshold



In the above example I used various lower Thresholds in order to increase the sensitivity of the model. The **minimum Cost** was found for **Threshold value equal to 0.1**. In this case the sensitivity of the model was **0.93**, which is pretty good.