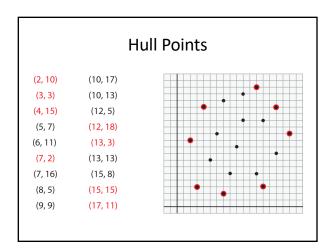
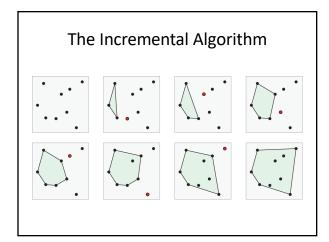
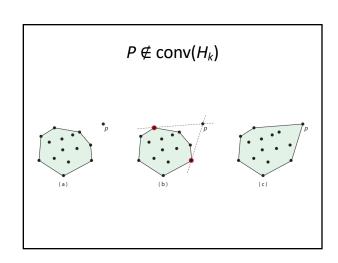
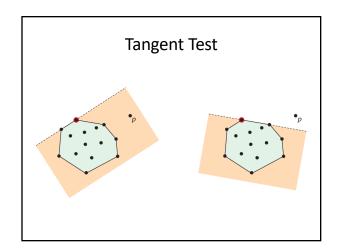
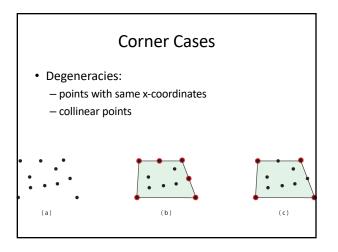
Computational Geometry Convex Hull









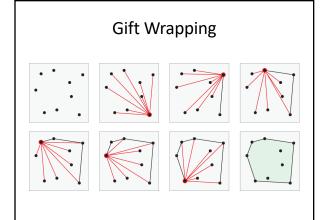


## Big-O

- O(f(n)) means cf(n) is an upper bound on the running time of the algorithm for some constant c > 0 and sufficiently large n.
- Anything that takes one step is O(1): i.e. whether or not an edge is visible to p.
- Sorting takes  $n\log(n)$  time.
- Loop steps are multiplied and sequential steps are added.

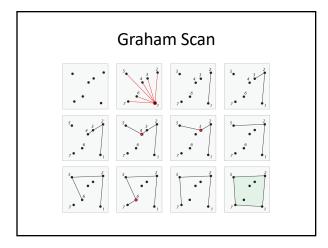
### Complexity

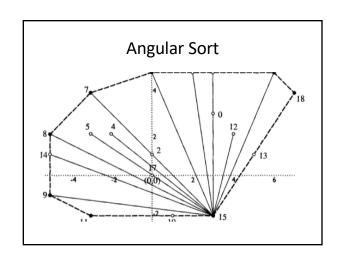
- Sort by x
- For each p, test each edge of the current hull for visibility to p
  - in the worst case, we may have to consider all edges in current hull
- O(n²)

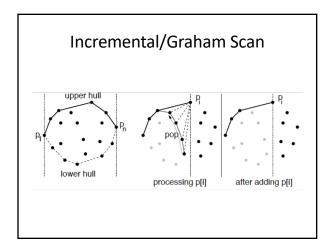


# Complexity

- Sort and find bottom (rightmost) point
- For each point on the hull, calculate angles to all other points
- O(nh)
- Output sensitive

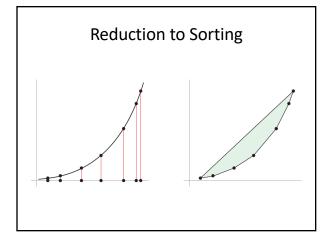






#### **Lower Bound**

- What is the best we can do?
- Denoted by  $\Omega$
- Can we do better than sorting?



## Theorem

• A lower bound for any algorithm that identifies the hull points of a point set in the plane is  $\Omega(n\log n)$