Full pad



$$\begin{pmatrix} \cos\left(\frac{-\pi}{4}\right) & -\sin\left(\frac{-\pi}{4}\right) \\ \sin\left(\frac{-\pi}{4}\right) & \cos\left(\frac{-\pi}{4}\right) \end{pmatrix} \begin{pmatrix} \cos\left(\frac{\pi}{4}\right) - i\sin\left(\frac{\pi}{4}\right) & 0 \\ 0 & \cos\left(\frac{\pi}{4}\right) + i\sin\left(\frac{\pi}{4}\right) \end{pmatrix} \begin{pmatrix} \cos\left(\frac{\pi}{4}\right) & -\sin\left(\frac{\pi}{4}\right) \\ \sin\left(\frac{\pi}{4}\right) & \cos\left(\frac{\pi}{4}\right) \end{pmatrix}$$

Solution

$$\begin{vmatrix} \frac{1}{\sqrt{2}} & i\frac{\sqrt{2}}{2} \\ i\frac{\sqrt{2}}{2} & \frac{1}{\sqrt{2}} \end{vmatrix}$$

Solution steps

$$\begin{pmatrix} \cos\left(\frac{-\pi}{4}\right) & -\sin\left(\frac{-\pi}{4}\right) \\ \sin\left(\frac{-\pi}{4}\right) & \cos\left(\frac{\pi}{4}\right) \end{pmatrix} \begin{pmatrix} \cos\left(\frac{\pi}{4}\right) - i\sin\left(\frac{\pi}{4}\right) \\ 0 & \cos\left(\frac{\pi}{4}\right) + i\sin\left(\frac{\pi}{4}\right) \end{pmatrix} \begin{pmatrix} \cos\left(\frac{\pi}{4}\right) & -\sin\left(\frac{\pi}{4}\right) \\ \sin\left(\frac{\pi}{4}\right) & \cos\left(\frac{\pi}{4}\right) \end{pmatrix}$$

$$\begin{pmatrix} \cos\left(\frac{-\pi}{4}\right) & -\sin\left(\frac{-\pi}{4}\right) \\ \sin\left(\frac{-\pi}{4}\right) & \cos\left(\frac{-\pi}{4}\right) \end{pmatrix} \begin{pmatrix} \cos\left(\frac{\pi}{4}\right) - i\sin\left(\frac{\pi}{4}\right) & 0 \\ 0 & \cos\left(\frac{\pi}{4}\right) + i\sin\left(\frac{\pi}{4}\right) \end{pmatrix} = \begin{pmatrix} \frac{1}{2} - i\frac{1}{2} & \frac{1}{2} + i\frac{1}{2} \\ -\frac{1}{2} + i\frac{1}{2} & \frac{1}{2} + i\frac{1}{2} \end{pmatrix}$$

$$= \begin{pmatrix} \frac{1}{2} - i\frac{1}{2} & \frac{1}{2} + i\frac{1}{2} \\ -\frac{1}{2} + i\frac{1}{2} & \frac{1}{2} + i\frac{1}{2} \end{pmatrix} \begin{pmatrix} \cos\left(\frac{\pi}{4}\right) & -\sin\left(\frac{\pi}{4}\right) \\ \sin\left(\frac{\pi}{4}\right) & \cos\left(\frac{\pi}{4}\right) \end{pmatrix}$$

$$\begin{pmatrix} \frac{1}{2} - i\frac{1}{2} & \frac{1}{2} + i\frac{1}{2} \\ -\frac{1}{2} + i\frac{1}{2} & \frac{1}{2} + i\frac{1}{2} \end{pmatrix} \begin{pmatrix} \cos\left(\frac{\pi}{4}\right) & -\sin\left(\frac{\pi}{4}\right) \\ \sin\left(\frac{\pi}{4}\right) & \cos\left(\frac{\pi}{4}\right) \end{pmatrix} = \begin{pmatrix} \frac{1}{\sqrt{2}} & i\frac{\sqrt{2}}{2} \\ i\frac{\sqrt{2}}{2} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

$$= \begin{pmatrix} \frac{1}{\sqrt{2}} & i\frac{\sqrt{2}}{2} \\ i\frac{\sqrt{2}}{2} & \frac{1}{\sqrt{2}} \end{pmatrix}$$