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# Assugnment 1: Modeling of Electron Transport

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## Introduction

The purpose of this code is to ilstate how Monte carlo simulations can be used to model the movement of electorns through an N type silicon semiconductor. This report will analyses the mean thermal velocity, mean free path, time between colisions , temperature and density of electrons.

## Part 1

This section look at the analysis of a system where electrons do not colide within the semiconductor and experience simple boundry conditions. The boundry conditions that were used caused the electrons to bounce off of the top and bottom of the semiconductor and allowed for periodic travel of electrons from one side of the semiconductor to the other. In orhter words when an electron traveled past the side of the semiconductor it was teleported to the otherside with the same velocity.

The code below was used to compleat the first section of the Assignment. This code was also used to compleat the other two sections by modifying the partial\_colission, boxes, and specular variables to match the combinations required for the individual parts.

```
clc;clear;close all
global C

C.q_0 = 1.60217653e-19;           % electron charge
C.hb = 1.054571596e-34;          % Dirac constant
C.h = C.hb * 2 * pi;             % Planck constant
C.m_0 = 9.10938215e-31;          % electron mass
C.kb = 1.3806504e-23;            % Boltzmann constant
C.eps_0 = 8.854187817e-12;       % vacuum permittivity
C.mu_0 = 1.2566370614e-6;        % vacuum permeability
C.c = 299792458;                 % speed of light
C.g = 9.80665; %metres (32.1740 ft) per sÂ²

% partical_colission = 0;% part 2
% boxes =0;%part 3
% specular = 1 ;% part 3 one is on zero is off
%
% T= 300;%k temperature
% Eme= 0.26* C.m_0;% kg effective mass of electron
% Tmn = 0.2e-12%s mean time between colissions
% vth = sqrt(2*C.kb*T/Eme)% m/s thermal velocity
```

```
% MFP = vth*Tmn %m
% m= 500;% length of sim
% dt = 7e-15;% time step
% N = 10000; %number of electons
% dimx =200e-9;%m
% dimy =100e-9;%m
% % create boxes
% if (boxes)
%     box1 =
        [dimx-125e-9,dimx-75e-9,dimx-75e-9,dimx-125e-9,dimx-125e-9;dimy,dimy,
        dimy-40e-9,dimy-40e-9,dimy];
%     box2 =
        [dimx-125e-9,dimx-75e-9,dimx-75e-9,dimx-125e-9,dimx-125e-9;40e-9,40e-9,
        0,0,40e-9];
% else
%     box1 =[0 0 0 0 0 ; 0 0 0 0 0];
%     box2 =[0 0 0 0 0 ; 0 0 0 0 0];
% end
% % initiates points and ensures that they donot spawn ouside the
    boundaries
% if ~boxes
%     xpos = (randi((dimx*1e9)+1,1,N)-1)/1e9;% m electron position x
%     ypos = (randi((dimy*1e9)+1,1,N)-1)/1e9;% m electron position y
% elseif(boxes)
%     for l =1:N
%         xpos(1,l) =(randi((dimx*1e9)+1,1,1)-1)/1e9 ;
%         ypos(1,l) =(randi((dimy*1e9)+1,1,1)-1)/1e9;
%         while (ypos(1,l)<=0|ypos(1,l)>=dimy|
xpos(1,l)>=box1(1,1)&xpos(1,l)<=box1(1,2)&(ypos(1,l)<=box2(2,1)|
ypos(1,l)>=box1(2,3)))
%             xpos(1,l) =(randi((dimx*1e9)+1,1,1)-1)/1e9 ;
%             ypos(1,l) =(randi((dimy*1e9)+1,1,1)-1)/1e9;
%         end
%     end
% end
% % while(sum ((xpos>=box1(1,1)&xpos<= box1(1,1)& ypos>= box1(2,3))|
(xpos>=box2(1,1)&xpos<= box2(1,1)& ypos>= box2(2,3)))>=1)
% %     xpos = (randi((dimx*1e9)+1,1,N)-1)/1e9;% m electron position x
% %     ypos = (randi((dimy*1e9)+1,1,N)-1)/1e9;% m electron position y
% % end
%
% vx  = zeros(1,N);%m/s velocity in x
% vy  = zeros(1,N);%m/s velocity in y
% colision_count = zeros(1,N);
% dtraveled=zeros(1,N);
% colour = [[1 0 0];[0 1 0];[0 0 1];[0 1 1];[1 0 1];[1 1 0];[0 0 0];
[0 0.447 0.741];[0.85 0.325 0.098];[0.929 0.694 0.125];[0.466 0.674
0.188]];
% Temp = T;
%
% % initiated the partical velocities
% if ~partical_colission
%     angle = rand(1,N);
%     vx = vth* cos(angle*2*pi);
```

```
%      vy = vth* sin(angle*2*pi);
% else
%      vx =randn(1,N)*sqrt(C.kb*T/Eme);
%      vy=randn(1,N)*sqrt(C.kb*T/Eme);
% end
% v = sqrt(vx.^2+vy.^2);
%
%
%
% if boxes
%     figure (2)
%     subplot(2,1,1);
%     plot (box1(1,:),box1(2,:), '-k')
%     hold on
%     plot (box2(1,:),box2(2,:), '-k')
% end
% if partical_colission
%     figure
%     histogram(v)
%     p =1-exp(-dt/Tmn);
% else
%     p=0;
% end
% for l=1:m
%
%     %updates position
%     xpos=[xpos;xpos(l,:)+vx*dt];
%     ypos=[ypos;ypos(l,:)+vy*dt];
%     % finds the distance traveled by each partical
%     dtraveled = dtraveled + sqrt ((xpos(l,:)-xpos(l
+1,:)).^2+(ypos(l,:)-ypos(l+1,:)).^2);
%     slope =(vy./vx);
%     % sets up colision detection by determining if the particals
%     have the
%     % distance to the edges
%     dtt = sqrt(((dimy -ypos(l+1,:)).^2)+((((dimy-ypos(l+1,:))./
slope)).^2));
%     dtb = sqrt(((0 -ypos(l+1,:)).^2)+(((((-ypos(l+1,:))./
slope)).^2));
%     if(boxes)
%         dttbf = ((xpos(l+1,:)>=box1(1,1)&xpos(l+1,:)<=box1(1,2))).*
sqrt(((box1(2,3) -ypos(l+1,:)).^2)+((((box1(2,3)-ypos(l+1,:))./
slope)).^2))+~((xpos(l+1,:)>=box1(1,1)&xpos(l+1,:)<=box1(1,2))).*100;
%         dtbbf = ((xpos(l+1,:)>=box1(1,1)&xpos(l
+1,:)<=box1(1,2))).*sqrt(((box2(2,1) -ypos(l+1,:)).^2)+((((box2(2,1)-
ypos(l+1,:))./slope)).^2))+~((xpos(l+1,:)>=box1(1,1)&xpos(l
+1,:)<=box1(1,2))).*100;
%         dts1 =( ypos(l+1,:)<=box2(2,1)|ypos(l+1,:)>=box1(2,3)).*
sqrt((slope.*(box1(1,1)-xpos(l+1,:)).^2+(box1(1,1)-xpos(l+1,:)).^2)
+~( ypos(l+1,:)<=box2(2,1)|ypos(l+1,:)>=box1(2,3))).*100;
%         dts2=( ypos(l+1,:)<=box2(2,1)|ypos(l+1,:)>=box1(2,3)).*
sqrt((slope.*(box1(1,2)-xpos(l+1,:)).^2+(box1(1,2)-xpos(l+1,:)).^2)
+~( ypos(l+1,:)<=box2(2,1)|ypos(l+1,:)>=box1(2,3))).*100;
%     else
```

```

%           dttbf =100;
%           dtbbf = 100;
%           dts1 =100;
%           dts2=100;
%
%       end
%       %counts the number of colissions that have occured and
%       c=((dts1<4e-9|dts2<4e-9)|((dtt<4e-9|dtb<4e-9|dttbf<4e-9|
dtbbf<4e-9)))));
%       colision_count = colision_count+((dts1<4e-9|dts2<4e-9|
((dtt<4e-9|dtb<4e-9|dttbf<4e-9|dtbbf<4e-9)))));
%       if specular
%           % basic colission part one
%           vy= -((dtt<4e-9|dtb<4e-9|dttbf<4e-9|dtbbf<4e-9).*2-1).*vy;
%           vx= -((dts1<4e-9|dts2<4e-9).*2-1).*vx;
%       else
%           % re thermalized velocities for part 3
%           %if rethermalized volocity is in the same direction as
previous
%           %than flip signs
%           signx=sign(vx);
%           signy=sign(vy);
%
%           vx= (((dts1<4e-9|dts2<4e-9)|((dtt<4e-9|dtb<4e-9|dttbf<4e-9|
dtbbf<4e-9))))).*(randn(1,N)*sqrt(C.kb*T/Eme)) +(~(((dts1<4e-9|
dts2<4e-9)|((dtt<4e-9|dtb<4e-9|dttbf<4e-9|dtbbf<4e-9))))).*vx;
%           vy= (((dts1<4e-9|dts2<4e-9)|((dtt<4e-9|dtb<4e-9|dttbf<4e-9|
dtbbf<4e-9))))).*(randn(1,N)*sqrt(C.kb*T/Eme)) +(~(((dts1<4e-9|
dts2<4e-9)|((dtt<4e-9|dtb<4e-9|dttbf<4e-9|dtbbf<4e-9))))).*vy;
%           vx = ((dts1<4e-9|dts2<4e-9)&signx==sign(vx)).*-1.*vx
+ (~(((dts1<4e-9|dts2<4e-9)&signx==sign(vx))))).*vx;
%           vy = (((dtt<4e-9|dtb<4e-9|dttbf<4e-9|
dtbbf<4e-9)&signy==sign(vy)).*-1.*vy+ (~(((dtt<4e-9|dtb<4e-9|
dttbf<4e-9|dtbbf<4e-9)&signy==sign(vy))))).*vy;
%
%
%
%       end
%       % loop condition for end boundries
%       xpos(l+1,:) = (xpos(l+1,*)>dimx).*0+(xpos(l+1,*)<0).*dimx
+ ~(xpos(l+1,*)>=dimx|xpos(l+1,*)<=0).*xpos(l+1,:);
% % colisions with other particals are only alouwed when partical is
away
% % from the edges and has not colided with an edge Part 2 and 3
%       colision = p>rand(1,N)&~(((dts1<10e-9|dts2<10e-9)|((dtt<10e-9|
dtb<10e-9|dttbf<10e-9|dtbbf<10e-9))))&~c;
%       colision_count = colision_count+colision;
%       vy=colision.*(randn(1,N)*sqrt(C.kb*T/Eme))+(~colision).*vy;
%       vx=colision.*(randn(1,N)*sqrt(C.kb*T/Eme))+(~colision).*vx;
%
%
%
%       % skips the plot of the x boundry transition
%       skip = (xpos(l+1,*)>=dimx|xpos(l+1,*)<=0);

```

```
%      % progress = (1/m)*100
%      v = sqrt(vx.^2+vy.^2);
%      c=0;
%      %finds the current temperature
%      Temp =[Temp, ((mean((vy).^2)+mean((vx).^2))*Eme/(2*C.kb))];
%      % plots the electrons
%      figure (2)
%      for k =1:10
%          if skip(k)==0
%              subplot(2,1,1);
%              plot([xpos(1,k),xpos(1+1,k)],[ypos(1,k),ypos(1
+1,k)], '-','color',colour(k,:))
%          end
%          xlim([0,dimx])
%          ylim([0,dimy])
%          hold on
%          %quiver(xpos(:,k),ypos(:,k),vx+xpos(:,k),vy
+ypos(:,k),0.0001)
%          drawnow limitrate
%      end
%      subplot(2,1,2)
%      plot([dt*(1-1),dt*(1)],Temp(1:1+1),'b-')
%      hold on
%      xlabel('time (s)')
%      ylabel('temperature (k)')
%
%      xlim([0,m*dt])
%      ylim([0,T+100])
% end
% %finds the mean free path and mean time between colission for part 2
and
% %plots a final velocity hystegram
% if (partical_colission)
%     colision_count(colision_count<=0) = 1
%     MFP2 = mean (dtraveled./(colision_count))
%     Tmn2= mean( m*dt./(colision_count))
%     figure(3)
%     histogram(v)
%     xlabel('volocity (m/s)')
%     ylabel('probablility')
% end
% %findes the dencity and temperature of the electrons part 3
%     squarcount= zeros(round(dimy/1e-9),round(dimx/1e-9));
%     temps= zeros(round(dimy/1e-9),round(dimx/1e-9));
%     for k =1:N
%
%         yindex = min((round(dimy/1e-9))-ceil(ypos(m
+1,k)/1e-9)+1,round(dimy/1e-9));
%         xindex = min(ceil(xpos(m+1,k)/1e-9)+1,round(dimx/1e-9));
%         % excludes particals that violate boundry conditions.
%         if ((yindex>0&xindex>0) & ~(((ypos(m+1,k)>=box1(2,3))|
(ypos(m+1,k)<=box2(2,1))))&(xpos(m+1,k)>= box1(1,1)&xpos(m
+1,k)<=box1(1,2))))
```

```
%          squarcount(yindex,xindex) =squarcount(yindex,xindex) +1;
%          temps(yindex,xindex)=v(k)*Eme/
(2*C.kb)+temps(yindex,xindex);
%          end
%      end
%      temps=temps./squarcount;
%      squarcount =squarcount./((1e-9)*(1e-9));
%
%      figure
%      subplot(1,2,1)
%      bar3(squarcount)
%      xlabel('x position (nm)')
%      ylabel('y position (nm)')
%      zlabel('Density of Electrons (electron/m)')
%      subplot(1,2,2)
%
%      bar3(temps)
%      xlabel('x position (nm)')
%      ylabel('y position (nm)')
%      zlabel('Temperature (k)')
```

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