# Analyse\_3: Graph analysis.

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```
library("dplyr")
library("tidyr")
library("lubridate")
library("readr")
library("ggplot2")
library("ggmap")
library("igraph")
library("popgraph")
library("zipcode")
trip_read
            <- read_csv("trip_full_updated2.csv")</pre>
status_read <- read_csv("status_full_updated.csv")</pre>
             <- dplyr::tbl_df(trip_read)</pre>
trip
             <- dplyr::tbl_df(status_read)
status
```

### Introduction

We're going to do use some graph theory to analyse the BABS bike network. This will help us figure out which stations are the most integral to the network.

### Create the network

We'll first create a network out of our bike network with stations as the nodes and number of trips between stations as the weights on the edges. We'll normalise these weights.

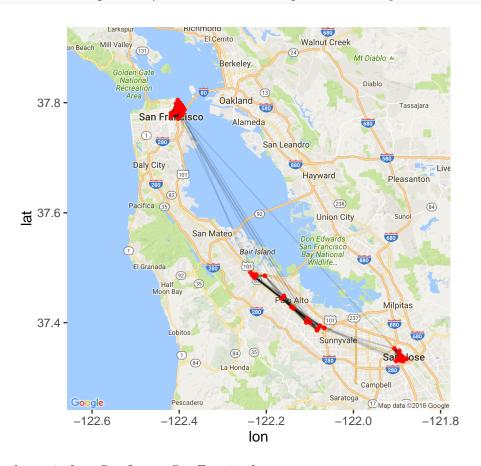
```
station <-read_csv("201508_station_data.csv")
station <- dplyr::tbl_df(station)
station$name[36] = "Washington at Kearny" #correct the misspellings!
station$name[37] = "Post at Kearny"

tripNumbers <- trip %>%
    group_by(Start.Station,End.Station) %>%
    summarise(weight = n()) %>%
    ungroup() %>%
    mutate(weight = (weight - min(weight))/(max(weight)-min(weight)))

bikeGraph <- graph_from_data_frame(tripNumbers, directed=TRUE) %>%
set_vertex_attr("latitude", value = station$lat) %>%
set_vertex_attr("longitude", value = station$long) %>%
set_vertex_attr("city", value = station$landmark)
```

### Visualise the network

We can firstly visualise our network:



That's a pretty long trip from San Jose to San Francisco!

```
Subscriber.Type)
longTrip
```

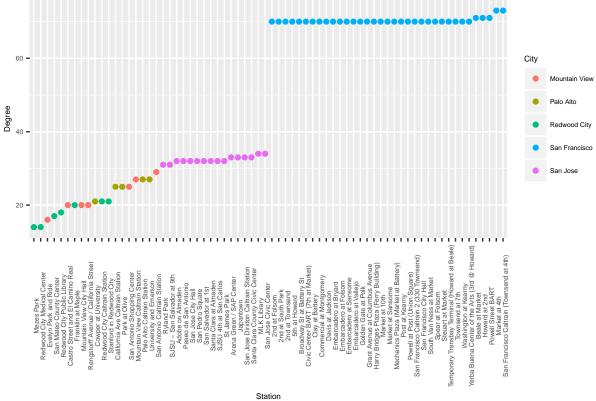
```
## # A tibble: 1 x 7
     Trip.ID Duration
                               Start_trip Start.Station
                                                                   End trip
##
      <int>
                <int>
                                   <time>
                                                  <chr>
                                                                     <time>
## 1 695326
                29942 2015-03-24 13:04:00
                                            MLK Library 2015-03-24 21:23:00
## # ... with 2 more variables: End.Station <chr>, Subscriber.Type <chr>
```

### Degree

The degree of a node tells us how many stations it connects to. We'll calculate the sum of the in and out degrees for each station

```
deg <- degree(bikeGraph, mode= "total")</pre>
deg <- sort(deg)</pre>
degDF <- data.frame(station = names(deg), degree = deg)</pre>
degDF <- dplyr::tbl_df(degDF)</pre>
degreeDF <- left_join(degDF, station, by = c("station" = "name"))</pre>
ggplot(degreeDF, aes(x=station, y = degree, col = landmark)) +
  geom_point() +
  theme(text = element_text(size=6), axis.text.x = element_text(angle=90, vjust=1))+
  labs(x="Station", y= "Degree", col = "City", title = "BABS station degrees") +
  scale_x_discrete(limits = degreeDF$station)
```



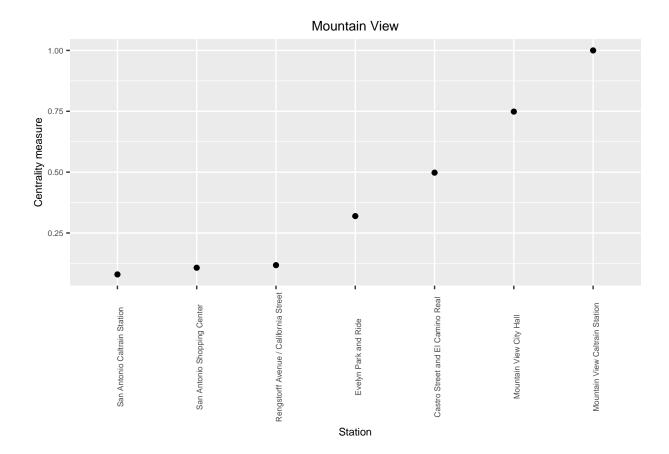


This is interesting but we can use a more discriminatory property.

### Eigenvalue centrality

We'll now split the network up and analyse the individual cities by calculating the eigenvalue centrality.

```
tripNumbers <- trip %>%
  filter(startLandmark == "Mountain View", endLandmark == "Mountain View") %>%
  group_by(Start.Station,End.Station) %>%
  summarise(weight = n()) %>%
  ungroup() %>%
  mutate(weight = (weight - min(weight))/(max(weight)-min(weight)))
bikeGraph <- graph_from_data_frame(tripNumbers, directed=TRUE)</pre>
bikeE <- eigen_centrality(bikeGraph, directed = TRUE)</pre>
bikeEigen <- data.frame(station = names(bikeE$vector), eig = bikeE$vector)</pre>
bikeEigen <- dplyr::tbl_df(bikeEigen)</pre>
bikeEigen <- mutate(bikeEigen, station = as.character(station))</pre>
bikeEigen <- arrange(bikeEigen, eig)</pre>
ggplot(bikeEigen, aes(x=station, y = eig))+
  geom_point()+
  theme(text = element_text(size=8), axis.text.x = element_text(angle=90, vjust=1))+
  labs(x="Station", y= "Centrality measure", title = "Mountain View")+
  scale_x_discrete(limits = bikeEigen$station)
```



```
tripNumbers <- trip %>%
  filter(startLandmark == "Palo Alto", endLandmark == "Palo Alto") %>%
  group_by(Start.Station,End.Station) %>%
  summarise(weight = n()) %>%
  ungroup() %>%
  mutate(weight = (weight - min(weight))/(max(weight)-min(weight)))
bikeGraph <- graph_from_data_frame(tripNumbers, directed=TRUE)</pre>
bikeE <- eigen_centrality(bikeGraph, directed = TRUE)</pre>
bikeEigen <- data.frame(station = names(bikeE$vector), eig = bikeE$vector)</pre>
bikeEigen <- dplyr::tbl_df(bikeEigen)</pre>
bikeEigen <- mutate(bikeEigen, station = as.character(station))</pre>
bikeEigen <- arrange(bikeEigen, eig)</pre>
ggplot(bikeEigen, aes(x=station, y = eig))+
  geom_point()+
 theme(text = element_text(size=8), axis.text.x = element_text(angle=90, vjust=1))+
  labs(x="Station", y= "Centrality measure", title = "Palo Alto")+
  scale_x_discrete(limits = bikeEigen$station)
```

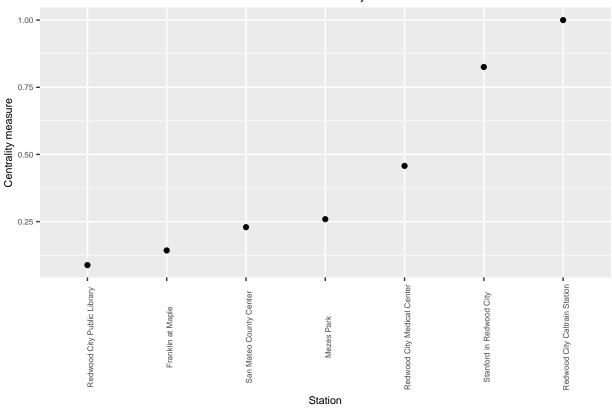
# Pale Alto Cowper at University and Emerson Cowper at University and Emerson Cowper at University and Emerson

```
tripNumbers <- trip %>%
  filter(startLandmark == "Redwood City", endLandmark == "Redwood City") %>%
  group_by(Start.Station,End.Station) %>%
  summarise(weight = n()) %>%
  ungroup() %>%
  mutate(weight = (weight - min(weight))/(max(weight)-min(weight)))
```

Station

```
bikeGraph <- graph_from_data_frame(tripNumbers, directed=TRUE)
bikeE <- eigen_centrality(bikeGraph, directed = TRUE)
bikeEigen <- data.frame(station = names(bikeE$vector), eig = bikeE$vector)
bikeEigen <- dplyr::tbl_df(bikeEigen)
bikeEigen <- mutate(bikeEigen, station = as.character(station))
bikeEigen <- arrange(bikeEigen, eig)
ggplot(bikeEigen, aes(x=station, y = eig))+
    geom_point()+
    theme(text = element_text(size=8), axis.text.x = element_text(angle=90, vjust=1))+
    labs(x="Station", y= "Centrality measure", title = "Redwood City")+
    scale_x_discrete(limits = bikeEigen$station)</pre>
```

### Redwood City

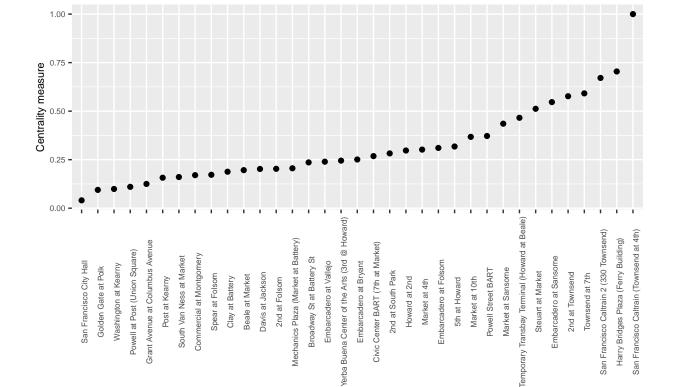


```
tripNumbers <- trip %>%
  filter(startLandmark == "San Francisco", endLandmark == "San Francisco") %>%
  group_by(Start.Station,End.Station) %>%
  summarise(weight = n()) %>%
  ungroup() %>%
  mutate(weight = (weight - min(weight))/(max(weight)-min(weight)))

bikeGraph <- graph_from_data_frame(tripNumbers, directed=TRUE)
bikeE <- eigen_centrality(bikeGraph, directed = TRUE)
bikeEigen <- data.frame(station = names(bikeE$vector), eig = bikeE$vector)
bikeEigen <- dplyr::tbl_df(bikeEigen)
bikeEigen <- mutate(bikeEigen, station = as.character(station))
bikeEigen <- arrange(bikeEigen, eig)</pre>
```

```
ggplot(bikeEigen, aes(x=station, y = eig))+
  geom_point()+
  theme(text = element_text(size=8), axis.text.x = element_text(angle=90, vjust=1))+
  labs(x="Station", y= "Centrality measure", title = "San Francisco")+
  scale_x_discrete(limits = bikeEigen$station)
```

San Francisco



Spear at Folsom Clay at Battery Beale at Market Davis at Jackson

2nd at Folsom

Post at Kearny

2nd at South Park

Station

Howard at 2nd

Market at 4th

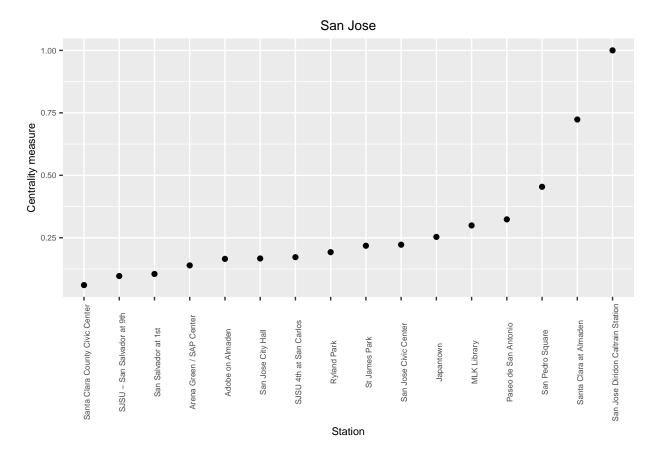
Market at 10th

5th at Howard

2nd at Townsend

Townsend at 7th

```
tripNumbers <- trip %>%
  filter(startLandmark == "San Jose", endLandmark == "San Jose") %>%
  group_by(Start.Station,End.Station) %>%
  summarise(weight = n()) %>%
  ungroup() %>%
  mutate(weight = (weight - min(weight))/(max(weight)-min(weight)))
bikeGraph <- graph_from_data_frame(tripNumbers, directed=TRUE)</pre>
bikeE <- eigen_centrality(bikeGraph, directed = TRUE)</pre>
bikeEigen <- data.frame(station = names(bikeE$vector), eig = bikeE$vector)</pre>
bikeEigen <- dplyr::tbl_df(bikeEigen)</pre>
bikeEigen <- mutate(bikeEigen, station = as.character(station))</pre>
bikeEigen <- arrange(bikeEigen, eig)</pre>
ggplot(bikeEigen, aes(x=station, y = eig))+
  geom_point()+
  theme(text = element text(size=8), axis.text.x = element text(angle=90, vjust=1))+
  labs(x="Station", y= "Centrality measure", title = "San Jose")+
  scale_x_discrete(limits = bikeEigen$station)
```



Interestingly we see that the busiest station in each city is located by a train station. This is important if we want to expand into new cities as people seem to be using them as part of their commute. We can investigate this further by analysing the types of trips being taken.

```
tripTypes <- trip %>%
group_by(Start.Station, End.Station) %>%
summarise(count =n()) %>%
ungroup() %>%
arrange(desc(count)) %>%
left_join(station, by = c("Start.Station" = "name"))
```

We can look at the most common trips in each city

```
## # A tibble: 10 x 3
## Start.Station End.Station count
## 

chr> <chr> <int>
## 1 Mountain View Caltrain Station Mountain View City Hall 1419
## 2 Mountain View City Hall Mountain View Caltrain Station 1308
```

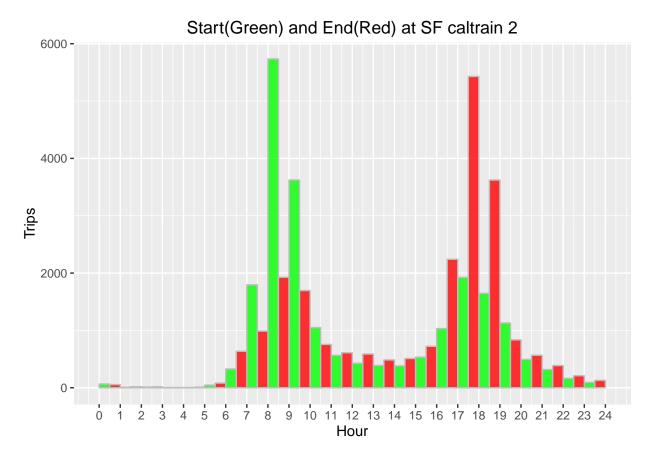
```
CastroStreetandElCaminoReal Mountain View Caltrain Station 1041
## 4 Mountain View Caltrain Station
                                        CastroStreetandElCaminoReal
                                                                      940
                Evelyn Park and Ride Mountain View Caltrain Station
## 5
                                                                      808
## 6
        San Antonio Caltrain Station
                                        San Antonio Shopping Center
                                                                      768
## 7
         San Antonio Shopping Center
                                       San Antonio Caltrain Station
                                                                      740
## 8 Mountain View Caltrain Station
                                               Evelyn Park and Ride
                                                                      608
## 9 Mountain View Caltrain Station Mountain View Caltrain Station
                                                                      254
## 10 RengstorffAvenu/CalifornStreet Mountain View Caltrain Station
                                                                      218
tripTypes %>%
  filter(landmark == "Palo Alto") %>%
  select(Start.Station, End.Station, count) %>%
  mutate(Start.Station = abbreviate(Start.Station, 35),
         End.Station = abbreviate(End.Station, 35))%>%
  slice(1:10)
## # A tibble: 10 x 3
##
                        Start.Station
                                                          End.Station count
##
                                                                <chr> <int>
                                <chr>>
## 1
           Palo Alto Caltrain Station
                                                 Cowper at University
                                                                        387
## 2
                                           Palo Alto Caltrain Station
                 Cowper at University
## 3
               University and Emerson
                                               University and Emerson
                                                                        348
## 4
           Palo Alto Caltrain Station
                                                        Park at Olive
                                                                        241
## 5
           Palo Alto Caltrain Station California Ave Caltrain Station
                                                                        215
## 6
                        Park at Olive
                                           Palo Alto Caltrain Station
                                                                        174
## 7
           Palo Alto Caltrain Station
                                           Palo Alto Caltrain Station
                                                                        162
## 8 California Ave Caltrain Station
                                               University and Emerson
                                                                        101
## 9 California Ave Caltrain Station
                                           Palo Alto Caltrain Station
                                                                         95
## 10 California Ave Caltrain Station California Ave Caltrain Station
                                                                         85
tripTypes %>%
  filter(landmark == "Redwood City") %>%
  select(Start.Station, End.Station, count) %>%
  mutate(Start.Station = abbreviate(Start.Station, 35),
         End.Station = abbreviate(End.Station, 35)) %>%
  slice(1:10)
## # A tibble: 10 x 3
##
                      Start.Station
                                                      End.Station count
##
                              <chr>>
                                                            <chr> <int>
## 1
           Stanford in Redwood City Redwood City Caltrain Station
                                                                    337
     Redwood City Caltrain Station
                                         Stanford in Redwood City
                                                                    332
## 3
      Redwood City Caltrain Station
                                      Redwood City Medical Center
                                                                    202
## 4
                         Mezes Park Redwood City Caltrain Station
                                                                    175
## 5 Redwood City Caltrain Station
                                                       Mezes Park
                                                                    112
## 6
       Redwood City Medical Center Redwood City Caltrain Station
                                                                    109
## 7
     Redwood City Caltrain Station
                                          San Mateo County Center
                                                                     74
     Redwood City Caltrain Station Redwood City Caltrain Station
                                                                     70
                                                Franklin at Maple
## 9
     Redwood City Caltrain Station
                                                                     61
## 10
           Stanford in Redwood City
                                         Stanford in Redwood City
                                                                     49
```

```
tripTypes %>%
  filter(landmark == "San Francisco") %>%
  select(Start.Station, End.Station, count) %>%
  mutate(Start.Station = abbreviate(Start.Station, 30),
         End.Station = abbreviate(End.Station, 30)) %>%
  slice(1:10)
## # A tibble: 10 x 3
##
                       Start.Station
                                                         End.Station count
##
                                <chr>
                                                                <chr> <int>
                                                     Townsend at 7th 3748
## 1
    SanFranciscCaltran2(330Twnsnd)
      HarryBridgesPlaz(FerryBuildng)
                                              Embarcadero at Sansome
## 3
                     2nd at Townsend HarryBridgesPlaz(FerryBuildng)
                                                                       2973
## 4
                     Townsend at 7th SanFranciscCaltran2(330Twnsnd)
                                                                       2734
## 5
      HarryBridgesPlaz(FerryBuildng)
                                                     2nd at Townsend
                                                                      2640
## 6
               Embarcadero at Folsom SanFranciscCaltrn(Twnsndat4th)
                                                                       2439
                   Steuart at Market
## 7
                                                     2nd at Townsend
                                                                      2356
## 8
              Embarcadero at Sansome
                                                   Steuart at Market
                                                                       2330
## 9
                     Townsend at 7th SanFranciscCaltrn(Twnsndat4th)
                                                                       2192
## 10 TemporaryTrnsbyTrmnl(HwrdatBl) SanFranciscCaltrn(Twnsndat4th)
                                                                       2184
tripTypes %>%
  filter(landmark == "San Jose") %>%
  select(Start.Station, End.Station, count) %>%
  mutate(Start.Station = abbreviate(Start.Station, 30),
         End.Station = abbreviate(End.Station, 30)) %>%
  slice(1:10)
## # A tibble: 10 x 3
##
                      Start.Station
                                                       End.Station count
##
                               <chr>
                                                              <chr> <int>
## 1
      SanJoseDiridonCaltrainStation
                                            Santa Clara at Almaden
                                                                    1232
             Santa Clara at Almaden SanJoseDiridonCaltrainStation
## 2
                                                                     1214
## 3
      SanJoseDiridonCaltrainStation
                                                  San Pedro Square
                                                                      687
## 4
                        MLK Library SanJoseDiridonCaltrainStation
                                                                      668
## 5
                   San Pedro Square SanJoseDiridonCaltrainStation
                                                                      614
## 6
     SanJoseDiridonCaltrainStation
                                              Paseo de San Antonio
                                                                      497
      SanJoseDiridonCaltrainStation
                                                       MLK Library
                                                                      461
## 8
                        Ryland Park SanJoseDiridonCaltrainStation
                                                                      395
## 9
                      St James Park SanJoseDiridonCaltrainStation
                                                                      335
## 10 SanJoseDiridonCaltrainStation
                                                     St James Park
                                                                      318
From which we see how integral the train stations are to this bike network. Who is taking these trips? Is it
subscribers?
trip %>% filter(Start.Station == "San Francisco Caltrain 2 (330 Townsend)") %>%
 group_by(Subscriber.Type) %>% summarise(count = n())
## # A tibble: 2 x 2
     Subscriber. Type count
##
               <chr> <int>
## 1
            Customer
                       835
```

## 2

Subscriber 20923

We see it is mainly subscribers using this station. What time of day is it being used?



From which we see it it mainly at the hours of people arriving for work and leaving from work.

Where do they live? we can use the zipcode information to answer this combined with the zipcode data and library package.

```
data("zipcode")
zips <- trip %>%
```

```
filter(Start.Station == "San Francisco Caltrain 2 (330 Townsend)") %>%
group_by(Zip.Code) %>%
summarise(count = n()) %>%
ungroup() %>%
mutate(zip = clean.zipcodes(Zip.Code)) %>%
merge(zipcode, by.x='zip', by.y='zip') %>%
arrange(desc(count))
```

```
zip Zip.Code count
                               city state latitude longitude
##
          94107 5192 San Francisco CA 37.76653 -122.3958
## 1 94107
            94103 896 San Francisco CA 37.77233 -122.4109
## 2 94103
## 3 94403
            94403 663
                          San Mateo CA 37.53969 -122.3027
## 4 94102 94102 617 San Francisco CA 37.77933 -122.4192
## 5 94402
            94402 490
                         San Mateo
                                     CA 37.55159 -122.3277
## 6 94010
            94010
                   487
                          Burlingame
                                      CA 37.57494 -122.3633
```

But note there is one subscriber from as far as Hawaii!

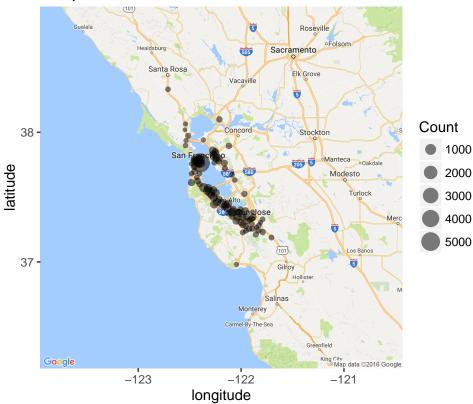
```
filter(zips, state == "HI")
```

```
## zip Zip.Code count city state latitude longitude
## 1 96818 96818 1 Honolulu HI 21.36425 -157.9632
```

(I doubt they are commuting though)

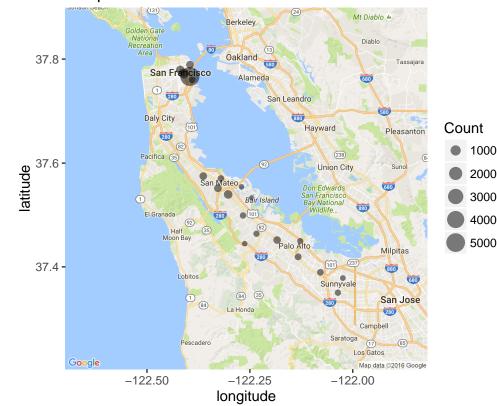
Let's look at the top 100 zipcodes which are all in California.

# Zip codes of users of SF Caltrain 2 station.



People travel from afar to use this station. Let's look more specifically by choosing the top 20 zipcodes.





### Clusters

Let's try to find communities within the city of San Francisco using the infomap algorithm Here is our network:

```
tripNumbers <- trip %>%
  filter(startLandmark == "San Francisco", endLandmark == "San Francisco") %>%
  group_by(Start.Station,End.Station) %>%
  summarise(weight = n()) %>%
  ungroup() %>%
  mutate(weight = (weight - min(weight)+0.0000001)/(max(weight)-min(weight)))

stationSF <- station %>% filter(landmark == "San Francisco") %>% arrange(name)

bikeGraph <- graph_from_data_frame(tripNumbers, directed=TRUE)
location <- c( mean(stationSF$long), mean(stationSF$lat))

BABSmap <- get_map(location,maptype="roadmap", zoom=14)</pre>
```

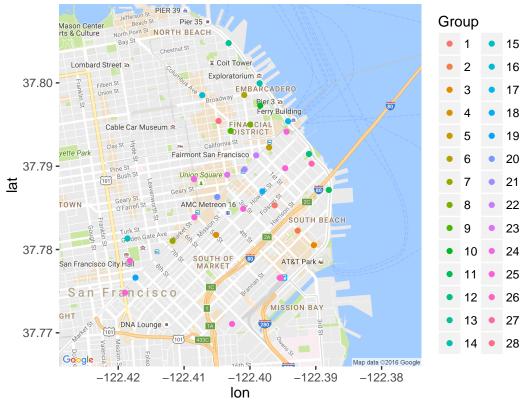
Let's look at some clustering algorithms

```
clus_eb <- cluster_edge_betweenness(bikeGraph)
clus_op <- cluster_optimal(bikeGraph)
clus_sg <- cluster_spinglass(bikeGraph)
clus_wt <- cluster_walktrap(bikeGraph)</pre>
```

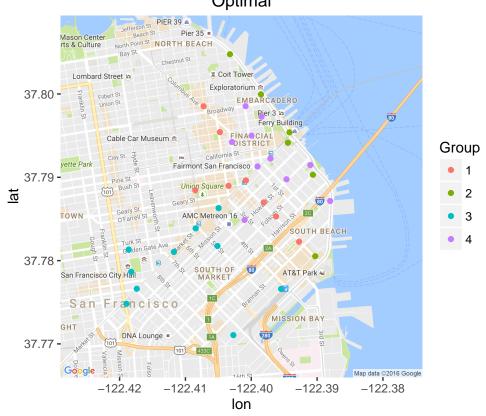
```
stationSF$eb <-clus_eb$membership
stationSF$op <-clus_op$membership
stationSF$sg <-clus_sg$membership
stationSF$wt <-clus_wt$membership</pre>
```

and see what results they give us

# Edge betweeness



# **Optimal**

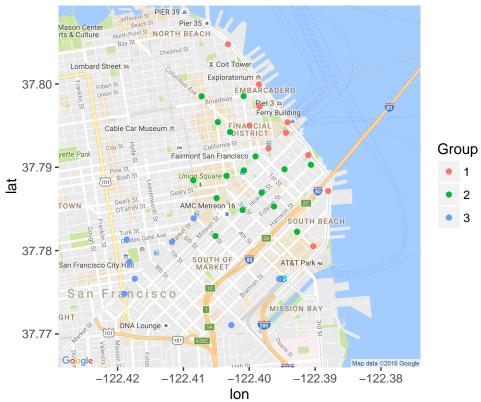


# Spin glass



```
ggmap(BABSmap)+
  geom_point(data = stationSF,
             aes( y= lat,
                 x =long,
                  col = as.factor(wt)))+
  labs(title = "Walk trap", col ="Group")
```

# Walk trap



The useful clusterings seem to be mainly correlated with location, indicating lots of short trips within these clusters.