

4. (a) if we want converge.

$$\log(A)_{k+1} - \log(A)_k = \frac{(I-A)^{k+1}}{k+1} \leq \frac{-(I-A)^k}{k}$$

$$\Rightarrow \frac{-(I-A)^{k+1}}{k+1} = -\frac{(I-A)^k}{k} \cdot (I-A) \cdot \frac{k}{k+1} \Rightarrow$$

$$\frac{k}{k+1} (I-A) < 1 \Rightarrow \|I-A\| < \frac{k}{k+1}$$

(b) For each $(I-A)$, Computational complexity is n^2 .

For each $(I-A) \cdot (I-A)$, Computational complexity is n^3 .

$$\text{For } k=1, \quad O(n) = n^2$$

$$k=2, \quad O(n) = 2n^2 + n^3$$

$$k=k, \quad O(n) = kn^2 + (k-1)n^3$$

$$\text{Total computational complexity} = \frac{(k+1) \cdot k}{2} n^2 + \frac{(k-1)k}{2} n^3$$